

1 **It's Hard to Know How Hard It Is:**
2 **Mapping the Design Space of LLM Item**
3 **Difficulty Estimation**

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6 **Abstract.** Can LLMs estimate how hard a test question is? Published
7 results disagree wildly—correlations range from near-zero to $r = 0.87$ —
8 but each study typically tests one prompt on one model on one dataset.
9 We map the design space systematically: 15 prompts grounded in learn-
10 ing science, 6 models, 3 datasets, and multiple temperature settings
11 (~ 250 conditions, $\sim \$80$ in API calls). Prompts that direct the model
12 to enumerate structural item features—prerequisites, cognitive load, er-
13 ror paths—achieve $\rho = 0.65\text{--}0.69$ on open-ended items. However, this
14 advantage attenuates on MCQs: on two independent datasets (DBE-
15 KT22, BEA 2024), prompts achieve $\rho \approx 0.45\text{--}0.58$, with simple teacher
16 judgment nearly matching structured prompts. Prompt design is the
17 primary lever; model size, deliberation, and temperature each contribute
18 minimally ($\eta^2 < 0.05$). Methodologically, we find that correlations from
19 small item sets ($n < 50$) are unreliable, and that unbalanced hyper-
20 parameter sweeps produce Simpson's paradox artifacts—we recommend
21 two-stage sequential DOE for future work. LLM difficulty estimates can
22 triage items into difficulty bands at $\sim \$0.05$ per item, but the signal is
23 strongest for items whose difficulty varies across knowledge domains.

24 **Keywords:** item difficulty estimation · LLM evaluation · design of
25 experiments · psychometrics · prompt engineering

26 **1 Introduction**

27 A well-designed test gives each student questions at the right level of challenge—
28 hard enough to reveal what they know, easy enough to avoid frustration. Getting
29 this right depends on knowing how difficult each question is before it reaches a
30 student. In practice, this means field-testing items with hundreds or thousands
31 of real students and computing how many answer correctly. In classical test
32 theory, this proportion is called p -correct; item response theory refines it with a
33 latent difficulty parameter b that accounts for examinee ability [8]. Either way,
34 calibrating each item requires collecting responses from 200 to 1,000+ students
35 depending on the IRT model [5], making difficulty estimation one of the most
36 resource-intensive steps in assessment development.

37 That cost is becoming a bottleneck. LLMs can now generate assessment items
38 at scale [15], but generated items arrive without calibrated difficulty estimates.

³⁹ Without such estimates, items cannot be assembled into well-targeted tests,
⁴⁰ used in adaptive systems, or compared to existing item banks. The question
⁴¹ is whether LLMs can also estimate difficulty—replacing or supplementing the
⁴² expensive field-testing step.

⁴³ The task is harder than it appears. LLMs are trained on expert-written text
⁴⁴ and tend to find most items trivial; Li, Chen et al. [13] find that high model per-
⁴⁵ formance paradoxically impedes difficulty estimation—models that solve items
⁴⁶ easily cannot perceive what makes them hard for humans. This “curse of knowl-
⁴⁷ edge” creates a systematic bias: models overestimate student ability and com-
⁴⁸ press difficulty estimates toward the easy end of the scale. Expert teacher judg-
⁴⁹ ment, by comparison, achieves median correlations of $r = 0.66$ [11] to mean
⁵⁰ $r = 0.63$ [19] with actual student performance—a useful reference point, though
⁵¹ these studies measure judgment of individual students rather than aggregate
⁵² item difficulty.

⁵³ Recent work reports correlations ranging from $r \approx 0$ for direct estimation [1]
⁵⁴ to $r = 0.87$ when LLM-extracted features are combined with gradient boost-
⁵⁵ ing [17]. A systematic review of 37 papers on text-based difficulty prediction
⁵⁶ found rapid growth but no consensus on methods, and noted that fine-tuned
⁵⁷ small language models (BERT, RoBERTa) outperform LLMs on structured pre-
⁵⁸ diction tasks [16,14]. The first shared task on automated difficulty prediction
⁵⁹ (BEA 2024) [22] found that best results only marginally beat baselines on 667
⁶⁰ medical items. Li, Chen et al. [13] evaluated 20+ models across multiple assess-
⁶¹ ment domains and found that models converge on a shared “machine consensus”
⁶² that systematically diverges from human difficulty perception.

⁶³ A key limitation is that each study typically tests one model with one prompt
⁶⁴ on one dataset. When results disagree, it is unclear whether the discrepancy
⁶⁵ reflects model choice, prompt design, item properties, or student population.
⁶⁶ We address this by mapping the design space rather than testing any single
⁶⁷ configuration.

⁶⁸ Our optimization target is **rank-order agreement** between LLM-predicted
⁶⁹ difficulty and empirical p -correct, measured by Spearman’s ρ . We choose rank
⁷⁰ correlation because practical applications—item sequencing, adaptive test as-
⁷¹ sembly, item bank stratification—depend on difficulty *ordering* rather than ex-
⁷² act calibration. Each experimental condition prompts an LLM to estimate the
⁷³ proportion of students who would answer each item correctly; we then correlate
⁷⁴ these estimates against observed p -correct from real student responses.

⁷⁵ 2 Related Work

⁷⁶ We organize prior work by approach and extract testable claims from each.

⁷⁷ *Direct LLM Estimation.* Razavi & Powers [17] report $r = 0.83$ (math) and
⁷⁸ $r = 0.81$ (reading) on K–5 items using GPT-4o. However, Acquaye et al. [1] find
⁷⁹ $r \approx 0$ for direct estimation on NAEP items, and Li, Chen et al. [13] find average
⁸⁰ $\rho = 0.28$ across 20+ models on four assessment domains. *Testable claim: direct*

81 *estimation produces meaningful correlations ($\rho > 0.30$) on curriculum-aligned
82 items.*

83 *Feature Extraction + ML.* Razavi & Powers [17] achieve their strongest results
84 ($r = 0.87$) by extracting features from LLMs and training gradient-boosted
85 models. *Testable claim: LLM-extracted features combined with ML outperform
86 direct estimation.*

87 *Simulated Classrooms.* Acquaye et al. [1] simulate classrooms of LLM students
88 at multiple ability levels, achieving $r = 0.75\text{--}0.82$ on NAEP items. Counter-
89 intuitively, weaker math models predicted difficulty better than stronger ones.
90 However, Li, Chen et al. [13] find significant misalignment between AI and human
91 difficulty perception. *Testable claim: simulation outperforms direct estimation.*

92 *Model Uncertainty.* Zotos et al. [23] use LLM uncertainty features (first-token
93 probability, choice-order sensitivity) to predict difficulty. *Testable claim: items
94 the model finds uncertain are items students find difficult.*

95 *Reasoning Augmentation.* Feng et al. [9] report up to 28% MSE reduction when
96 generating reasoning before predicting difficulty. However, Li, Jiao et al. [14] find
97 minimal improvements from chain-of-thought prompting for fine-tuned models.
98 *Testable claim: structured deliberation improves difficulty estimation.*

99 *Cognitive Item Models.* A separate tradition predicts difficulty from structural
100 item features. Embretson's [7] cognitive design system counts processing steps
101 and working memory demands. Gorin [10] manipulates item features to generate
102 items at target difficulties. The KLI framework [12] posits that the number and
103 nature of knowledge components drive learning difficulty. Recent work has used
104 LLMs for KC tagging [15], but not to operationalize cognitive item models as
105 difficulty estimation prompts. *Testable claim: prompts grounded in cognitive item
106 modeling outperform atheoretical prompts.*

107 3 Hypotheses

108 We derive hypotheses from three sources: replication of prior claims, predictions
109 from learning science theory, and exploratory questions about the design space.
110 Table 1 lists all 13 hypotheses with their sources and predictions.

111 4 Method

112 4.1 Datasets

113 *SmartPaper (India, Open-ended)—Primary.* 140 open-ended questions from In-
114 dian state assessments across four subjects (English, Mathematics, Science, So-
115 cial Science), Grades 6–8, with 728,000+ responses. Ground truth: classical p -
116 correct (proportion scoring full marks). Difficulty range: 0.04–0.83, mean 0.29.

Table 1: Hypotheses tested in this study. Verdicts: ✓ = supported, ✗ = rejected, ~ = partial/mixed.

#	Hypothesis	Source/Theory	Prediction	Verdict
<i>From Prior Work (Replication)</i>				
H1	Direct estimation yields $\rho > 0.30$	Razavi & Powers	$\rho > 0.30$	✓ .56
H2	Simulation beats direct	Acquaye et al.	$\rho_{\text{sim}} > \rho_{\text{direct}}$	✗ .19<.56
H3	Larger models do better	Scaling expectation	Larger → higher ρ	~ mixed
<i>From Learning Science Theory</i>				
H4	Item analysis beats direct	Embretson (1998)	$\rho_{\text{analysis}} > \rho_{\text{direct}}$	✓ .69>.56
H5	Prerequisite counting works	KLI (Koedinger)	More prereqs → harder	✓ .69
H6	Cognitive load counting works	CLT (Sweller)	More elements → harder	✓ .67
H7	Buggy rules analysis works	Brown & Burton	More error paths → harder	✓ .66
<i>Exploratory (Design Space)</i>				
H8	Temperature enhances predictions	Stochastic diversity	Higher temp → higher ρ	✗ $\eta^2=.001$
H9	Multi-sample averaging helps	Wisdom of crowds	$\rho_{3\text{-rep}} > \rho_{1\text{-rep}}$	~ +.03
H10	Prompt is primary lever	Design space	Prompt > model + temp	~ dataset-dep.
H11	Analysis needs capable models	Capacity limits	Analysis × capability	✓ interaction
H12	Signal transfers across datasets	Generalizability	Signal on D1 → D2	✓ attenuates

Table 2: Experimental stages.

Stage	Purpose	Dataset	Design
Screening	Map prompt space	SmartPaper (140)	15 prompts × 2–5 temps × 3 reps
Model survey	Model generalization	SmartPaper (140)	6 models × 3 prompts × 3 reps
Confirmation	Cross-dataset transfer	DBE-KT22 (168)	3 prompts × 2 temps × 3 reps
Validation	Published benchmark	BEA 2024 (595)	3 prompts × 1 temp × 3 reps

¹¹⁷ *DBE-KT22 (South Africa, MCQ)—Confirmation.* 168 undergraduate computer
¹¹⁸ science MCQs spanning 27 knowledge components, administered to 1,300+ stu-
¹¹⁹ dents. Ground truth: classical p -correct. Differs from SmartPaper in format,
¹²⁰ domain, and population.

¹²¹ *BEA 2024 Shared Task (USA, USMLE MCQ)—Validation.* 595 text-only items
¹²² from the BEA 2024 automated difficulty prediction shared task [22], compris-
¹²³ ing USMLE Steps 1–3 questions (667 total items minus 72 requiring images).
¹²⁴ Ground truth: IRT difficulty parameters from operational administrations. This
¹²⁵ benchmark allows direct comparison with other difficulty estimation approaches.

¹²⁶ 4.2 Design Space

¹²⁷ 4.3 Prompts

¹²⁸ All 15 prompts share a common output: the LLM predicts what proportion of
¹²⁹ students would answer each item correctly. They differ along two binary dimen-

Table 3: Prompt taxonomy with factor coding. Item = analyzes item structure; Pop. = models student population. All 15 prompts except synthetic_students were tested in screening.

Prompt	Item	Pop.	Theory/Prior Work
teacher			PCK (Shulman, 1986)
verbalized_sampling			Wisdom of crowds
familiarity_gradient	✓		Transfer distance
contrastive	✓		Comparative judgment
prerequisite_chain	✓		KC theory (Koedinger et al.)
cognitive_load	✓		CLT (Sweller, 1988)
cognitive_profile	✓		CLT + profiling
devil_advocate		✓	Debiasing heuristics
teacher_decomposed		✓	IRT stratification
classroom_sim		✓	Acquaye et al. (2025)
imagine_classroom		✓	Imagery-based reasoning
synthetic_students*		✓	Student simulation
error_analysis	✓	✓	Error analysis tradition
error_affordance	✓	✓	Brown & Burton (1978)
buggy_rules	✓	✓	Brown & Burton (1978)
misconception_holistic	✓	✓	Chi et al. (1994)

*Tested in model survey only ($\rho = 0.19$, worst performer).

130 sions: whether the prompt directs the model to *analyze structural item features*
131 (prerequisites, steps, cognitive demands) before estimating, and whether it di-
132 rectes the model to *model the student population* (reason about proficiency levels,
133 struggles). Table 3 lists all 15 prompts. All are available in the project repository.

134 4.4 Models

135 Six models spanning 8B to frontier-scale: Gemini 3 Flash (screening model),
136 GPT-4o, Llama-3.3-70B, Gemma-3-27B, Llama-4-Scout (17B active/109B MoE),
137 and Llama-3.1-8B. Qwen3-32B was tested but excluded due to low parse rates
138 (<50% valid responses).

139 4.5 Statistical Approach

140 Our primary metric is Spearman’s ρ between LLM-predicted and observed p -
141 correct. We report 95% bootstrap confidence intervals (10,000 resamples) for
142 primary results and MAE as a calibration measure. Each condition uses 3 repli-
143 cations; reported ρ is the averaged-prediction correlation (mean prediction across
144 reps correlated with ground truth).

Table 4: Prompt screening results (SmartPaper, $n = 140$), ranked by best ρ . CIs shown for prompts advanced to model survey.

Prompt	Item	Pop.	Best ρ	Temp	95% CI	MAE
prerequisite_chain	✓		0.686	0.5	[.576,.775]	.155
cognitive_load	✓		0.673	2.0	[.550,.766]	.190
buggy_rules	✓	✓	0.655	1.0	[.532,.752]	.117
misconception_holistic	✓	✓	0.636	2.0	—	.204
error_analysis	✓	✓	0.596	2.0	—	.121
devil_advocate		✓	0.596	1.0	—	.098
cognitive_profile	✓		0.586	1.0	[.456,.693]	.214
contrastive	✓		0.584	1.0	—	.123
classroom_sim		✓	0.562	2.0	—	.240
teacher			0.555	1.0	[.422,.664]	.439

145 5 Results

146 We present results in five parts: the headline finding on item analysis prompts,
 147 the mechanism behind it, factors that matter less than expected, generalization
 148 across three datasets, and practical implications.

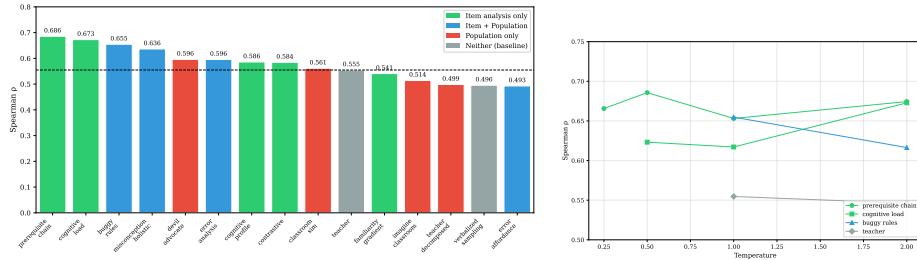
149 5.1 Item Analysis Prompts Achieve $\rho = 0.65\text{--}0.69$

150 Fifteen prompts were screened on SmartPaper (140 open-ended items) using
 151 Gemini 3 Flash at 2–5 temperature settings with 3 replications per condition.
 152 The top three prompts—all directing the model to analyze structural item fea-
 153 tures before estimating difficulty—achieved $\rho = 0.65\text{--}0.69$ (Table 4, Figure 1a):
 154 **prerequisite_chain** ($\rho = 0.686$) enumerates knowledge prerequisites before
 155 estimating; **cognitive_load** ($\rho = 0.673$) counts interacting memory elements;
 156 and **buggy_rules** ($\rho = 0.655$) identifies procedural error paths. For context,
 157 meta-analyses report that experienced teachers can predict individual student
 158 performance with $r = 0.63\text{--}0.66$ [11,19]. The constructs differ substantially—
 159 teachers judge individual students while we predict aggregate item difficulty—so
 160 direct comparison is inappropriate, but the magnitude suggests LLM estimates
 161 capture meaningful difficulty information.

162 5.2 The Mechanism: Item Analysis, Not Population Modeling

163 Grouping prompts by their 2×2 factor membership (Table 3) reveals a clear pat-
 164 tern (Table ??): item analysis is the primary driver. Prompts that model student
 165 populations without analyzing item structure perform *worse* than baseline.

166 Grouping by 2×2 factor membership: item analysis only achieves mean $\rho =$
 167 0.61 (4 prompts), item + population $\rho = 0.59$ (5 prompts), neither (baseline)
 168 $\rho = 0.52$ (3 prompts), and population only $\rho = 0.47$ (4 prompts). This parallels
 169 Embretson’s [7] cognitive design system, where item difficulty is predicted from



(a) Prompt screening. Color = factor membership (green = item only, blue = item + pop, red = pop only, grey = neither). Dashed = teacher baseline. (b) Temperature effects. Most prompts show minimal sensitivity ($\Delta\rho < 0.05$).

Fig. 1: (a) Prompt screening results on SmartPaper ($n = 140$). (b) Temperature sensitivity for selected prompts.

counts of processing steps and working memory demands. The LLM operationalizes similar constructs when directed to enumerate prerequisites or interacting elements.

Population modeling alone is unreliable. Explicit student simulation (synthetic_students: $\rho = 0.19$) performs worst, consistent with Li, Chen et al.'s [13] finding that proficiency simulation does not reliably improve difficulty estimation.

5.3 What Doesn't Matter

Three factors had minimal effects (each unique $\eta^2 < 0.05$):

Temperature. Most prompts show $\Delta\rho < 0.05$ across temperatures 0.5–2.0 (Figure 1b). The exception: prerequisite_chain peaks at $t = 0.5$ while cognitive_load peaks at $t = 2.0$.

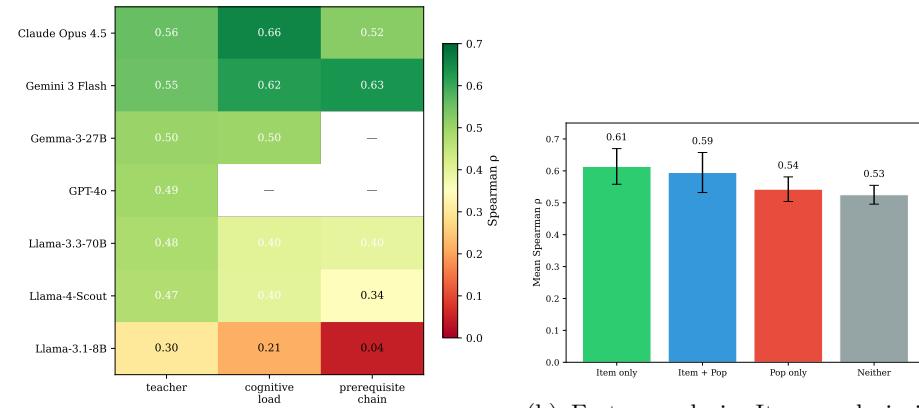
Model size. GPT-4o ($\rho = 0.49$) underperforms Gemini 3 Flash ($\rho = 0.55$) and matches Gemma-3-27B. Llama-3.1-8B struggles ($\rho = 0.30$), but scaling alone does not predict success (Table 5).

Deliberation. Undirected chain-of-thought reasoning degrades performance. The structured prompts that work use *directed* analysis—they specify exactly what to enumerate (prerequisites, interacting elements, error paths). Undirected “think step by step” produces unfocused reasoning that drifts toward solving the item.

Surface features. Text length correlates $\rho = -0.44$ with difficulty on SmartPaper (shorter questions are harder). Controlling for text length, partial $\rho = 0.59$ –0.66 for item analysis prompts—the correlation barely changes ($\Delta\rho < 0.04$), confirming that LLM predictions are not merely proxies for question length.

Table 5: Model survey (ρ , SmartPaper, $t = 1.0$). “—” indicates condition not run or <50 valid responses.

Model	Params	teacher	cog_load	prereq
Gemini 3 Flash	—	0.55	0.62	0.63
Gemma-3-27B	27B	0.50	0.50	—
GPT-4o	—	0.49	—	—
Llama-3.3-70B	70B	0.48	0.40	0.40
Llama-4-Scout	17B/109B	0.47	0.40	0.35
Llama-3.1-8B	8B	0.30	0.21	0.04



(a) Model survey. Frontier models achieve $\rho > 0.50$; Llama-8B fails on structured prompts.

(b) Factor analysis. Item analysis is the primary driver; population modeling alone underperforms baseline.

Fig. 2: (a) Model \times prompt heatmap on SmartPaper. (b) Mean ρ by 2×2 factor membership with 95% CIs.

193 One interaction matters: item analysis prompts help capable models but hurt
 194 weak ones. On Gemini, prerequisite_chain gains +0.08 over teacher; on Llama-
 195 8B, it loses -0.26.

196 5.4 Generalization Across Datasets

197 We validated on two additional datasets: DBE-KT22 (168 undergraduate CS
 198 MCQs) and the BEA 2024 shared task (595 USMLE medical MCQs with IRT
 199 difficulty). Table 6 shows results.

200 The signal transfers: all prompts achieve significant correlations on all three
 201 datasets. However, the item analysis advantage attenuates on MCQs. On Smart-
 202 Paper, prerequisite_chain beats teacher by +0.13; on DBE-KT22, buggy_rules
 203 achieves the highest $\rho = 0.58$ but the gap over teacher is only +0.06; on BEA,
 204 all three prompts are equivalent ($\rho \approx 0.45$).

Table 6: Cross-dataset generalization (Gemini 3 Flash, best temperature per dataset).

Dataset	<i>n</i>	teacher	prereq	buggy	Best	95% CI
SmartPaper (open-ended)	140	0.56	0.69	0.66	[.58,.78]	
DBE-KT22 (CS MCQ)	168	0.52	0.53	0.58	[.46,.68]	
BEA 2024 (USMLE MCQ)	595	0.45	0.44	0.45	[.39,.52]	

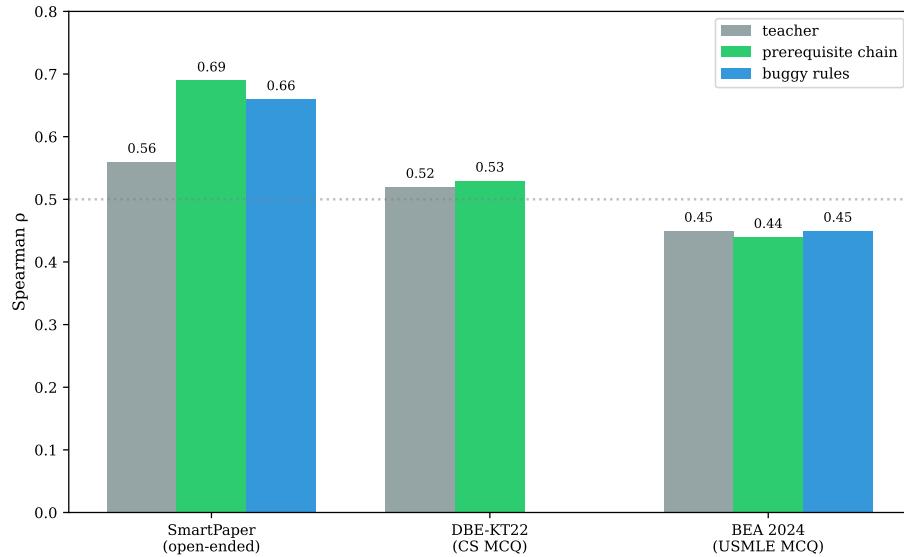


Fig. 3: Cross-dataset generalization. The item-analysis advantage (prerequisite_chain, green) is strongest on open-ended items and attenuates on MCQs, where simple teacher judgment (grey) nearly matches structured prompts.

205 This suggests a **structural predictability hypothesis**: LLMs estimate dif-
 206 ficulty well when it varies across knowledge domains (open-ended items span-
 207 ning topics), but the advantage of counting prompts diminishes when difficulty is
 208 driven by distractor design within a domain. Simple teacher judgment is equally
 209 effective for MCQs.

210 5.5 Practical Implications

211 At approximately \$0.05 per item (3 replications × Gemini 3 Flash pricing), LLM
 212 difficulty estimation is orders of magnitude cheaper than field testing. Rankings
 213 transfer across datasets; absolute calibration does not—models overestimate stu-
 214 dent ability on SmartPaper (MAE≈0.15–0.20) but the rank-order is preserved.

215 For practitioners: use a capable model (Gemini, GPT-4o), prompt it to analyze
 216 structural item features, and average 3+ replications. For standard MCQs,
 217 simple teacher judgment suffices.

218 6 Discussion

219 *Directed vs. Undirected Analysis.* The item analysis prompts that work use *di-
 220 rected* analysis—they specify exactly what to enumerate. This contrasts with
221 undirected chain-of-thought (“think step by step”), which produces unfocused
222 reasoning that drifts toward solving the item rather than analyzing its struc-
223 tural difficulty. Directed analysis channels implicit pedagogical content knowl-
224 edge productively; undirected deliberation disrupts it.

225 *Structural Predictability.* Our three-dataset comparison suggests a structural
 226 predictability pattern: LLMs estimate difficulty well when it varies across knowl-
 227 edge domains (SmartPaper: $\rho = 0.69$), but the item-analysis advantage dimin-
 228 ishes on MCQs where difficulty may be driven by distractor design (DBE-KT22:
 229 $\rho = 0.52\text{--}0.58$; BEA: $\rho = 0.45$, all prompts equivalent).

230 We conjecture that items whose difficulty is driven by structural features
 231 (prerequisite count, cognitive load, error paths) are predictable by LLMs, while
 232 items whose difficulty is driven by familiarity, exposure, or subtle distractor plau-
 233 sibility are not—because this information is absent from the item text. Testing
 234 this hypothesis would require datasets with item-level annotations of difficulty
 235 sources.

236 *Methodological Recommendations.* Our design-space exploration surfaced three
 237 lessons. (1) *Beware Simpson’s paradox in unbalanced designs.* We initially swept
 238 temperature only for promising prompts; a marginal ANOVA showed tempera-
 239 ture as dominant ($\eta^2 = 0.74$), but this was an artifact—low temperatures were
 240 confounded with high-performing prompts. When restricted to balanced con-
 241 ditions, temperature explained < 1% of variance. (2) *Use two-stage sequential
 242 DOE.* Screen all prompts cheaply (1 rep, single temp) to eliminate the bottom
 243 half, then run a balanced factorial on survivors. (3) *Validate on ≥ 100 items.* Our
 244 20-item probe yielded $\rho = 0.46$; the full 140-item set achieved $\rho = 0.55$. Boot-
 245 strap analysis showed only 2.5% of 20-item subsets would produce $\rho \geq 0.50$.
 246 Many published results use <50 items—treat such samples as exploratory only.

247 *Limitations.* Three limitations warrant mention. First, all 15 prompts were
 248 screened on a single model (Gemini 3 Flash); the model survey shows effects gen-
 249 eralize but with diminished magnitude. Second, calibration does not transfer—
 250 models overestimate ability on SmartPaper but rankings are preserved, so population-
 251 specific adjustment would be needed for absolute predictions. Third, we do not
 252 compare to fine-tuned models; fine-tuned BERT/RoBERTa can outperform zero-
 253 shot LLMs when training data is available [14], but our approach targets the
 254 zero-shot case where items arrive without calibration data.

255 **7 Conclusion**

256 We mapped the design space for LLM item difficulty estimation across 15 prompts,
 257 6 models, and 3 datasets (~250 conditions, ~\$80 in API calls). Item analysis
 258 prompts that enumerate structural features (prerequisites, cognitive load, error
 259 paths) achieve $\rho = 0.65\text{--}0.69$ on open-ended items, but this advantage attenuates
 260 on MCQs ($\rho \approx 0.45\text{--}0.58$), where simple teacher judgment nearly matches.
 261 Prompt design is the primary lever; model size, temperature, and deliberation
 262 each contribute $\leq 0.05 \rho$. Rankings transfer across datasets but calibration does
 263 not—at ~\$0.05 per item, LLM estimates can triage items into difficulty bands,
 264 but absolute predictions require population-specific adjustment. Methodologically,
 265 correlations from <50 items are unreliable, and unbalanced hyperparameter
 266 sweeps produce Simpson’s paradox artifacts; we recommend two-stage se-
 267 quential DOE.

268 *Ethics Statement.* This study uses anonymized, aggregated student response
 269 data. SmartPaper data consists of item-level statistics without individual student
 270 identifiers. DBE-KT22 and BEA 2024 are publicly available research datasets.
 271 No personally identifiable information was accessed or processed.

272 *Data and Code Availability.* Prompts and analysis code are available in the
 273 project repository. SmartPaper data are available upon request from the orig-
 274 inating organization. DBE-KT22 is publicly available [6]. BEA 2024 data are
 275 available through the shared task organizers.

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