

# EE313 Lecture 19

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## 1 Test review

- Properties of Fourier transform
- (see O&W ex 3.9)
- 'Detective story'
- crib sheet
- DFT (O&W 3.4)

## 2 DFT

DTFS, period  $N$ .

definitions:

$$x[n] = \sum a_k \cdot e^{j2\frac{\pi}{N}kn}$$

$$k \in \{0, 1, \dots, N-1\}$$

$$a_N = \frac{1}{N} \sum x[n] \cdot e^{-j2\frac{\pi}{N}kn}$$

$$n \in \{0, 1, \dots, N-1\}$$

Example:

$$x[n] = \sin\left(\frac{2\pi}{5}n\right) = \frac{1}{2j}e^{j(\frac{2\pi}{5})n} - \frac{1}{2j}e^{-j(\frac{2\pi}{5})n}$$

$$\therefore a_1 = \frac{1}{2j}, a_{-1} = -\frac{1}{2j}$$

$$a_{-1} = a_4,$$

$$a_1 = a_5$$

Plot the graph.

## 3 DE's and the transfer function

$$RC = \frac{dx}{dt} + V_c(t) = V_s(t)$$

constant coefficient linear DE  $\rightarrow$  LTI and causal.

Assuming initial rest,

$$V_s(t) = e^H \xrightarrow{LTI} H j\omega e^{st}.$$

Laplace of Impulse

To find transfer function:

$$RC \cdot \frac{dv_c(t)}{dt} + v_c(t) = v_s(t)$$

maek transfer function

...

$$H(s) = \frac{1}{1+RCs}$$

Also maek freq resp:

...

$$H(jw) = \frac{1}{1+RCjw}$$

Maek plot.

Watch filter. (see O&W 3.10.2 High pass ex)

## 4 Recapitulation

- Properties of Systems (memoryless, LTI, etc.)
- Discrete and Continuous convolutions
- DFT, CFT, properties of Fourier transforms, computing basic signals (square pulse, sinusoids)
- Solving DE's to get transfer function and frequency response  
Also be able to plot the magnitude and angle of the freq. response.
- No inverse Fourier transform. Read examples.