

# PHYS 250 Homework 10

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## Problem 1

```
def linear_leastqs(x, y, sigma = None):
    """ Returns a1, a2, should include sigma_a1, sigma_a2 """

    if sigma is None:
        sigma = np.ones_like(y)
    else:
        sigma = y.copy().fill(sigma)

    N      = length(x)

    Sx      = sum(x)
    Sy      = sum(y)
    Sxy     = sum(x*y)
    Sxx     = sum(x**2)
    Delta = N * Sxx - Sx**2
    a1      = (Sxx * Sy - Sx * Sxy) / Delta
    a2      = (N * Sxy - Sx * Sy) / Delta

    return [a1, a2]
```

## Problem 2

Our previous function can return the  $a_1$  and  $a_2$  values for line fit.

We define a function to calculate chi-squared,

```
def chisq(model, x, y, sigma = None):
    if sigma == None:
```

```

        sigma = np.ones_like(y)
    else:
        sigma = y.copy().fill(sigma)

    return sum(((y - model(x , *params) / sigma )**2)

```

We calculate the degrees of freedom (DoF) as the difference between the number of parameters and number of data points, then divide the chi-squared by the DoF to determine the reduced chi-squared. So the output of the attached code for problem 2 (i) is:

```

Parameter a1 is -4
Parameter a2 is 0
Chi-squared: 15
Reduced Chi-squared: 5

```

\* Obviously wrong because the y-intercept is -3....

We would want to remove the outlier (-1,-7) and relaunch the same code to solve for (iii). (Once we found out bug.)

## Problem 3

Each bin has a width of  $\frac{8}{51} = 0.15686$ . We'll shift the bins to the right by half of this width to center them (moving all of the x values to the right by about 0.8).

See attached code for problem outline.