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A.I. MP3 Report

Problem 1

IMPLEMENTATION

In this problem we first read in all of the training data in order to build our P(Fiil class). Once we were able to build this probability for every pixel in every numeric character, we were able to calculate our P(class) based on the frequency of occurrence of each character. Once all of this was stored in a database we were able to calculate $P(class) \cdot P(f_{1,1} \mid class) \cdot P(f_{1,2} \mid class) \cdot ... \cdot$ $P(f_{28,28} \mid class)$ with the logarithmic adjustment for each image in the test data for each class. The class that returned the highest value would be our estimate. We then saved the most and least prototypical instances of each class by selecting the highest and lowest $P(class) \cdot P(f_{1,1} \mid class)$. $P(f_{1,2} \mid class) \cdot ... \cdot P(f_{28,28} \mid class)$ values. After this we were able to calculate the percentage of the test images that were classified properly along with the confusion matrix. We were able to achieve 77.1% correct classification of the images so we are confident in our design. An interesting fact about our approach is that it is very dynamic and flexible. You can make this program run on images with any dimensions you want, with as many characters as you want, and with as many training/test cases as you want and it will calculate all the same output data. This is because we defined everything in terms of constants located at the beginning of the DigitClassification.h file so to change any of the attributes mentioned above you simply need to change the corresponding constant to the appropriate value. This made doing the facial classification much simpler as we only had to edit the constant values.

Smoothing Value = 1

Char	acter	Correct			Attempts			Percentage		
0 76 1 104 2 80 3 79 4 83 5 62 6 69 7 77 8 61 9 80			90 108 103 100 107 92 91 106 103 100			84.4444% 96.2963% 77.6699% 79% 67.3913% 75.8242% 72.6415% 59.2233% 80%				
Tota	l	771			1000			77.1%		
Conf	usion Matr 0	ix: 1	2	3	4	5	6	7	8	9
0	84.444	0.000	1.111	0.000	1.111	5.556	3.333	0.000	4.444	0.000
1	0.000	96.296	0.926	0.000	0.000	1.852	0.926	0.000	0.000	0.000
2	0.971	2.913	77.670	3.883	0.971	0.000	5.825	0.971	4.854	1.942
3	0.000	2.000	0.000	79.000	0.000	3.000	2.000	6.000	2.000	6.000
4	0.000	0.935	0.000	0.000	77.570	0.000	2.804	0.935	1.869	15.888
5	2.174	2.174	1.087	13.043	3.261	67.391	1.087	1.087	2.174	6.522
6	1.099	5.495	4.396	0.000	4.396	6.593	75.824	0.000	2.198	0.000
7	0.000	5.660	2.830	0.000	2.830	0.000	0.000	72.642	2.830	13.208
8	0.971	0.971	2.913	13.592	1.942	7.767	0.000	0.971	59.223	11.650
9	1.000	1.000	1.000	3.000	9.000	2.000	0.000	2.000	1.000	80.000

For Character '0' this is the most prototypical image:

+#++ +####+ +######+ +#######++ +#####+ +##+ +###+++ +##+ ####+ +##+ +###+ ##+ ####+ ##+ ###+ +## ###+ ##+ ###+ ##+ ###+ +##+ ###+ +##+ ####+ +###+ +###++ +####+ #####++####+ +#######++ +######+ +++++

For Character '0' this is the least prototypical image:

```
+++++#++
  +#######++
 +#############
+#########+++++++++
#######++ ++###+
######+
            ####
 +###+
           +###+
            +###+
 +###
             ###+
 ####
 ####
              ####
 ###+
             ####
 ####
              ####
 ####+
              ####
 +####+
              ####
  +####
              ####
   +###++
              ####
    +####++++####
     +########+++
      +#######++
       +++#######
```

For Character '1' this is the most prototypical image:

```
+#+
    +##+
    +##+
    ###+
    ###+
    ###
   +##+
   +##+
   +##+
   ###+
  ###
  +##+
  +##+
  ###+
 +###
 +##+
+###+
+####
+###+
 +#+
```

For Character '1' this is the least prototypical image:

```
+#
      ##+
     +#++
     ++#+
    +#+#+
   +#+++
   ##+#+
  +#++#+
 +#+ ++
+#+ +#+
+#+ ++
+##+######+++
 ++##++++++++
  #+
  +#+
  +#
  +#
  #+
  #+
  #+
```

For Character '2' this is the most prototypical image:

```
+++++
 #####++
+######+
+#++ +###+
 ++
       +##+
        +##
        +##
         +#
         +#
         +#
        +#+
        +#+
  +++++ ##+
+#####+##
+#######+
+##++++####+
##+ +###+##++
##++###+ +##+
+#####++
+##++
```

For Character '2' this is the least prototypical image:

```
+++#+
 +####+
 +##+++
##+
+##
+#+
+#+
##+
+#+
+#+
##
##+
           +++
          +####+
+##
         +###++##+
 +#+
  ##+
         ###
              +##
  +##+ +##+
               +#+
   ++##+ ##+
               +#+
     ++####+ +##
       +#########
          ++++++
```

For Character '3' this is the most prototypical image:

```
+####++
   +######+
      +++###+
          ++##
          +##+
          +##+
        ++##+
       +###+
      +###+
     +####+
     ###+###+
     ++ +##+
          +#+
          +##
          +##
         +##+
        ++##+
+++++++###+
+#######++
+++#####++
```

For Character '3' this is the least prototypical image:

```
++++++++#+
++############
+########+++
+##++++++++
##+
+#+
+##+
+##+++++++++
+#########++++++
+########+#++
 ++++++ +++ +##+
             +##+
             +##+
             +##+
             +##+
 ++
 #+
             +##
##+
            +##+
 +##+++++++##+
  +########++
   ++######+
```

For Character '4' this is the most prototypical image:

```
+#
    +#+
             +#
    ##+
             +#
           +++#
   +##+
  +###
           +##+
  +##+
           +##+
  ###
           +##+
  ##+
          +###+
        ++####+
  #+
++###+#####
+++######++
    +++++##+
        +#+
        +#+
        ##+
       +##+
       +#+
       +#+
       +#+
       +#+
```

For Character '4' this is the least prototypical image:

```
+##++++
      ++#######+
    ++########+
 ++#########+#####
+######++++++++
+####+
               +#+
####+
               ##+
###+
             ++##+
###+
           +++###+
#####++++########+
+###################
+########++ +###
  +++++++
               +###
              +###
               +##+
               +##+
               +###
               +##+
               +##+
               +##+
```

For Character '5' this is the most prototypical image:

```
++#+
     +++++####+
    #######+
    ###++++
    +#++
    +#+
   +##
   +#++++
  +#####+
  +##+++##
       +#+
       +#+
        +#+
        ##
+#+
        ##+
        +##
+#+
##+
       ###
+##+
       +##+
##+++##+
    ###++
```

For Character '5' this is the least prototypical image:

```
++############
 ++++###########+
 +##+#####++++++
+####++
+###++
+###+++++
#######++
 +++########+++
   +++++######++
       +++#####+
           ++####
##+
             ###+
###+
             +###+
+###++
           +####+
 +###++ +++###+
 ++##########+
   ++#######+++
     +++###+++
```

For Character '6' this is the most prototypical image:

```
+#+
     +###+
    +###+
   +###+
   +###+
  +###+
 +###+
 +##+
 +##+
+###+
+##+
+##+
      ++##+
+###+ +###+
+###++#####+
+##+ +#####+
+###+#####+
+#######+
+######+
 +####+
   +##+
```

For Character '6' this is the least prototypical image:

```
#+
+##+
+##+
+##+
+##+
+###
+###
+###
+###
+##+
+##+
       +######+
      +####+##++
+#+
+##
      +##++ +##+
+##+ +###+ +##+
 ##+ +##+
             +##+
 +###++##+
           +###+
   ######+ ++##+
   ++#####+##+
      ++#####++
         +++++
```

For Character '7' this is the most prototypical image:

```
+#++ +++++
########++
++###++++#+
 +++
        +#+
       +##+
       +##+
      +##+
      +##+
      +##+
      +##+
      +##+
     ##+
    +##+
    ##+
   +##+
   +#+
  +##
   +##
   +##
   +++
```

For Character '7' this is the least prototypical image:

```
####++##+
########++
########++
+########++++
+++#######+
   +++++####++
        ++####+
         ++#####
          ++####
           ++###+
            +####+
            +#####
            +#####
            +####+
            +####+
            +###+
             +###
             +###+
             +####
             +#####
```

For Character '8' this is the most prototypical image:

```
+##+
     ++####+
   ++#####+
  +####++##+
 ++###+ +##+
 +##+ +##+
 ###
        +#++
 ###
       ++###
 +##++++##++
 +######++
  ####++
 +#####
+#####+
###++##+
+##+ ###+
+##+ ###+
+##+ +###
+######+
+#####+
 ++##++
```

For Character '8' this is the least prototypical image:

```
+++####+
  +###+++##++++
 +####++
         ++###+
+###+
           ###+
+##
            ###
+##
            ###
+###
      +++++###+
 +###+++#######+
 +#####+++++++
  +####
 +####+
 +#+++##++
 ##+ +###+
 ##+ +##+
+#++ +##+
  ###++ ++##+
  +###+ +##+
    +####+++###+
      ++######+
        +++###++
```

For Character '9' this is the most prototypical image:

```
++##++
   +#####+
 +####++++#+
 +###+
       ++##
+##+
       +####
+##+
       +####
+##+
       +###+
+##+ ++###
+#######+
 +######+
  +++++##+
     +##+
     +##+
     +#+
    +##+
    +##+
    +##
    +#+
    +#+
    +#+
```

For Character '9' this is the least prototypical image:

```
++++####++
 ++########+++
+###+++++++###+
      +###+
##+
+##+
          +####
       +####+
+###++
+####++++##++++
 ++#######+
    ++#####++
     +######+
     +#+ +###+
     ##+
          +###+
     +##+
          +###+
      ##+
            ##+
             ###+
      +##
      +##+
            +##
      +##+
            +#+
      +###+++##+
       +######+
         +##+++
```

This is the odds ratio for 0/5:

```
++++++++
   --++++++++
  ----+++++++++
 + --- ++++++++
 +--- +++++++++
 - +++++++++++
 -+++++++ +++++++----
-+++++++ - +++++++--
 -+++++ ---- ++++++-
 +++++
+ ++++++-----++++++++
 ++++++
-++++++
-++++++
-++++++-----+++++++
- +++++++ ---+++++++
--+++++++
__+++++++++++++++++++++
 ++++++++++++++++++
++++++++
 _____
```

This is the odds ratio for 5/3:
++++++++++++++++++++++++++++++++++++++
+++++++++++++++++++++++++++++++++++++++
+++++++++++++++++++++++++++++++++++++++
+++++
++++++++++
+++ +++++++
+++ +++++++
+-+ +++++++
+++ +++++ ++++++
++++++++
++ +++++++++++
+++-++++++++++++
+++++++++++++++
+++-++++++ +++++
+++++++++++ +++++
++++++++++++++-+
++++++++++++
++ ++++++++++++
++ ++++++++++++
++ +++++++++++
++ ++++++++++
++
++ +++++
++ ++++++
+++ ++++++++
+++ +++ ++++++++
++++++++++++
+++++++++++++++++++++++++++++++++++++++

This is the odds ratio for 8/3 :

```
----++++
 ----- ++++++++
---- ++++++
-- +++++++++++
 -++++++++
 +++++++ --- +++++++++
 -++++ -
      +++++
 -+++--- +++++----+++
 --- -- ++++++---- + -
----+
----+
----+
-----
----+
------ ---++
----- ++ ++++
 ----- ++++++++++ -
 -----+++++ --
    ----- ++
```

This is the odds ratio for 8/9 :

++++++++
+ +++++++++++++++
+++++++++++++++++++
+ +++++++++++++++++++
+++++++ ++++++++
+++++ +++++++
+ + ++++++
+++ - ++++++
++++ ++++++
+++++ ++++++
++++
++++ ++ -
++-
++++ ++++
++++++ +++++
++++++++ +++++
-++++++++++++++
-+++++++ ++++++
+++++++++++++++++
+++++++++++++++++++++++++++++++++++++++
-+++++++++++
-++++++++

Problem 2

IMPLEMENTATION

This part of the MP was done in Python.

In order to implement problem 2.1, we first had make sure we had all of our word likelihoods saved somewhere. In order to do this, we saved the likelihoods of each word from the training data into a dictionary based on whichever label it had. Then we went through each document of the test data and classified it into one label. We had to go through each line and find the sum of the likelihood that the document would fit a certain label. For multinomial naive Bayes we calculated the sum of every word's likelihood and frequency for each label. The email was then classified as whichever likelihood was greater, and the confusion matrix was updated. To implement the Bernoulli Naive Bayes problem, we commented out the line where the likelihood accounted for the word frequency. The classification rate for both models and both datasheets were the same (email - 97%, movie - 75%). To have our code work for the movie datasheet, we just had to change the way we searched for labels by changing a number in our conditional statement (labels were -1 and 1 instead of 0 and 1). To find the classification rates we divided the number of documents we labeled correctly by the total number of documents.

CONFUSION MATRIX

Bernoulli:

	Not Spam	Spam
Not Spam	126	4
Spam	2	128

Classification Rate: 97.6%

	Good Review	Bad Review
Good Review	382	118
Bad Review	126	374

Classification Rate: 75.6%

Multinomial:

	Not Spam	Spam
Not Spam	126	4
Spam	2	128

Classification Rate: 97.6%

	Good Review	Bad Review
Good Review	383	117
Bad Review	124	376

Classification Rate: 75.9%

The top 20 for words for the emails are listed below. They are in the format word_(# of occurrences)

TOP 20 WORDS FOR EMAILS

TOP SPAM WORDS

email_1380

s_1207

order 1159

report_1053

our 965

address 954

mail_923

program 828

send_800

free_744

money 722

list 713

receive 662

name_627

business 608

one 553

d 541

work 528

com_524

TOP NORMAL WORDS

language_1130

university_906

s 661

linguistic_477

de 445

information_444

conference 378

workshop_360

email 321

paper_320

e_314

```
english_312
one_280
please_278
include_277
edu_271
http_264
research_259
abstract_253
```

TOP 20 WORDS FOR MOVIES

The top 20 for words for the movies are listed below. They are in the format word_(# of occurrences)

TOP NEGATIVE REVIEW WORDS

```
movie 290
film_227
like 163
one_143
-- 114
bad 87
story_85
much 83
time 75
even 70
characters 64
good_64
little 62
would 58
comedy 57
never_53
nothing 52
makes 51
plot 51
TOP POSITIVE REVIEW WORDS
film 285
movie_187
--_136
one_111
like 99
story_94
good 84
comedy 83
way_80
even 76
time 73
```

best_72

much_66 performances_62 funny_60 make_60 life_58 us_58 makes_58

EXTRA CREDIT

Problem 1 extra credit: Facial Recognition:

*see description of problem 1 for details as it has the same implementation.

Smoothing Value = 10

Character	Correct	Attempts	Percentage	
0 1	54 72	77 73	70.1299% 98.6301%	
Total	126	150	84%	

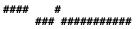
Confusion Matrix:

0 1

0 70.130 29.870

1 1.370 98.630

For Character '0' this is the most prototypical image:



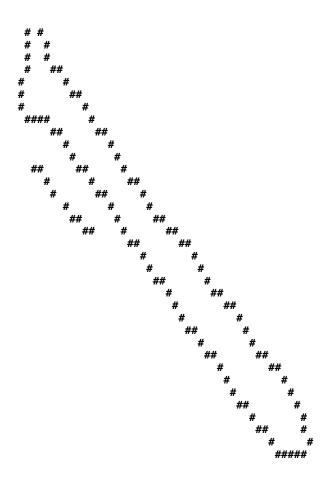


#

For Character '0' this is the least prototypical image:

#######

For Character '1' this is the most prototypical image:



For Character '1' this is the least prototypical image:

		###	#		####	ŧ		###
Ħ	<i>!#######################</i>	##				####	####	##
#		#						#
#		#						#
#		#						#
#	##	#	ш	#	#	####		#
#	== ==	* #	#				#	#
#		* # # #				#		#
#		"				# #		#
#	#	# #		· #			#	#
#	#	##	#		#		#	#
#	# #	#	#			#	#	#
#	## ##	#	#		#	# #	‡	#
#	# #	##	#	###	#	#	#	#
#	# ####					#	#	#
#	#					#		#
#	#					#	#	#
#	#					#		#
#	.# 				-	####		#
#	#				##		#	#
#	# #						#	#
#	#				#			#
#	#			##:	####		<i>+</i> #	#
#	#			#		#		#
#	#			#	#	#"#		#
#		##			#	##		#
#		###			#	# #		#
#	####		#	#	#	# #	##	#
#	####		#	#	#	#		#
#	###		#	#	#	# #	‡	#
#	#		#			# #	‡	#
#	# #####		#	#		###	-	#
#			#					#
#	# #	#			#			### #
#	# #		#				##	••
#	# # ####### # #					####		#
#	# # !#### #	#####	##		###	•	#	#### #
#	*******						#	· #
							π	
							#	
#	####						# #	#
							# # #	
#	#### # #				####	! ##	#	#
#	### # # # ### ##	####	####	###			#	# # #
# # #	### # # # ### ## # # # #	#####	*####	###		###	# # # # #	# # #
######################################	### # # # ### ## # # # # # # # #	#####	####	:###:		###	# # # # # #	# # # # # #
######################################	### # # # ### ## # # # # # # # # # # # #				#	###	# # # # # #	######################################
######################################	#### # # ### ## ### ## # # # # # # # # # # # #					###	######################################	#######################################
#########	#### # # ### ## ### ## # # # # # # # # # # # #				#	###	##########	#######################################
.##########	### # # ### ## ### ## # # # # # # # # # # # # # # # #	####			#	###	######################################	##############
.###########	#### # # ### ## #	#### ###			#	###	# # # # # # # # # # #	#######################################
.############	#### # # # # # # # # # # # # # # # # #	#### ### #			#	###	##############	*####################
#############	#### # # # # # # # # # # # ###	#### ### #	####		#	###	###############	.################
###############	#### ### # # # ###	#### ### #	:#### :#	###	#	##; # # !###	################	.################
#################	#### ### # # # ###	#### ### #	####	:###:	#####	##; # # ###	################	.#################
###############	#### ### # # # ###	#### ### #	:#### :#	:###:	#	##; # # ###	################	.################
##################	#### ### # # ######	#### ### #	:#### :#	:###:	#####	### ### #### ####	###############	.################
##################	#### ### # # ######	#### ### #	:#### :#	:###:	#####	### ### #### #########################	################	.###################
################	#### ### # # # ### # # # # # # # # #	#### ### #	:#### :#	:###:	#####	### ### #### #########################	#################	.###################
################	#### ### # # # # # # # # # # # # # # #	#### ### #	:#### :#	:###:	#####	### ### #### #########################	#################	.######################################
#######################################	#### #	#### ### #	*#### *# ####	###: ## ##:	# ##### #####	##; ### ### ### ###	***************************************	.#####################################
.#####################################	#### #	#### ### # #	*#### *# ####	###: ## ##:	# ##### #####	##; ### ### ### ###	######################################	######################################
.#####################################	#### #	#### ### # #	*#### *# ####	###: ## ##:	# ##### #####	##; ### ### ### ###	######################################	######################################

Problem 2 extra credit:

We have implemented problem 2.2. The only thing different about this problem was that there were many more labels. We added more dictionaries to store word frequencies and likelihoods for words in each label, but the way we updated the confusion matrixes and found the classification rates were the same.

Bernoulli Confusion Matrix

			1				1	
	sci.spa ce	comp.s ys.ibm .pc.har dware	rec.spo rt.base ball	comp. windo ws.x	talk.po litics.m isc	misc.fo rsale	rec.spo rt.hock ey	comp. graphi cs
sci.spa ce	33	0	0	0	1	0	0	0
comp.s ys.ibm .pc.har dware	0	28	0	4	1	0	0	0
rec.spo rt.base ball	0	0	35	0	0	0	0	1
comp. windo ws.x	0	0	0	25	1	0	0	2
talk.po litics.m isc	1	0	0	0	46	0	0	0
misc.fo rsale	0	4	0	0	1	4	0	1
rec.spo rt.hock ey	0	0	0	0	0	0	46	0
comp. graphi cs	1	1	0	2	0	0	0	25

Classification Rate: 92.015%

Multinomial Confusion Matrix

	sci.spa ce	comp.s ys.ibm .pc.har dware	rec.spo rt.base ball	comp. windo ws.x	talk.po litics.m isc	misc.fo rsale	rec.spo rt.hock ey	comp. graphi cs
sci.spa ce	32	0	0	0	2	0	0	0
comp.s ys.ibm .pc.har dware	0	27	0	4	2	0	0	0
rec.spo rt.base ball	0	0	35	0	0	0	1	0
comp. windo ws.x	0	0	0	24	1	0	0	3
talk.po litics.m isc	1	0	1	0	45	0	0	0
misc.fo rsale	1	2	0	0	1	4	0	2
rec.spo rt.hock ey	0	0	0	0	0	0	46	0
comp. graphi cs	1	1	0	1	1	0	0	25

Classification Rate: 90.49%

The top 20 for words for the newsgroups are listed below. They are in the format word_(# of occurrences)

TOP 20 WORDS FOR EACH CATEGORY (2.2)

TOP sci_space WORDS space_1030 nt_593

```
would 560
one 384
launch 352
nasa 345
earth_332
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Contributions

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