

Group 2/

1) Averages

2) Problem on Ages

[1] Averages

Average \rightarrow equitable distribution = $\frac{\text{Sum of all}}{\text{Total of all}}$
(E.D)

\Downarrow

$$\text{Total Sum} = \text{Average} \times \text{Total}$$

Questions

- 1) Knowing that Vijay's expense for 1st 3 days is Rs. 100, 125 and Rs. 85, what is his 4th day expense as his 4 days average expense is ₹ 90?

Soln: $Av = \frac{S}{T} \rightarrow 90 = \frac{100 + 125 + 85 + x}{4}$

$$90 = \frac{310 + x}{4} \Rightarrow x = 360 - 310$$

$$\boxed{x = 50 \text{ Rs}}$$

- 2) What will be avg price of all goods bought, if Ajay buys 30 erasers for ₹ 3 each, 35 chocolates for Rs. 10 each, 25 clips at rate Rs. 4 each?

Soln $Av = \frac{S}{T}$ | Sum of all prices = $3 \times 30 + 10 \times 35 + 25 \times 4$

$$= 90 + 350 + 100$$

$$\text{Total items} = 30 + 35 + 25$$

$$\boxed{S = 540}$$

$$\boxed{T = 90}$$

$$A = \frac{S}{T} \Rightarrow \frac{540}{90}$$

$$\boxed{A = 6}$$

// \rightarrow avg. of all goods

3) Out of 20 cycles sold by ajay, avg cost of 12 cycles is ₹ 18000. In total he earned ₹ 300000. What was avg cost of remaining cycles?

Soln ∴ Out of 20 cycles → 12 cycle sold for one avg
8 cycle sold for another avg

given 12 cycles → avg cost = 18000

$$\text{Sum} = \text{avg} \times \text{no of total}$$

$$= 18000 \times 12$$

$$\text{price of Total sum} = 216000$$

$$\text{So price of 12 cycles} \Rightarrow 216000$$

Also from question

$$\text{total price of 20 cycles} = 300000$$

$$\begin{aligned} \text{So remaining 8 cycle cost} &= 300000 - 216000 \\ &= 84000 \end{aligned}$$

$$\text{Total cost of 8 cycles} = 84000$$

$$\text{No of cycles} = 8$$

$$\text{Avg of remaining 8 cycles} = \frac{84000}{8}$$

$$\boxed{₹ = 10500}$$

4) Without considering salary of boss, avg salary

reduces by ₹ 1000. What will be salary of boss if average salary of 11 employees and boss is ₹ 18000?

Soln ∴ Here (2 average)

$$\text{without boss (11)} \rightarrow 18000$$

$$\text{with boss (11+1)} \rightarrow 18000$$

$$\text{without boss (11)} \rightarrow 18000 - 1000 \rightarrow 17000$$

with boss avg :-

$$18000 = \frac{S_1}{11+1 \rightarrow \text{boss employee}}$$

$$S_1 = 18000 \times 12$$

$$S_1 = 216000$$

Total salary include boss

without boss avg :-

$$18000 - 1000 = \frac{S_2}{11}$$

$$17000 \times 11 = S_2$$

$$S_2 = 187000$$

Total salary without boss

$$\text{Boss salary} = 216000 - 187000$$

$$= 29000 //$$

- 5) Avg age of 5 people is 42 years. Another group has 8 people who have avg age of $\frac{81}{n}$ years. When both groups are mixed what is average age of all people?

Soln: what we need avg of all people $\rightarrow \text{Avg} = \frac{S}{T}$ (Total age year)
 $5+8$ (total people)
 so $S \Rightarrow ?$

given

avg of 5 people :-

$$42 = \frac{x}{5}$$

$$x = 210 \text{ years}$$

avg of 8 people:

$$81 = \frac{x}{8}$$

$$x = 648 \text{ years}$$

Total age year of
 $5+8 \Rightarrow 13$ people

is $648 + 210$

$$858 \Rightarrow 858 \text{ years}$$

$$\text{Avg} = \frac{S}{T} \Rightarrow \frac{858}{13}$$

$\Rightarrow 66 \text{ years}$

avg
 Avg of all people = 66 years.

6) 3 boxes have some average weight. When one box which 89kg is replaced by another box, average weight increases by 5kg. How much new box weighs?

Soln: Seems complex but simple sum:-

3 boxes w_1, w_2, w_3 \rightarrow 3 boxes w_1+5, w_2+5, w_3+5 (Normal assumption)
 avg $\rightarrow Z$ avg increases by 5 $\rightarrow Z+5$

total weight increases
 \rightarrow avg $\times 3 \times$ no of it
 $\Rightarrow 5 \times 3 = 15$

In question above change in avg by 5kg done by replacing single 89kg box with new box

so it should be heavier $(5 \times 3 \Rightarrow 15 \text{ kg})$

so new replaced box weight $\Rightarrow 89+15$

$\Rightarrow 104 \text{ kg}$

Note: if in question if avg decreases by 5kg then replaced box must be $89-15 \text{ kgs}$.

7) How old will Raju be if ratio of his age and one of his twin grandsons is 11:2 and average age of his and his both grandsons is 50 years?

Soln: Raju age : grandson age $\rightarrow 11:2$

they are twin grandson so both ages are same

so Raju : 1st grandson : 2nd grandson

$11:2:2$

Now avg of all age $\Rightarrow 50$

$$\text{Avg} = \frac{S}{T} \Rightarrow 50 = \frac{\text{Total ages sum}}{3}$$

Total sum of ages = 150

$$150 = 11k + 2k + 2k$$

$$150 = 15k$$

$$k = 10$$

$$\text{Raju age} \Rightarrow 11k \Rightarrow 11 \times 10$$

$$\boxed{\text{Raju} = 110 \text{ years}}$$

8) Had a player scored 18 runs more in his 3rd innings and 4 runs more in his 7th innings, his average would have become 66 runs. But it is 64 runs. How many innings did he play?

Soln.: $\text{Avg} = \frac{S}{T}$, Let no. of innings be N
avg is 64

1st case	2nd case
For N innings	$N + (18 + 4)$
64 avg	66 avg

increase of 2 runs avg (i.e. 2 run increase in N terms)

$2N$ is also equal to $18 + 4$

$$2N = 22$$

$$\boxed{N = 11}$$

$$\boxed{\text{No. of innings is 11}}$$

9) In a group of people, the eldest and the youngest have an age difference of 100 years. If these two are left out of counting, then avg age of remaining 40 people is 28. The average age of entire group being 30, how old is eldest person?

Soln: Let youngest age = N

eldest age = $N + 100$

Avg of all people $\rightarrow 30 = \frac{S_{all}}{42} \rightarrow 40 + \text{young + old}$

$$S_{all} = 1260 \text{ years}$$

Avg of 40 people $\rightarrow 28 = \frac{S_{40}}{40} \rightarrow$

$$S_{40} = 1120 \text{ years}$$

$$\frac{S_{all} - S_{40}}{1260 - 1120} = (N + N + 100) \rightarrow \text{both age of old, young}$$

$$2N = 140 - 100$$

$$2N = 40$$

$$N = 20 \rightarrow \text{youngest age}$$

$$\text{eldest} = N + 100$$

$$= 120 \text{ age}$$

10) A batsman played 11 innings and has a certain average. This average increases by 2 runs when his 3 innings of 32 runs, 33 runs and 34 runs are replaced by 3 other innings. Find the average of these 3 new innings?

Soln: N of innings $\rightarrow 11$ Total Avg $\Rightarrow x$

1st
11 innings

2nd
3 innings of 11
replaced
(earlier 32, 33, 34)

Avg $\Rightarrow x$

Avg $\Rightarrow x+2$

\rightarrow all 11 innings increased by 2
 $11 \times 2 \rightarrow 22$ total runs increase

Avg of 3 replaced innings run (A) = $\frac{S}{T}$

$A = \frac{32+33+34+22}{3}$

\rightarrow early runs
 \rightarrow new increased total runs

$A = \frac{121}{3}$

$A = 40 \frac{1}{3}$ runs //