

Lecture 8: More performance

Friday, January 25, 2019 10:40 AM

Outline

- More Iron law examples
- Comparing performance of systems
- Intro to pipelining

System A: CPI $\rightarrow 5$ @ 500 MHz } application: 1 million instructions
System B: CPI $\rightarrow 3$ @ 200 MHz

$$\begin{aligned} \text{time}_A &= \frac{\text{sec}}{\text{cycle}} \cdot \frac{\text{cycle}}{\text{inst.}} \cdot \# \text{ inst.} & \text{time}_B &= \frac{1}{200 \cdot 10^6} \cdot 3 \cdot 10^6 \\ &= \frac{1}{500 \cdot 10^6} \cdot 5 \cdot 1 \cdot 10^6 & &= \frac{3}{200} \text{ s} \\ &= 10 \text{ ms} = \frac{1}{100} \text{ s} & &= 15 \text{ ms} \end{aligned}$$

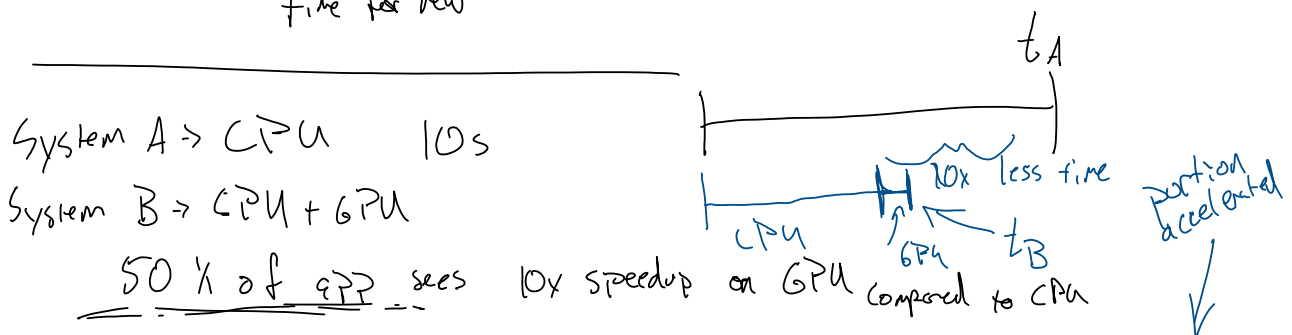
$$t_A < t_B \quad \frac{t_A}{t_B} \rightarrow \text{time for A is } \frac{2}{3} \text{ time for B}$$

$$\frac{t_B}{t_A} \rightarrow 1.5 \times \quad t_A \text{ is 1.5 times faster than } t_B$$

System A System B

or system A provides a 1.5x speedup over system B

$$\text{Speedup} = \frac{\text{time for old}}{\text{time for new}}$$



Speedup of system B over system A?

$$\begin{aligned} \text{Speedup} &= 10 \times ? \\ &= 10 \times ? \end{aligned}$$

$$\frac{t_{\text{old}}}{t_{\text{new}}} = \frac{10 \text{ s}}{5.5 \text{ s}}$$

Speedup = 1.81x

$$\begin{aligned} t_{\text{new}} &= t_{\text{old}} \cdot 0.5 + \frac{0.5 \cdot t_{\text{old}}}{10} \\ &= 10 \cdot 0.5 + \frac{5}{10} \\ &= 5.5 \text{ s} \end{aligned}$$

↑
speedup

Andahl's law

Assume ...

$$\text{Speedup} = \frac{1}{(1 - F_e) + \frac{F_e}{S_e}}$$

fraction enhanced

Speedup of enhancement

$$\text{Speedup} = \frac{t_{old}}{t_{new}} = \frac{1}{1 - F_e + \frac{F_e}{S_e}}$$

$$\text{Speedup}_n = \frac{1}{1 - \frac{P}{n} + \frac{P}{n} \leftarrow \# \text{ of procs}}$$

Parallel portion

Parallel programs
part of the program is inherently serial
parallel fraction < 90%

$$t_{new} = t_{old} \cdot (1 - F_e) + t_{old} \cdot \frac{F_e}{S_e}$$

90% parallel speedup w/ 2 procs over 1 proc?

$$\begin{aligned} \text{Speedup} &= \frac{1}{1 - .9 + \frac{.9}{2}} = \frac{1}{.1 + .45} = \frac{1}{.55} = 1.82x \\ &= \frac{1}{1 - .9 + \frac{.9}{4}} = \frac{1}{.1 + .225} = 3.08x \end{aligned}$$

most speedup? parallel portion in 0 time $\rightarrow \frac{1}{1 - .9} = \frac{1}{.1} = 10x$

Gustafson's Law

\rightarrow speedup with respect to data size growing

	Base line system	System A	system B
inst. mix	30% lds	1x	1x
	20% st.	1x	1x
	10% div	5x speedup	1x
	40% ALU	1x	1.5x speedup

$$\text{Speedup A: Amdahl's law} \rightarrow \frac{1}{1 - .1 + \frac{.1}{5}} = \frac{1}{.92} = 1.09x$$

$$\boxed{\text{Speedup B}} \quad " \rightarrow \frac{1}{1 - .4 + \frac{.4}{1.5}} = \frac{1}{.6 + \frac{.4}{1.5}} = 1.15x$$

$$S_B > S_A$$

$$\frac{S_B}{S_A} = \frac{1.15x}{1.09x} = 1.055 \rightarrow \text{speedup of B over A}$$

Perf of single-cycle CPU

latency + physics

↳ latency is mostly fixed

↳ due to no more Dennard scaling + Moore's Law

→ How to incr. perf?

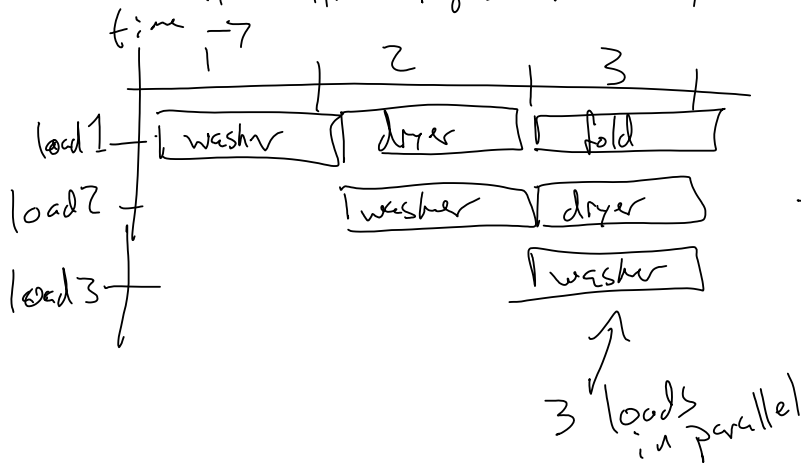
parallelism ★ → incr bandwidth $\frac{\text{\# things done}}{\text{cycle}}$

↳ laundry

washer ~ 1hr + dryer ~ 1h + fold ~ 1h

1 load takes 3 hrs

Overlap diff. stages of laundry



latency for
a load of
laundry?

3 hrs.

what's the throughput
or bandwidth?

1 load
hour