

Ramaprasad Bhar
and
Shigeyuki Hamori

Hidden Markov Models

Applications to Financial
Economics

Advanced Studies in
Theoretical and Applied Econometrics



K L U W E R A C A D E M I C P U B L I S H E R S

Hidden Markov Models

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Hidden Markov Models

Applications to Financial Economics

by

Ramaprasad Bhar

*School of Banking and Finance,
The University of New South Wales, Sydney, Australia*

and

Shigeyuki Hamori

*Graduate School of Economics,
Kobe University, Japan*

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To Rajiv, Mitra,
Hitoshi, Makoto, and
Naoko

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