1 Instructions for compiling and running DDalpha

In order to compile the software MPI has to be installed. With this requirement it is enough to run the Makefile to build DDalpha

This will generate two executables: dd_alpha_amg and dd_alpha_amg_db. The latter is the developer version, which is not relevant here. The program requires many input parameters to run properly. These are explained in detail in the documentation user_doc.pdf). However, I provide two sample scripts, sample4.ini and sample8.ini, for facilitating the usage. They correspond to an inversion of the Dirac matrix on 4⁴ and 8⁴ lattices respectively using a two-grid method. The right-hand side of the matrix problem can be chosen to be random or a vector with all its entries equal to one. The sample files choose a vector with ones. DDalpha also requires a gauge configuration to run. Given the boundary conditions (periodic in the samples) and a configuration, the correspondent Dirac matrix is inverted by the program. Random configurations can be created by compiling the source file conf/random/random_conf.c

When executing this program the lattice dimensions have to be passed through the terminal

This generates a binary file, NtxNzxNyxNx_random, with a SU(3) gauge configuration. DDalpha does not assemble the Dirac matrix due to its large size. However, in case that it is necessary to have the matrix information, one can compile conf/random/dirac matrix.c in a similar manner as random conf.c.

to build the matrix for a given configuration and dump its non-zero entries into a binary file. Once again, the lattice dimensions have to be passed from the terminal

and the configuration has to be in the same directory. For the moment this program only assembles the matrix with periodic boundary conditions. Essentially, it implements the following formula

$$D(\vec{n}, \vec{m}) = (m_0 + 4) \frac{1}{a} I_{12} \delta_{\vec{n}, \vec{m}}$$

$$- \frac{1}{2a} \sum_{\mu=0}^{3} \left[(I_4 - \gamma_{\mu}) \otimes U_{\mu}(\vec{n}) \delta_{\vec{n} + \hat{\mu}, \vec{m}} + (I_4 - \gamma_{\mu}) \otimes U_{\mu}^{\dagger} (\vec{n} - \hat{\mu}) \delta_{\vec{n} - \hat{\mu}, \vec{m}} \right],$$

where m_0 is a free parameter (I fixed it to -0.5), a is the lattice spacing (I fixed it to one), I_{12} and I_4 are the twelve and four dimensional identity matrices respectively, γ_{μ} are the Dirac matrices

$$\gamma_0 = \gamma_x = \begin{pmatrix} & & i \\ & i \\ -i & \end{pmatrix}, \quad \gamma_1 = \gamma_y = \begin{pmatrix} & & -1 \\ & 1 & \\ -1 & & \end{pmatrix}$$

$$\gamma_2 = \gamma_z = \begin{pmatrix} & i \\ & & -i \\ -i & & \\ i & & \end{pmatrix}, \quad \gamma_3 = \gamma_t = \begin{pmatrix} & 1 \\ & & 1 \\ 1 & & \\ & 1 & \end{pmatrix}.$$

The vectors \vec{n} refer to the lattice sites which live in the volume

$$V = {\vec{n} = (n_0, n_1, n_2, n_3) | n_\mu = 0, 1, \dots, N_\mu - 1; \mu = 0, 1, 2, 3},$$

$$N_0 = N_x$$
, $N_1 = N_y$, $N_2 = N_z$, $N_3 = N_t$.

and $\hat{\mu}$ is a unit vector in the direction indexed by μ . The gauge links $U_{\mu}(\vec{n})$ are random SU(3) matrices stored in the configuration file. To read the binary with $D(\vec{n}, \vec{m})$ I provide the file conf/random/read_matrix.c. It can be modified for handling the non-zero entries of the Dirac matrix as you need.

The path to the configuration file can be changed in the sample files. To simplify the execution you can use the run script. In case it does not work, perhaps you have to modify lines 190 and 200, which depend on how you excecute programs with MPI on your machine. The sample files have to be passed as input parameters at the execution call, for instance

In the future it will be convenient to use configurations from real physical simulations I will provide this data, but for now random configurations should be enough for testing.

2 Printing the test vectors

The interpolator is built by arranging the test (complex) vectors in columns over the aggregates, as explained in Ref. [1]. DDalpha computes this vectors in the setup phase. The number of test vectors is a free parameter of the code, it can be changed in the sample files. By experimenting it was observed that between 20 and 30 vectors works fine. The test vectors at level l are printed in a file with name testvector_levell.txt. They are arranged in a single column separated by dashed lines. For the finest level (highest value of l) each vector has $12 \times N_x \times N_y \times N_z \times N_t$ complex entries, which correspond to the Dirac matrix dimensions.

References

[1] A. Frommer, K. Kahl, S. Krieg, B. Leder and M. Rottmann. Adaptive aggregation based domain decomposition multigrid for the lattice Wilson Dirac operator. *SIAM J. Sci. Comp.*, **36**(4):A1581–A1608, (2014).