

◆ Sorting Algorithms – Coding Exercises

1. Selection Sort Exercises

Goal: Practice finding the minimum and swapping.

Exercise 1.1 — Manual Minimum Swap

- Write a function that takes a list and finds the smallest number in the list.
- Swap it with the first element.
- Print the modified list.

Exercise 1.2 — Full Selection Sort

- Extend your function so it keeps repeating the process to fully sort the list.
- Test it with `[64, 25, 12, 22, 11]`.

Exercise 1.3 — Step Tracker

- Modify your function so that after each pass, it prints the list (so you can see how the list is sorted step by step).

2. Insertion Sort Exercises

Goal: Practice shifting elements into the right position.

Exercise 2.1 — Insert One Card

- Imagine a list that is partly sorted: `[3, 7, 9, | 5]` (the vertical bar separates sorted and unsorted).
- Write code to insert "5" into the correct place among the sorted numbers.

Exercise 2.2 — Full Insertion Sort

- Create a function that sorts an entire list using the insertion sort technique.
- Test it with `[12, 11, 13, 5, 6]`.

Exercise 2.3 — Counting Shifts

- Modify your function so that it counts how many "shifts" (moving items one step right) occur during the sorting process.
- Print the total shifts used to sort the list.

3. Bubble Sort Exercises

Goal: Demonstrate repeated pairwise comparison and swapping.

Exercise 3.1 — One Bubble Pass

- Write a function that performs **just one pass** of bubble sort on `[5, 1, 4, 2, 8]`.
- Print the result.

Exercise 3.2 — Full Bubble Sort

- Extend the code to keep repeating passes until the entire list is sorted.
- Print the list after each pass.

Exercise 3.3 — Optimized Bubble Sort

- Modify your bubble sort so it stops early if *no swaps* are made in a pass.
- Compare how many passes are needed on:
 - `[1, 2, 3, 4, 5]` (already sorted)
 - `[5, 4, 3, 2, 1]` (reverse order)

4. Quicksort Exercises (Higher Level)

Goal: Understand recursion and partitioning.

Exercise 4.1 — Partition Step Only

- Write a function that picks the **last element as pivot** and rearranges the list so smaller numbers are on the left, and larger numbers are on the right.
- Test with `[10, 80, 30, 90, 40, 50, 70]`.

Exercise 4.2 — Full Recursive Quicksort

- Implement Quicksort using recursion.
- Test with `[10, 7, 8, 9, 1, 5]`.

Exercise 4.3 — Quicksort Variation

- Change your implementation so the pivot is chosen at **random** instead of the last element.
- Compare the performance on different datasets.

◆ Extension Exercises – For Stronger Students

These require deeper thinking about efficiency, complexity, and edge cases.

Extension 1 — Timing Comparisons

- Use Python's `time` module to measure how long each algorithm takes to sort:
 - A list of 100 random numbers
 - A list of 100 numbers already sorted
 - A list of 100 numbers in reverse order
- Record and compare results.

Extension 2 — Hybrid Sort

- Write a function that uses **Insertion Sort** for small lists (length < 10) and **Quicksort** for larger lists.

- Test it on various list sizes.

Extension 3 — Visualization Challenge

- Using `matplotlib`, create a bar chart that updates at each step of a sorting algorithm (e.g., Bubble Sort).
- The bars should move as the sort progresses, visually showing the sorting process.

Extension 4 — Compare and Reflect

- Create a table showing for each algorithm:
 - Best case comparisons
 - Worst case comparisons
 - Memory usage
- Write a short reflection: Which one makes sense to use in real-world programming, and why?

If you are not sure where to start with the examples above then I have provided a starting template for each of the exercises to get you started.

◆ Sorting Algorithms – Starter Code Templates (Python)

1. Selection Sort

Exercise 1.1 — Manual Minimum Swap

```
def selection_one_step(arr):
    # TODO: Find the index of the smallest element in the list
    min_index = 0

    # Loop through arr to find smallest item
    for i in range(1, len(arr)):
        # TODO: Compare element with arr[min_index] and update if smaller
        pass

    # TODO: Swap the first element with smallest element found
    pass

    return arr

print(selection_one_step([64, 25, 12, 22, 11]))
```

Exercise 1.2 — Full Selection Sort

```
def selection_sort(arr):
```

```
# Repeat for each position in list
for i in range(len(arr)):
    # TODO: find index of the smallest element in remaining list
    min_index = i
    for j in range(i + 1, len(arr)):
        pass # compare and update min_index

    # TODO: Swap arr[i] with smallest element
    pass

return arr

print(selection_sort([64, 25, 12, 22, 11]))
```

2. Insertion Sort

Exercise 2.1 — Insert One Card

```
def insert_one(sorted_part, new_item):
    # Assume sorted_part is already sorted.
    i = len(sorted_part) - 1

    # TODO: Shift elements to the right until you find place for new_item
    while i >= 0 and sorted_part[i] > new_item:
        pass

    # TODO: Insert new_item into correct position
    pass

    return sorted_part

print(insert_one([3, 7, 9], 5))
```

Exercise 2.2 — Full Insertion Sort

```
def insertion_sort(arr):
    # Start with second element (first is "sorted")
    for i in range(1, len(arr)):
        current = arr[i]

        # TODO: shift larger elements to the right
        j = i - 1
        while j >= 0 and arr[j] > current:
            pass

        # TODO: insert current in correct place
        pass
    return arr
```

```
print(insertion_sort([12, 11, 13, 5, 6]))
```

Exercise 2.3 — Counting Shifts

```
def insertion_sort_with_count(arr):
    shifts = 0

    for i in range(1, len(arr)):
        current = arr[i]
        j = i - 1
        while j >= 0 and arr[j] > current:
            # Each move = one shift
            shifts += 1
            pass
        pass

    print("shifts:", shifts)
    return arr
```

3. Bubble Sort

Exercise 3.1 — One Pass

```
def bubble_pass(arr):
    # One full scan comparing pairs
    for i in range(len(arr)-1):
        # TODO: Compare arr[i] and arr[i+1], swap if needed
        pass
    return arr

print(bubble_pass([5, 1, 4, 2, 8]))
```

Exercise 3.2 — Full Bubble Sort

```
def bubble_sort(arr):
    n = len(arr)
    for pass_num in range(n - 1):
        # TODO: One bubble pass through list
        for i in range(n - 1):
            pass # swap if necessary
        print("After pass", pass_num+1, arr)
    return arr
```

Exercise 3.3 — Optimized Bubble Sort

```
def bubble_sort_optimized(arr):
    n = len(arr)
    for pass_num in range(n - 1):
        swapped = False
        for i in range(n - 1):
            pass # swap if needed and update swapped = True
        print("After pass", pass_num+1, arr)
        if not swapped:
            break
    return arr
```

4. Quicksort (Higher Level)

Exercise 4.1 — Partition Step

```
def partition(arr, low, high):
    pivot = arr[high] # last element as pivot
    i = low - 1 # tracks smaller elements

    for j in range(low, high):
        # TODO: if arr[j] <= pivot, move it to left partition
        pass

    # TODO: Place pivot into correct position
    pass

    return i + 1

print(partition([10, 80, 30, 90, 40, 50, 70], 0, 6))
```

Exercise 4.2 — Full Recursive Quicksort

```
def quicksort(arr, low, high):
    if low < high:
        # Partition
        pi = partition(arr, low, high)

        # TODO: Recursively sort partitions
        pass

    return arr

print(quicksort([10, 7, 8, 9, 1, 5], 0, 5))
```

◆ Extension Starters

Extension 1 — Timing Comparisons

```
import time, random

def measure_time(sort_func, arr):
    start = time.time()
    sort_func(arr[:]) # copy so original isn't affected
    end = time.time()
    return end - start

data = [random.randint(1, 1000) for _ in range(100)]
print("Selection sort time:", measure_time(selection_sort, data))
```

Extension 2 — Hybrid Sort

```
def hybrid_sort(arr):
    if len(arr) < 10:
        # TODO use insertion_sort
        pass
    else:
        # TODO use quicksort
        pass
    return arr
```

Extension 3 — Visualization (Bubble Sort Idea)

```
import matplotlib.pyplot as plt
import time

def bubble_sort_visual(arr):
    n = len(arr)
    for _ in range(n - 1):
        for i in range(n - 1):
            if arr[i] > arr[i+1]:
                arr[i], arr[i+1] = arr[i+1], arr[i]
            # draw array
            plt.bar(range(len(arr)), arr)
            plt.pause(0.1)
            plt.clf()
    plt.show()

bubble_sort_visual([5, 3, 8, 2, 1])
```

👉 This way, students get **guided templates** to fill in, rather than having to start from a blank screen — ideal for learning progression.

Jim, do you want me to also design a **student worksheet version** (without code, just pseudocode prompts and guiding questions), so you could differentiate between programming vs conceptual learners?