

# FPV Tutorübung

# Woche 1 Implications, Assertions and Conditions

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20.04.2023



# <u>Organisatorisches</u>

#### **Grade Bonus**

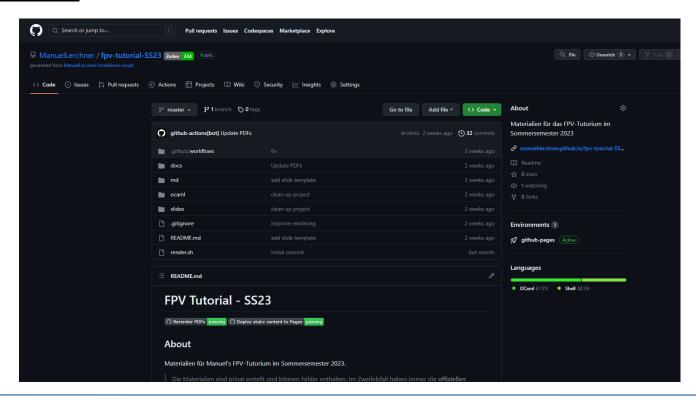
- Successful participation ( $\geq 70\%$ ) in quizzes and programming tasks will lead to a bonus of 0.3 in the final exam, provided that you passed the exam.
- Programming homework and quizzes are to be submitted individually.
- Discussing solutions before the end of the week is considered plagiarism.
- Plagiarism will not be tolerated and will (at the very least) lead to exclusion from the bonus system

#### Changes

- Manual correction of homework not possible.
   However, non-programming exercises remain
   crucial for the exam
- 20% of the exam will be Single-Choice
- To receive points in the exam, your code needs to compile
- We currently anticipate an in-person exam using Artemis

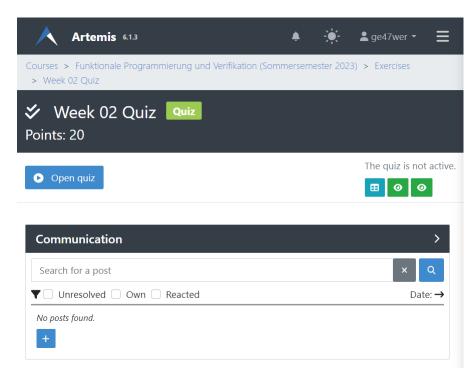


# **Materialien**





# <u>Quiz</u>



### Passwort:

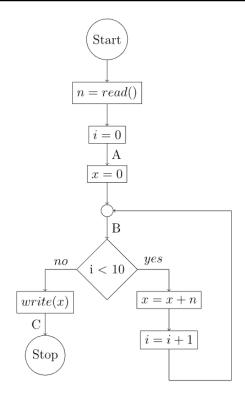


# T01: Recap Implications

```
1, x = 1 \implies 0 < x
 2. x < 6 \implies x = 3
 3. x > 0 \implies x > 0
 4. x = -2 \implies x < -1 \lor x > 1
 5. x = 0 \lor x = 7 \implies 4 \neq x
 6. x = 1 \implies x < 3 \land y > 0
 7. x < 8 \land y = x \implies y \neq 12
 8. x = 1 \lor y = 1 \implies x > 0
 9. x \neq 5 \implies false
10. true \implies x \neq y
11. false \implies x = 1
12. x > 1 \implies 2x + 3 = 5
13. A \wedge x = y \implies A
14. B \implies A \vee B
15. A \implies (B \implies A)
16. (A \Longrightarrow B) \Longrightarrow A
```



# T02: Assertions



- 1. Which of the following assertions hold at point A?
  - $\circ$  a)  $i \geq 0$
  - $\circ$  b) x=0
  - $\circ$  c)  $i \leq 10 \land x \neq 0$
  - $\circ$  d) true
  - $\circ$  e) i=0
  - $\circ$  f) x = i
- 2. Which of the following assertions hold at point B?
  - $\circ$  a)  $x=0 \land i=0$
  - $\circ$  b) x = i
  - $\circ$  c) i < x
  - $\circ$  d) 0 < i < 10
  - $\circ$  e)  $i \geq 0 \land x \geq 0$
  - $\circ$  f)  $n=1 \implies x=i$
- 3. Which of the following assertions hold at point C?
  - $\circ$  a)  $i \geq 0$
  - $\circ$  b) i=10
  - $\circ$  c) i>0
  - $\circ$  d)  $x \neq n$
  - $\circ$  e) x = 10n
  - $\circ$  f)  $x = i * n \wedge i = 10$

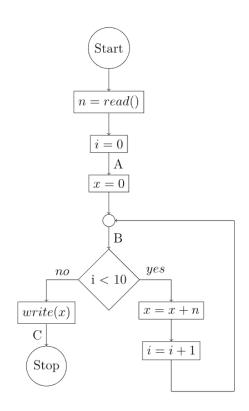


# T03: The Strong and the Weak

- 3. Which of the following assertions hold at point C?
  - $\begin{array}{l} \circ \text{ a) } i \geq 0 \\ \circ \text{ b) } i = 10 \\ \checkmark \\ \circ \text{ c) } i > 0 \\ \checkmark \\ \circ \text{ d) } x \neq n \\ \times \\ \circ \text{ e) } x = 10n \\ \checkmark \\ \circ \text{ f) } x = i*n \land i = 10 \\ \end{array}$

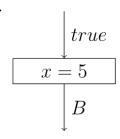
Again consider the assertions that hold at point C of assignment 2. Discuss the following questions:

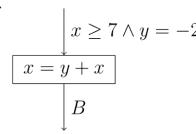
- 1. When annotating the control flow graph, can you say that one of the given assertions is "better" than the others?
- 2. Can you arrange the given assertions in a meaningful order?
- 3. How can you define a stronger than relation formally?
- 4. How do true and false fit in and what is their meaning as an assertion?
- 5. What are the strongest assertions that still hold at A, B and C?

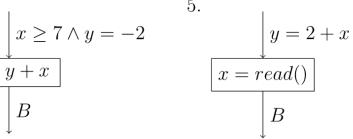


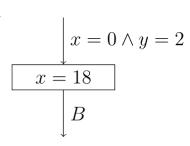


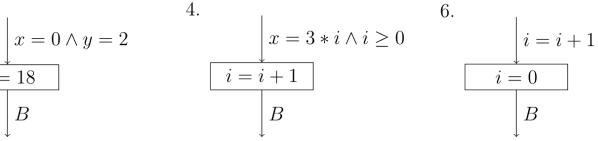
# T04: Strongest Postconditions 1

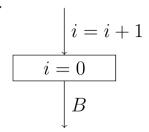








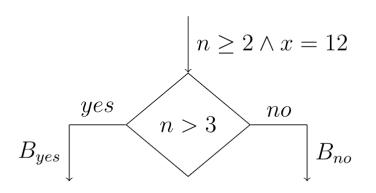




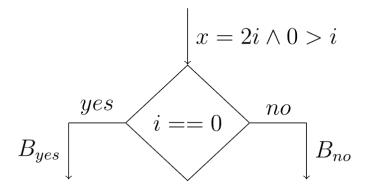


# T04: Strongest Postconditions 2

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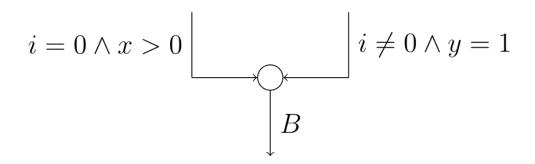
8.





# T04: Strongest Postconditions 3

9.





# FPV Tutorübung

Woche 2

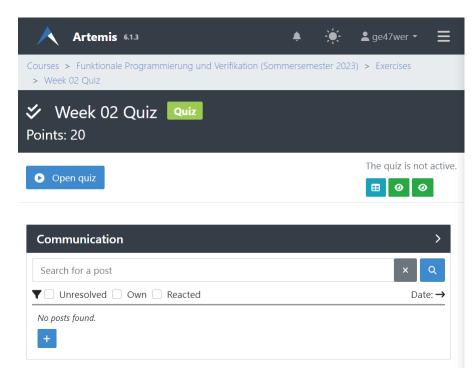
Preconditions, Postconditions and Local Consistency

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03.05.2023



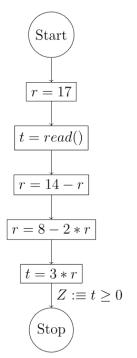
# <u>Quiz</u>



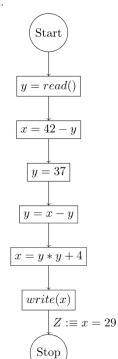
### Passwort:



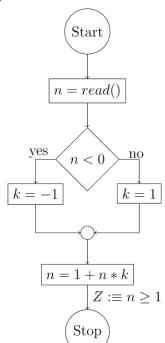
1.



2.



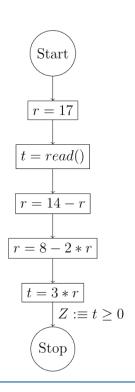
3.



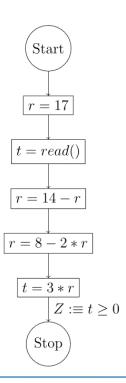
- 1. For each of these graphs show whether the assertion Z holds...
- (a) ...using strongest postconditions and
- (b) ...using weakest preconditions.
- 2. Discuss advantages and disadvantages of either approach.



Post-Condition:

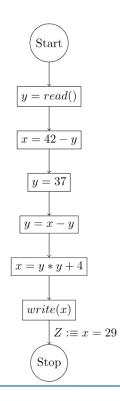


**Pre-Condition:** 

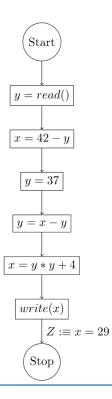




Post-Condition:

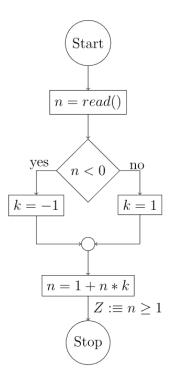


**Pre-Condition:** 

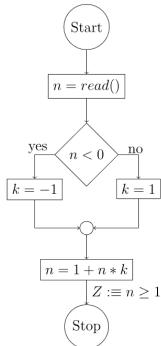




**Post-Condition:** 

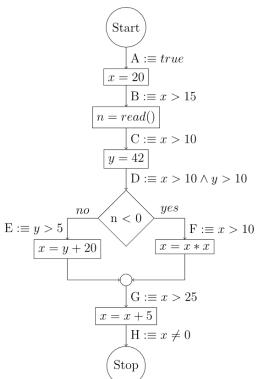


Pre-Condition:





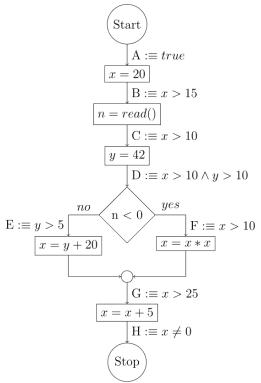
# T02: Local Consistency



Check whether the annotated assertions prove that the program computes an  $x \neq 0$  and discuss why this is the case.

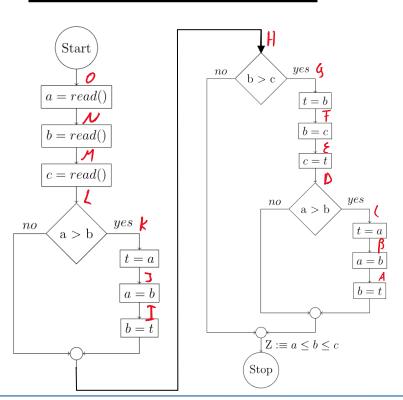


# T02: Local Consistency (Extra Space)





# T03: Trouble Sort



- 1. Annotate each program point in the following control flow diagram with a suitable assertion, then show that your annotations are locally consistent and prove that Z holds at the given program point.
- 2. Discuss the drawbacks of annotating each program point with an assertion before applying weakest preconditions, and discuss how you could optimize the approach to proving that Z holds.



# T03: Trouble Sort (Extra Space)

