

# FPV Tutorübung

Woche 1

## Implications, Assertions and Conditions

Manuel Lerchner

20.04.2023

# Organisatorisches

## Grade Bonus

- Successful participation ( $\geq 70\%$ ) in quizzes and programming tasks will lead to a bonus of 0.3 in the final exam, provided that you passed the exam.
- Programming homework and quizzes are to be submitted individually.
- Discussing solutions before the end of the week is considered plagiarism.
- Plagiarism will not be tolerated and will (at the very least) lead to exclusion from the bonus system

## Changes

- Manual correction of homework not possible. However, non-programming exercises remain crucial for the exam
- 20% of the exam will be Single-Choice
- To receive points in the exam, your code needs to compile
- We currently anticipate an in-person exam using Artemis

# Materialien

The screenshot displays the GitHub interface for the repository `ManuelLerchner / fpv-tutorial-SS23`. The repository is public and has 334 commits. The main branch is `master`, with 1 branch and 0 tags. The repository was generated from `ManuelLerchner/markdown-script`.

The repository structure includes the following files and folders:

- `.github/workflows`: fix (2 weeks ago)
- `docs`: Update PDFs (2 weeks ago)
- `md`: add slide template (2 weeks ago)
- `ocaml`: clean up project (2 weeks ago)
- `slides`: clean up project (2 weeks ago)
- `.gitignore`: improve rendering (2 weeks ago)
- `README.md`: add slide template (2 weeks ago)
- `render.sh`: initial commit (last month)

The `README.md` file is selected, showing the title **FPV Tutorial - SS23**. Below the title, there are two status indicators: `Rerender PDFs` (passing) and `Deploy static content to Pages` (passing). The **About** section states: "Materialien für Manuel's FPV-Tutorium im Sommersemester 2023." and "Die Materialien sind privat erstellt und können Fehler enthalten. Im Zweifelsfall haben immer die offiziellen".

The right sidebar shows the repository's **About** section, including the link `manuellernher.github.io/fpv-tutorial-SS...`, 0 stars, 1 watching, and 0 forks. The **Environments** section shows `github-pages` as active. The **Languages** section shows a progress bar for `OCaml` (61.5%) and `Shell` (38.5%).

# Quiz



Artemis 6.1.3

Courses > Funktionale Programmierung und Verifikation (Sommersemester 2023) > Exercises > Week 02 Quiz

✓ Week 02 Quiz **Quiz**

Points: 20

**Open quiz**

The quiz is not active.

**Communication**

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# T01: Recap Implications

1.  $x = 1 \implies 0 < x$
2.  $x < 6 \implies x = 3$
3.  $x > 0 \implies x \geq 0$
4.  $x = -2 \implies x < -1 \vee x > 1$
5.  $x = 0 \vee x = 7 \implies 4 \neq x$
6.  $x = 1 \implies x \leq 3 \wedge y > 0$
7.  $x < 8 \wedge y = x \implies y \neq 12$
8.  $x = 1 \vee y = 1 \implies x > 0$
9.  $x \neq 5 \implies \text{false}$
10.  $\text{true} \implies x \neq y$
11.  $\text{false} \implies x = 1$
12.  $x \geq 1 \implies 2x + 3 = 5$
13.  $A \wedge x = y \implies A$
14.  $B \implies A \vee B$
15.  $A \implies (B \implies A)$
16.  $(A \implies B) \implies A$

# T02: Assertions



1. Which of the following assertions hold at point *A*?

- a)  $i \geq 0$
- b)  $x = 0$
- c)  $i \leq 10 \wedge x \neq 0$
- d) *true*
- e)  $i = 0$
- f)  $x = i$

2. Which of the following assertions hold at point *B*?

- a)  $x = 0 \wedge i = 0$
- b)  $x = i$
- c)  $i < x$
- d)  $0 \leq i \leq 10$
- e)  $i \geq 0 \wedge x \geq 0$
- f)  $n = 1 \implies x = i$

3. Which of the following assertions hold at point *C*?

- a)  $i \geq 0$
- b)  $i = 10$
- c)  $i > 0$
- d)  $x \neq n$
- e)  $x = 10n$
- f)  $x = i * n \wedge i = 10$

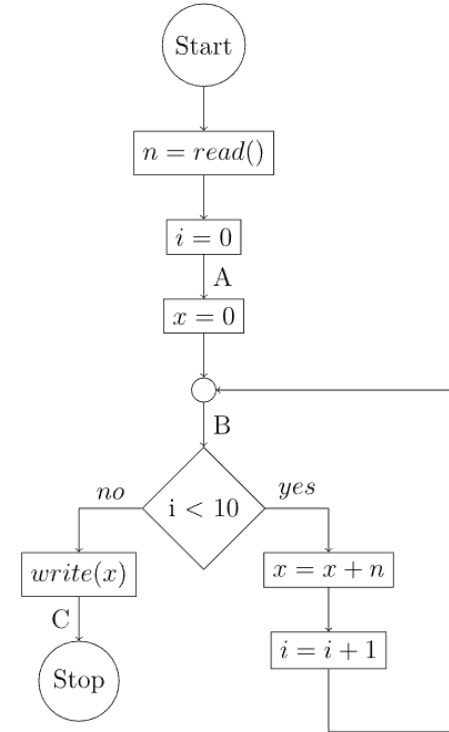
# T03: The Strong and the Weak

3. Which of the following assertions hold at point  $C$ ?

- a)  $i \geq 0$  ✓
- b)  $i = 10$  ✓
- c)  $i > 0$  ✓
- d)  $x \neq n$  ✗
- e)  $x = 10n$  ✓
- f)  $x = i * n \wedge i = 10$  ✓

Again consider the assertions that hold at point  $C$  of assignment 2. Discuss the following questions:

1. When annotating the control flow graph, can you say that one of the given assertions is "better" than the others?
2. Can you arrange the given assertions in a meaningful order?
3. How can you define a *stronger than* relation formally?
4. How do *true* and *false* fit in and what is their meaning as an assertion?
5. What are the strongest assertions that still hold at  $A$ ,  $B$  and  $C$ ?



# T04: Strongest Postconditions 1

1.



3.



5.



2.



4.



6.



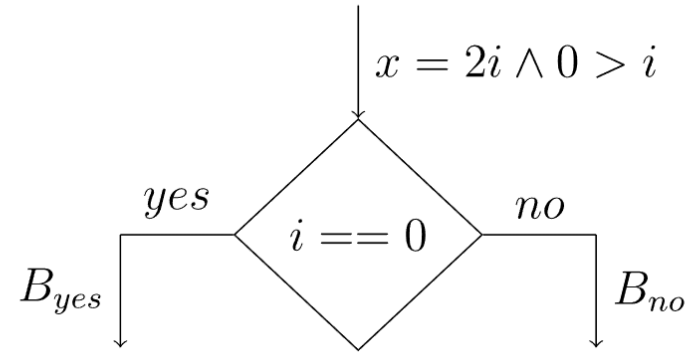


## T04: Strongest Postconditions 2

7.



8.



## T04: Strongest Postconditions 3

9.



# FPV Tutorübung

Woche 2

## Preconditions, Postconditions and Local Consistency

Manuel Lerchner

02.05.2023

# Quiz



Artemis 6.1.3

Courses > Funktionale Programmierung und Verifikation (Sommersemester 2023) > Exercises > Week 02 Quiz

✓ Week 02 Quiz **Quiz**

Points: 20

[Open quiz](#) The quiz is not active.

**Communication**

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# T01: From Post- to Preconditions

1.



2.



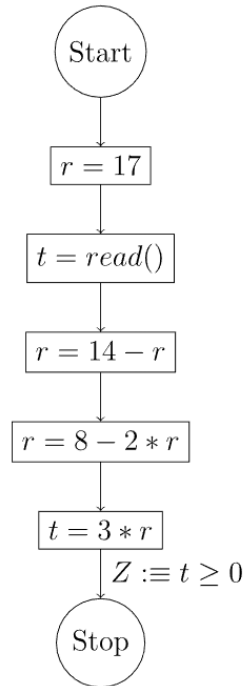
3.



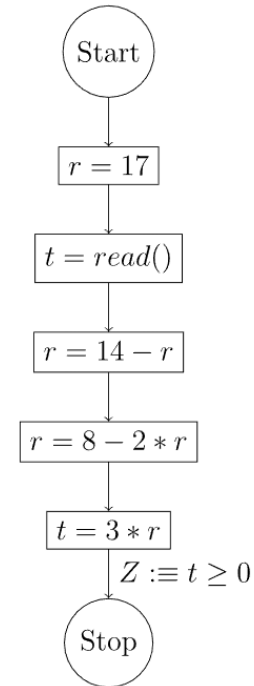
1. For each of these graphs show whether the assertion  $Z$  holds...
  - (a) ...using strongest postconditions and
  - (b) ...using weakest preconditions.
2. Discuss advantages and disadvantages of either approach.

# T01: From Post- to Preconditions 1

Post-Condition:

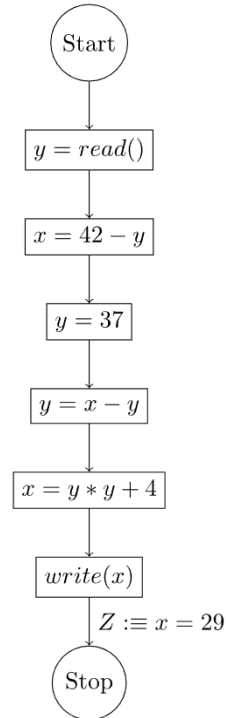


Pre-Condition:

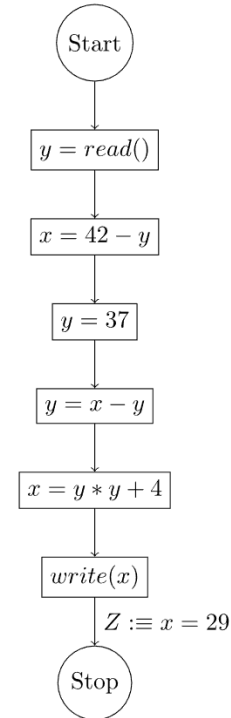


# T01: From Post- to Preconditions 2

Post-Condition:

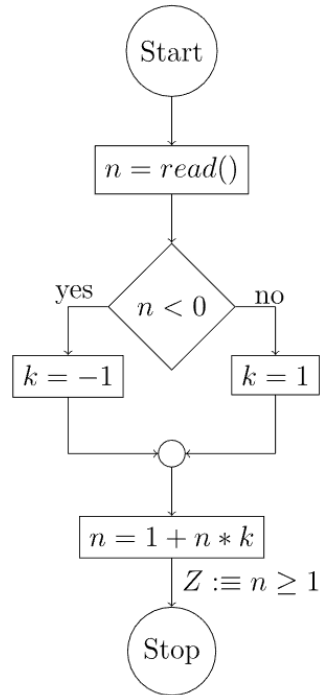


Pre-Condition:

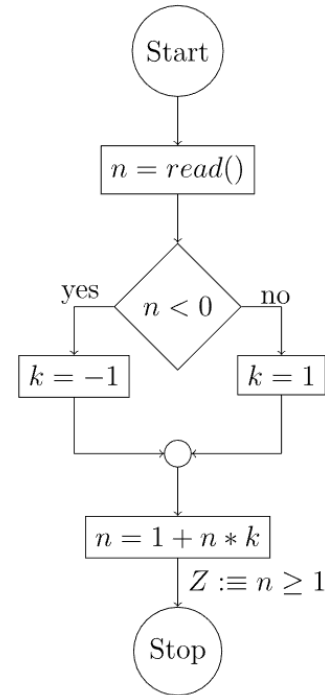


# T01: From Post- to Preconditions 3

Post-Condition:



Pre-Condition:



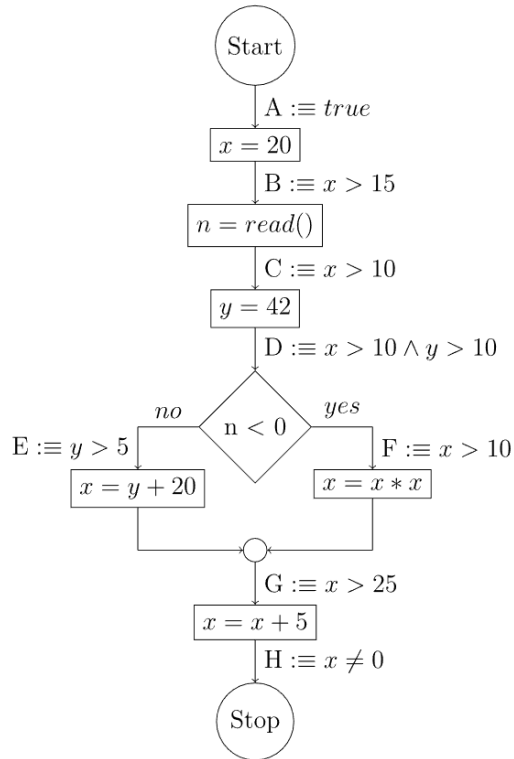


# T02: Local Consistency

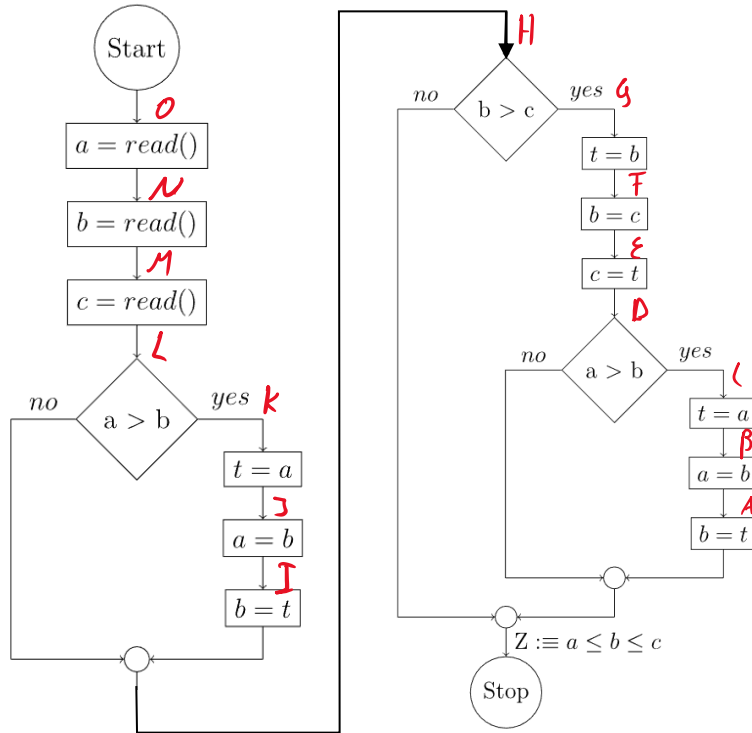


Check whether the annotated assertions prove that the program computes an  $x \neq 0$  and discuss why this is the case.

# T02: Local Consistency (Extra Space)



# T03: Trouble Sort



1. Annotate each program point in the following control flow diagram with a suitable assertion, then show that your annotations are locally consistent and prove that  $Z$  holds at the given program point.
2. Discuss the drawbacks of annotating each program point with an assertion before applying weakest preconditions, and discuss how you could optimize the approach to proving that  $Z$  holds.

# T03: Trouble Sort (Extra Space)

