# Multivariable Calculus (MATH 22)

## Teaching Assitant

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# Warm Up

Together in groups, discuss plain language definitions for the following terms:

- Function
- Limit
- Continuity
- Vector

- Derivative
- Integral
- Level set

## Problem 1

#### Problem 9.1.14

Find the equation of each of the following geometric objects.

- a. The plane parallel to the xy-plane that passes through the point (-4,5,-12).
- b. The plane parallel to the yz-plane that passes through the point (7, -2, -3).
- c. The sphere centered at the point (2,1,3) and has the point (-1,9,-1) on its surface.
- d. The sphere whose diameter has endpoints (-3,1,-5) and (7,9,-1).

## Problem 2

#### 9.1.16

 $\dots$  if we borrow \$18,000 to buy a car, the monthly payment M that we need to make to pay off the loan is given by the formula

$$M(r,t) = \frac{1500r}{1 - \frac{1}{(1 + \frac{r}{12})^{12t}}}.$$

- a. Find the monthly payments on this loan if the interest rate is 6% and the duration of the loan is 5 years.
- b. Create a table of values that illustrates the trace of M with r fixed at 5%. Use yearly values of t from 2 to 6. Round payments to the nearest penny. Explain in detail in words what this trace tells us about M.
- c. Create a table of values that illustrates the trace of M with t fixed at 3 years. Use rates from 3% to 11% in increments of 2%. Round payments to the nearest penny. Explain in detail what this trace tells us about M.
- d. Consider the combinations of interest rates and durations of loans that result in a monthly payment of \$200. Solve the equation M(r,t) = 200 for t to write the duration of the loan in terms of the interest rate. Graph this level curve and explain as best you can the relationship between t and t.

## Vector Spaces

A vector space V over a field F is a non empty-set V equiped with the binary operations of vector addition and scalar multiplication such that for u, v, w vectors and a, b scalars we have

Associativity of addition: u + (v + w) = (u + v) + w.

Commutativity of addition: u + v = v + u.

Additive identity: v + 0 = v for every v.

Addititive inverses: v + (-v) = 0 for every v.

Compatability of multiplication: a(bv) = (ab)v.

Multiplicative identity: 1v = v.

Distribution over vector addition: a(u+v) = au + av.

Distibution over field addition: (a+b)v = av + bv.

# Problems 3, 4 and 5

## 9.2.1

For each of the following, perform the indicated computation

- (a)  $(10\vec{i} + 7\vec{j} 5\vec{k}) (-6\vec{i} + 4\vec{j} + 7\vec{k})$ .
- (b)  $(10\vec{i} + 6\vec{j} 3\vec{k}) 2(-3\vec{i} + 10\vec{j} + 8\vec{k}).$

## 9.2.2

Find a vector a that has the same direction as (-6,7,6) but has length 5.

## 9.2.3

Let  $a = \langle -3, -4, -4 \rangle$  and  $b = \langle 2, 2, 4 \rangle$ . Show that there are scalars s and t so that  $sa + tb = \langle 20, 24, 32 \rangle$ .

