

1. Given a complex vector $\bar{\mathbf{x}} = [x_1 \ x_2 \ \dots \ x_n]^T$. Then, $\bar{\mathbf{x}}^H = [x_1^* \ x_2^* \ \dots \ x_n^*]$

Ans d

2. Give a Gaussian random variable \mathbf{X} with mean μ and variance σ^2 . The random variable $\frac{X-\mu}{\sigma}$ is termed a Standard Normal random variable

Ans d

3. Given the vectors $\bar{\mathbf{w}}_1 = [1 \ 1 \ 1]^T$ and $\bar{\mathbf{w}}_2 = [-2 \ -2 \ -2]^T$. These are Linearly dependent since $2\bar{\mathbf{w}}_1 + \bar{\mathbf{w}}_2 = 0$

Ans c

4. It can be seen that $\bar{\mathbf{w}}_1 = [1 \ 1 \ 1]^T$ and $\bar{\mathbf{w}}_2 = [-1 \ 2 \ -1]^T$ satisfy $\bar{\mathbf{w}}_2^T \bar{\mathbf{w}}_1 = 0$. Hence they are orthogonal. This also implies that they are linearly independent

Ans d

5. a_{ij} denotes the element in the i th row and j th column

Ans b

6. Given the matrix $\mathbf{A} = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$. One of its eigenvalues is $\sqrt{2}$

Ans a

7. Given a Hermitian symmetric matrix \mathbf{A} , i.e., $\mathbf{A} = \mathbf{A}^H$. Hence, all of its eigenvalues are real

Ans b

8. Given the vector $\bar{\mathbf{x}} = [1 \ 1 \ \dots \ 1]^T$ of size $n \times 1$. The quantity $\|\bar{\mathbf{x}}\|_2$ equals

$$\sqrt{1 + 1 + \dots + 1} = \sqrt{n}$$

Ans c

9. It is always true that $\text{rank}(\mathbf{A}) \leq \min\{m, n\}$

Ans a

10. Given the vector $\bar{\mathbf{x}} = [1 \ 2 \ \dots \ n]^T$. The quantity $\|\mathbf{x}\|_2$ equals

$$\sqrt{1 + 4 + \dots + n^2} = \sqrt{\frac{n(n+1)(2n+1)}{6}}$$

Ans c