



Transformer Architecture

CSCI 601-471/671 (NLP: Self-Supervised Models)

<https://self-supervised.cs.jhu.edu/sp2025/>

RNNs, Back to the Cons

- While RNNs in theory can represent long sequences, they quickly **forget** portions of the input.
- Vanishing/exploding gradients
- Difficult to parallelize
- The alternative solution we will see: Transformers!



Language Models: History Recap

- Probabilistic n-gram models of text generation [Jelinek+ 1980's, ...]
 - Applications: Speech Recognition, Machine Translation
- Statistical or shallow neural LMs (late 90's – mid 00's) [Bengio+ 2001, ...]
- Recurrent neural nets (2010s)
- Pre-training deep neural language models (2017's onward):
 - Many models based on: **Self-Attention**

Chapter Plan

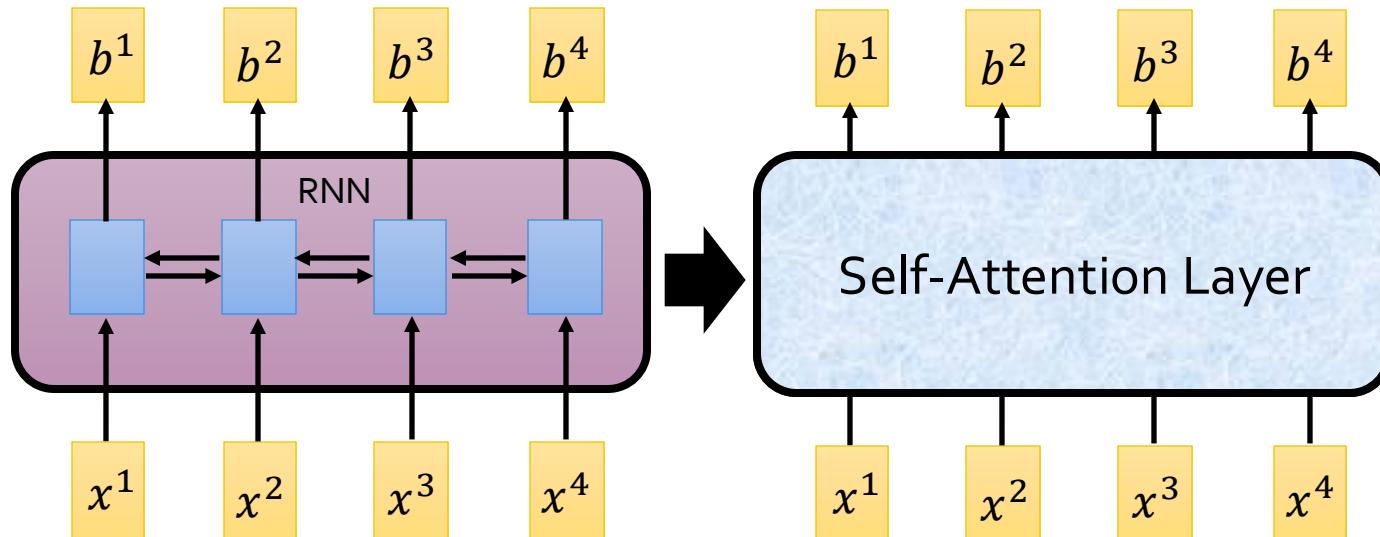
1. Self-Attention module
2. Transformer architecture
3. Computation/space cost
4. Thinking about Transformer implementation

Chapter goal — getting very comfortable with nuances involved in Transformers.

Self-Attention Module

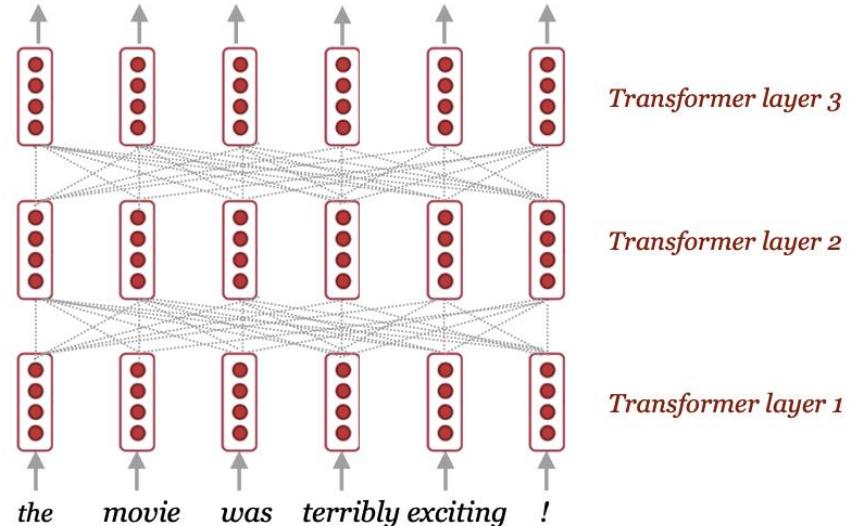
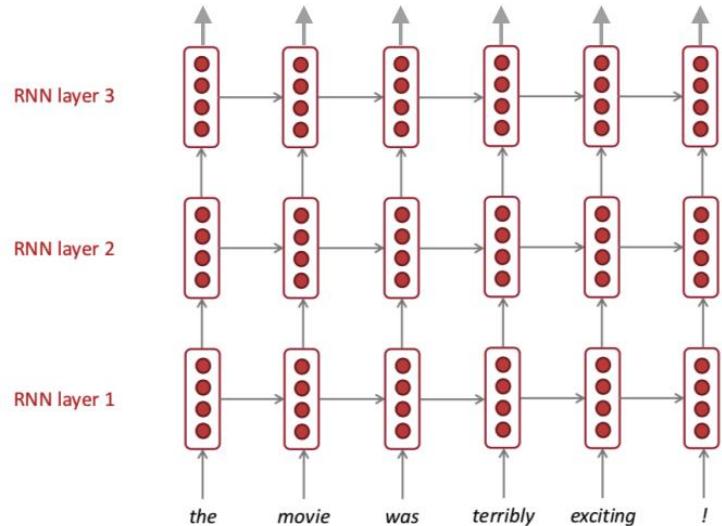
Self-Attention

- b^i is obtained based on the whole input sequence.
- can be parallelly computed.



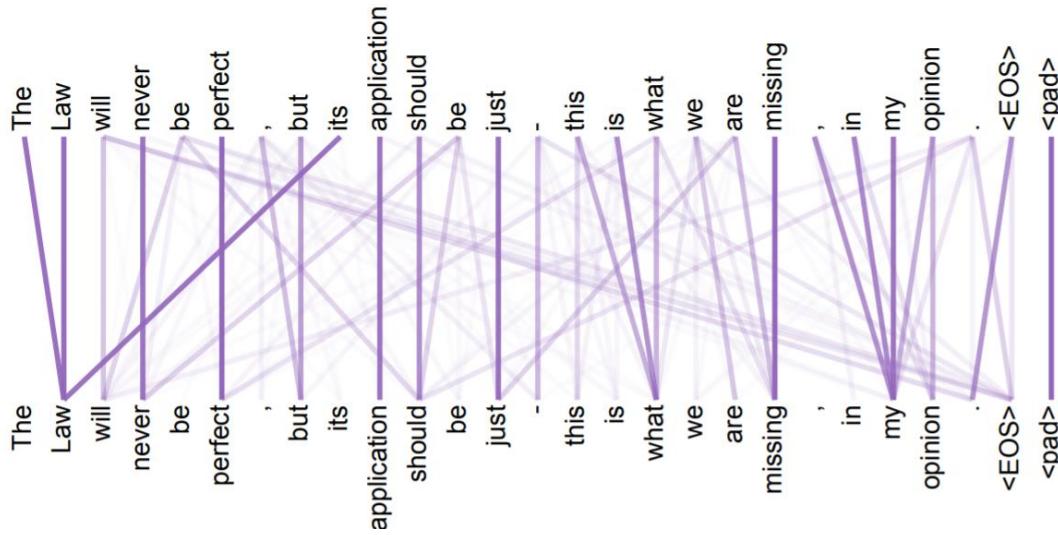
Idea: replace any thing done by RNN with **self-attention**.

RNN vs Transformer



Attention

- Core idea: build a mechanism to focus ("attend") on a particular part of the context.



Defining Self-Attention

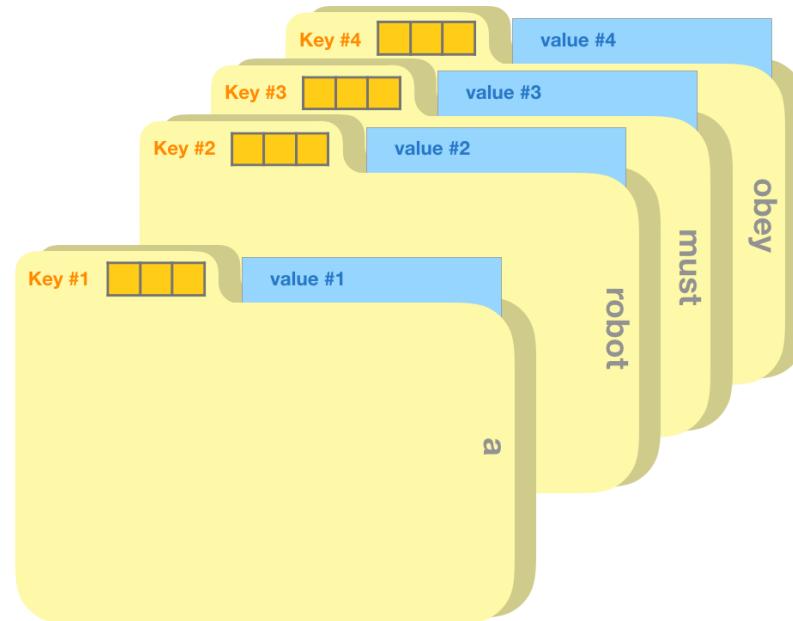
- Terminology:
 - **Query**: to match others
 - **Key**: to be matched
 - **Value**: information to be extracted

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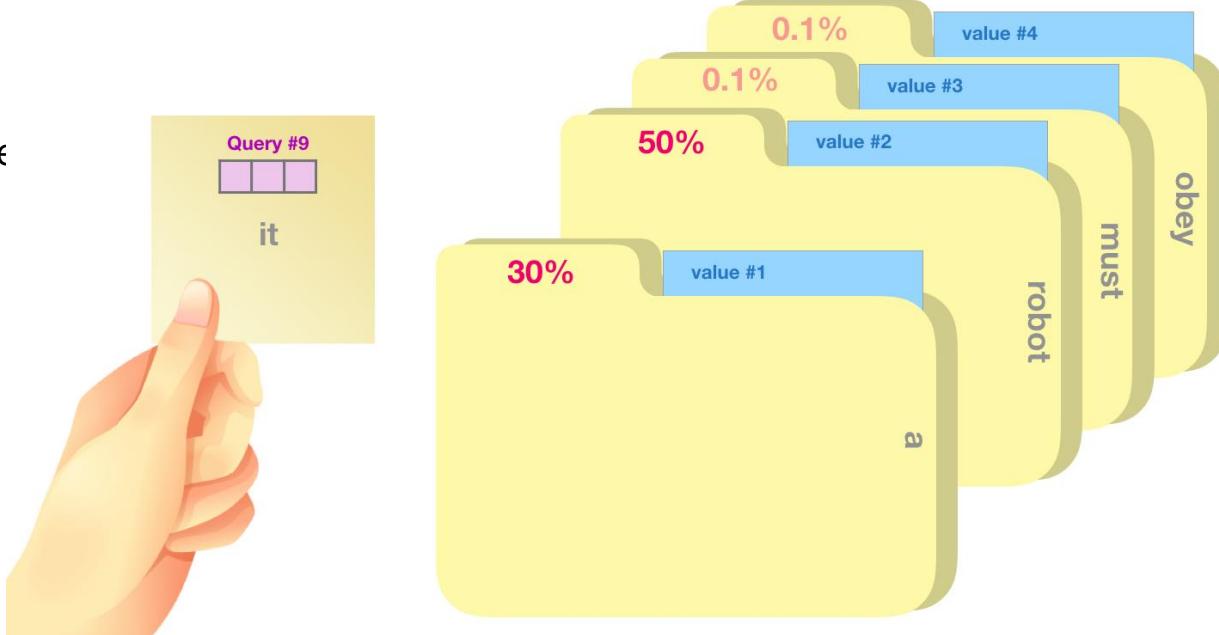


An analogy



Defining Self-Attention

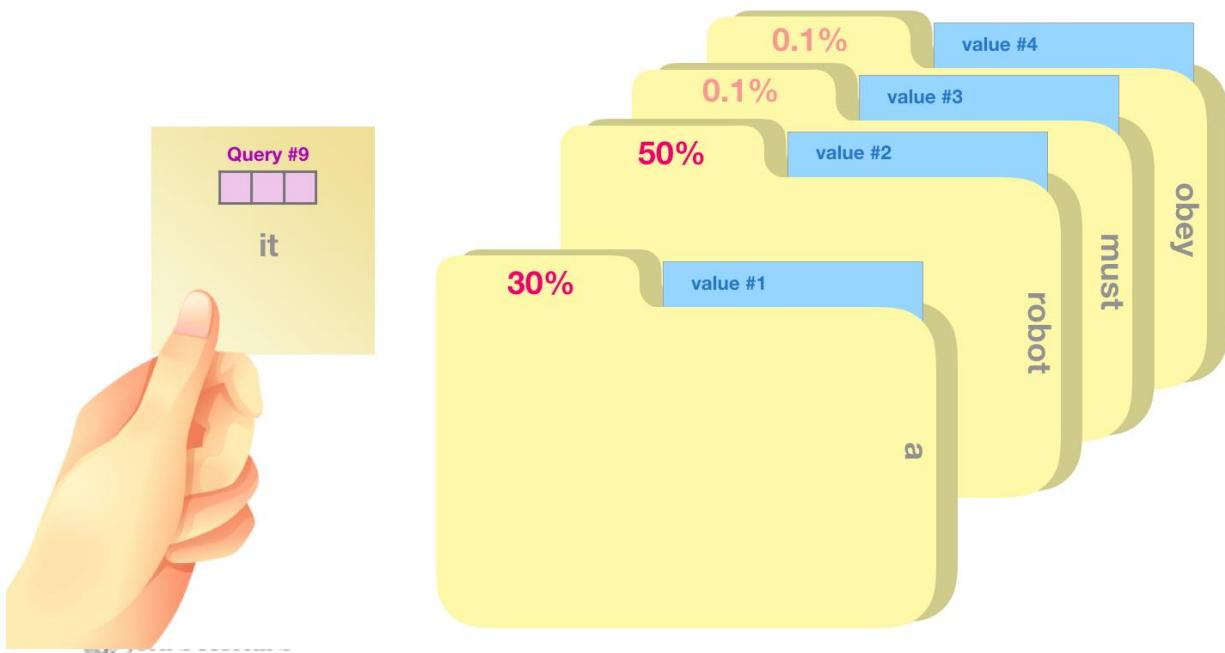
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 - **Query**: to match others
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q : query (to match others)
 $q_i = W^q x_i$

k : key (to be matched)
 $k_i = W^k x_i$

v : value (information to be extracted)
 $v_i = W^v x_i$



q : query (to match others)

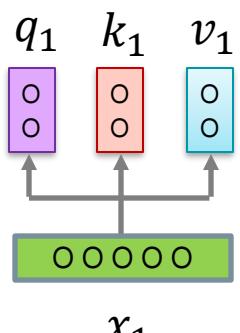
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The

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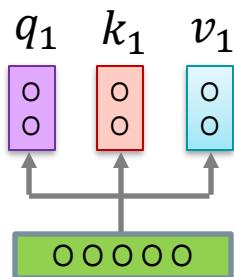
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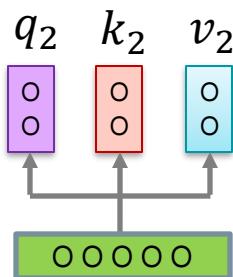
v: value (information to be extracted)

$$v_i = W^v x_i$$



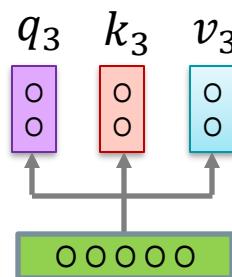
x_1

The



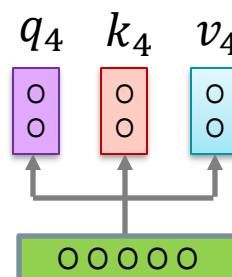
x_2

cat



x_3

sat



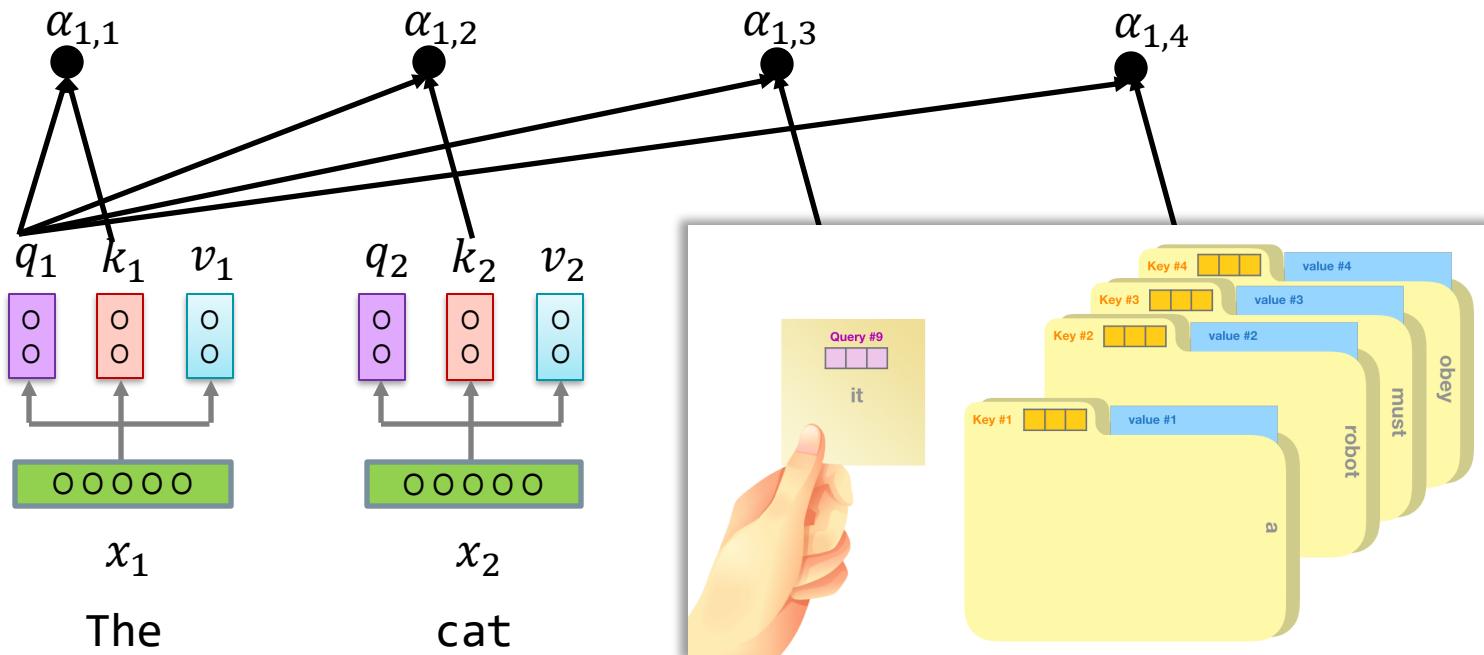
x_4

on

$$\alpha_{1,i} = \frac{q^1 \cdot k^i}{\sqrt{d}}$$

Scaled dot product

How much
should "The"
attend to other
positions?



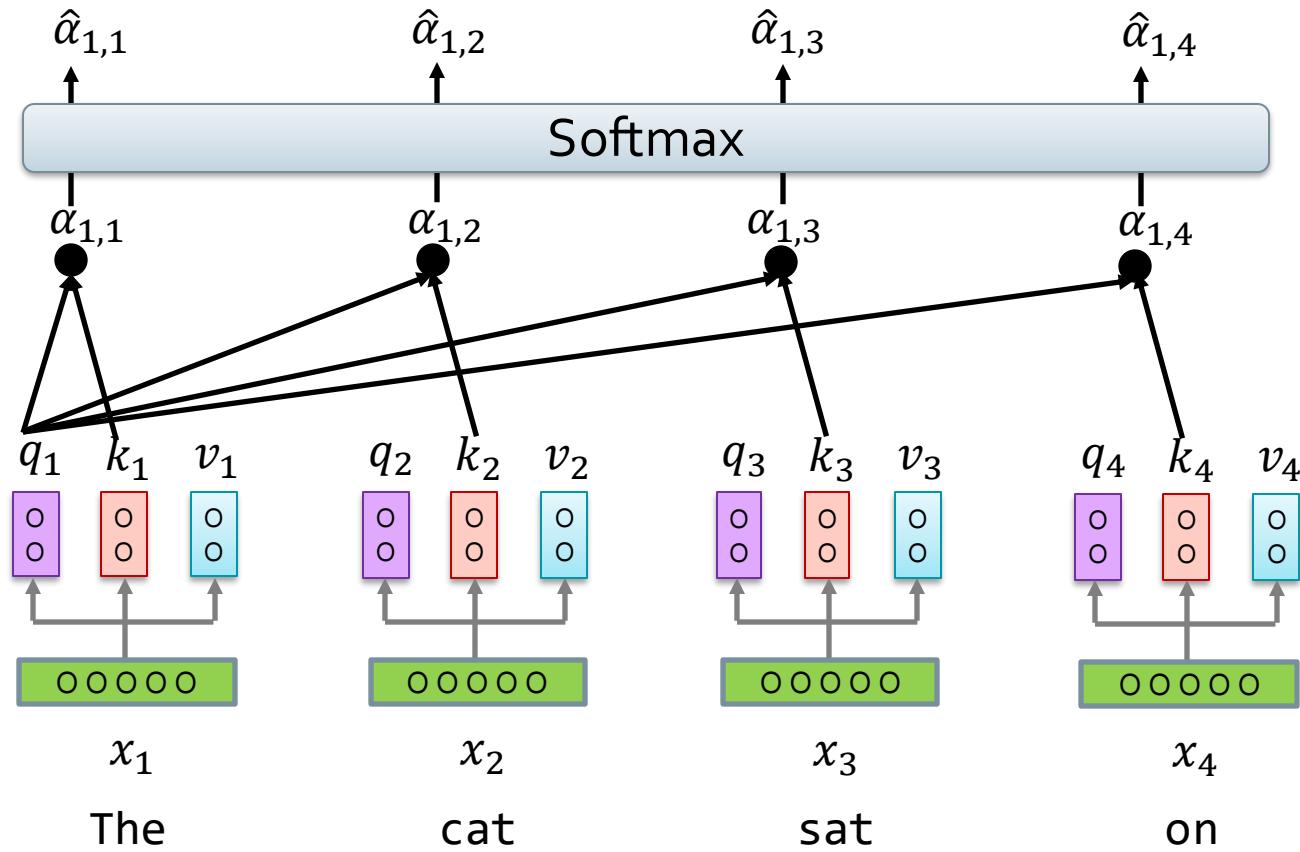
q : query (to match others)

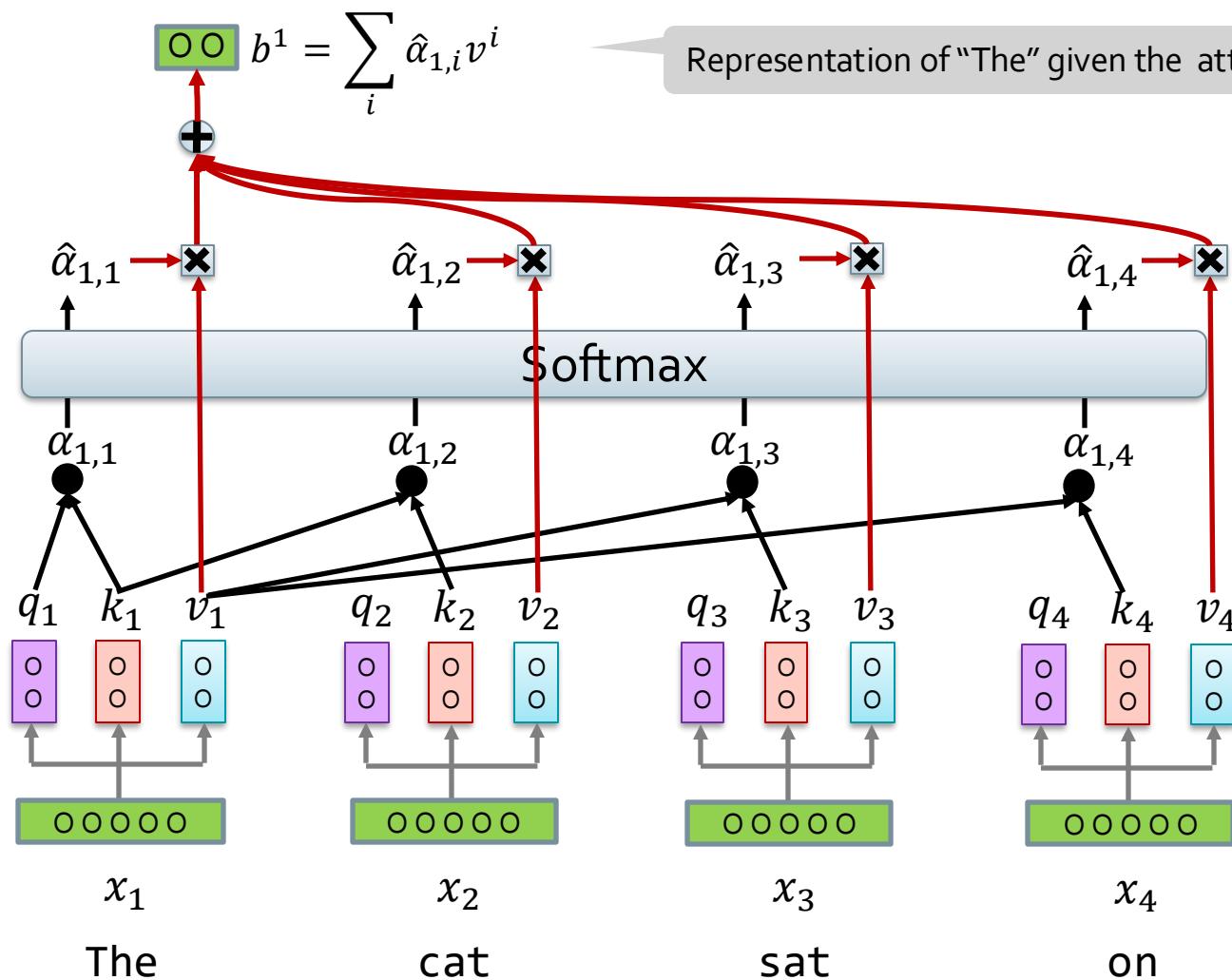
k : key (to be matched)

v : value (information to be extracted)

$$\sigma(z)_i = \frac{\exp(z_i)}{\sum_j \exp(z_j)}$$

How much
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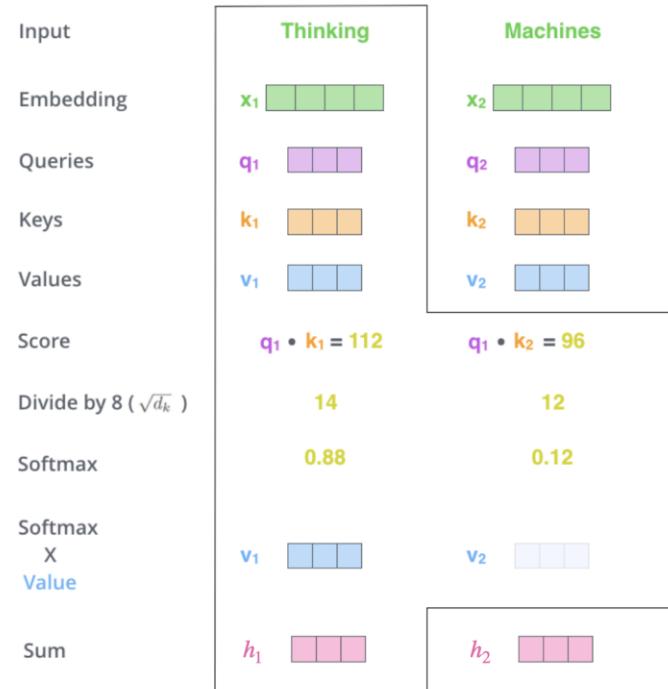




Question

- What would be the output vector for the word “Thinking”?

- (a) $0.5\mathbf{v}_1 + 0.5\mathbf{v}_2$
- (b) $0.54\mathbf{v}_1 + 0.46\mathbf{v}_2$
- (c) $0.88\mathbf{v}_1 + 0.12\mathbf{v}_2$
- (d) $0.12\mathbf{v}_1 + 0.88\mathbf{v}_2$



Self-Attention: Matrix Notation

$$X \in \mathbb{R}^{n \times d_1} \quad (n = \text{input length})$$

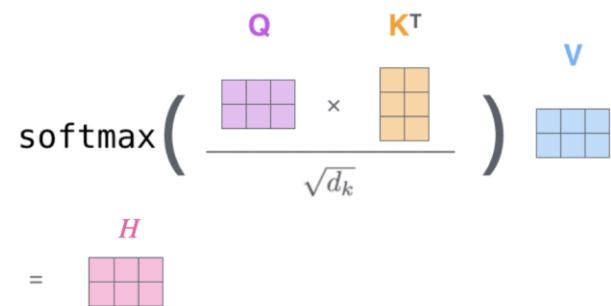
$$Q = XW^Q \quad K = XW^K \quad V = XW^V$$

$$W^Q \in \mathbb{R}^{d_1 \times d_q}, W^K \in \mathbb{R}^{d_1 \times d_k}, W^V \in \mathbb{R}^{d_1 \times d_v}$$

$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)V$$

n × d_q *d_k × n* *n*:

Q: What is this softmax operation?

$$\text{softmax}\left(\frac{\begin{matrix} Q \\ \times \\ K^T \end{matrix}}{\sqrt{d_k}}\right) \begin{matrix} V \\ = \\ H \end{matrix}$$


Self-Attention

- Can write it in matrix form:
- Given input \mathbf{x} :

$$Q = \mathbf{W}^q \mathbf{x}$$

$$K = \mathbf{W}^k \mathbf{x}$$

$$V = \mathbf{W}^v \mathbf{x}$$

$$\text{Attention}(\mathbf{x}) = \text{softmax}\left(\frac{QK^T}{\sqrt{d}}\right)V$$



hardmaru
@hardmaru

...

The most important formula in deep learning after 2018

Self-Attention

What is self-attention? Self-attention calculates a weighted average of feature representations with the weight proportional to a similarity score between pairs of representations. Formally, an input sequence of n tokens of dimensions d , $X \in \mathbf{R}^{n \times d}$, is projected using three matrices $W_Q \in \mathbf{R}^{d \times d_q}$, $W_K \in \mathbf{R}^{d \times d_k}$, and $W_V \in \mathbf{R}^{d \times d_v}$ to extract feature representations Q , K , and V , referred to as query, key, and value respectively with $d_k = d_q$. The outputs Q , K , V are computed as

$$Q = XW_Q, \quad K = XW_K, \quad V = XW_V. \quad (1)$$

So, self-attention can be written as,

$$S = D(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_q}}\right)V, \quad (2)$$

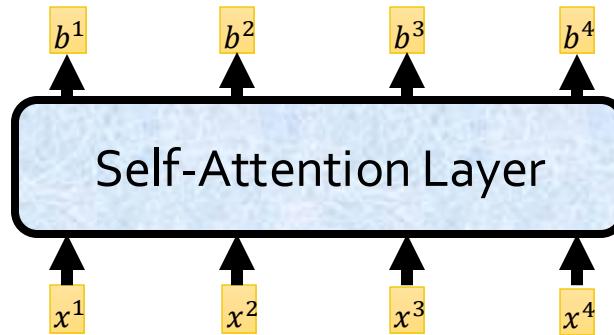
where softmax denotes a *row-wise* softmax normalization function. Thus, each element in S depends on all other elements in the same row.

9:08 PM · Feb 9, 2021 · Twitter Web App

553 Retweets 42 Quote Tweets 3,338 Likes

Self-Attention: Back to Big Picture

- **Attention** is a powerful mechanism to create context-aware representations
- A way to focus on select parts of the input



- Better at maintaining **long-distance dependencies** in the context.

Computational and Space Complexity

- The attention function:

$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)V$$

- $\dim(QK^T) = N^2 \rightarrow O(N^2 d_k)$ time complexity to calculate QK .
- Attention matrix $\dim\left(\text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)\right) = N \times N$
 - Storing the attention matrix for each head $\rightarrow O(N^2 h)$.
- If $N \gg d_k, h$, the time and space complexity is $O(N^2)$.
 - Scalability, resource consumption, adoption, etc.

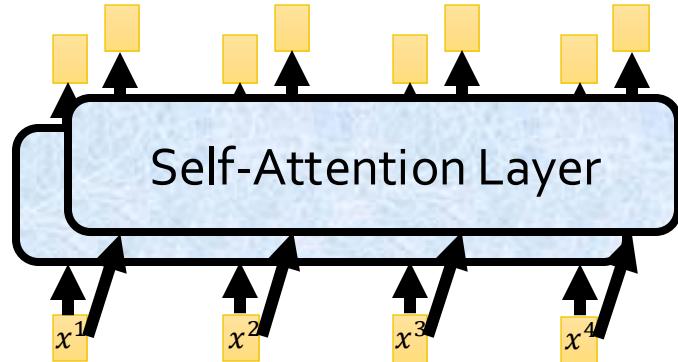
Computational and Space Complexity (2)

Layer Type	Complexity per Layer	Sequential Operations
Self-Attention	$O(n^2 \cdot d)$	$O(1)$
Recurrent	$O(n \cdot d^2)$	$O(n)$

- n = sequence length, d = hidden dimension
- Quadratic complexity, but:
 - $O(1)$ sequential operations (not linear like in RNN)
- Can be efficiently parallelized

Multi-Headed Self-Attention

- Multiple parallel attention layers.
 - Each attention layer has its own parameters.
 - Concatenate the results and run them through a linear projection.
- Main idea: Allows model to jointly attend to information from different representation subspaces (like ensembling)

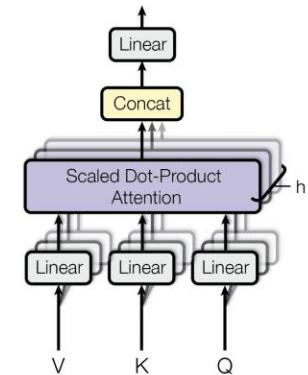


Multi-Headed Self-Attention

- Just concatenate all the heads and apply an output projection matrix.

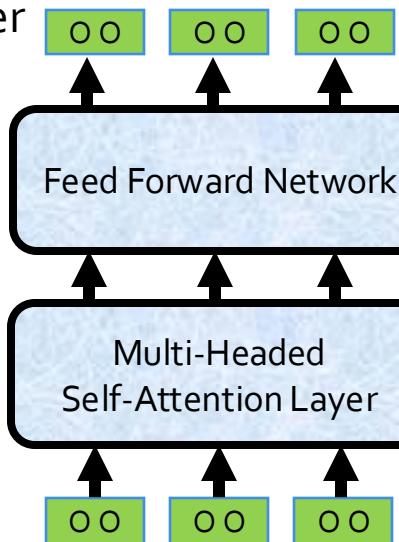
$$\begin{aligned}\text{head}_i &= \text{Attention}(\mathbf{W}_i^q \mathbf{x}, \mathbf{W}_i^k \mathbf{x}, \mathbf{W}_i^v \mathbf{x}) \\ \text{MultiHead}(Q, K, V) &= \text{Concat}(\text{head}_1, \dots, \text{head}_h) \mathbf{W}^o\end{aligned}$$

- In practice, we use a reduced dimension for each head.
 - Denote: d = hidden dimension, m = number of heads
$$\mathbf{W}_i^q \in \mathbb{R}^{d \times \frac{d}{m}}, \quad \mathbf{W}_i^k \in \mathbb{R}^{d \times \frac{d}{m}}, \quad \mathbf{W}_i^v \in \mathbb{R}^{d \times \frac{d}{m}}, \quad \mathbf{W}^o \in \mathbb{R}^{d \times d}$$
- The total computational cost is similar to that of single-head attention with full dimensionality.

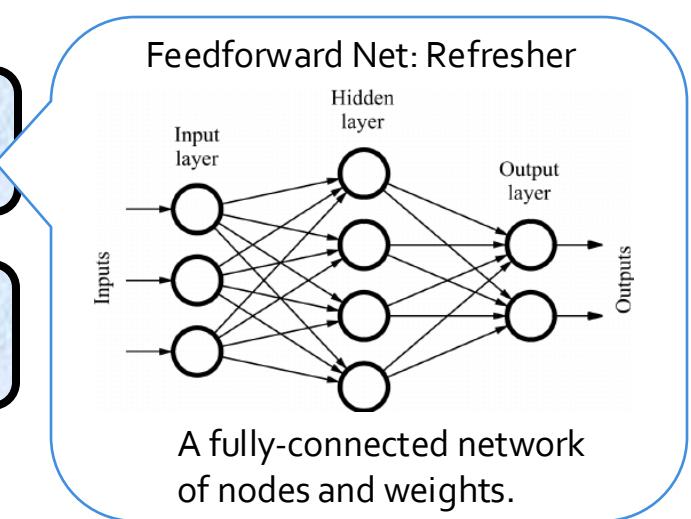


Combine with FFN

- Add a **feed-forward network** on top it to add more expressivity.
 - This allows the model to apply another transformation to the contextual representations (or “post-process” them).
 - Usually, the dimensionality of the hidden feedforward layer is 2-8 times larger than the input dimension.

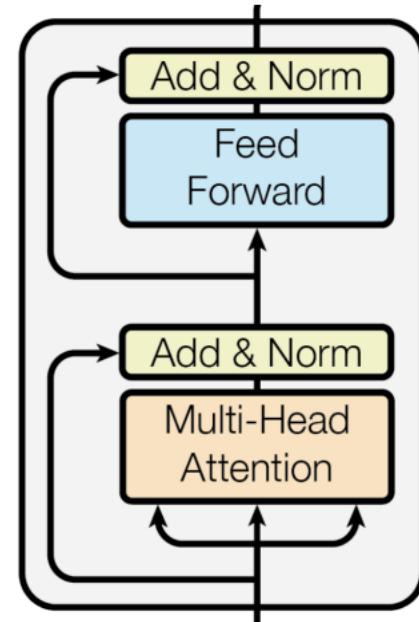


$$\text{FFN}(\mathbf{x}) = f(cW_1 + b_1)W_2 + b_2$$



How Do We Prevent Vanishing Gradients?

- Residual connections let the model “skip” layers
 - These connections are particularly useful for training deep networks
- Use layer normalization to stabilize the network and allow for proper gradient flow

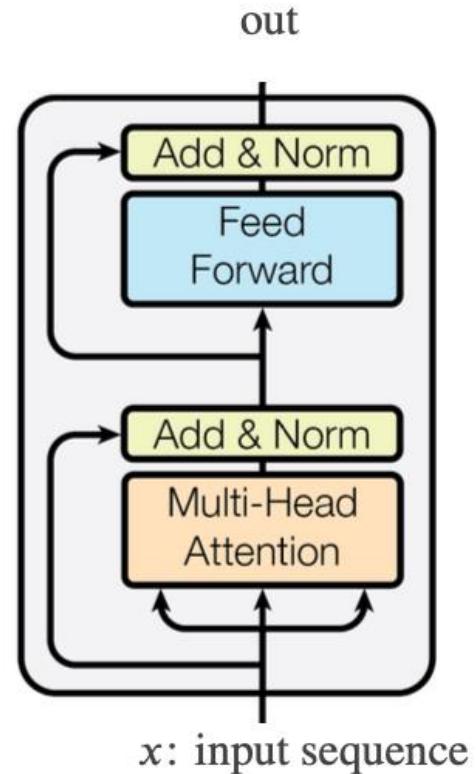


Putting it Together: Self-Attention Block

Given input \mathbf{x} :

$$\begin{aligned}\text{out} &= LN(\tilde{\mathbf{c}} + \mathbf{c}') \\ \tilde{\mathbf{c}} &= \text{FFN}(\mathbf{c}') = f(\mathbf{c}'W_1 + b_1)W_2 + b_2\end{aligned}$$

$$\begin{aligned}\mathbf{c}' &= LN(\mathbf{c} + \mathbf{x}) \\ \mathbf{c} &= \text{MultiHeadedAttention}(\mathbf{x}; \mathbf{W}^q, \mathbf{W}^k, \mathbf{W}^v)\end{aligned}$$



Summary: Self-Attention Block

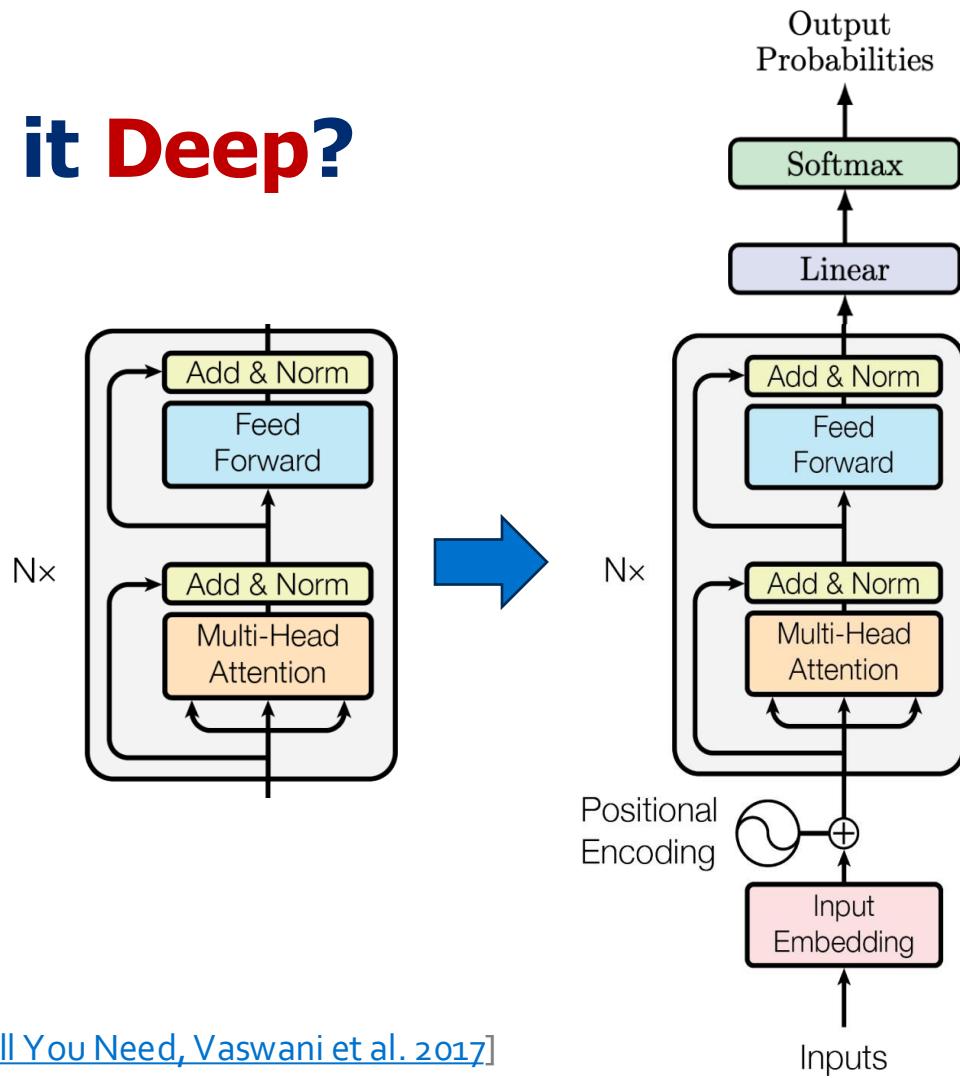
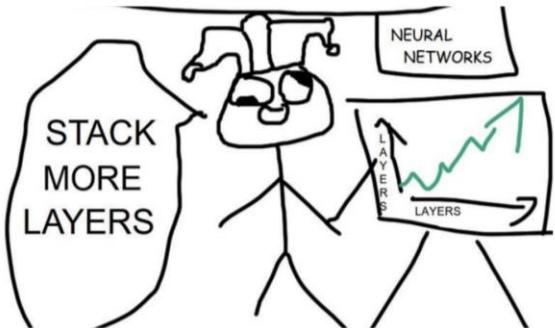
- **Self-Attention:** A critical building block of modern language models.
 - The idea is to compose meanings of words weighted according some similarity notion.
- **Next:** We will combine self-attention blocks to build various architectures known as Transformer.



Transformer

How Do We Make it Deep?

- Stack more layers!



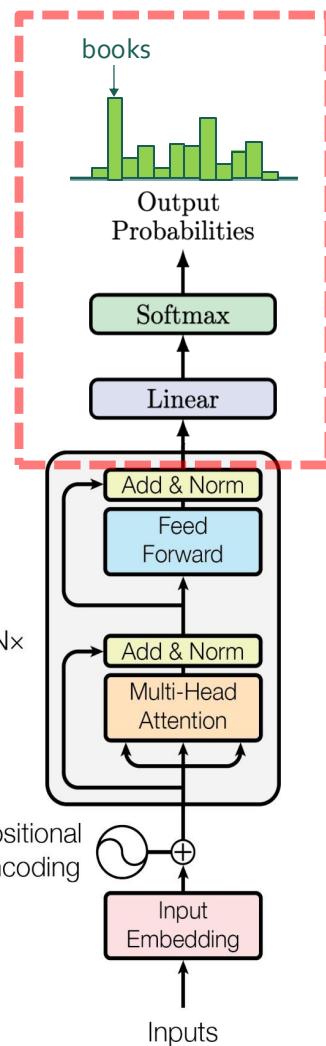
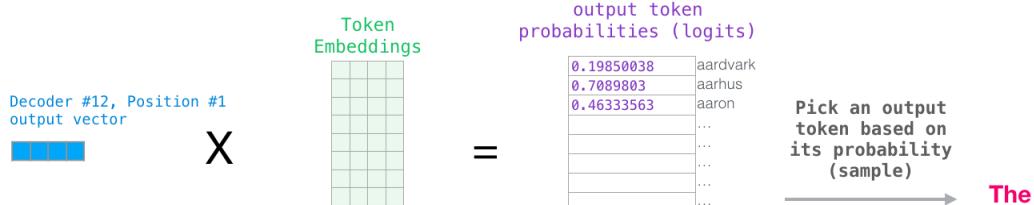
From Representations to Prediction

- To perform prediction, add a classification head on top of the final layer of the transformer.
- This can be per token (Language modeling)
- Or can be for the entire sequence (only one token)

$\text{out} \in \mathbb{R}^{S \times d}$ (S : Sequence length)

$\text{logits} = \text{Linear}_{(d, V)}(\text{out}) = f(\text{out} \cdot W_V) \in \mathbb{R}^{S \times V}$

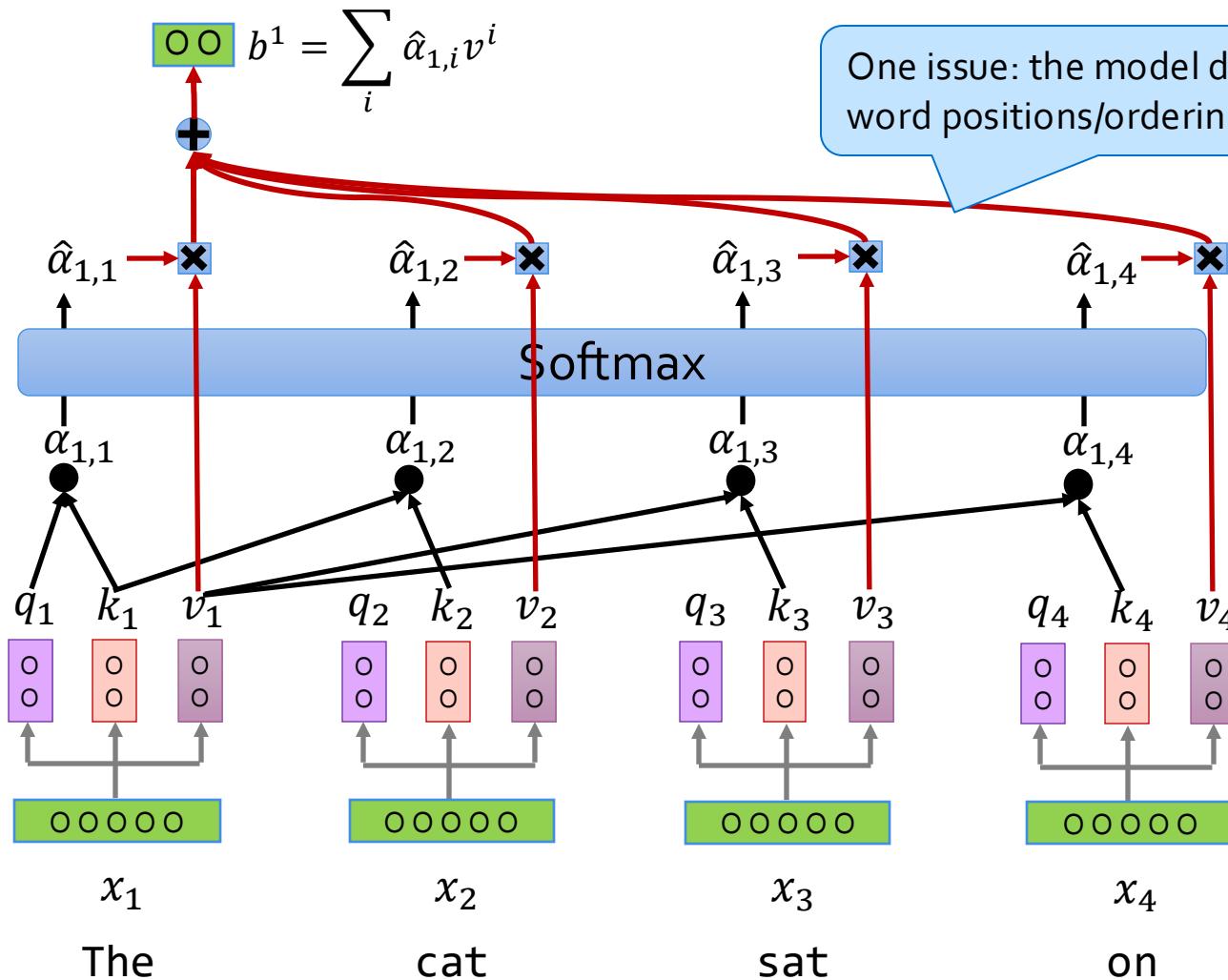
$\text{probabilities} = \text{softmax}(\text{logits}) \in \mathbb{R}^{S \times V}$





One last wrinkle though ...

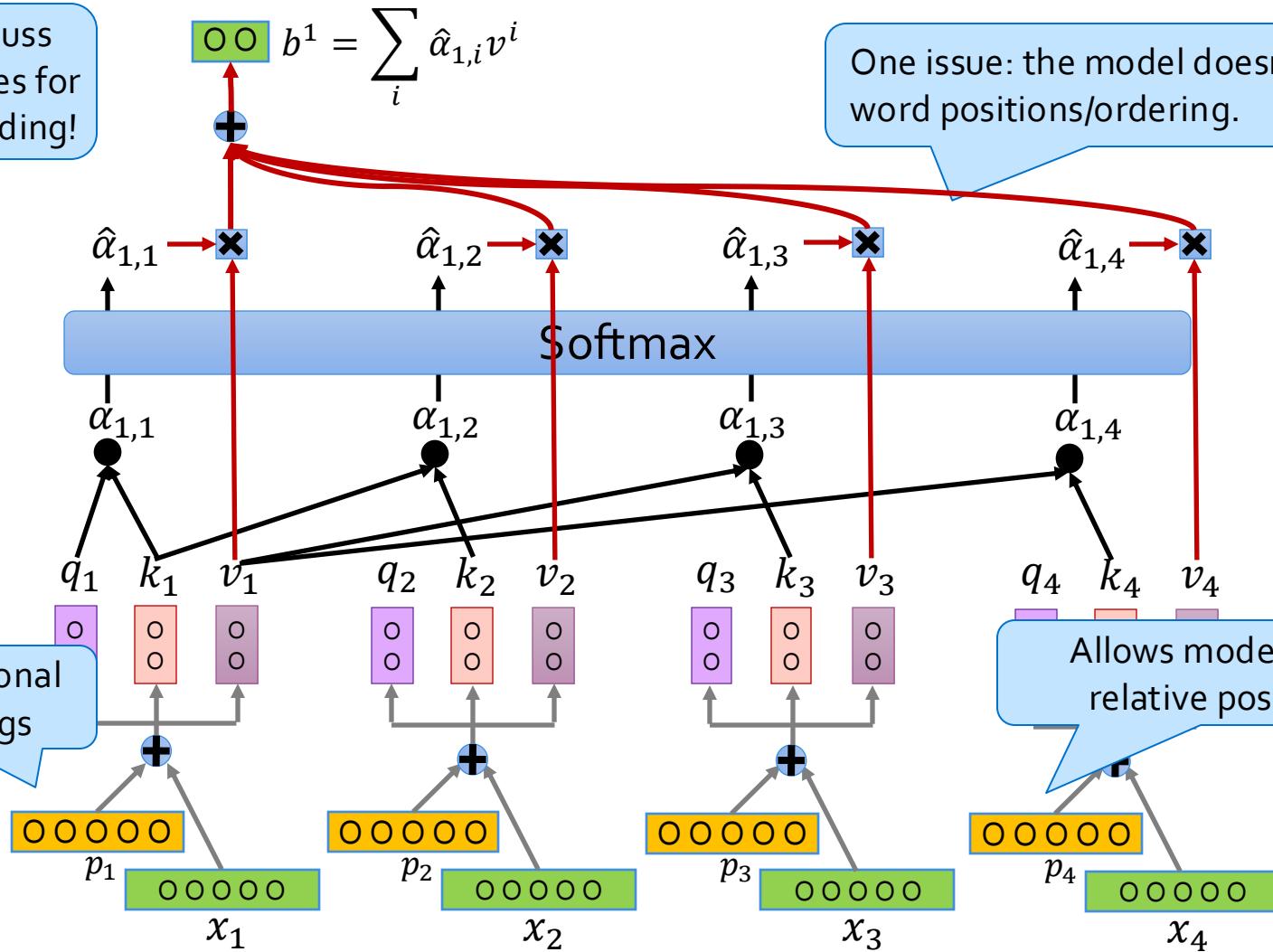




We will discuss various choices for these embedding!

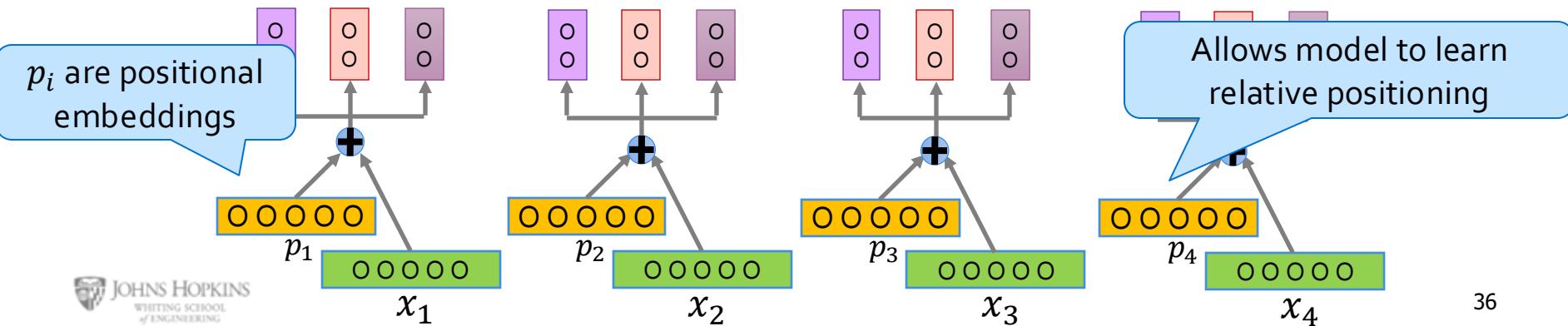
$$OO = b^1 + \sum_i \hat{\alpha}_{1,i} v^i$$

One issue: the model doesn't know word positions/ordering.



Absolute Positional Embeddings

- Why “add”? Why not, say, “concatenate and then project”?
 - “concatenate and then project” would be a more general approach with more trainable parameters.
 - In practice, “sum” works fine that
 - The intuition here is that “summing” forms point clouds of word embedding information around position embeddings unique to each position.



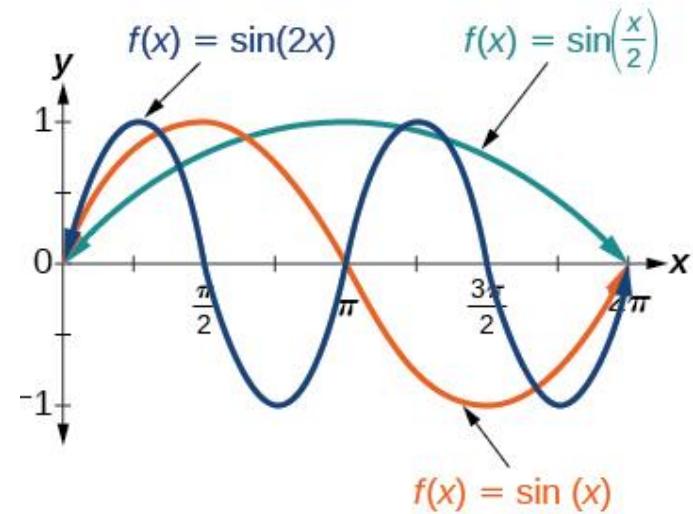
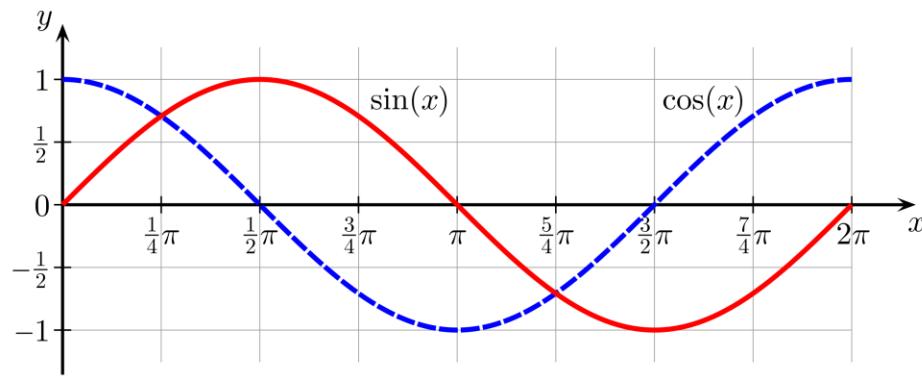
Absolute Positional Embeddings

- The idea is to create vectors that uniquely encoder each position.
- For example, consider vectors of binary values.
 - Example below shows 4-dimensional position encodings for 16 positions.

0 :	0	0	0	0	8 :	1	0	0	0
1 :	0	0	0	1	9 :	1	0	0	1
2 :	0	0	1	0	10 :	1	0	1	0
3 :	0	0	1	1	11 :	1	0	1	1
4 :	0	1	0	0	12 :	1	1	0	0
5 :	0	1	0	1	13 :	1	1	0	1
6 :	0	1	1	0	14 :	1	1	1	0
7 :	0	1	1	1	15 :	1	1	1	1

The issue with binary encoding is that the positional information is localized around a few bits.

Math Recap: Sine and Cosine Functions



Absolute Positional Embeddings

- Let t be a desired position. Then the i -th element of the positional vector is:

$$\vec{p}_t^{(i)} = f(t)^{(i)} := \begin{cases} \sin(\omega_k \cdot t), & \text{if } i = 2k \\ \cos(\omega_k \cdot t), & \text{if } i = 2k + 1 \end{cases} \quad \omega_k = \frac{1}{10000^{2k/d}}$$

- Here d is the maximum dimension.
- This provides unique vectors for each position.

Quiz

- Let t be a desired position:

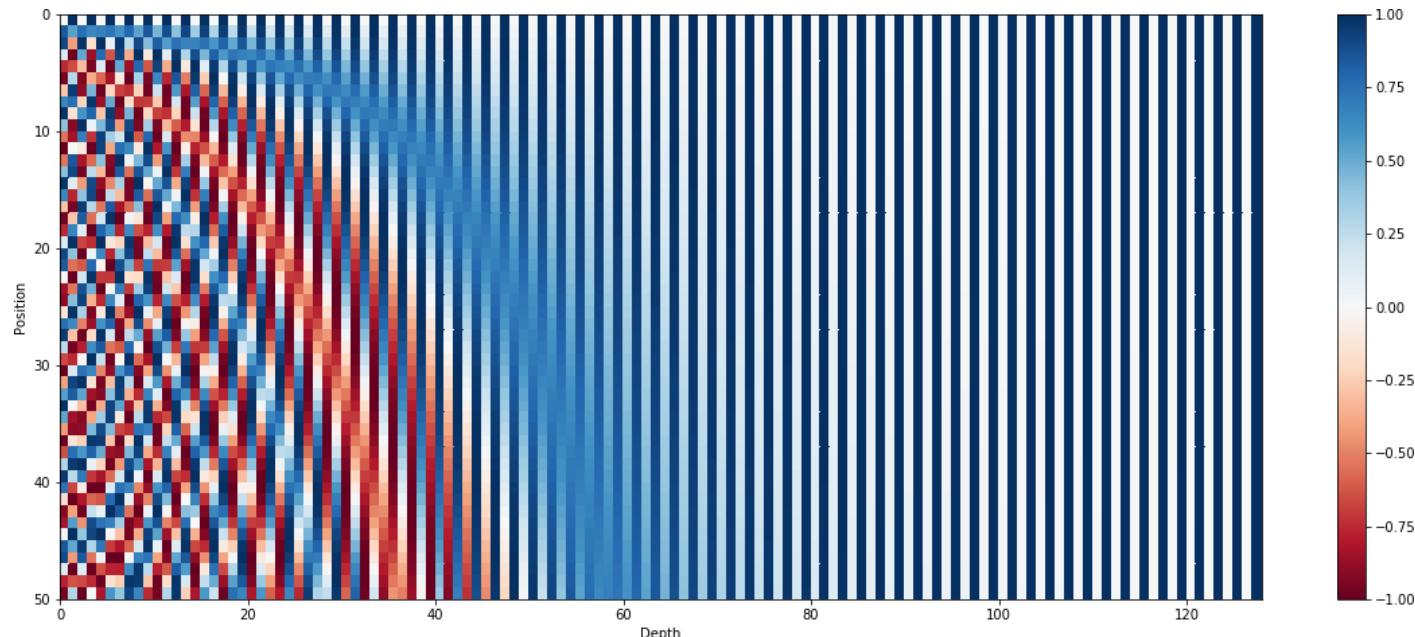
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$$\omega_k = \frac{1}{10000^{2k/d}}$$

- Q:** Are the frequencies increasing with dimension i ?
- Answer:** The frequencies are decreasing along the vector dimension.

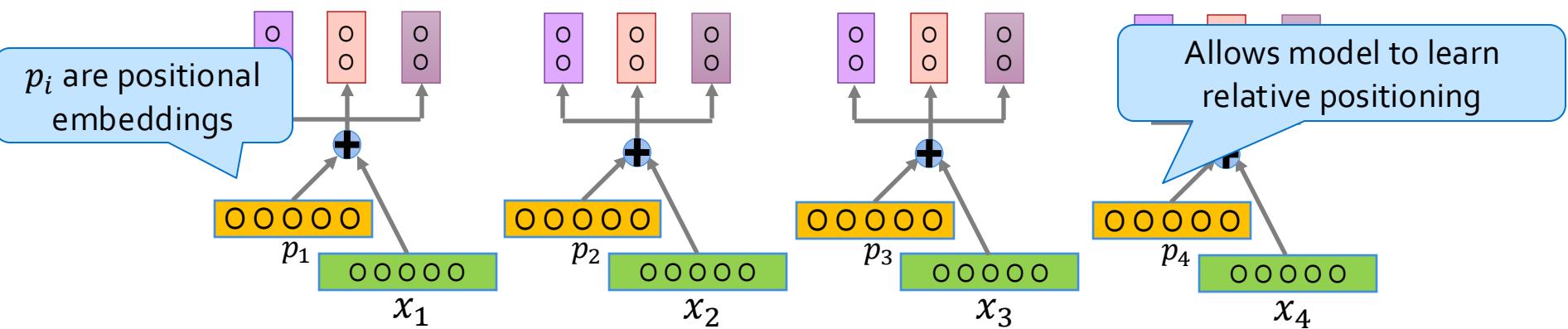
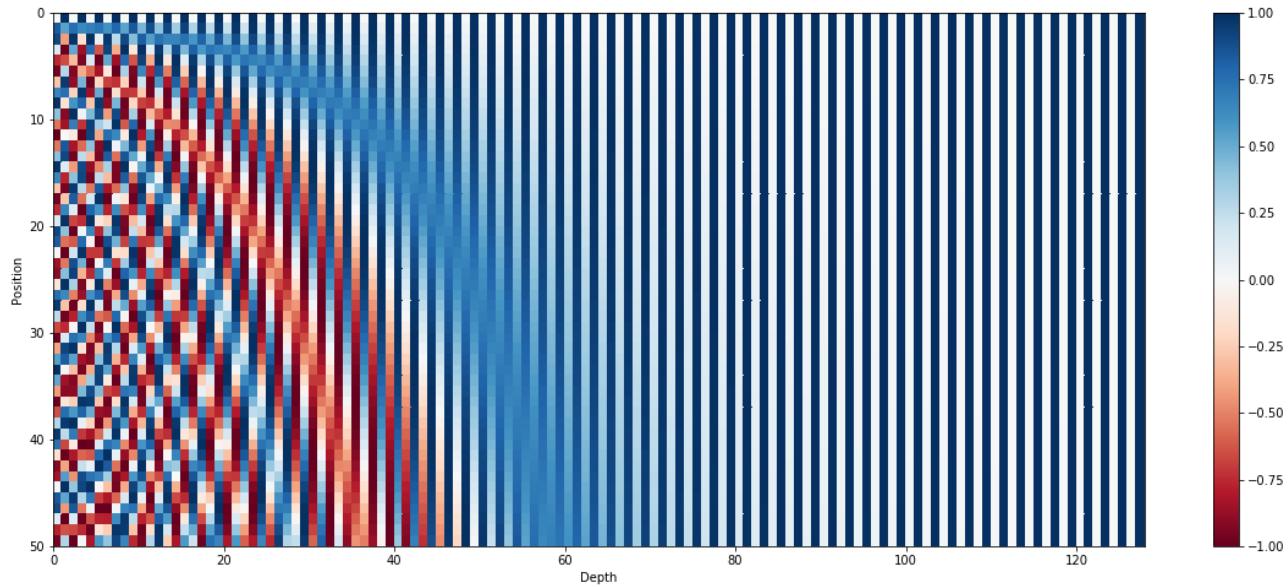
Visualizing Absolute Positional Embeddings

- Here positions range from 0-50, for an embedding dimension of 130.

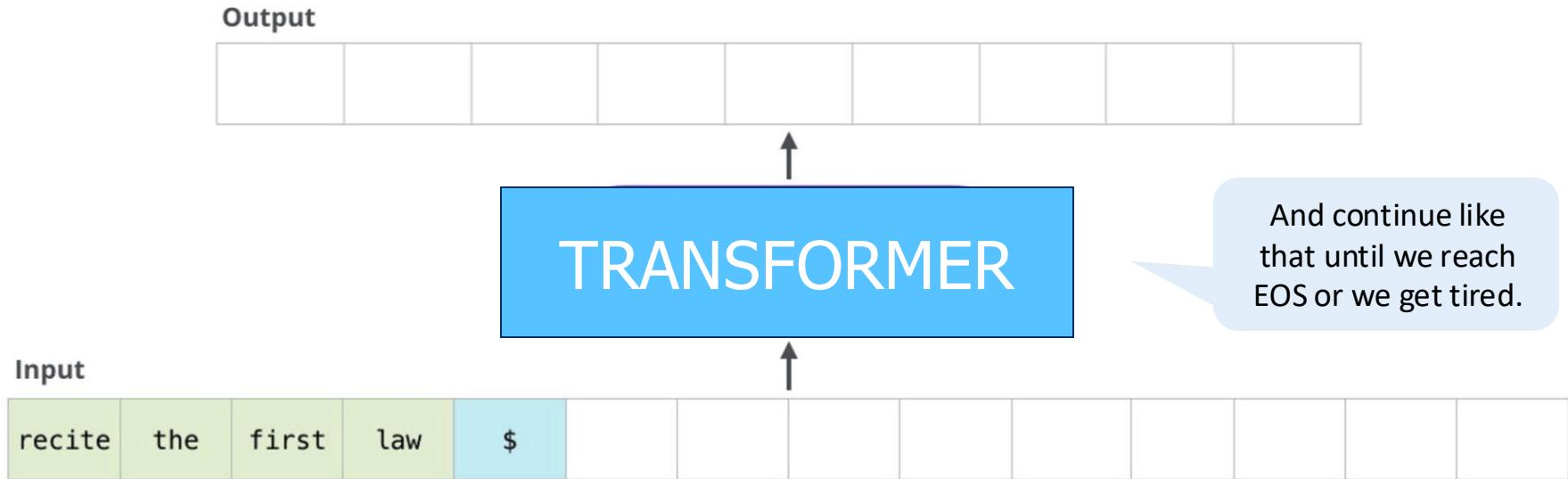


An approach:
Sine/Cosine encoding

$$p_i = \begin{cases} \sin(i/10000^{2*1/d}) \\ \cos(i/10000^{2*1/d}) \\ \vdots \\ \sin(i/10000^{2*\frac{d}{2}/d}) \\ \cos(i/10000^{2*\frac{d}{2}/d}) \end{cases}$$



Transformer-based Language Modeling



Training a Transformer Language Model

- **Goal:** Train a Transformer for language modeling (i.e., predicting the next word).
- **Approach:** Train it so that each position is predictor of the next (right) token.
 - We just shift the input to right by one, and use as labels

(gold output) $Y = \text{cat sat on the mat } </s>$

EOS special token



TRANSFORMER

$X = \text{the cat sat on the mat}$

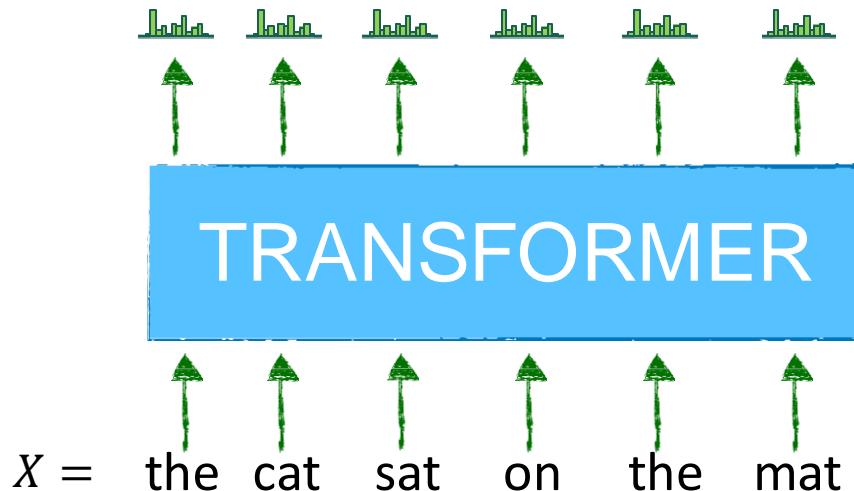
```
X = text[:, :-1]  
Y = text[:, 1:]
```

[Slide credit: Arman Cohan]

Training a Transformer Language Model

- For each position, compute their corresponding **distribution** over the whole vocab.

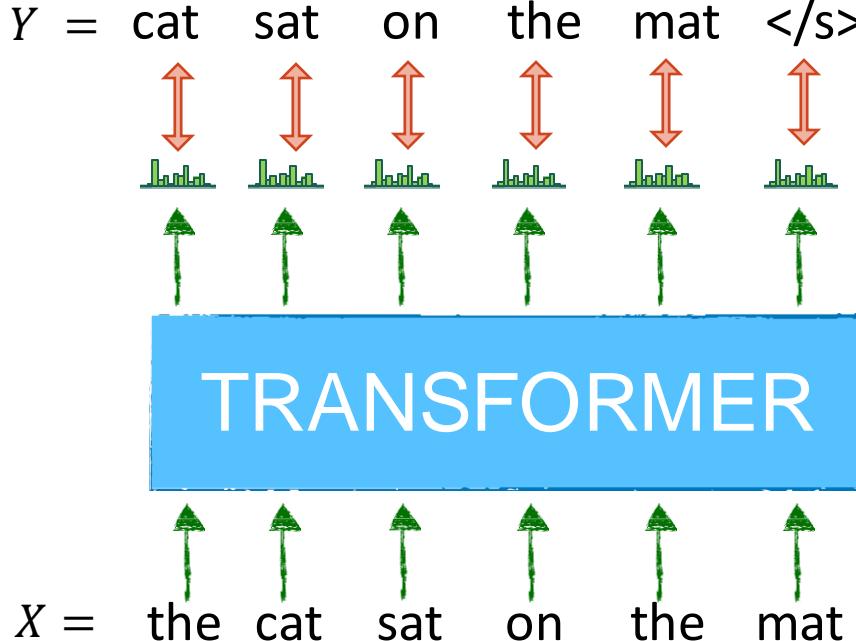
(gold output) $Y = \text{cat sat on the mat } </s>$



Training a Transformer Language Model

- For each position, compute the **loss** between the distribution and the gold output label.

(gold output) $Y = \text{cat sat on the mat } </s>$

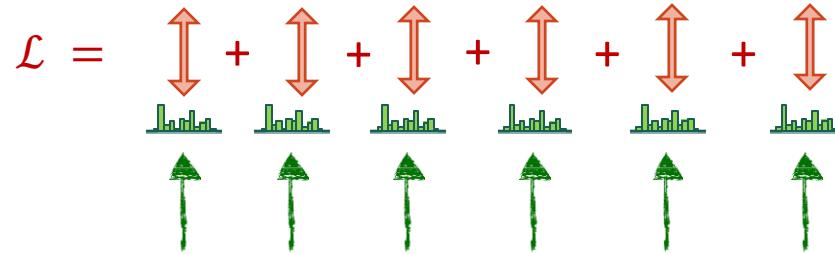


Training a Transformer Language Model

- Sum the position-wise loss values to obtain a **global loss**.

(gold output) $Y = \text{cat sat on the mat } </s>$

$$\mathcal{L} = \text{cat} + \text{sat} + \text{on} + \text{the} + \text{mat} + </s>$$

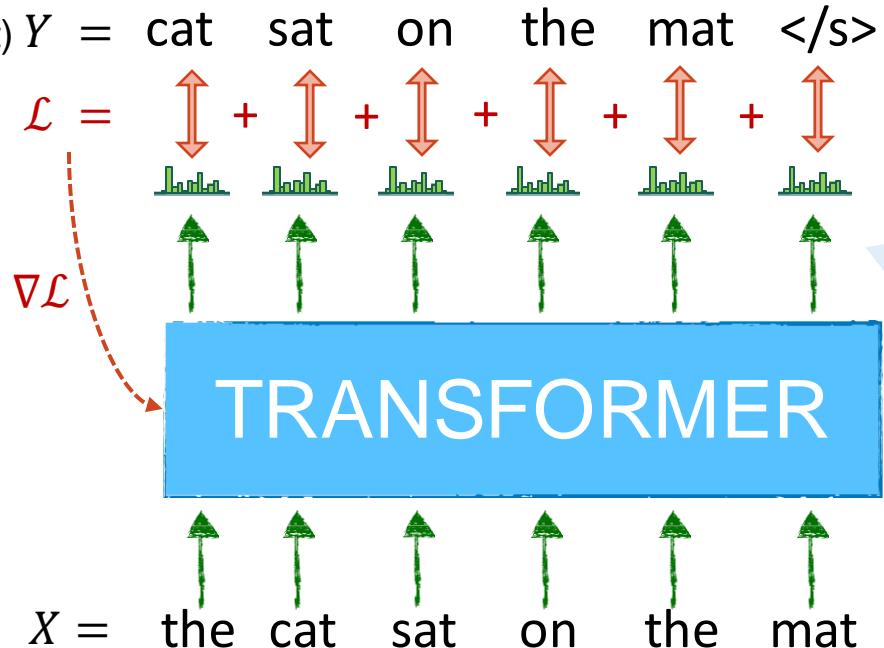


$X = \text{the cat sat on the mat}$

Training a Transformer Language Model

- Using this loss, do **Backprop** and **update** the Transformer parameters.

(gold output) $Y = \text{cat sat on the mat } </s>$

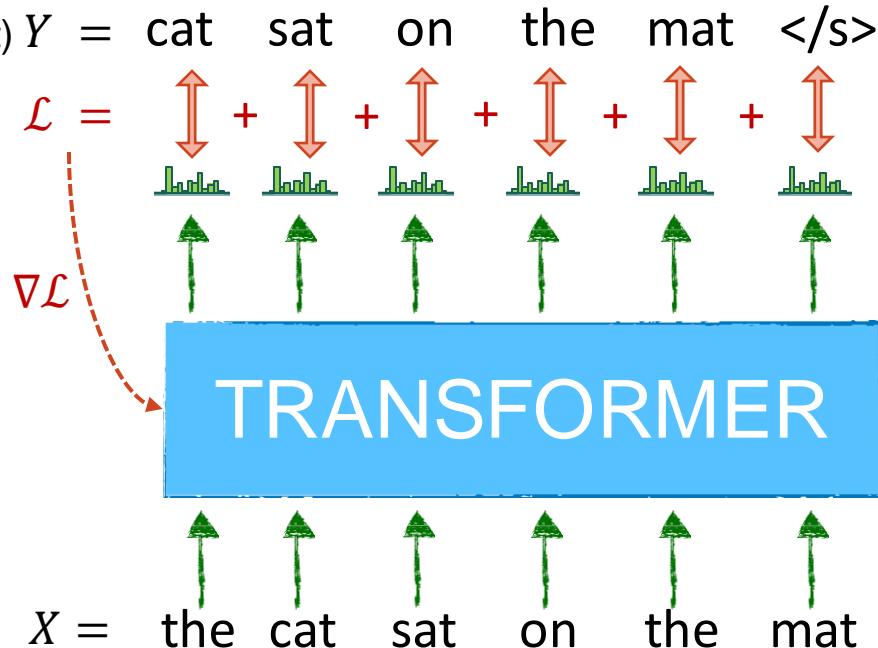


Well, this is not quite right 😊
...
what is the problem with this?

Training a Transformer Language Model

- The model would solve the task by **copying** the next token to output (data leakage).
 - Does **not** learn anything useful

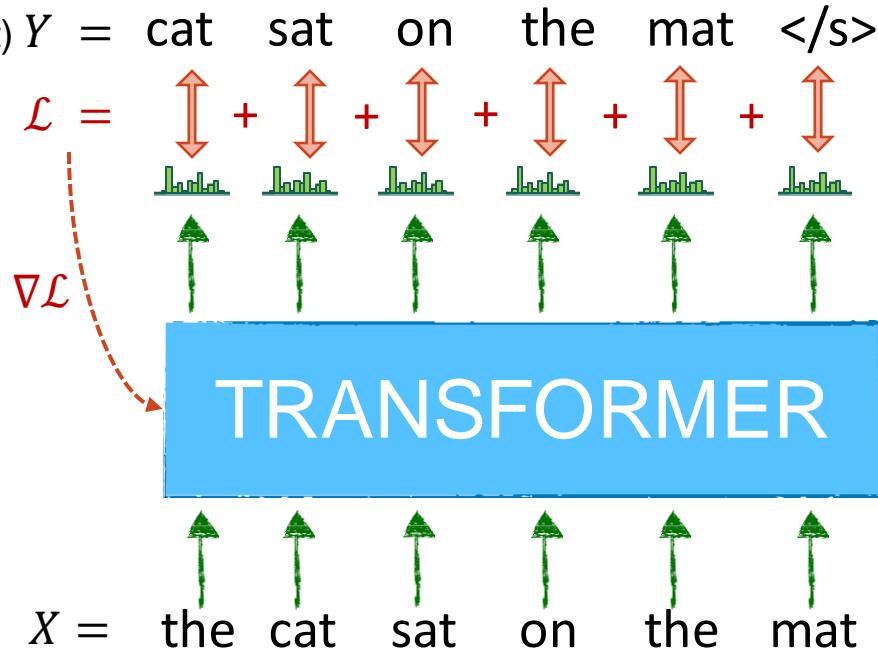
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Training a Transformer Language Model

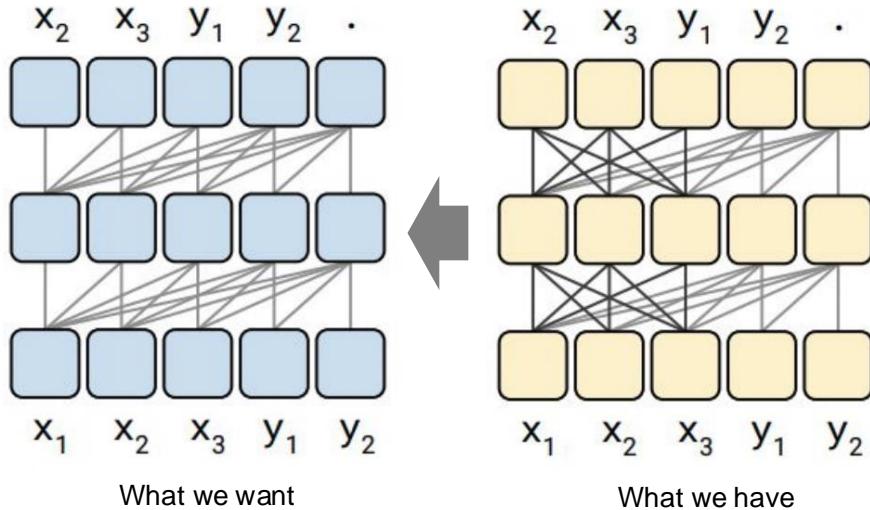
- We need to **prevent information leakage** from future tokens! How?

(gold output) $Y = \text{cat sat on the mat } </s>$

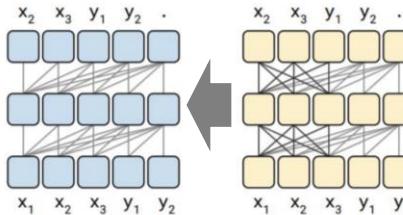


Attention mask

Attention raw scores												
0	-0.08	1.24	0.69	-0.98	1.43	-0.6	0.7	0.16	0.93	1.28	-1.61	-1.1
1	-0.09	-0.0	-0.7	0.06	0.25	0.23	0.26	0.18	0.78	-0.21	-1.01	1.01
2	0.86	1.19	1.59	0.86	-0.13	-0.15	-2.13	-0.98	-0.87	-1.72	1.87	-0.72
3	0.12	-0.03	-0.02	0.88	-0.46	-0.7	0.54	-0.42	-1.89	-0.38	0.04	-0.84
4	0.51	0.17	0.13	-1.64	0.24	-0.02	1.68	-0.36	0.64	0.36	0.27	0.66
5	0.24	-1.44	0.43	0.74	0.96	-1.21	-0.31	1.54	1.66	1.14	0.58	-1.44
6	0.26	-0.1	0.93	0.72	-0.38	1.65	0.47	-0.96	-0.17	-0.9	-1.57	0.22
7	-0.55	0.81	0.71	1.7	-0.8	-1.14	-0.32	1.78	-0.7	-0.04	1.54	0.81
8	0.74	-0.76	-0.44	-0.08	-1.38	-0.13	1.25	-1.37	1.84	0.3	0.57	0.74
9	-0.97	-0.91	0.15	0.35	-0.81	0.11	1.14	-1.52	1.06	1.87	0.5	-0.3
10	1.56	0.9	0.39	1.46	1.44	-1.05	0.9	-0.73	0.36	-0.67	-0.62	-0.43
11	0.32	0.74	0.44	-0.1	1.19	0.83	0.29	2.06	0.51	-0.26	1.51	0.11



Attention mask



Attention raw scores

	1	2	3	4	5	6	7	8	9	10	11	12
0	-0.08	1.24	0.69	-0.98	1.43	-0.6	0.7	0.16	0.93	1.28	-1.61	-1.1
1	-0.09	-0.0	-0.7	0.06	0.25	0.23	0.26	0.18	0.78	-0.21	-1.01	1.01
2	0.86	1.19	1.59	0.86	-0.13	-0.15	-2.13	-0.98	-0.87	-1.72	1.87	-0.72
3	0.12	-0.03	-0.02	0.88	-0.46	-0.7	0.54	-0.42	-1.89	-0.38	0.04	-0.84
4	0.51	0.17	0.13	-1.64	0.24	-0.02	1.68	-0.36	0.64	0.36	0.27	0.66
5	0.24	-1.44	0.43	0.74	0.96	-1.21	-0.31	1.54	1.66	1.14	0.58	-1.44
6	0.26	-0.1	0.93	0.72	-0.38	1.65	0.47	-0.96	-0.17	-0.9	-1.57	0.22
7	-0.55	0.81	0.71	1.7	-0.8	-1.14	-0.32	1.78	-0.7	-0.04	1.54	0.81
8	0.74	-0.76	-0.44	-0.08	-1.38	-0.13	1.25	-1.37	1.84	0.3	0.57	0.74
9	-0.97	-0.91	0.15	0.35	-0.81	0.11	1.14	-1.52	1.06	1.87	0.5	-0.3
10	1.56	0.9	0.39	1.46	1.44	-1.05	0.9	-0.73	0.36	-0.67	-0.62	-0.43
11	0.32	0.74	0.44	-0.1	1.19	0.83	0.29	2.06	0.51	-0.26	1.51	0.11

Attention mask

	0	1	2	3	4	5	6	7	8	9	10	11
0	1.0	-inf										
1	1.0	1.0	-inf									
2	1.0	1.0	1.0	-inf								
3	1.0	1.0	1.0	1.0	-inf							
4	1.0	1.0	1.0	1.0	1.0	-inf						
5	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf	-inf	-inf	-inf
6	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf	-inf	-inf
7	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf	-inf
8	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf
9	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf
10	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf
11	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf

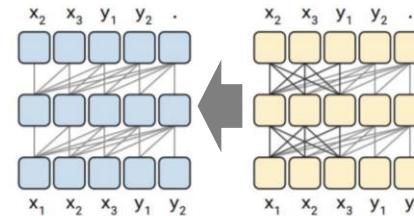


large negative numbers,
which leads to $\text{softmax}(-\infty) \approx 0$

Attention mask

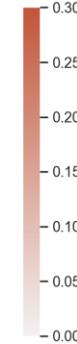
Attention raw scores												
0	-0.08	1.24	0.69	-0.98	1.43	-0.6	0.7	0.16	0.93	1.28	-1.61	-1.1
1	-0.09	-0.0	-0.7	0.06	0.25	0.23	0.26	0.18	0.78	-0.21	-1.01	1.01
2	0.86	1.19	1.59	0.86	-0.13	-0.15	-2.13	-0.98	-0.87	-1.72	1.87	-0.72
3	0.12	-0.03	-0.02	0.88	-0.46	-0.7	0.54	-0.42	-1.89	-0.38	0.04	-0.84
4	0.51	0.17	0.13	-1.64	0.24	-0.02	1.68	-0.36	0.64	0.36	0.27	0.66
5	0.24	-1.44	0.43	0.74	0.96	-1.21	-0.31	1.54	1.66	1.14	0.58	-1.44
6	0.26	-0.1	0.93	0.72	-0.38	1.65	0.47	-0.96	-0.17	-0.9	-1.57	0.22
7	-0.55	0.81	0.71	1.7	-0.8	-1.14	-0.32	1.78	-0.7	-0.04	1.54	0.81
8	0.74	-0.76	-0.44	-0.08	-1.38	-0.13	1.25	-1.37	1.84	0.3	0.57	0.74
9	-0.97	-0.91	0.15	0.35	-0.81	0.11	1.14	-1.52	1.06	1.87	0.5	-0.3
10	1.56	0.9	0.39	1.46	1.44	-1.05	0.9	-0.73	0.36	-0.67	-0.62	-0.43
11	0.32	0.74	0.44	-0.1	1.19	0.83	0.29	2.06	0.51	-0.26	1.51	0.11

X



Attention mask

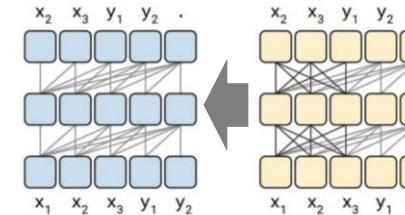
0	1	2	3	4	5	6	7	8	9	10	11
0	1.0	-inf									
1	1.0	1.0	-inf								
2	1.0	1.0	1.0	-inf							
3	1.0	1.0	1.0	1.0	-inf						
4	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf	-inf	-inf	-inf
5	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf	-inf	-inf
6	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf	-inf
7	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf	-inf
8	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf	-inf
9	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf
10	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	-inf
11	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0



Note matrix multiplication is quite fast in GPUs.

Arman Cohan

Attention mask



Attention raw scores												
x	1	2	3	4	5	6	7	8	9	10	11	12
o	0.08	1.34	0.09	0.39	1.43	-0.1	0.7	0.16	0.66	1.08	1.01	-1.1
o	-0.09	0.5	-0.7	0.9	0.25	0.28	0.28	0.18	0.78	-0.21	1.01	1.01
o	0.09	1.19	0.98	0.98	0.15	0.15	-0.11	0.05	-0.07	1.97	-0.72	
o	0.12	0.03	-0.02	0.88	-0.46	-0.1	0.54	-0.42	1.04	-0.38	0.04	0.86
o	0.51	0.17	0.5	0.54	0.24	-0.02	0.68	-0.36	0.64	0.37	0.27	0.89
o	0.28	-1.04	0.43	0.74	0.98	1.1	-0.31	1.54	1.06	1.14	0.98	-1.41
o	0.26	-0.1	0.63	0.72	0.39	0.84	0.47	0.96	-0.17	-0.5	1.01	0.22
o	0.05	0.81	0.77	1.7	-0.8	1.16	-0.32	1.78	-0.7	-0.04	1.54	0.81
o	0.76	-0.76	-0.84	0.88	-1.31	0.13	1.25	-1.37	1.84	0.3	0.57	0.74
o	0.97	-0.91	0.15	0.35	0.81	0.11	1.14	-1.12	1.08	1.07	0.5	-0.23
o	0.02	0.74	0.44	0.1	1.19	0.83	0.29	2.06	0.01	-0.26	1.51	0.11

Raw attention scores												
x	1	2	3	4	5	6	7	8	9	10	11	12
o	1.14	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07
o	0.07	1.14	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07
o	0.07	0.07	1.14	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07
o	0.07	0.07	0.07	1.14	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07
o	0.07	0.07	0.07	0.07	1.14	0.07	0.07	0.07	0.07	0.07	0.07	0.07
o	0.07	0.07	0.07	0.07	0.07	1.14	0.07	0.07	0.07	0.07	0.07	0.07
o	0.07	0.07	0.07	0.07	0.07	0.07	1.14	0.07	0.07	0.07	0.07	0.07
o	0.07	0.07	0.07	0.07	0.07	0.07	0.07	1.14	0.07	0.07	0.07	0.07
o	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	1.14	0.07	0.07	0.07
o	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	1.14	0.07	0.07
o	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	1.14	0.07
o	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	1.14

X

=

Masked attention raw scores

0	-0.08	-inf	-inf	-inf	-inf	-inf						
1	-0.09	-0.0	-inf	-inf	-inf	-inf	-inf	-inf	-inf	-inf	-inf	-inf
2	0.86	1.19	1.59	-inf	-inf	-inf	-inf	-inf	-inf	-inf	-inf	-inf
3	0.12	-0.03	-0.02	0.88	-inf	-inf	-inf	-inf	-inf	-inf	-inf	-inf
4	0.51	0.17	0.13	-1.64	0.24	-inf	-inf	-inf	-inf	-inf	-inf	-inf
5	0.24	-1.44	0.43	0.74	0.96	-1.21	-inf	-inf	-inf	-inf	-inf	-inf
6	0.26	-0.1	0.93	0.72	-0.38	1.65	0.47	-inf	-inf	-inf	-inf	-inf
7	-0.55	0.81	0.71	1.7	-0.8	-1.14	-0.32	1.78	-inf	-inf	-inf	-inf
8	0.74	-0.76	-0.44	-0.08	-1.38	-0.13	1.25	-1.37	1.84	-inf	-inf	-inf
9	-0.97	-0.91	0.15	0.35	-0.81	0.11	1.14	-1.52	1.06	1.87	-inf	-inf
10	1.56	0.9	0.39	1.46	1.44	-1.05	0.9	-0.73	0.36	-0.67	-0.62	-inf
11	0.32	0.74	0.44	-0.1	1.19	0.83	0.29	2.06	0.51	-0.26	1.51	0.11

Slide credit: Arman Cohan

Attention mask

The effect is more than just pruning out some of the wirings in self-attention block.

Attention raw scores												
	1	2	3	4	5	6	7	8	9	10	11	12
o	0.08	1.34	0.09	0.39	1.43	-0.1	0.7	0.16	0.66	1.08	1.01	-1.1
-o	-0.09	-0.05	-0.7	0.09	0.25	0.29	0.26	0.18	0.76	-0.21	1.01	1.01
>	0.09	1.19	1.99	0.98	-0.15	0.15	-0.11	-0.05	-0.07	-0.12	1.97	-0.72
<	0.12	-0.03	-0.02	-0.89	-0.46	-0.7	0.54	-0.42	1.06	-0.38	0.04	-0.86
=	0.01	0.17	0.55	0.54	0.24	0.02	1.08	-0.36	0.64	0.27	0.09	-1.04
#	0.28	-1.04	0.43	0.74	0.98	1.2	-0.31	1.54	1.06	1.14	0.08	-1.04
*	0.06	-0.1	0.03	0.72	0.39	1.04	0.47	0.96	-0.17	-0.5	1.01	0.22
.	0.05	0.81	0.71	1.7	-0.18	-0.32	1.78	-0.17	-0.04	-0.04	1.54	0.81
~	0.76	-0.76	-0.84	0.88	-0.31	0.13	1.25	1.37	1.04	0.3	0.57	0.76
g	0.97	0.01	0.15	0.35	0.81	0.11	1.14	-0.12	1.08	1.07	0.5	-0.3
g	1.00	0.09	0.39	1.46	1.44	1.05	0.9	0.73	0.36	-0.07	0.62	-0.43
z	0.02	0.74	0.44	0.1	1.19	0.83	0.29	2.06	0.01	-0.26	1.51	0.11

X

Raw attention scores												
	1	2	3	4	5	6	7	8	9	10	11	12
o	1.00	0.10	0.10	0.10	0.10	0.10	0.10	0.10	0.10	0.10	0.10	0.10
-o	-0.09	-0.05	-0.7	0.09	0.25	0.29	0.26	0.18	0.76	-0.21	1.01	1.01
>	0.09	1.19	1.99	0.98	-0.15	0.15	-0.11	-0.05	-0.07	-0.12	1.97	-0.72
<	0.12	-0.03	-0.02	-0.89	-0.46	-0.7	0.54	-0.42	1.06	-0.38	0.04	-0.86
=	0.01	0.17	0.55	0.54	0.24	0.02	1.08	-0.36	0.64	0.27	0.09	-1.04
#	0.28	-1.04	0.43	0.74	0.98	1.2	-0.31	1.54	1.06	1.14	0.08	-1.04
*	0.06	-0.1	0.03	0.72	0.39	1.04	0.47	0.96	-0.17	-0.5	1.01	0.22
.	0.05	0.81	0.71	1.7	-0.18	-0.32	1.78	-0.17	-0.04	-0.04	1.54	0.81
~	0.76	-0.76	-0.84	0.88	-0.31	0.13	1.25	1.37	1.04	0.3	0.57	0.76
g	0.97	0.01	0.15	0.35	0.81	0.11	1.14	-0.12	1.08	1.07	0.5	-0.3
g	1.00	0.09	0.39	1.46	1.44	1.05	0.9	0.73	0.36	-0.07	0.62	-0.43
z	0.02	0.74	0.44	0.1	1.19	0.83	0.29	2.06	0.01	-0.26	1.51	0.11

Masked attention raw scores												
	1	2	3	4	5	6	7	8	9	10	11	12
o	-0.08	-inf	inf	inf	inf							
-o	-0.09	-0.0	inf	inf	inf							
>	0.06	1.19	1.99	inf	inf	inf						
<	0.12	-0.03	-0.02	-0.89	-0.46	-0.7	0.54	-0.42	1.06	-0.38	0.04	-0.86
=	0.01	0.17	0.55	0.54	0.24	0.02	1.08	-0.36	0.64	0.27	0.09	-1.04
#	0.24	1.04	0.43	0.74	0.98	1.2	-0.31	1.54	1.06	1.14	0.08	-1.04
*	0.06	-0.1	0.03	0.72	0.39	1.04	0.47	0.96	-0.17	-0.5	1.01	0.22
.	0.05	0.81	0.71	1.7	-0.18	-0.32	1.78	-0.17	-0.04	-0.04	1.54	0.81
~	0.74	-0.76	-0.84	0.88	-0.31	0.13	1.25	1.37	1.04	0.3	0.57	0.76
g	0.97	0.01	0.15	0.35	0.81	0.11	1.14	-0.12	1.08	1.07	0.5	-0.3
g	1.00	0.09	0.39	1.46	1.44	1.05	0.9	0.73	0.36	-0.07	0.62	-0.43
z	0.02	0.74	0.44	0.1	1.19	0.83	0.29	2.06	0.01	-0.26	1.51	0.11

softmax

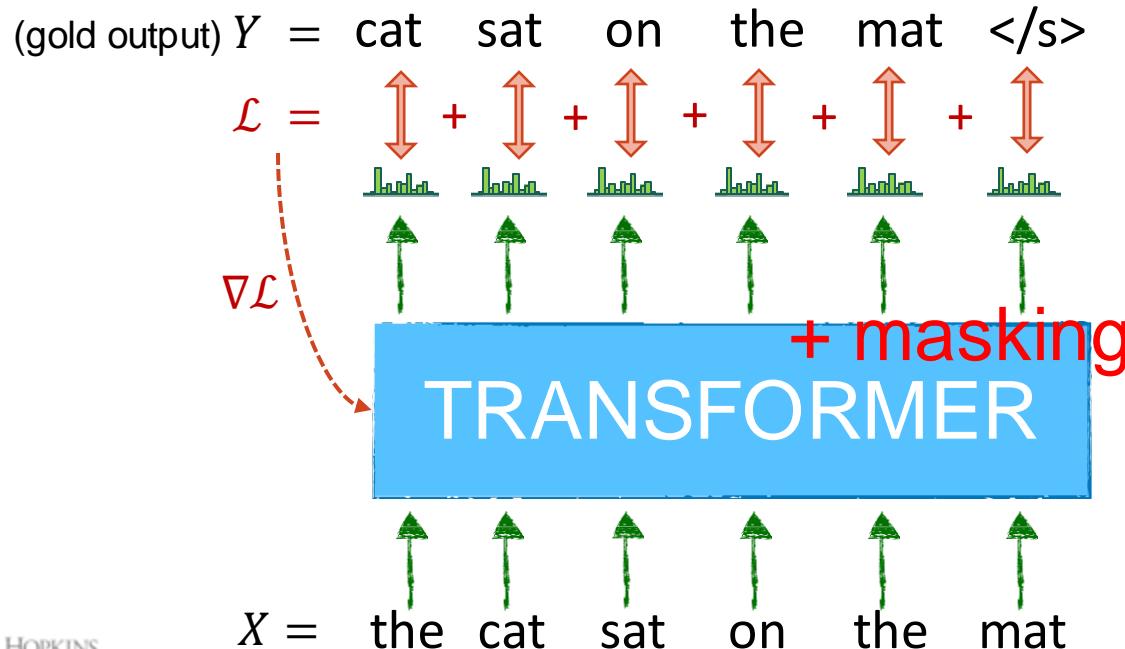


Slide credit: Alman Cohan



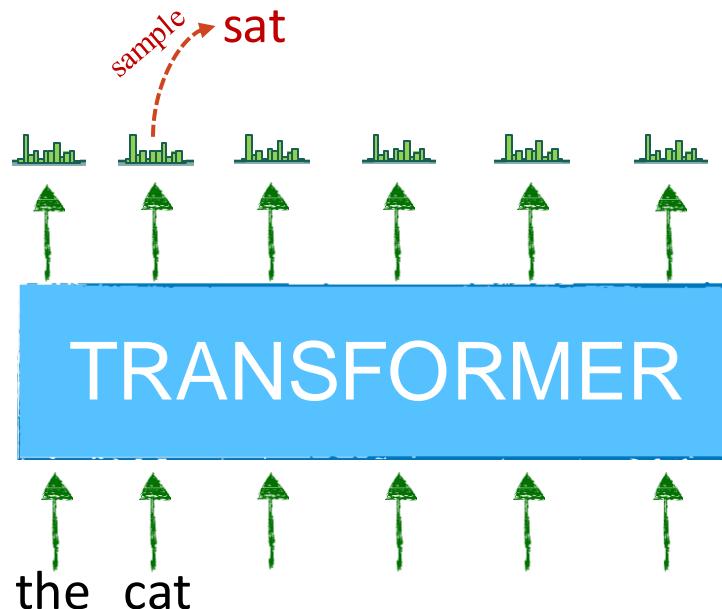
Training a Transformer Language Model

- We need to **prevent information leakage** from future tokens! How?



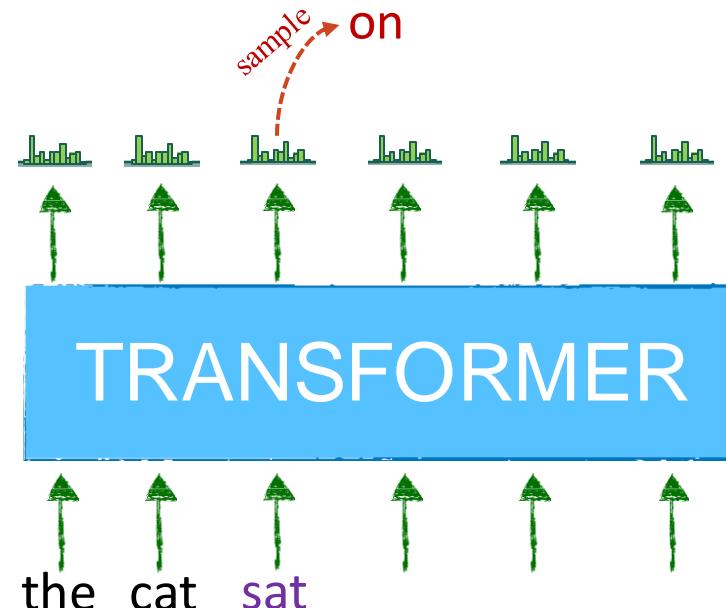
How to use the model to generate text?

- Use the output of previous step as input to the next step repeatedly



How to use the model to generate text?

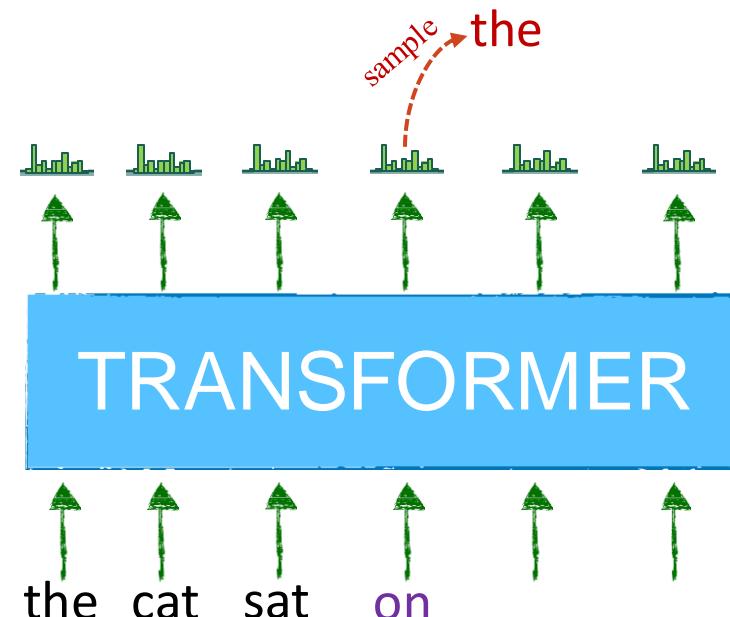
- Use the output of previous step as input to the next step repeatedly



The probabilities get revised upon adding a new token to the input.

How to use the model to generate text?

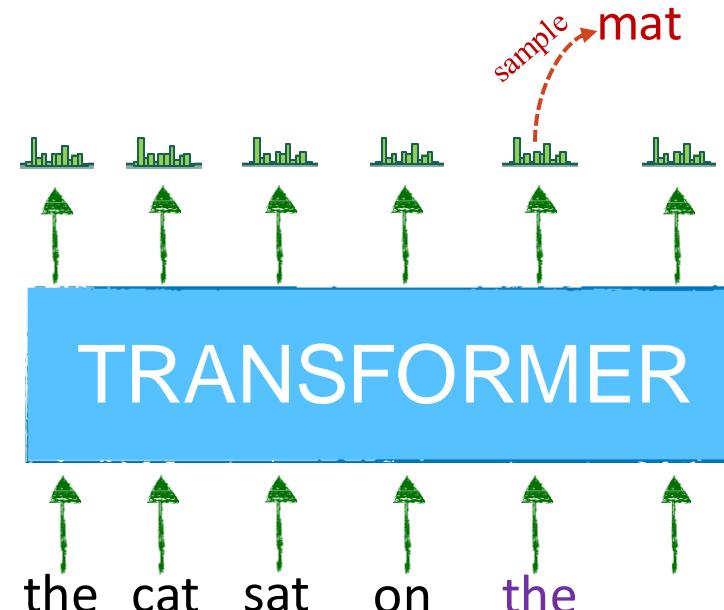
- Use the output of previous step as input to the next step repeatedly



The probabilities get revised upon adding a new token to the input.

How to use the model to generate text?

- Use the output of previous step as input to the next step repeatedly

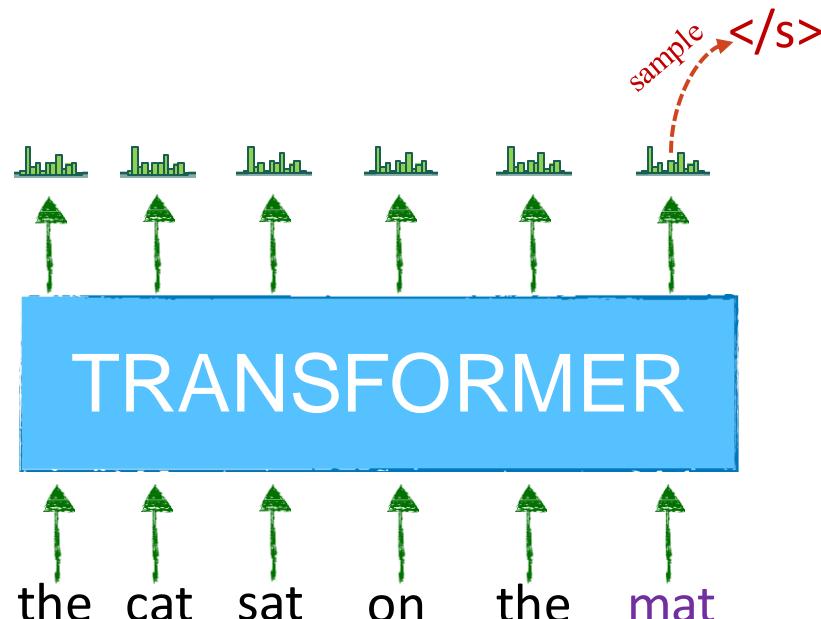


The probabilities get revised upon adding a new token to the input.

How to use the model to generate text?

- Use the output of previous step as input to the next step repeatedly

The probabilities get revised upon adding a new token to the input.



Summary

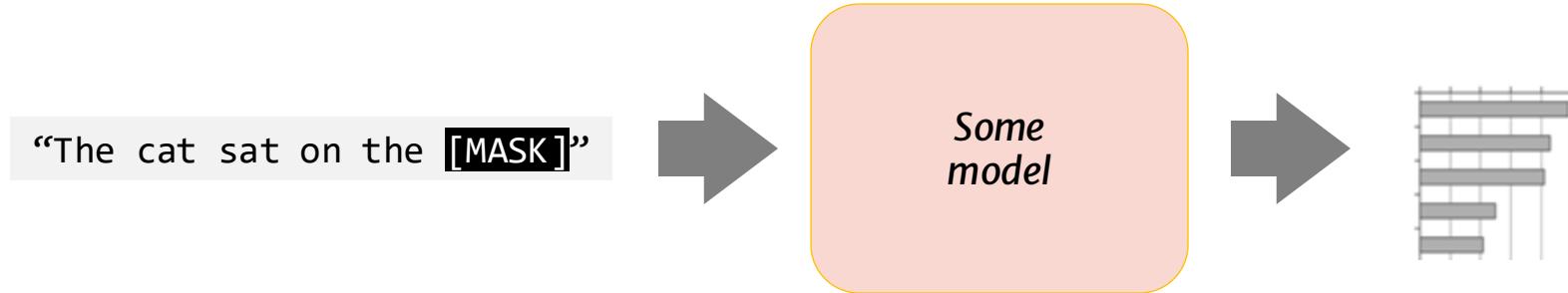
- This is a very generic Transformer!
- We will implement this in HW5 to build a simple Transformer Language Model!!
- **Next:**
 - Architectural variants



Transformer Architectural Variants

Encoder-Decoder Architectures

- It is useful to think of generative models as two sub-models.

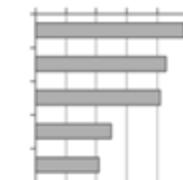
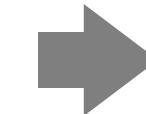
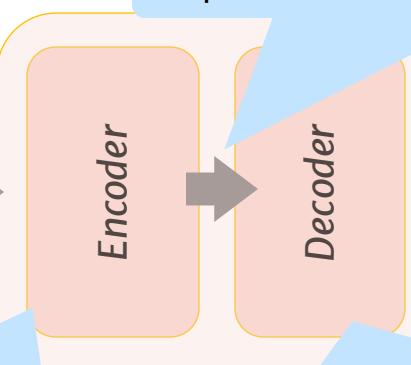
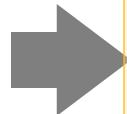


Encoder-Decoder Architectures

- It is useful to think of generative models as two sub-models

Representation (compression) of the context

“The cat sat on the [MASK]”

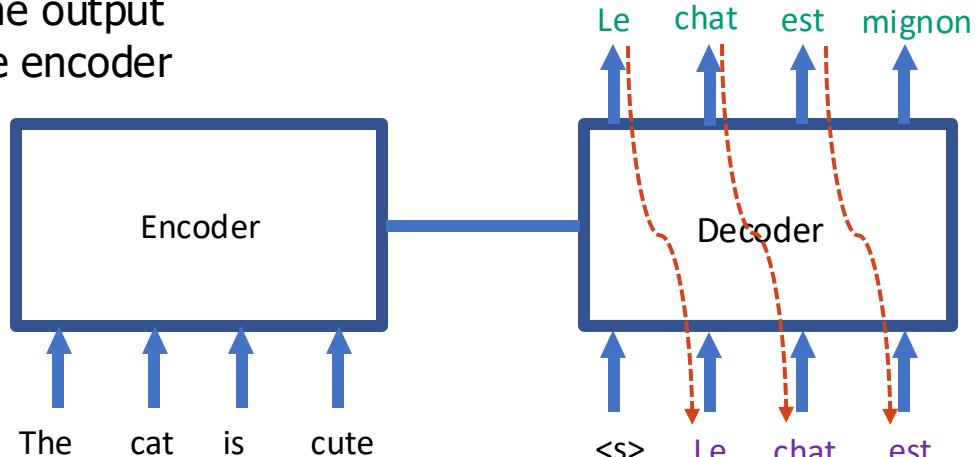


Processes the context and compiles it into a vector.

Produces the output sequence item by item using the representation of the context.

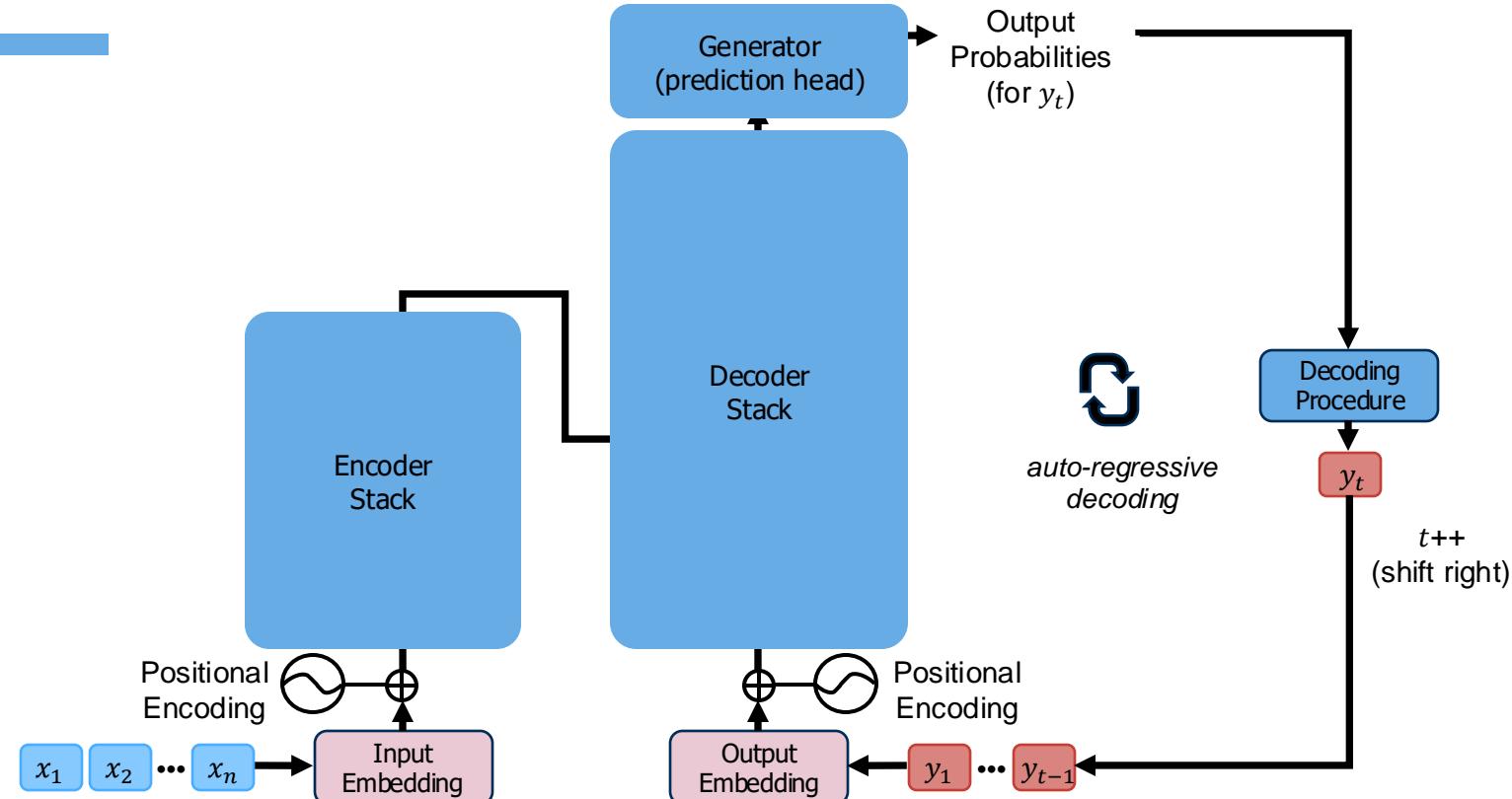
Encoder-decoder models

- Transformer is two blocks
- Encoder = read or encode the input,
 - Architecture is as we've seen
- Decoder = generate or decode the output
 - Architecture is identical to the encoder but we give it the ability to also attend to the input



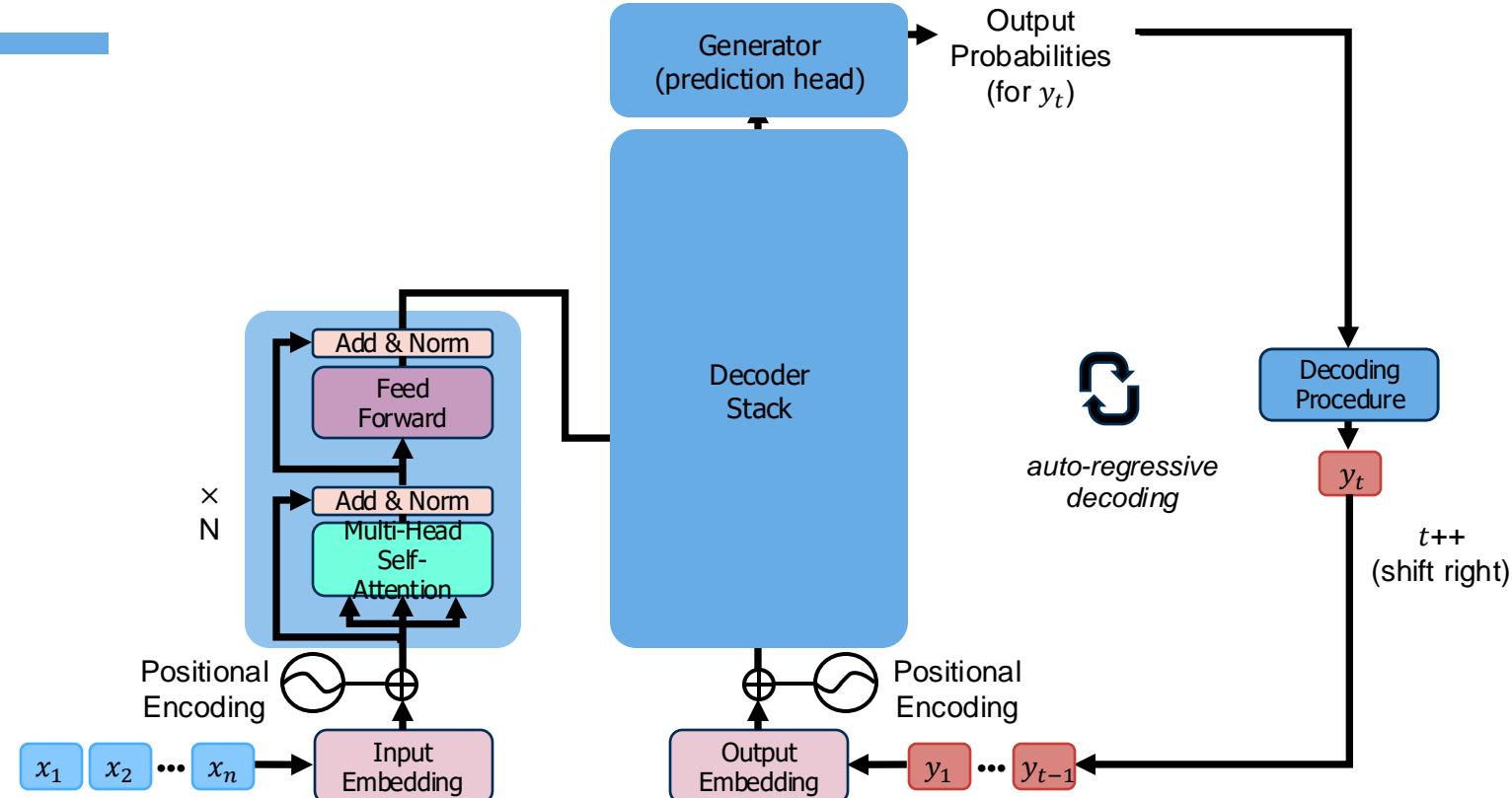
Transformer

[Vaswani et al. 2017]



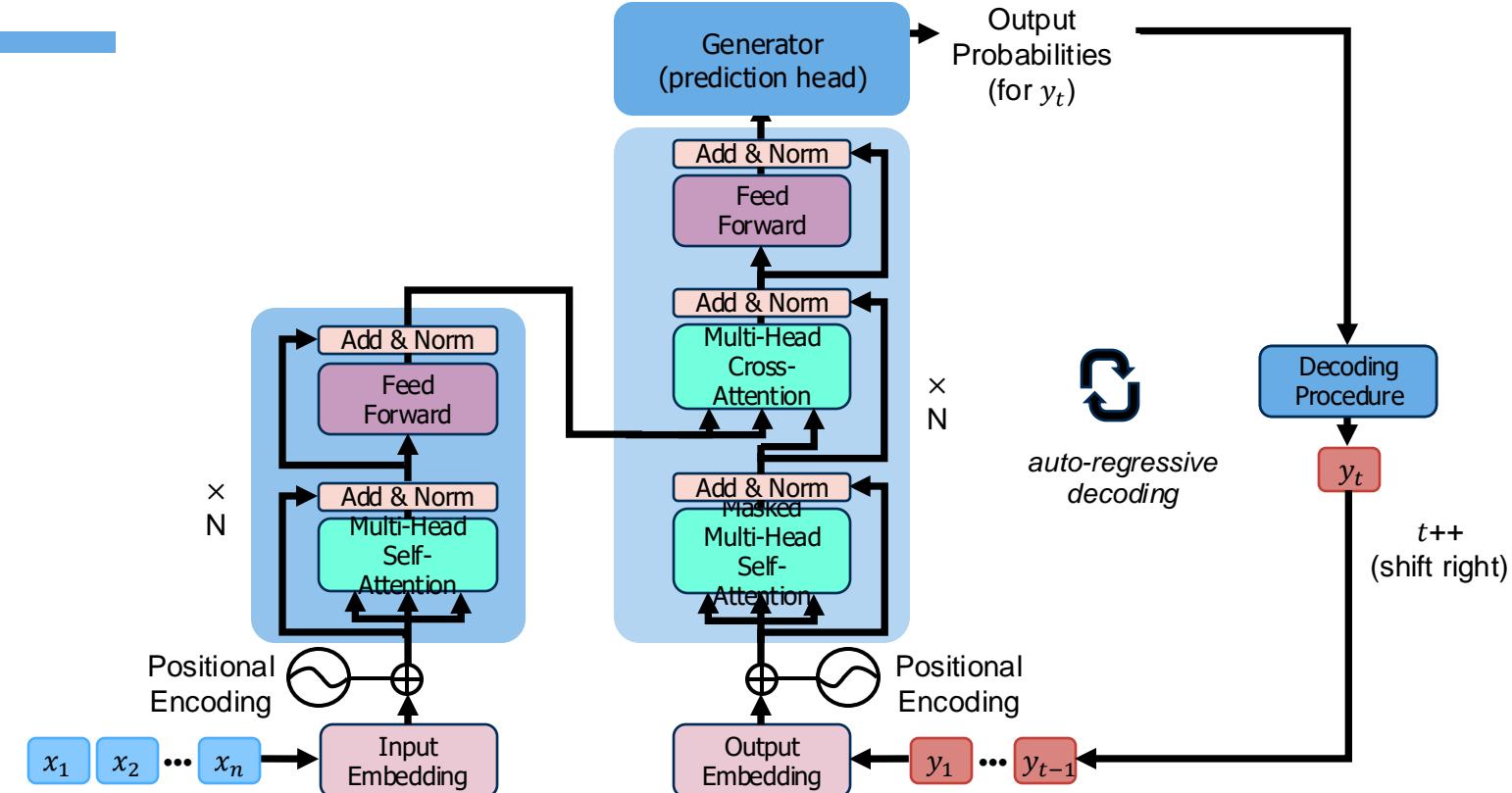
Transformer

[Vaswani et al. 2017]



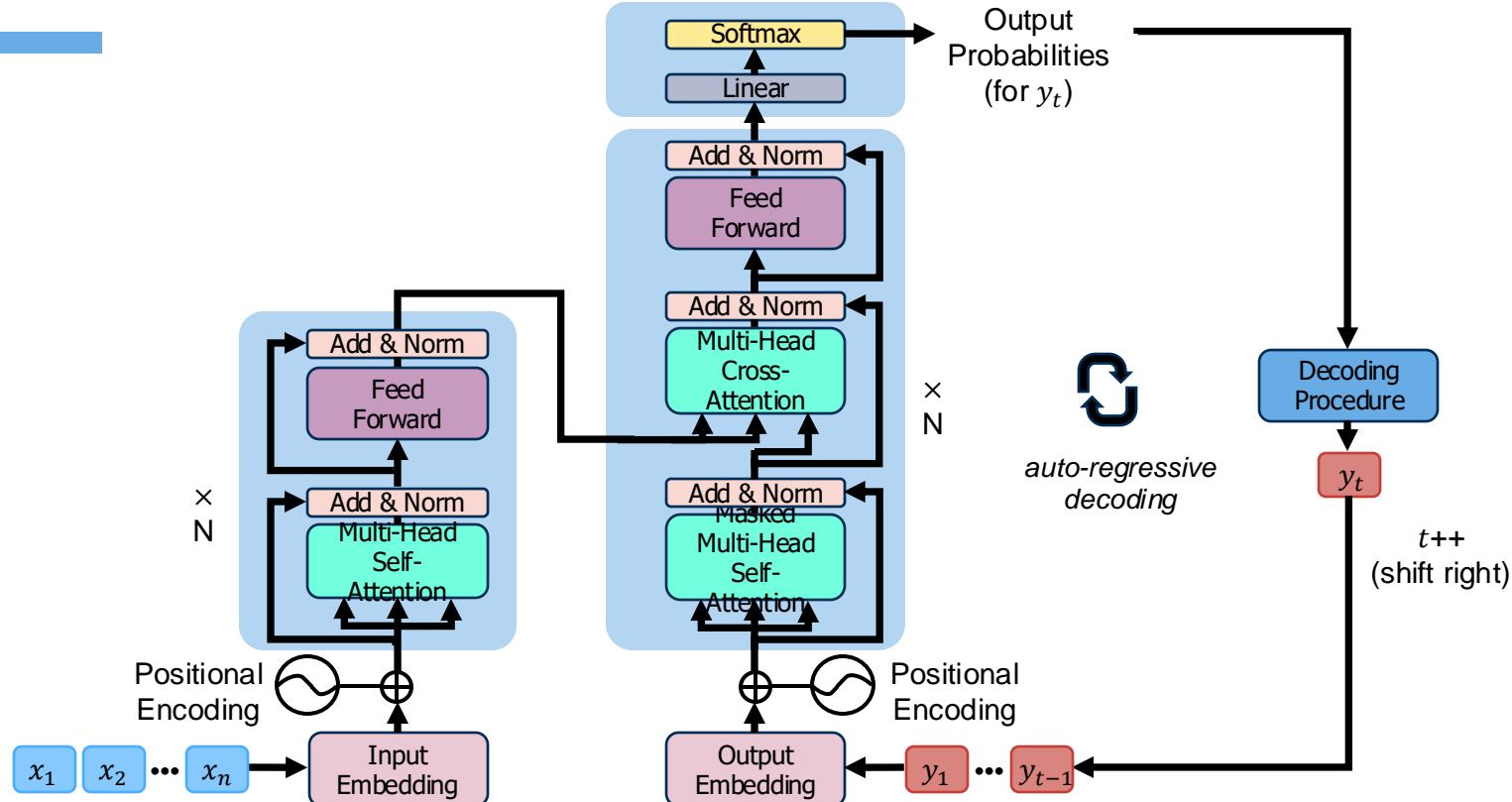
Transformer

[Vaswani et al. 2017]



Transformer

[Vaswani et al. 2017]



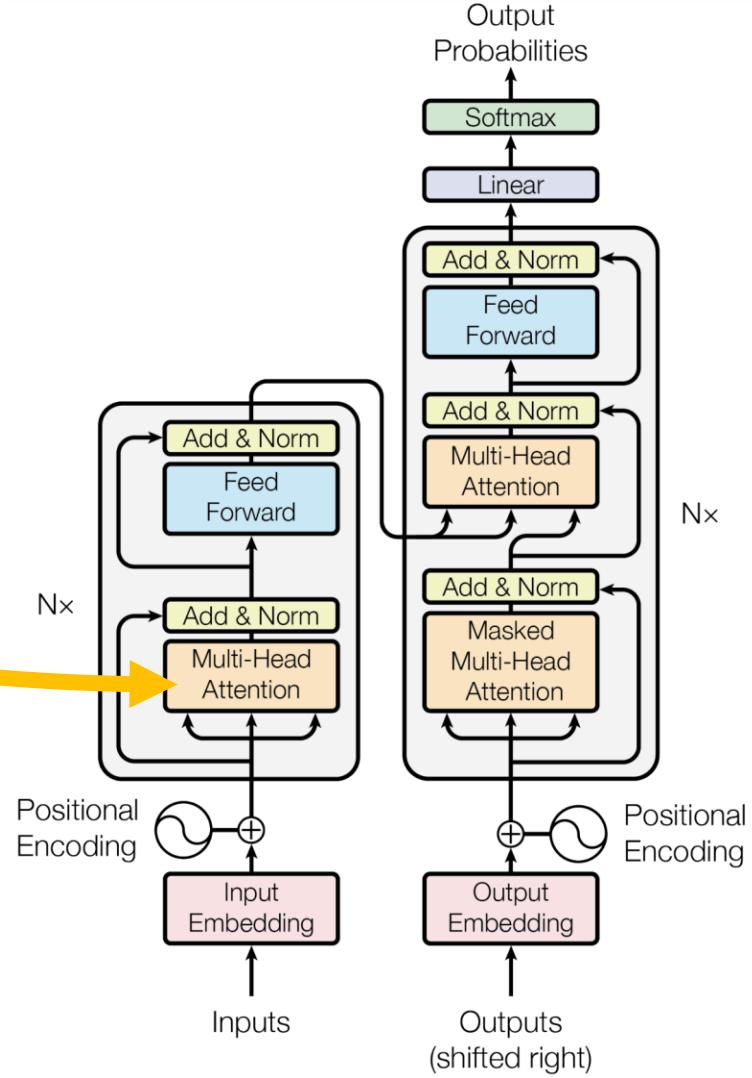
Transformer

[Vaswani et al. 2017]

- Computation of **encoder** attends to both sides.



Encoder Self-Attention



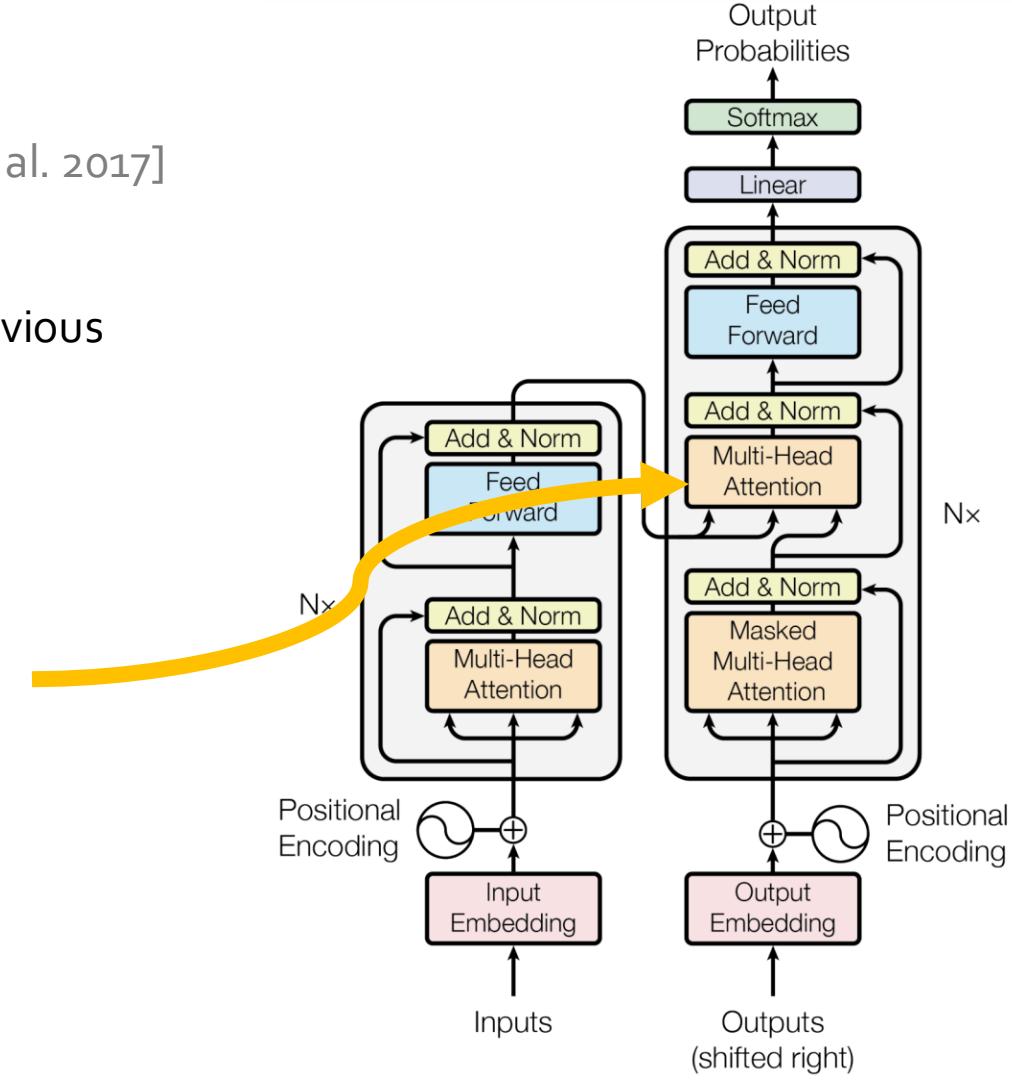
Transformer

[Vaswani et al. 2017]

- At any step of **decoder**, it attends to previous computation of **encoder**



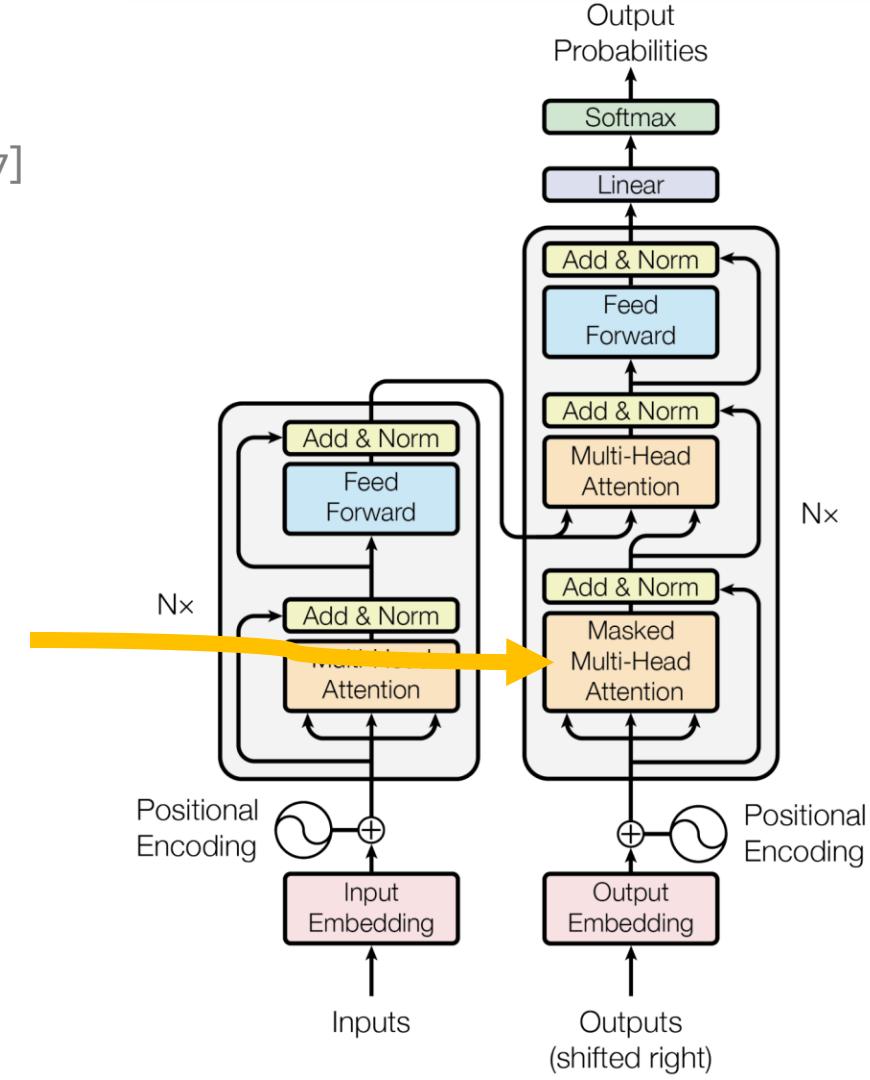
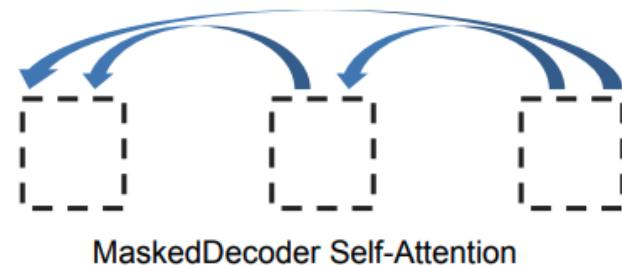
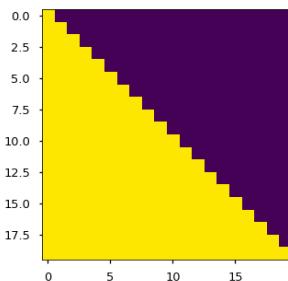
Encoder-Decoder Attention



Transformer

[Vaswani et al. 2017]

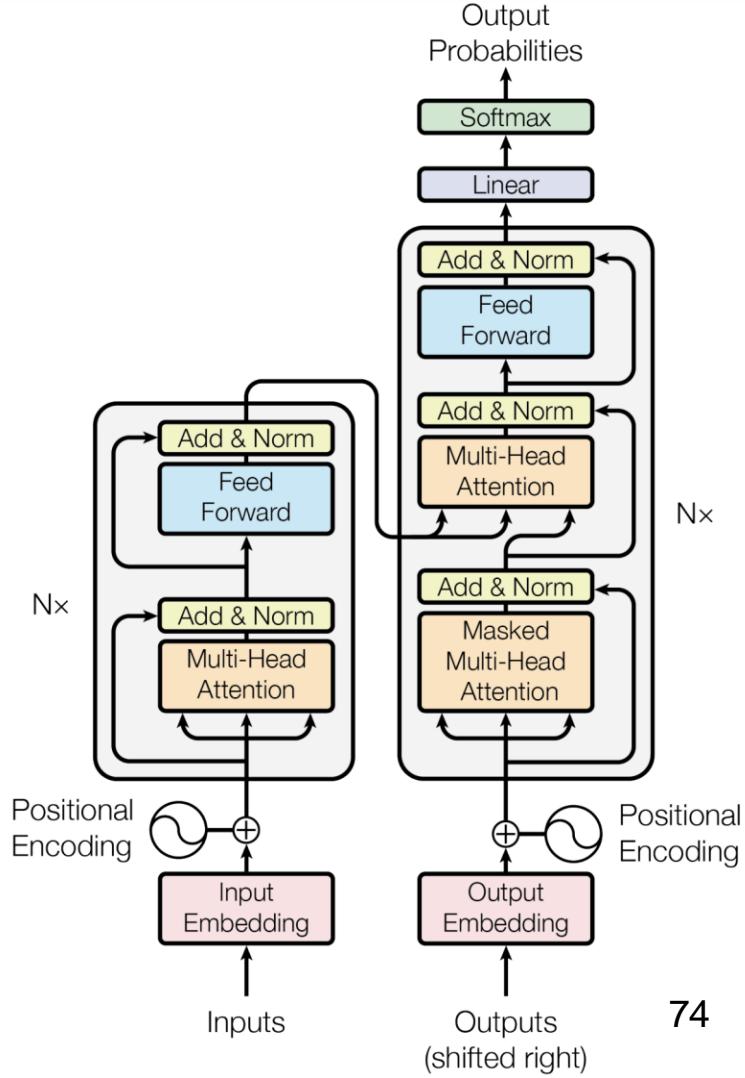
- At any step of **decoder**, it attends to previous computation of **encoder** as well as **decoder's** own generations



Transformer

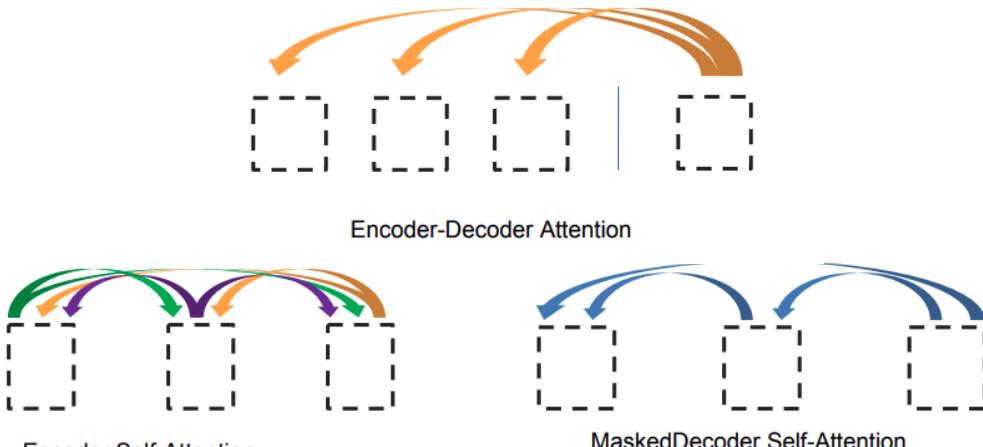
[Vaswani et al. 2017]

- At any step of **decoder**, it attends to previous computation of **encoder** as well as **decoder's** own generations
- At any step of **decoder**, **re-use** previous computation of **encoder**.
- Computation of **decoder** is **linear**, instead of quadratic.

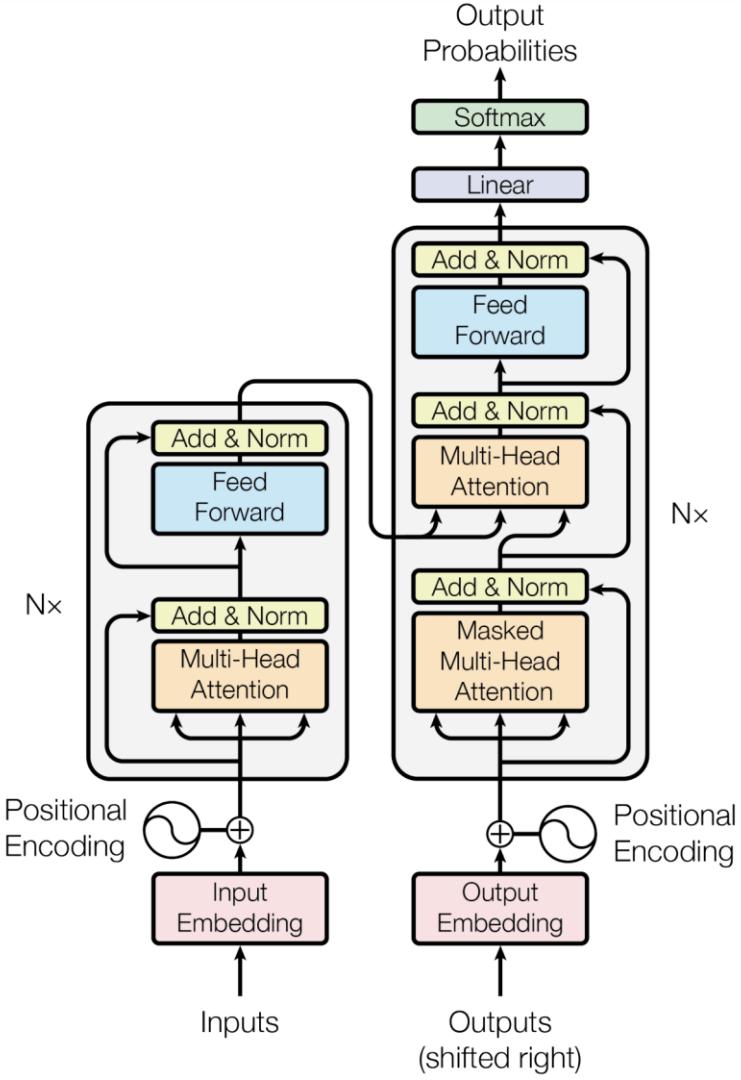


Recap: Transformer

- Yaaay we know Transformers now! 🎉
- An **encoder-decoder** architecture
- 3 forms of attention



[[Attention Is All You Need, Vaswani et al. 2017](#)]



Quiz: Enc-Dec Cost

- Source data (large!):
 - The references for a Wikipedia article.
 - Web search using article section titles, ~ 10 web pages per query.
- For a passage of length N and a summary of length M , the complexity of the attention is:
 - $O(N) + O(M)$
 - $O(N) + O(M) + O(NM)$
 - $O(N^2) + O(M^2) + O(NM)$
 - $O(N^2) + O(M^2)$

No, self attention is all-to-all
and so quadratic.

Quiz: Enc-Dec Cost

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No, self attention is all-to-all
and so quadratic in M and N .

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 - $O(N) + O(M) + O(NM)$
 - $O(N^2) + O(M^2) + O(NM)$
 - $O(N^2) + O(M^2)$

No, cross attention is missing.

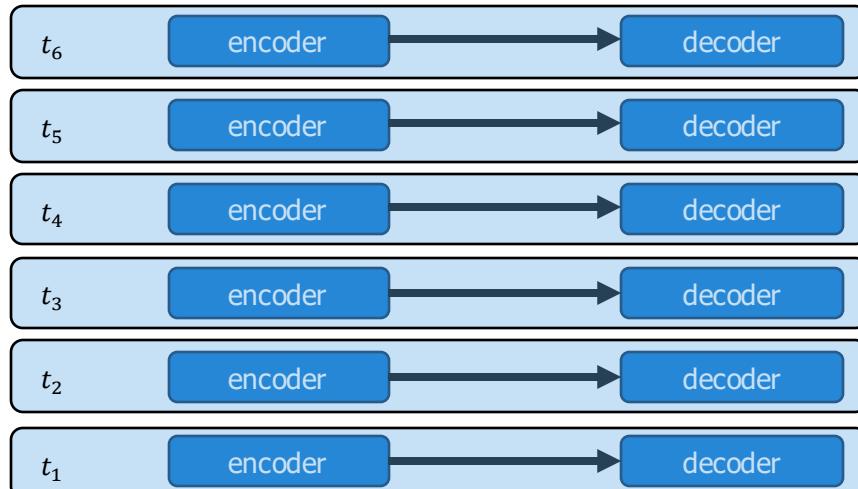
Quiz: Enc-Dec Cost

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 - The references for a Wikipedia article.
 - Web search using article section titles, ~ 10 web pages per query.
- For a passage of length N and a summary of length M , the complexity of the attention is:
 - $O(N) + O(M)$
 - $O(N) + O(M) + O(NM)$
 - $O(N^2) + O(M^2) + O(NM)$
 - $O(N^2) + O(M^2)$

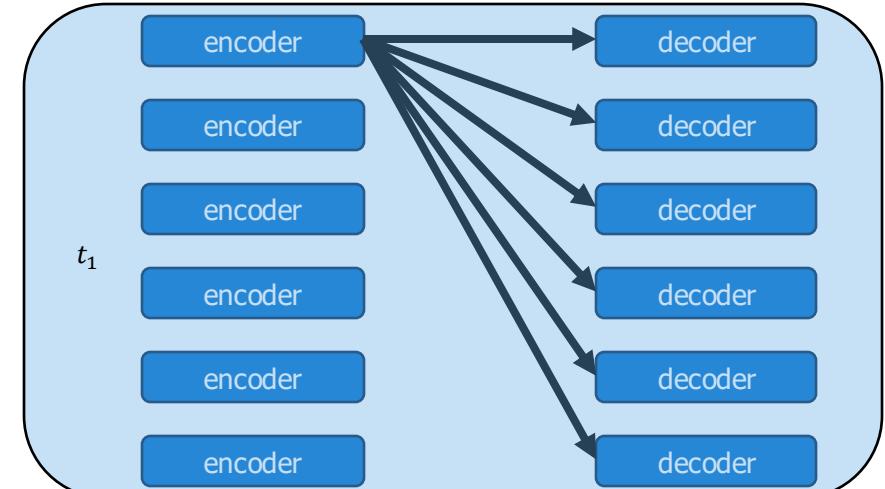
Yes. The three terms are respectively the Encoder self-attention, Decoder self-attention, and Cross attention.

Quiz: Enc-Dec Connections

- Which best represents encoder-decoder connections?



Incorrect



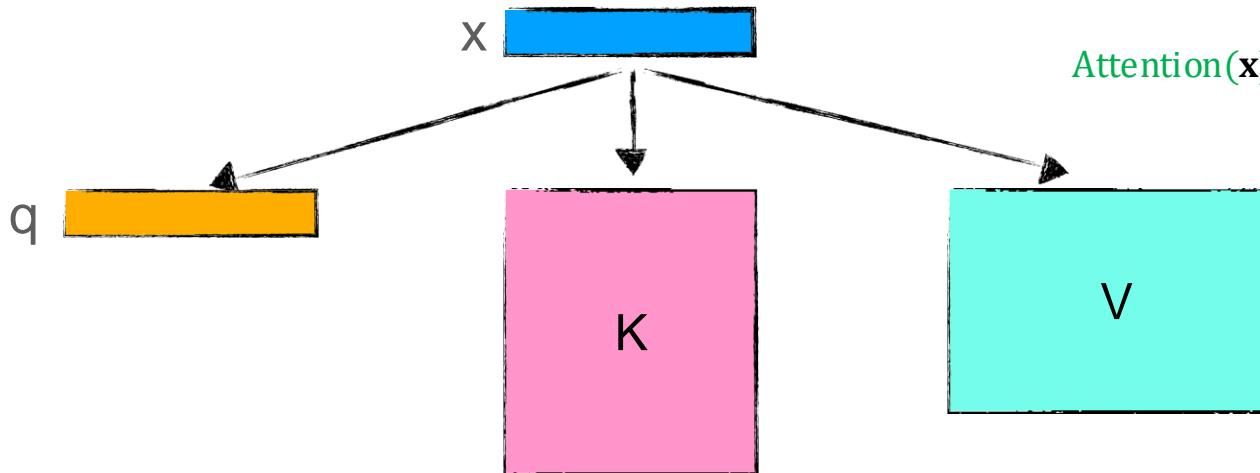
Correct

Considerations about computational cost in Transformers

Making decoding more efficient

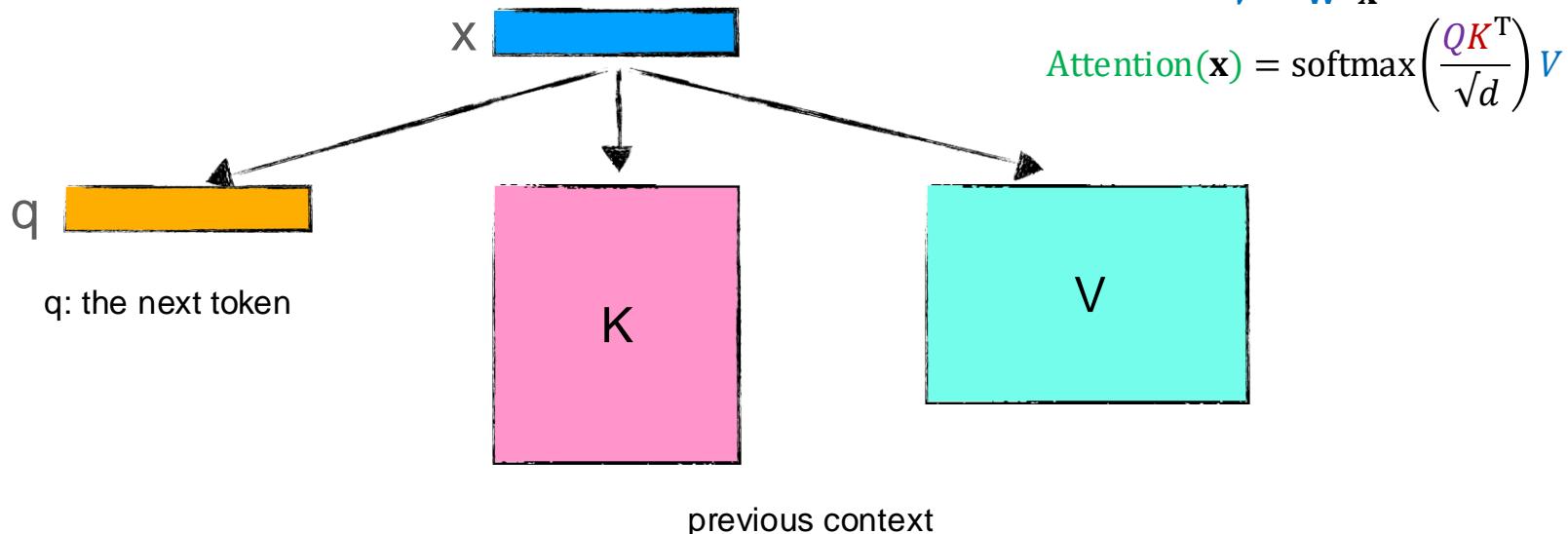
$$\begin{aligned} Q &= \mathbf{W}^q \mathbf{x} \\ K &= \mathbf{W}^k \mathbf{x} \\ V &= \mathbf{W}^v \mathbf{x} \end{aligned}$$

$$\text{Attention}(\mathbf{x}) = \text{softmax}\left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d}}\right)\mathbf{V}$$



[Slide credit: Arman Cohan]

Making decoding more efficient



[Slide credit: Arman Cohan]

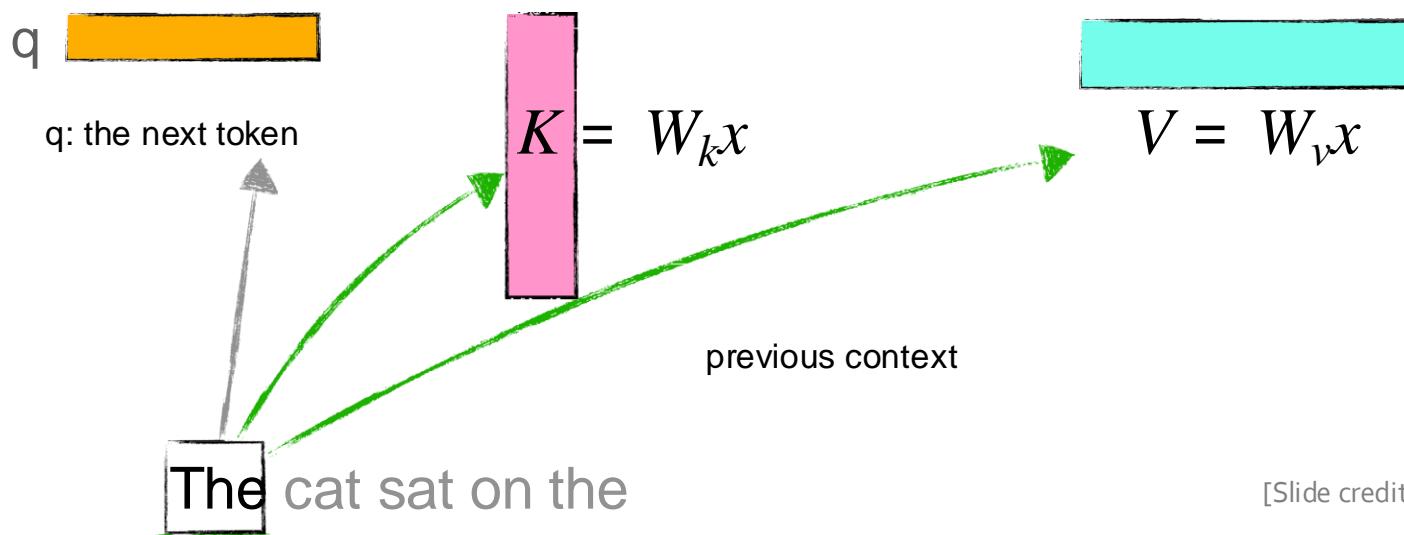
Making decoding more efficient

$$Q = W^q \mathbf{x}$$

$$K = W^k \mathbf{x}$$

$$V = W^v \mathbf{x}$$

$$\text{Attention}(\mathbf{x}) = \text{softmax}\left(\frac{QK^T}{\sqrt{d}}\right)V$$



[Slide credit: Arman Cohan]

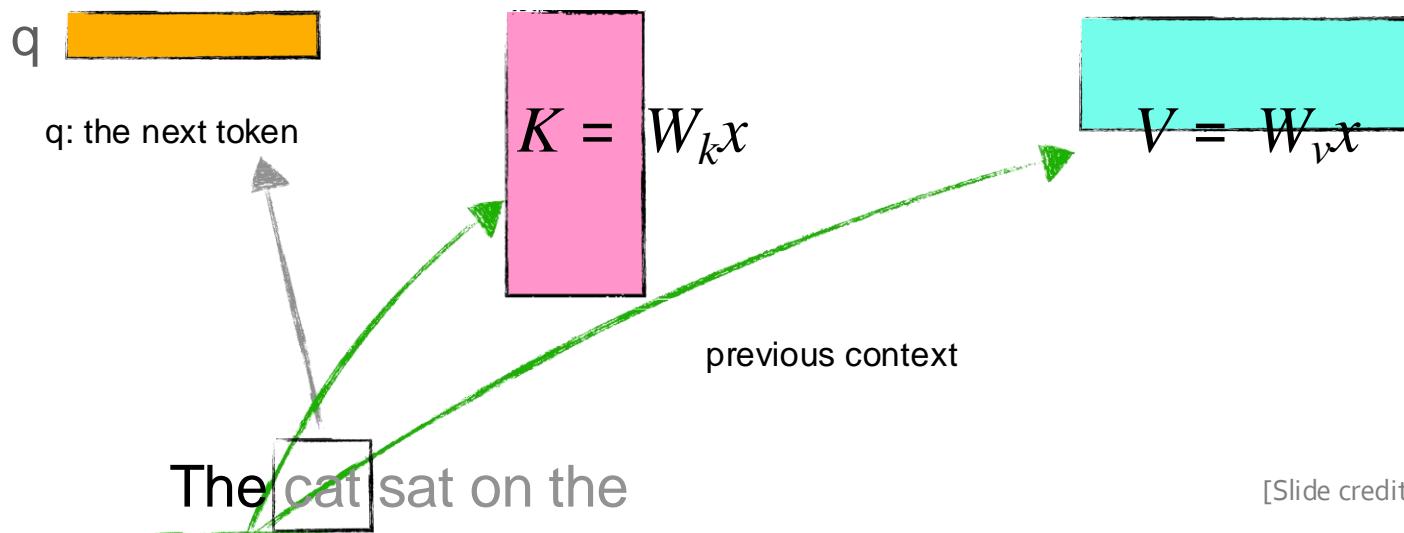
Making decoding more efficient

$$Q = W^q x$$

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$$V = W^v x$$

$$\text{Attention}(x) = \text{softmax}\left(\frac{QK^T}{\sqrt{d}}\right)V$$



[Slide credit: Arman Cohan]

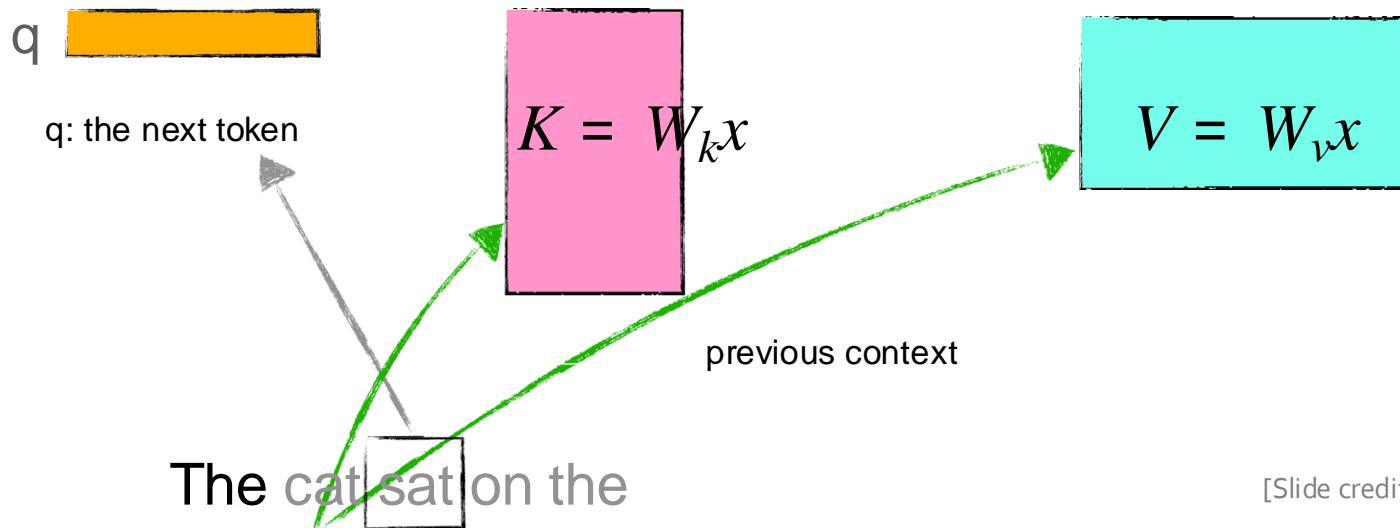
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[Slide credit: Arman Cohan]

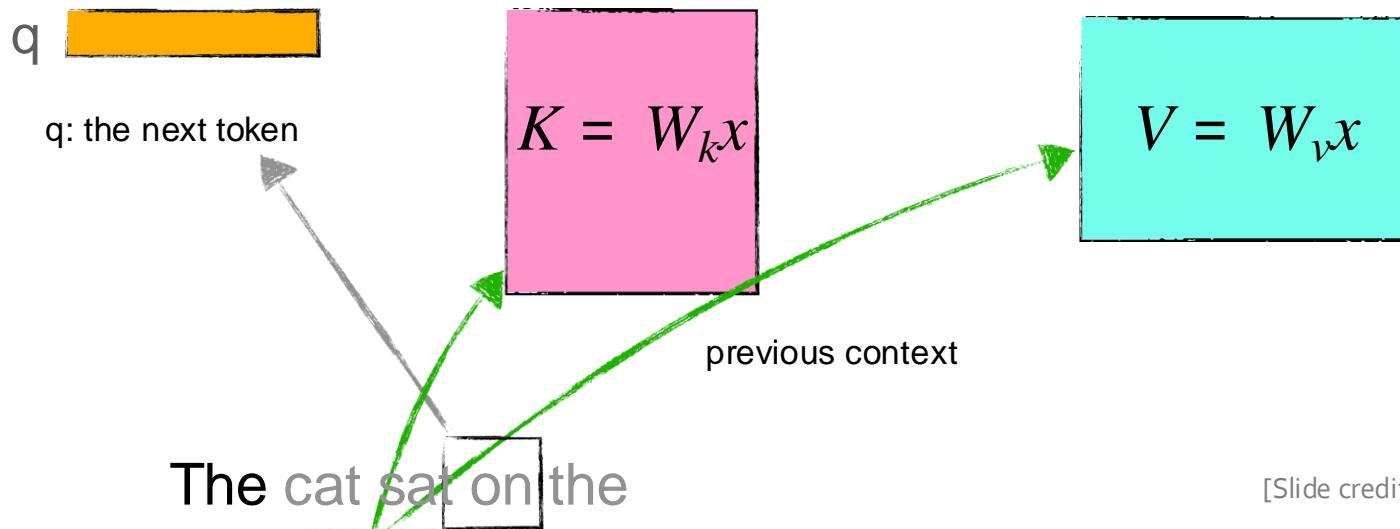
Making decoding more efficient

$$Q = \mathbf{W}^q \mathbf{x}$$

$$K = \mathbf{W}^k \mathbf{x}$$

$$V = \mathbf{W}^v \mathbf{x}$$

$$\text{Attention}(\mathbf{x}) = \text{softmax}\left(\frac{QK^T}{\sqrt{d}}\right)V$$



[Slide credit: Arman Cohan]

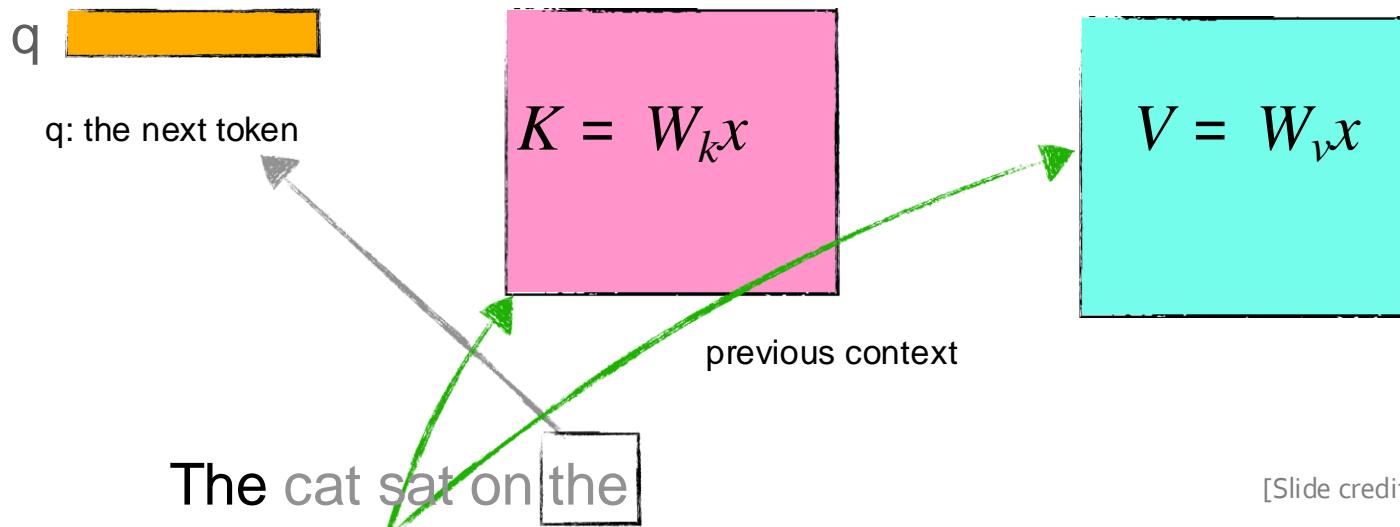
Making decoding more efficient

$$Q = W^q x$$

$$K = W^k x$$

$$V = W^v x$$

$$\text{Attention}(x) = \text{softmax}\left(\frac{QK^T}{\sqrt{d}}\right)V$$



[Slide credit: Arman Cohan]

Making decoding more efficient

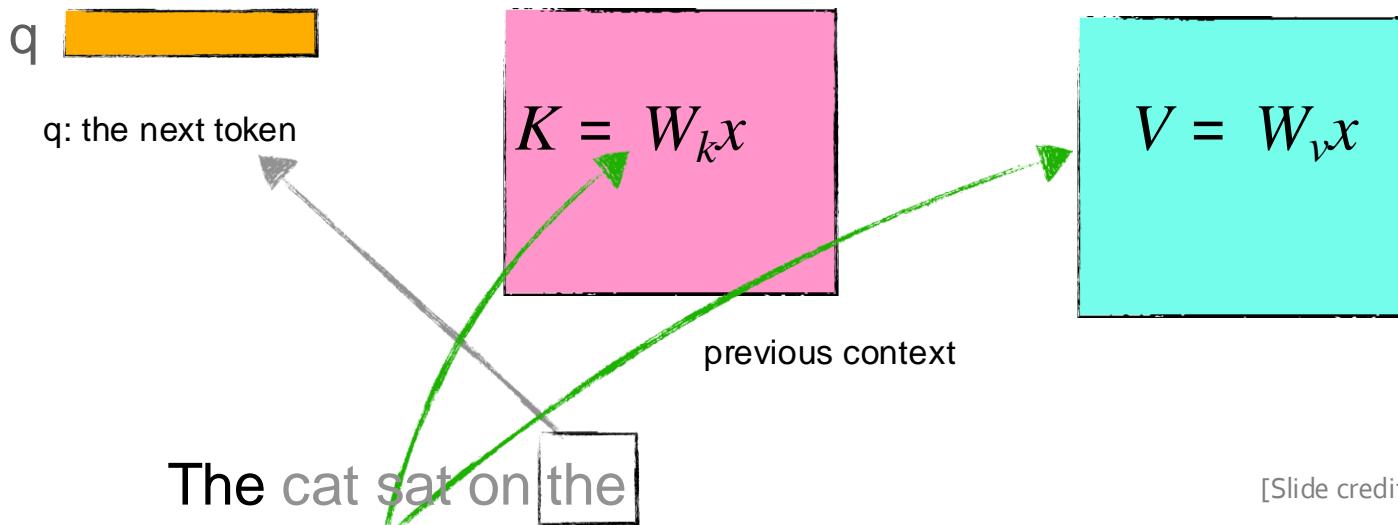
- We are computing the Keys and Values many times!
 - Let's reduce redundancy! 😊

$$Q = \mathbf{W}^q \mathbf{x}$$

$$K = \mathbf{W}^k \mathbf{x}$$

$$V = \mathbf{W}^v \mathbf{x}$$

$$\text{Attention}(\mathbf{x}) = \text{softmax}\left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d}}\right)\mathbf{V}$$



[Slide credit: Arman Cohan]

Making decoding more efficient

- We are computing the Keys and Values many times!
 - Let's reduce redundancy! 😊

$$Q = \mathbf{W}^q \mathbf{x}$$

$$K = \mathbf{W}^k \mathbf{x}$$

$$V = \mathbf{W}^v \mathbf{x}$$

$$\text{Attention}(\mathbf{x}) = \text{softmax}\left(\frac{QK^T}{\sqrt{d}}\right)V$$

$$k_{new} = W_k \mathbf{x}[:, : - 1]$$

q
q: the next token

K Cached

V Cached

previous context

$$v_{new} = W_v \mathbf{x}[:, : - 1]$$

The cat sat on the

[Slide credit: Arman Cohan]

Making decoding more efficient

- **Question:** How much memory does this K, V cache require?

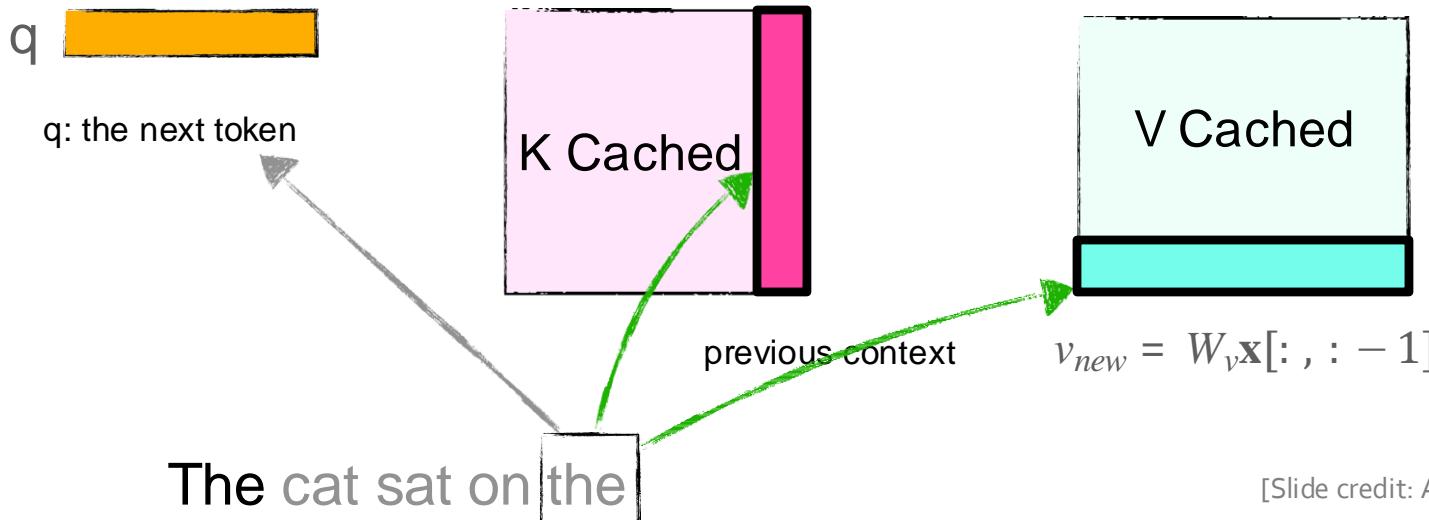
$$Q = \mathbf{W}^q \mathbf{x}$$

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$$V = \mathbf{W}^v \mathbf{x}$$

$$\text{Attention}(\mathbf{x}) = \text{softmax}\left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d}}\right)\mathbf{V}$$

$$k_{new} = W_k \mathbf{x}[:, : - 1]$$



[Slide credit: Arman Cohan]

Writing our own Transformer

Clone Helper Function

- Create N copies of pytorch nn.Module
- The Transformer's structure contains a lot of design repetition (like VGG)
- Remember these clones shouldn't share parameters (for the most part)

```
def clones(module, N):
    "Produce N identical layers."
    return nn.ModuleList([copy.deepcopy(module) for _ in range(N)])
```

Create Embedding

- Create vector representation of sequence vocabulary
- nn.Embedding creates a lookup table to map sequence vocabulary to unique vectors

```
class Embeddings(nn.Module):  
    def __init__(self, d_model, vocab):  
        super(Embeddings, self).__init__()  
        self.lut = nn.Embedding(vocab, d_model)  
        self.d_model = d_model  
  
    def forward(self, x):  
        return self.lut(x) * math.sqrt(self.d_model)
```

Positional Encoding

- Add information about an element's position in a sequence to its representation
- Element wise addition of sinusoidal encoding



```
class PositionalEncoding(nn.Module):
    "Implement the PE function."

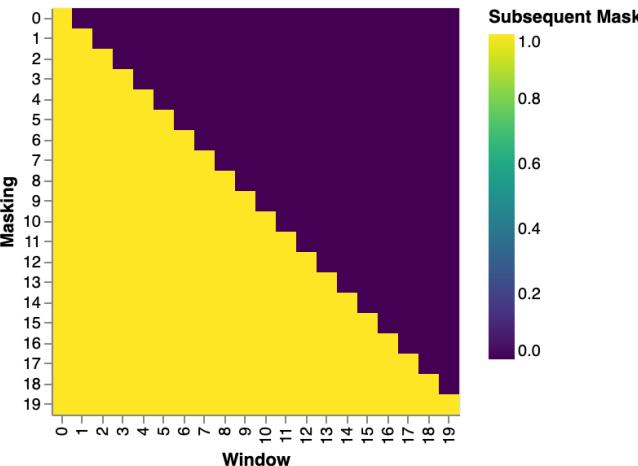
    def __init__(self, d_model, dropout, max_len=5000):
        super(PositionalEncoding, self).__init__()
        self.dropout = nn.Dropout(p=dropout)

        # Compute the positional encodings once in log space.
        pe = torch.zeros(max_len, d_model)
        position = torch.arange(0, max_len).unsqueeze(1)
        div_term = torch.exp(
            torch.arange(0, d_model, 2) * -(math.log(10000.0) / d_model))
        )
        pe[:, 0::2] = torch.sin(position * div_term)
        pe[:, 1::2] = torch.cos(position * div_term)
        pe = pe.unsqueeze(0)
        self.register_buffer("pe", pe)

    def forward(self, x):
        x = x + self.pe[:, :, :x.size(1)].requires_grad_(False)
        return self.dropout(x)
```

Attention block

```
def attention(query, key, value, mask=None, dropout=None):
    "Compute 'Scaled Dot Product Attention'"
    d_k = query.size(-1)
    scores = torch.matmul(query, key.transpose(-2, -1)) / math.sqrt(d_k)
    if mask is not None:
        scores = scores.masked_fill(mask == 0, -1e9)
    p_attn = scores.softmax(dim=-1)
    if dropout is not None:
        p_attn = dropout(p_attn)
    return torch.matmul(p_attn, value), p_attn
```



$-1e9$ is a large negative number, which leads to $\text{softmax}(-1e9) \approx 0$

Multi-Head Attention

```
class MultiHeadedAttention(nn.Module):
    def __init__(self, h, d_model, dropout=0.1):
        "Take in model size and number of heads."
        super(MultiHeadedAttention, self).__init__()
        assert d_model % h == 0
        # We assume d_v always equals d_k
        self.d_k = d_model // h
        self.h = h
        self.linears = clones(nn.Linear(d_model, d_model), 4)
        self.attn = None
        self.dropout = nn.Dropout(p=dropout)
```

```
def forward(self, query, key, value, mask=None):
    "Implements Figure 2"
    if mask is not None:
        # Same mask applied to all h heads.
        mask = mask.unsqueeze(1)
    nbatches = query.size(0)

    # 1) Do all the linear projections in batch from d_model => h x d_k
    query, key, value = [
        lin(x).view(nbatches, -1, self.h, self.d_k).transpose(1, 2)
        for lin, x in zip(self.linears, (query, key, value))
    ]

    # 2) Apply attention on all the projected vectors in batch.
    x, self.attn = attention(
        query, key, value, mask=mask, dropout=self.dropout
    )

    # 3) "Concat" using a view and apply a final linear.
    x = (
        x.transpose(1, 2)
        .contiguous()
        .view(nbatches, -1, self.h * self.d_k)
    )
    del query
    del key
    del value
    return self.linears[-1](x)
```

[Slide credit: CS886 at Waterloo]

FeedForward Layer

```
class PositionwiseFeedForward(nn.Module):
    "Implements FFN equation.

    def __init__(self, d_model, d_ff, dropout=0.1):
        super(PositionwiseFeedForward, self).__init__()
        self.w_1 = nn.Linear(d_model, d_ff)
        self.w_2 = nn.Linear(d_ff, d_model)
        self.dropout = nn.Dropout(dropout)

    def forward(self, x):
        return self.w_2(self.dropout(self.w_1(x).relu()))
```

Sublayer Connections

```
class SublayerConnection(nn.Module):
    """
    A residual connection followed by a layer norm.
    Note for code simplicity the norm is first as opposed to last.
    """

    def __init__(self, size, dropout):
        super(SublayerConnection, self).__init__()
        self.norm = LayerNorm(size)
        self.dropout = nn.Dropout(dropout)

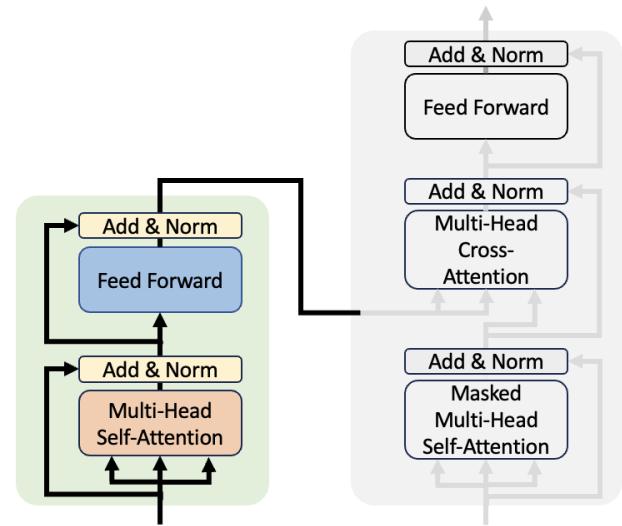
    def forward(self, x, sublayer):
        "Apply residual connection to any sublayer with the same size."
        return x + self.dropout(sublayer(self.norm(x)))
```

Encoder Layer

```
class EncoderLayer(nn.Module):
    "Encoder is made up of self-attn and feed forward (defined below)"

    def __init__(self, size, self_attn, feed_forward, dropout):
        super(EncoderLayer, self).__init__()
        self.self_attn = self_attn
        self.feed_forward = feed_forward
        self.sublayer = clones(SublayerConnection(size, dropout), 2)
        self.size = size

    def forward(self, x, mask):
        "Follow Figure 1 (left) for connections."
        x = self.sublayer[0](x, lambda x: self.self_attn(x, x, x, mask))
        return self.sublayer[1](x, self.feed_forward)
```



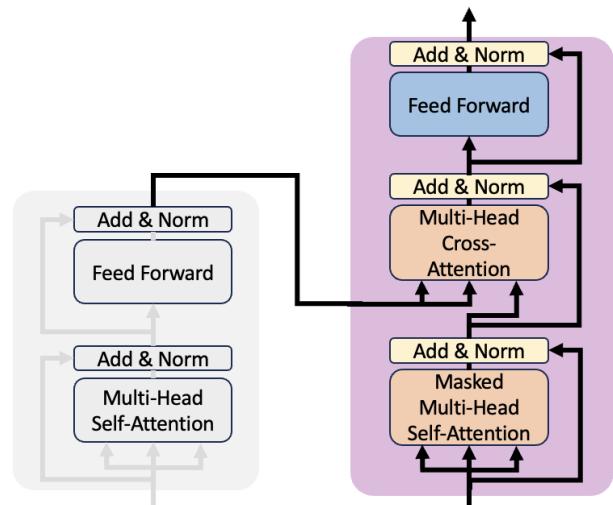
Decoder Layer

- Same as encoder layers other than:
 - the additional multi-head attention block to perform cross-attention with the output representation from the encoder

```
class DecoderLayer(nn.Module):
    "Decoder is made of self-attn, src-attn, and feed forward (defined below)"

    def __init__(self, size, self_attn, src_attn, feed_forward, dropout):
        super(DecoderLayer, self).__init__()
        self.size = size
        self.self_attn = self_attn
        self.src_attn = src_attn
        self.feed_forward = feed_forward
        self.sublayer = clones(SublayerConnection(size, dropout), 3)

    def forward(self, x, memory, src_mask, tgt_mask):
        "Follow Figure 1 (right) for connections."
        m = memory
        x = self.sublayer[0](x, lambda x: self.self_attn(x, x, x, tgt_mask))
        x = self.sublayer[1](x, lambda x: self.src_attn(x, m, m, src_mask))
        return self.sublayer[2](x, self.feed_forward)
```



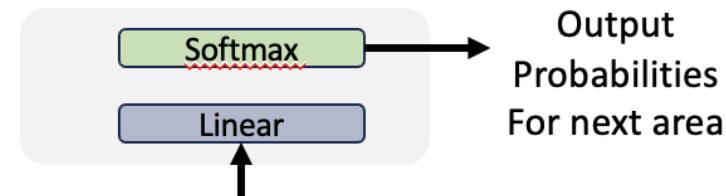
The Prediction Head

- A final linear mapping
- Apply softmax to convert logits to probabilities

```
class Generator(nn.Module):
    "Define standard linear + softmax generation step."

    def __init__(self, d_model, vocab):
        super(Generator, self).__init__()
        self.proj = nn.Linear(d_model, vocab)

    def forward(self, x):
        return log_softmax(self.proj(x), dim=-1)
```



Build each block

```
class Encoder(nn.Module):
    "Core encoder is a stack of N layers"

    def __init__(self, layer, N):
        super(Encoder, self).__init__()
        self.layers = clones(layer, N)
        self.norm = LayerNorm(layer.size)

    def forward(self, x, mask):
        "Pass the input (and mask) through each layer in turn."
        for layer in self.layers:
            x = layer(x, mask)
        return self.norm(x)
```

```
class Decoder(nn.Module):
    "Generic N layer decoder with masking."

    def __init__(self, layer, N):
        super(Decoder, self).__init__()
        self.layers = clones(layer, N)
        self.norm = LayerNorm(layer.size)

    def forward(self, x, memory, src_mask, tgt_mask):
        for layer in self.layers:
            x = layer(x, memory, src_mask, tgt_mask)
        return self.norm(x)
```

Putting it Together

```
class EncoderDecoder(nn.Module):
    """
    A standard Encoder-Decoder architecture. Base for this and many
    other models.
    """

    def __init__(self, encoder, decoder, src_embed, tgt_embed, generator):
        super(EncoderDecoder, self).__init__()
        self.encoder = encoder
        self.decoder = decoder
        self.src_embed = src_embed
        self.tgt_embed = tgt_embed
        self.generator = generator

    def forward(self, src, tgt, src_mask, tgt_mask):
        "Take in and process masked src and target sequences."
        return self.decode(self.encode(src, src_mask), src_mask, tgt, tgt_mask)

    def encode(self, src, src_mask):
        return self.encoder(self.src_embed(src), src_mask)

    def decode(self, memory, src_mask, tgt, tgt_mask):
        return self.decoder(self.tgt_embed(tgt), memory, src_mask, tgt_mask)
```

Initialize the model

```
def make_model(
    src_vocab, tgt_vocab, N=6, d_model=512, d_ff=2048, h=8, dropout=0.1
):
    "Helper: Construct a model from hyperparameters."
    c = copy.deepcopy
    attn = MultiHeadedAttention(h, d_model)
    ff = PositionwiseFeedForward(d_model, d_ff, dropout)
    position = PositionalEncoding(d_model, dropout)
    model = EncoderDecoder(
        Encoder(EncoderLayer(d_model, c(attn), c(ff), dropout), N),
        Decoder(DecoderLayer(d_model, c(attn), c(attn), c(ff), dropout), N),
        nn.Sequential(Embeddings(d_model, src_vocab), c(position)),
        nn.Sequential(Embeddings(d_model, tgt_vocab), c(position)),
        Generator(d_model, tgt_vocab),
    )

    # This was important from their code.
    # Initialize parameters with Glorot / fan_avg.
    for p in model.parameters():
        if p.dim() > 1:
            nn.init.xavier_uniform_(p)
    return model
```