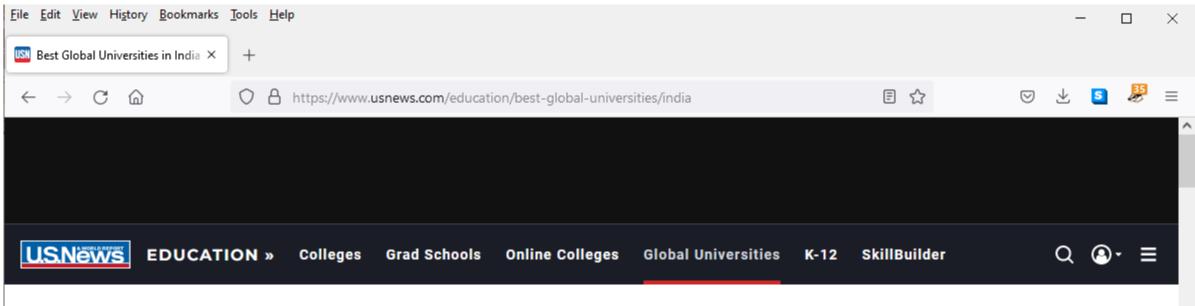
Ranking Analysis

CS5154/6054

Yizong Cheng

9/15/2022



Home / Education / Global Universities / Best Global Universities Rank... / India

Best Global Universities in India

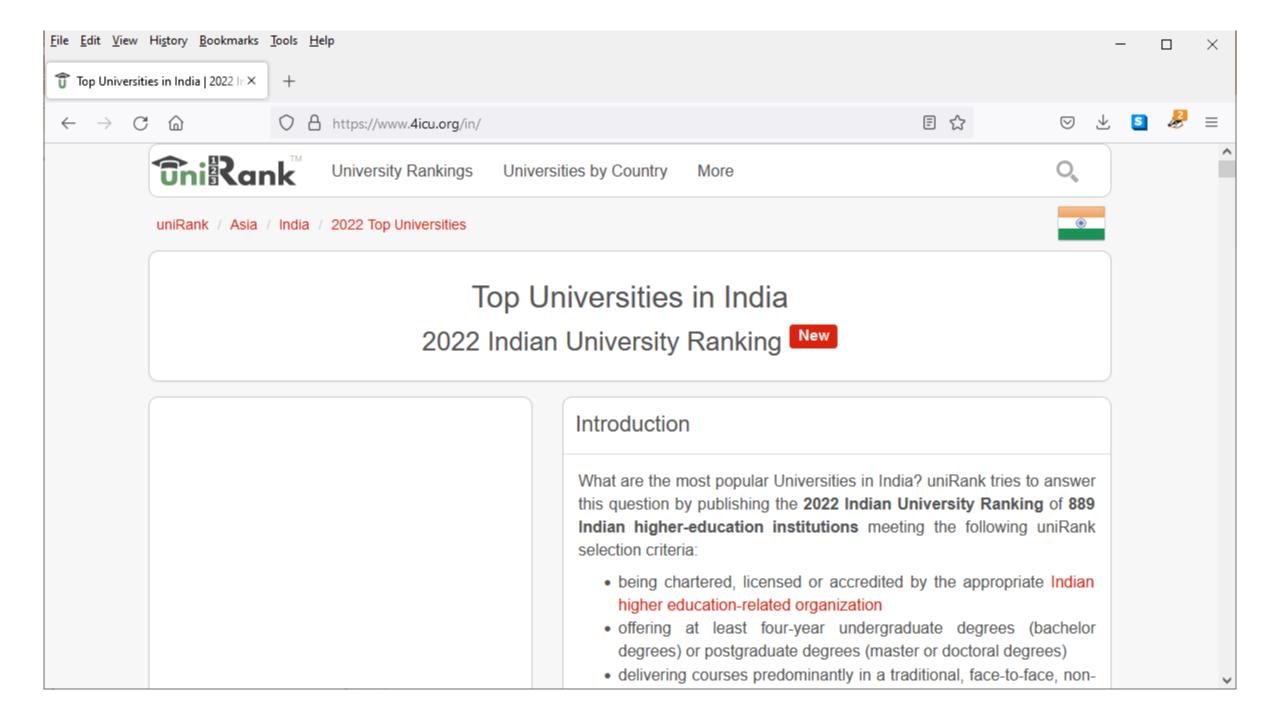
These universities in India have been numerically ranked based on their positions in the overall Best Global Universities rankings. Schools were evaluated based on their research performance and their ratings by members of the academic community around the world and within Asia. These are the top global universities in India. Read the methodology »

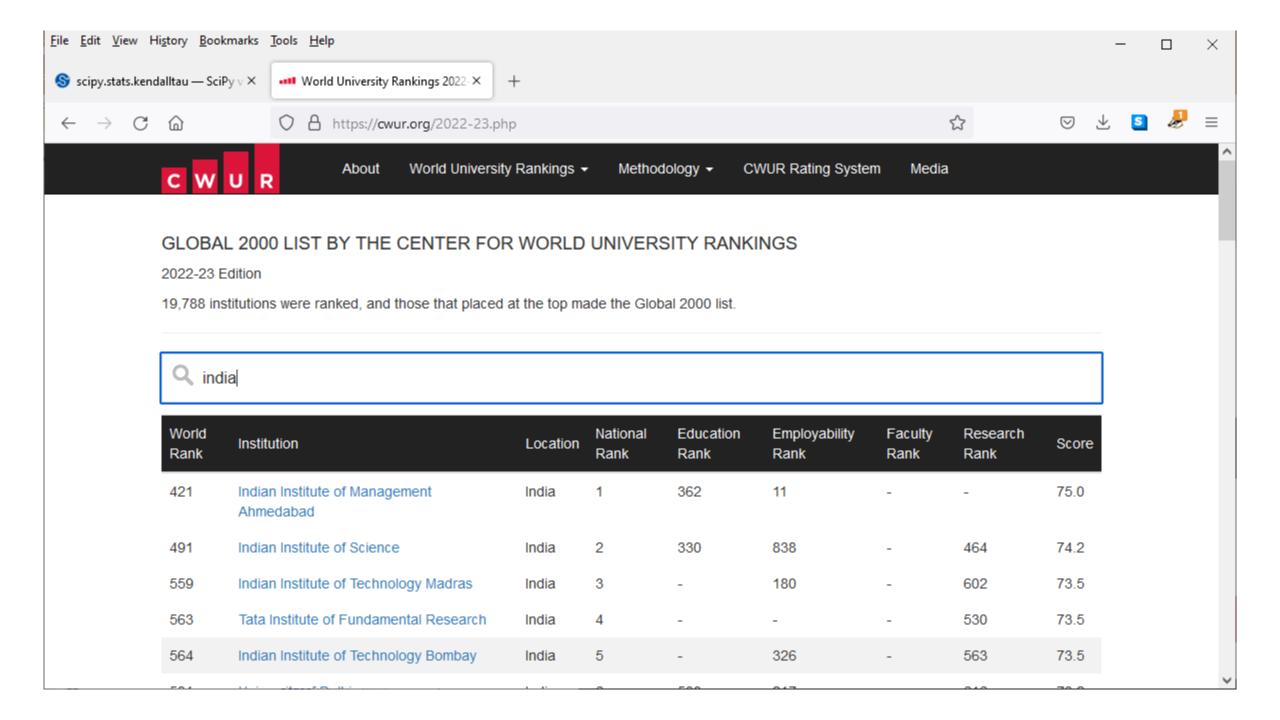
To unlock more data and access tools to help you get into your dream school, sign up for the U.S. News College Compass!

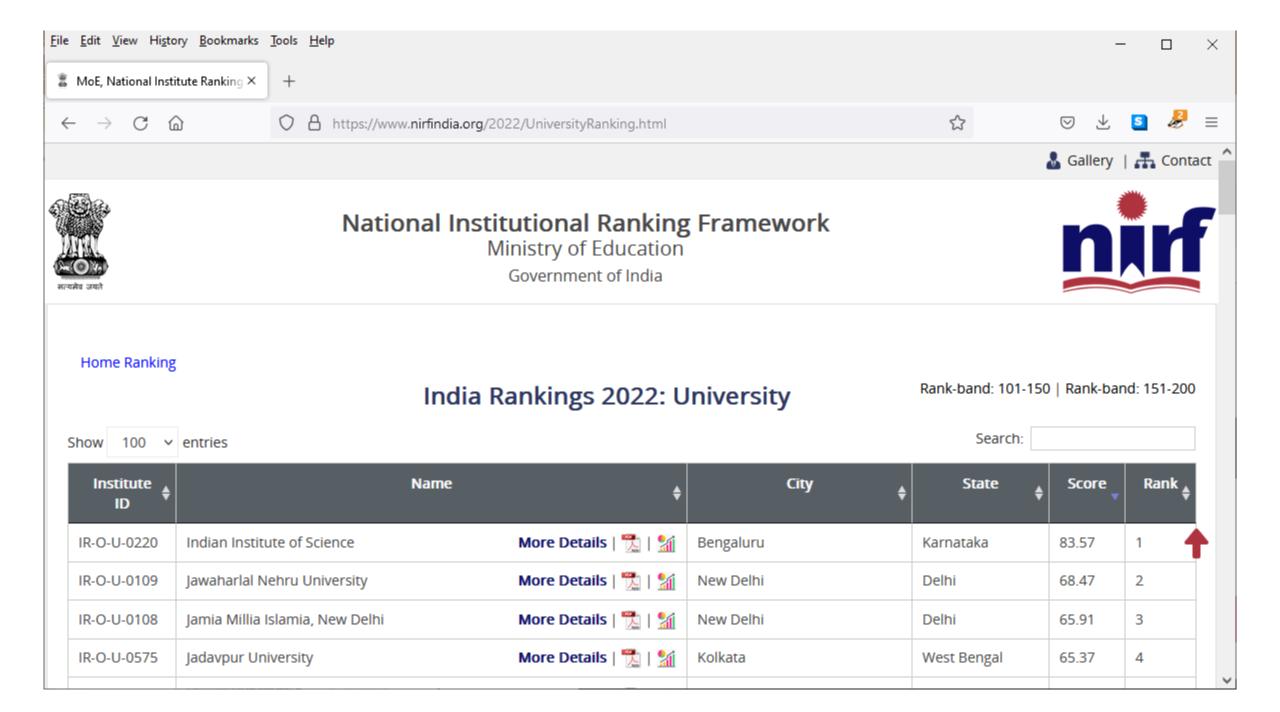


SUMMARY ~



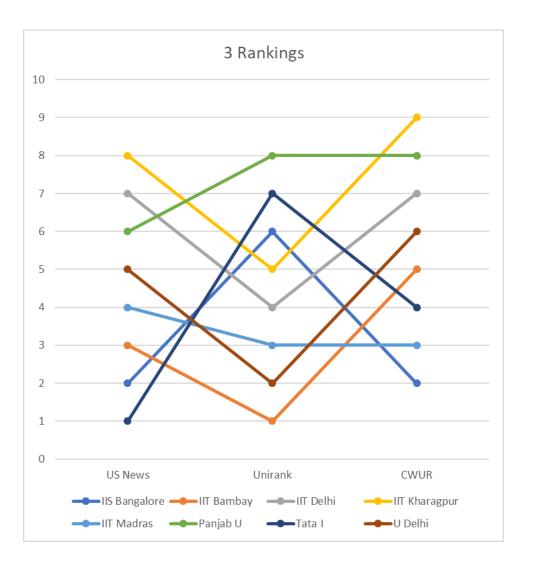


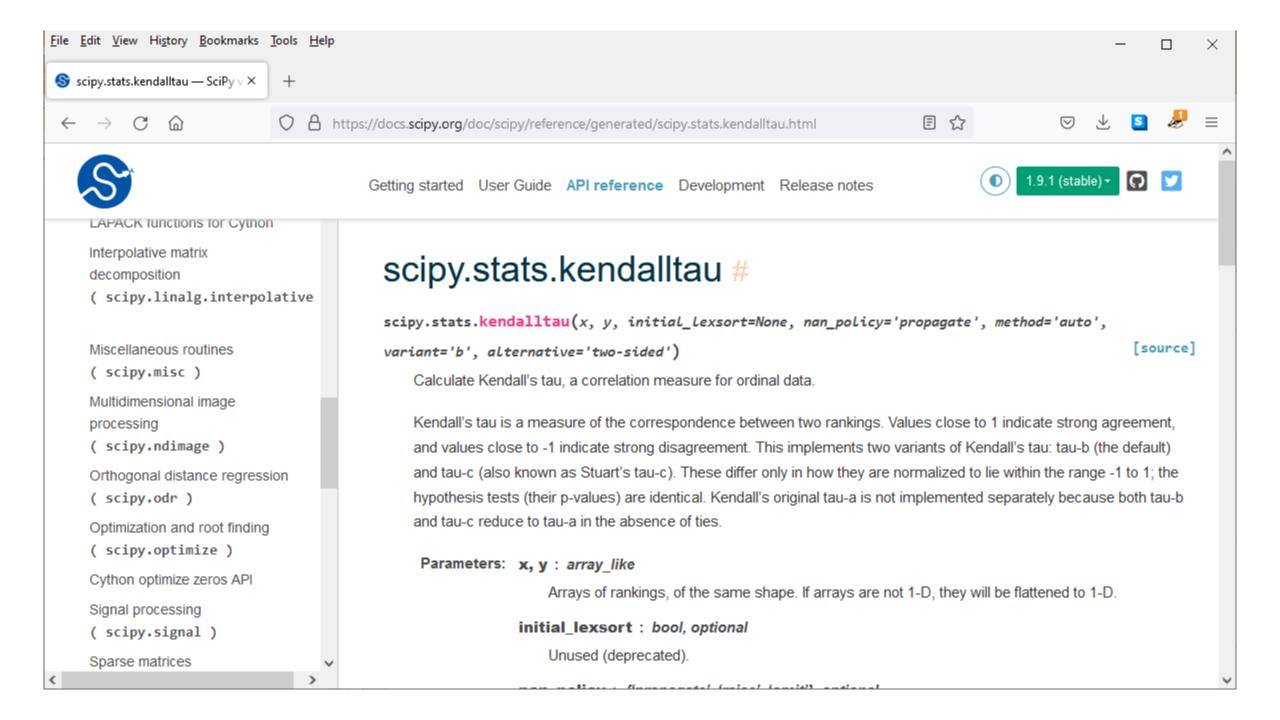




Excel Jump Chart

Name	US News	Unirank	CWUR
IIS Bangalore	2	6	2
IIT Bambay	3	1	5
IIT Delhi	7	4	7
IIT Kharagpur	8	5	9
IIT Madras	4	3	3
Panjab U	6	8	8
Tata I	1	7	4
U Delhi	5	2	6





from scipy.stats import kendalltau

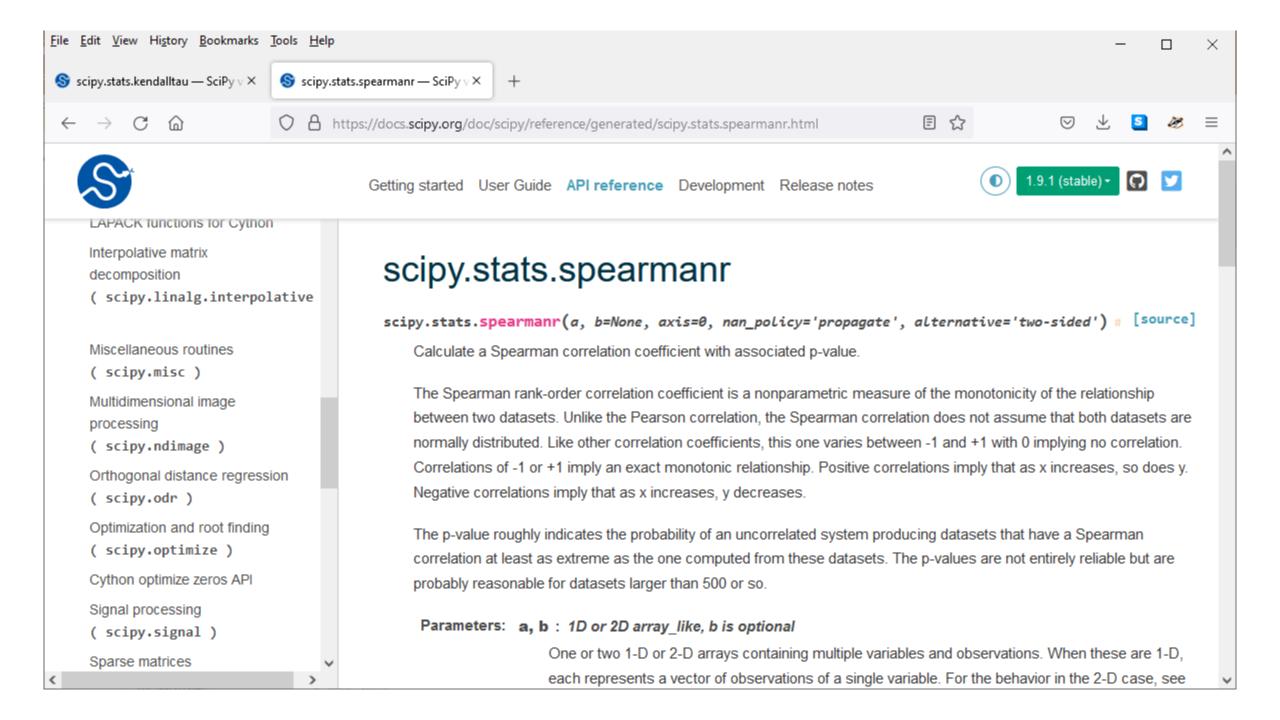
```
usnews = [2, 3, 7, 8, 4, 6, 1, 5]
unirank = [6, 1, 4, 5, 3, 8, 7, 2]
cwur = [2, 5, 7, 9, 3, 8, 4, 6]
```

```
tau, p = kendalltau(usnews, unirank)
print('usnews:unirank', tau, p)
tau, p = kendalltau(usnews, cwur)
print('usnews:cwur', tau, p)
tau, p = kendalltau(cwur, unirank)
print('cwur:unirank', tau, p)
```

usnews:unirank 0.0 1.0

usnews:cwur 0.7142857142857142 0.014136904761904762

cwur:unirank 0.14285714285714285 0.7195436507936508



from scipy.stats import spearmanr

```
usnews = [2, 3, 7, 8, 4, 6, 1, 5]

unirank = [6, 1, 4, 5, 3, 8, 7, 2]

cwur = [2, 5, 7, 9, 3, 8, 4, 6]

rho, p = spearmanr(usnews, unirank)

print('usnews:unirank', rho, p)

rho, p = spearmanr(usnews, cwur)

print('usnews:cwur', rho, p)

rho, p = spearmanr(cwur, unirank)

print('cwur:unirank', rho, p)
```

usnews:unirank -0.04761904761904763 0.9108491685195836 usnews:cwur 0.8571428571428572 0.006530017254715292 cwur:unirank 0.11904761904761905 0.7788857260523797

Rank-Biserial Correlation of Cureton

PSYCHOMETRIKA—VOL. 21, NO. 3 SEPTEMBER, 1956

RANK-BISERIAL CORRELATION

EDWARD E. CURETON

UNIVERSITY OF TENNESSEE

A formula is developed for the correlation between a ranking (possibly including ties) and a dichotomy, with limits which are always ± 1 . This formula is shown to be equivalent both to Kendall's τ and Spearman's ρ .

Rank-Biserial Correlation

- Used with ordinal vs dichotomous variables.
- rb = (2/n)(Y0 Y1)
- where
- n is the number of ranked entries,
- Y1 is the mean rank of those scoring 1 on the dichotomy, and
- Y0 is the mean rank of those scoring 0 on the dichotomy.
- Justin Fister, correlation analysis of on-page attributes and search engine rankings, UC MS of CS theses 2007

Example for Rank-Biserial Correlation

- rank: 01234 56789 1011121314 1516171819
- biserial: RRRRR RNNNN NNNN NNNNN
- mean rank Y1 = (0 + 1 + ... + 5) / 6 = 5 * 6 / 2 / 6 = 15 / 6 = 2.5
- mean rank Y0 = (6 + ... + 19) / 14 = (190 15) / 14 = 175 / 14 = 12.5
- rb = (Y0 Y1) / (n/2) = 10 / 10 = 1
- biserial: NNNNN NNNNN NNNNR RRRRR
- Y0 = (0 + 1 + ... + 13) / 14 = 13 * 14 / 2 / 14 = 91 / 14 = 13 / 2 = 6.5
- Y1 = (14 + ... + 19) / 6 = (190 91) / 6 = 99 / 6 = 33 / 3 = 16.5
- rb = (Y0 Y1) / (n/2) = -10 / 10 = -1

8.4 Evaluation of ranked retrieval results

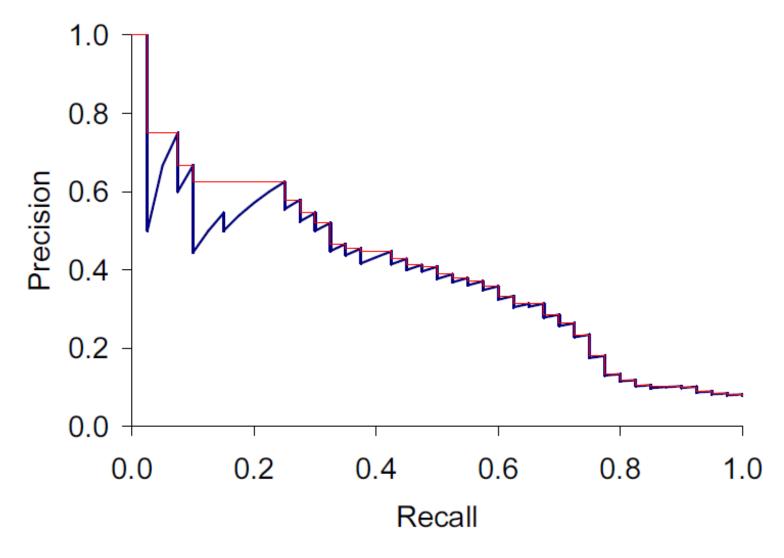
PRECISION-RECALL CURVE

INTERPOLATED PRECISION

Precision, recall, and the F measure are set-based measures. They are computed using unordered sets of documents. We need to extend these measures (or to define new measures) if we are to evaluate the ranked retrieval results that are now standard with search engines. In a ranked retrieval context, appropriate sets of retrieved documents are naturally given by the top k retrieved documents. For each such set, precision and recall values can be plotted to give a *precision-recall curve*, such as the one shown in Figure 8.2. Precision-recall curves have a distinctive saw-tooth shape: if the $(k+1)^{th}$ document retrieved is nonrelevant then recall is the same as for the top kdocuments, but precision has dropped. If it is relevant, then both precision and recall increase, and the curve jags up and to the right. It is often useful to remove these jiggles and the standard way to do this is with an interpolated precision: the *interpolated precision* p_{interp} at a certain recall level r is defined as the highest precision found for any recall level $r' \geq r$:

$$(8.7) p_{interp}(r) = \max_{r' > r} p(r')$$

The justification is that almost anyone would be prepared to look at a few more documents if it would increase the percentage of the viewed set that were relevant (that is, if the precision of the larger set is higher). Interpolated precision is shown by a thinner line in Figure 8.2. With this definition, the interpolated precision at a recall of 0 is well-defined (Exercise 8.4).



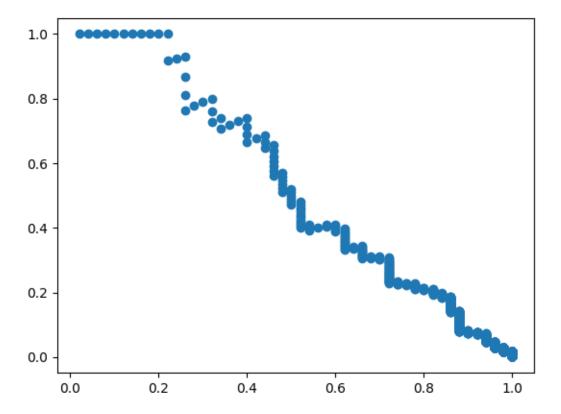
► Figure 8.2 Precision/recall graph.

```
# IR8A.py CS5154/6054 cheng 2022
# TfidfVectorizer and CountVectorizer (binary=True) are used
# a random doc is the query and the top 50 cosine similarity
# in Tfidf are considered relevent.
# CountVectors are ranked using cosine similarity
# precision and recall at each retrieval level are computed
# and the precision-recall graph (Fig 8.2 iir) is plotted
# Usage: python IR8A.py
import re
import numpy as np
import random
from sklearn.feature_extraction.text import CountVectorizer
from sklearn.feature extraction.text import TfidfVectorizer
from sklearn.metrics.pairwise import cosine_similarity
from matplotlib import pyplot as plt
relevant = 50
f = open("bible.txt", "r")
docs = f.readlines()
f.close()
```

```
tfidf = TfidfVectorizer(max_df=0.4, min_df=2)
dt = tfidf.fit_transform(docs)
N = len(docs)
query = random.randint(0, N)
print(query, docs[query])
sim = cosine similarity(dt[query], dt)
toptfidf = set()
for index in np.argsort(sim)[0][::-1][0:relevant]:
  toptfidf.add(index)
print(toptfidf)
cv = CountVectorizer(binary=True, max_df=0.4, min_df=2)
dt2 = cv.fit transform(docs)
sim2 = cosine_similarity(dt2[query], dt2)
sorted = np.argsort(sim2)[0][::-1]
```

```
precision = np.zeros(N)
recall = np.zeros(N)
m = 0
for i in range(N):
    if sorted[i] in toptfidf:
        m = m + 1
        # tp = m, fn = relevant - m, fp = i + 1 - m, tn = N - tp - fn - fp
    precision[i] = ?
    recall[i] = ?

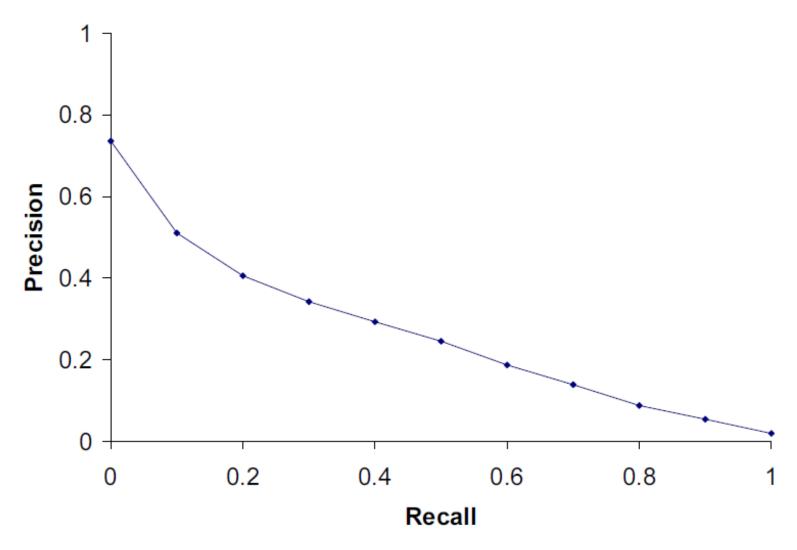
plt.scatter(recall, precision)
plt.show()
```



11-POINT INTERPOLATED AVERAGE PRECISION Examining the entire precision-recall curve is very informative, but there is often a desire to boil this information down to a few numbers, or perhaps even a single number. The traditional way of doing this (used for instance in the first 8 TREC Ad Hoc evaluations) is the 11-point interpolated average precision. For each information need, the interpolated precision is measured at the 11 recall levels of 0.0, 0.1, 0.2, ..., 1.0. For the precision-recall curve in Figure 8.2, these 11 values are shown in Table 8.1. For each recall level, we then calculate the arithmetic mean of the interpolated precision at that recall level for each information need in the test collection. A composite precision-recall curve showing 11 points can then be graphed. Figure 8.3 shows an example graph of such results from a representative good system at TREC 8.

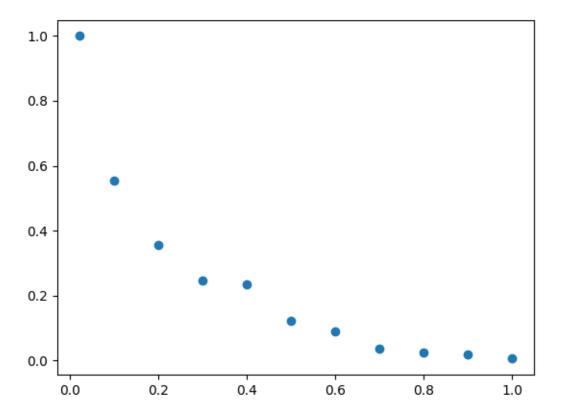
Recall	Interp.	
	Precision	
0.0	1.00	
0.1	0.67	
0.2	0.63	
0.3	0.55	
0.4	0.45	
0.5	0.41	
0.6	0.36	
0.7	0.29	
0.8	0.13	
0.9	0.10	
1.0	0.08	

▶ Table 8.1 Calculation of 11-point Interpolated Average Precision. This is for the precision-recall curve shown in Figure 8.2.



▶ Figure 8.3 Averaged 11-point precision/recall graph across 50 queries for a representative TREC system. The Mean Average Precision for this system is 0.2553.

```
eleven_recalls = np.zeros(11)
interpolated = np.zeros(11)
n = 0
for i in range(N):
  if n <= 10 and recall[i] * 10 >= n:
    interpolated[n] = max(precision[i:])
    eleven_recalls[n] = recall[i]
    print(n, precision[i], interpolated[n])
    n = n + 1
  if n > 10:
    break
plt.scatter(eleven_recalls, interpolated)
plt.show()
```



MEAN AVERAGE PRECISION In recent years, other measures have become more common. Most standard among the TREC community is *Mean Average Precision* (MAP), which provides a single-figure measure of quality across recall levels. Among evaluation measures, MAP has been shown to have especially good discrimination and stability. For a single information need, Average Precision is the average of the precision value obtained for the set of top k documents existing after each relevant document is retrieved, and this value is then averaged over information needs. That is, if the set of relevant documents for an information need $q_j \in Q$ is $\{d_1, \ldots d_{m_j}\}$ and R_{jk} is the set of ranked retrieval results from the top result until you get to document d_k , then

(8.8)
$$MAP(Q) = \frac{1}{|Q|} \sum_{j=1}^{|Q|} \frac{1}{m_j} \sum_{k=1}^{m_j} Precision(R_{jk})$$

When a relevant document is not retrieved at all,¹ the precision value in the above equation is taken to be 0. For a single information need, the average precision approximates the area under the uninterpolated precision-recall curve, and so the MAP is roughly the average area under the precision-recall curve for a set of queries.

PRECISION AT k

The above measures factor in precision at all recall levels. For many prominent applications, particularly web search, this may not be germane to users. What matters is rather how many good results there are on the first page or the first three pages. This leads to measuring precision at fixed low levels of retrieved results, such as 10 or 30 documents. This is referred to as "Precision at k", for example "Precision at 10". It has the advantage of not requiring any estimate of the size of the set of relevant documents but the disadvantages that it is the least stable of the commonly used evaluation measures and that it does not average well, since the total number of relevant documents for a query has a strong influence on precision at k.

R-PRECISION

An alternative, which alleviates this problem, is *R-precision*. It requires having a set of known relevant documents *Rel*, from which we calculate the precision of the top *Rel* documents returned. (The set *Rel* may be incomplete, such as when *Rel* is formed by creating relevance judgments for the pooled top k results of particular systems in a set of experiments.) R-precision adjusts for the size of the set of relevant documents: A perfect system could score 1 on this metric for each query, whereas, even a perfect system could only achieve a precision at 20 of 0.4 if there were only 8 documents in the collection relevant to an information need. Averaging this measure across queries thus makes more sense. This measure is harder to explain to naive users than Precision at k but easier to explain than MAP. If there are |Rel|relevant documents for a query, we examine the top |Rel| results of a system, and find that r are relevant, then by definition, not only is the precision (and hence R-precision) r/|Rel|, but the recall of this result set is also r/|Rel|. Thus, R-precision turns out to be identical to the break-even point, another measure which is sometimes used, defined in terms of this equality relationship holding. Like Precision at k, R-precision describes only one point on the precision-recall curve, rather than attempting to summarize effectiveness across the curve, and it is somewhat unclear why you should be interested in the break-even point rather than either the best point on the curve (the point with maximal F-measure) or a retrieval level of interest to a particular application (Precision at *k*). Nevertheless, R-precision turns out to be highly correlated with MAP empirically, despite measuring only a single point on the curve.

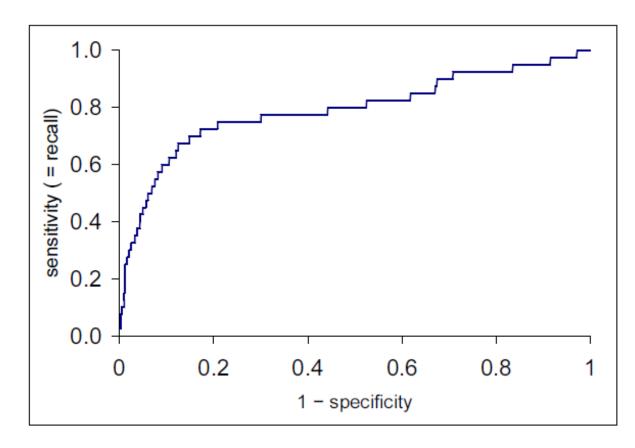
BREAK-EVEN POINT

ROC CURVE

SENSITIVITY

SPECIFICITY

Another concept sometimes used in evaluation is an ROC curve. ("ROC" stands for "Receiver Operating Characteristics", but knowing that doesn't help most people.) An ROC curve plots the true positive rate or sensitivity against the false positive rate or (1 - specificity). Here, sensitivity is just another term for recall. The false positive rate is given by fp/(fp+tn). Figure 8.4 shows the ROC curve corresponding to the precision-recall curve in Figure 8.2. An ROC curve always goes from the bottom left to the top right of the graph. For a good system, the graph climbs steeply on the left side. For unranked result sets, specificity, given by tn/(fp+tn), was not seen as a very useful notion. Because the set of true negatives is always so large, its value would be almost 1 for all information needs (and, correspondingly, the value of the false positive rate would be almost 0). That is, the "interesting" part of Figure 8.2 is 0 < recall < 0.4, a part which is compressed to a small corner of Figure 8.4. But an ROC curve could make sense when looking over the full retrieval spectrum, and it provides another way of looking at the data. In many fields, a common aggregate measure is to report the area under the ROC curve, which is the ROC analog of MAP. Precision-recall curves are sometimes loosely referred to as ROC curves. This is understandable, but not accurate.



▶ Figure 8.4 The ROC curve corresponding to the precision-recall curve in Figure 8.2.

```
rocx = np.zeros(N)
recall = np.zeros(N)
m = 0
for i in range(N):
    if sorted[i] in toptfidf:
        m = m + 1
        # tp = m, fn = relevant - m, fp = i + 1 - m, tn = N - tp - fn - fp
    rocx[i] = ?
    recall[i] = ?

plt.scatter(rocx, recall)
plt.show()
```

