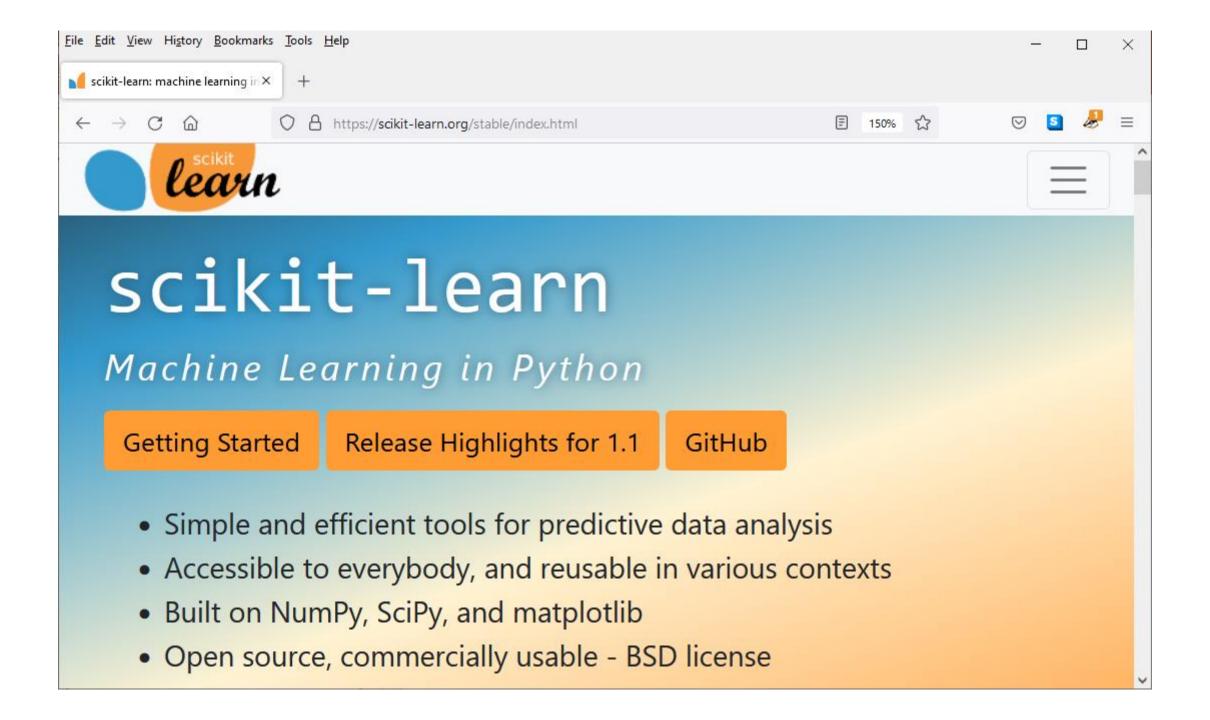
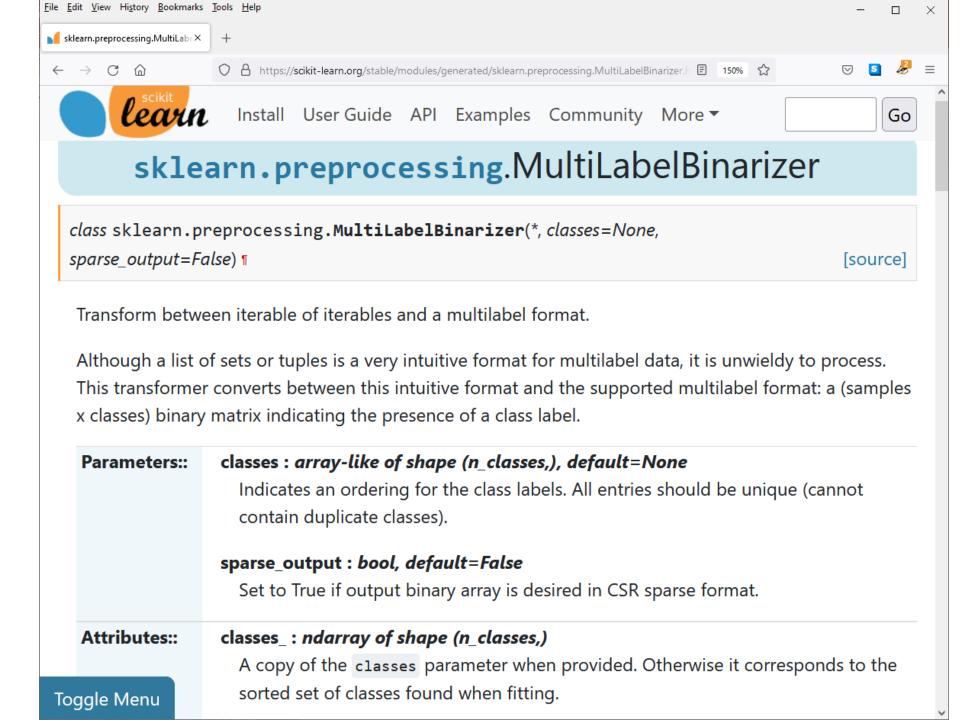
The Vector Space Model

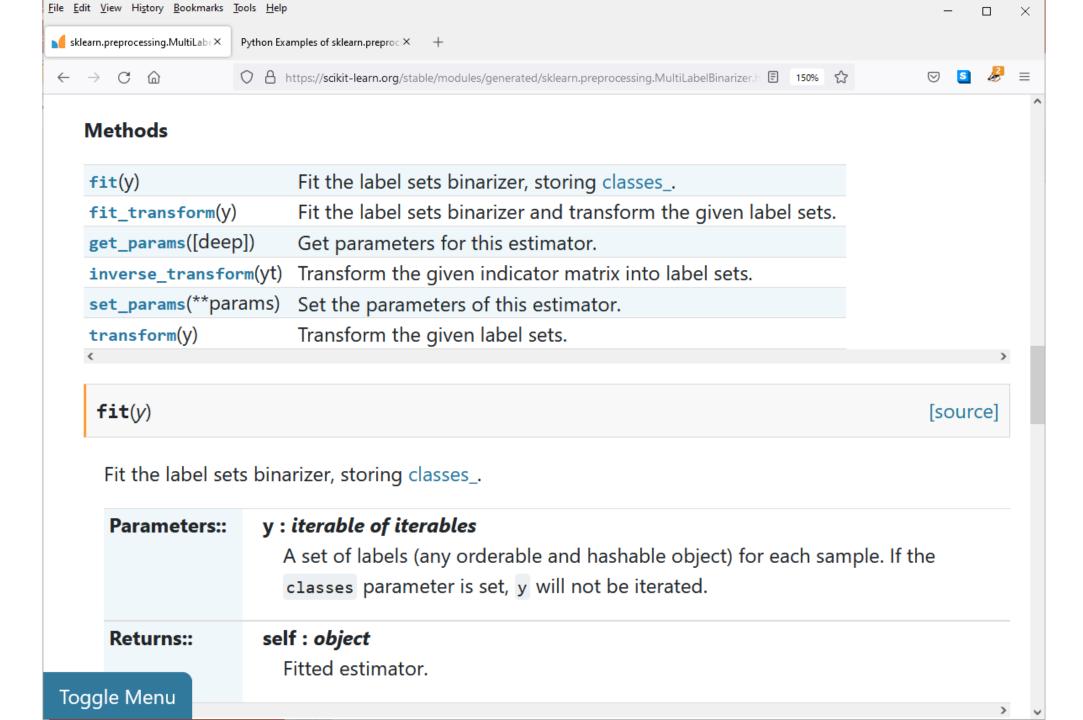
CS5154/6054

Yizong Cheng

9/8/2022







iirexercise1-2.txt

breakthrough drug for schizophrenia new schizophrenia drug new approach for treatment of schizophrenia new hopes for schizophrenia patients

```
import re
import numpy as np
from sklearn.preprocessing import MultiLabelBinarizer

f = open("iirexercise1-2.txt", "r")
docs = f.readlines()
f.close()
tokens = list(map(lambda s: re.findall('\w+', s), docs))
lb = MultiLabelBinarizer()
lb.fit(tokens)
print(lb.classes_)
```

['approach' 'breakthrough' 'drug' 'for' 'hopes' 'new' 'of' 'patients' 'schizophrenia' 'treatment']

The Document-Term Incidence Matrix

```
f = open("iirexercise1-2.txt", "r")
docs = f.readlines()
f.close()
tokens = list(map(lambda s: re.findall('\w+', s), docs))
lb = MultiLabelBinarizer()
lb.fit(tokens)
vectors = lb.transform(tokens)
print(vectors)
```

```
[[0 1 1 1 0 0 0 0 1 0]

[0 0 1 0 0 1 0 0 1 0]

[1 0 0 1 0 1 1 0 1 1]

[0 0 0 1 1 1 0 1 1 0]]
```

From Sets to Vectors

- A set {'new', 'schizophrenia', 'drug'} representing Doc2 is now
- A vector [0 0 1 0 0 1 0 0 1 0].
- In a ten-dimensional Euclidean space.
- Two vectors in the same space can have dot product (innerproduct).
 - Defined as sum of element products in all dimensions.
- Dot product = intersection.

Term-Document Matrix

	Anthony	Julius	The	Hamlet	Othello	Macbeth	
	and	Caesar	Tempest				
	Cleopatra						
Anthony	1	1	0	0	0	1	
Brutus	1	1	0	1	0	0	
Caesar	1	1	0	1	1	1	
Calpurnia	0	1	0	0	0	0	
CLEOPATRA	1	0	0	0	0	0	
MERCY	1	0	1	1	1	1	
WORSER	1	0	1	1	1	0	

Each document is represented as a binary vector $\in \{0,1\}^{|V|}$.

Binary Vector Representation of Documents

	Anthony	Julius	The	Hamlet	Othello	Macbeth	
	and	Caesar	Tempest				
	Cleopatra						
Anthony	1	1	0	0	0	1	
Brutus	1	1	0	1	0	0	
Caesar	1	1	0	1	1	1	
Calpurnia	0	1	0	0	0	0	
CLEOPATRA	1	0	0	0	0	0	
MERCY	1	0	1	1	1	1	
WORSER	1	0	1	1	1	0	

. . .

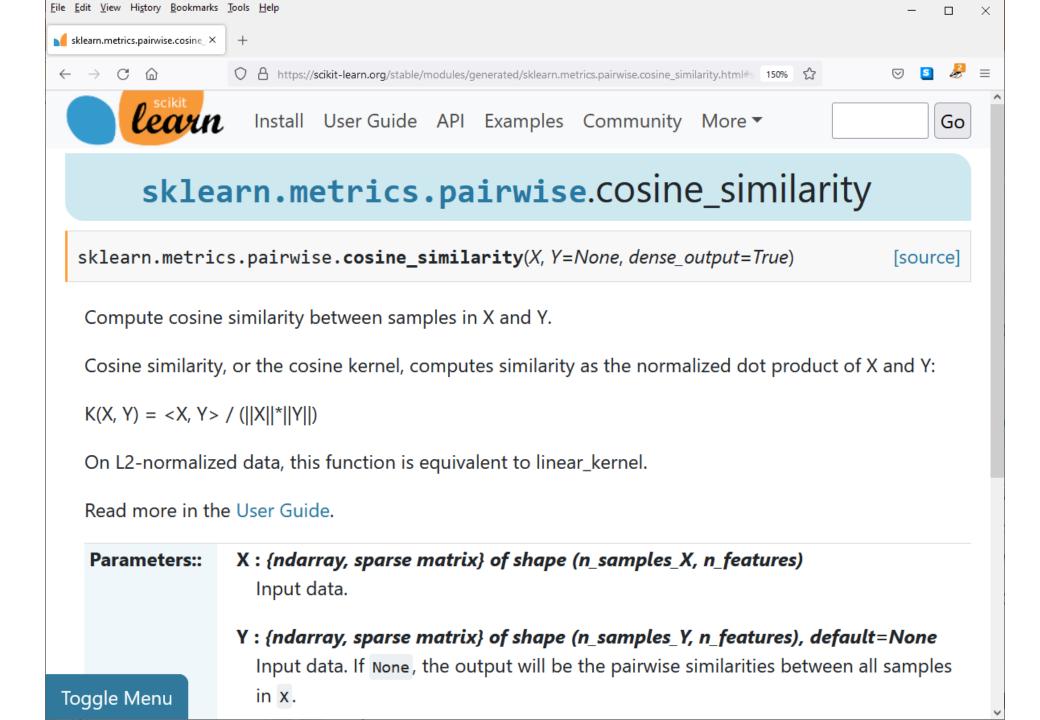
Each document is represented as a binary vector $\in \{0,1\}^{|V|}$.

Set Intersection is Vector Dot Product

```
f = open("iirexercise1-2.txt", "r")
docs = f.readlines()
f.close()
tokens = list(map(lambda s: re.findall('\w+', s), docs))
lb = MultiLabelBinarizer()
lb.fit(tokens)
vectors = lb.transform(tokens)
print(vectors)

print(np.dot(vectors[0], vectors[1]))
```

```
[[0111000010]
[0010010010]
[1001011011]
[0001110110]]
```



Cosine Similarity $|A \cap B|/V(|A||B|)$

```
import numpy as np
from sklearn.preprocessing import MultiLabelBinarizer
from sklearn.metrics.pairwise import cosine similarity
f = open("iirexercise1-2.txt", "r")
docs = f.readlines()
f.close()
tokens = list(map(lambda s: re.findall('\w+', s), docs))
lb = MultiLabelBinarizer()
lb.fit(tokens)
vectors = lb.transform(tokens)
print(vectors)
print(cosine similarity(vectors))
```

import re

```
[[0 1 1 1 0 0 0 0 1 0]

[0 0 1 0 0 1 0 0 1 0]

[1 0 0 1 0 1 1 0 1 1]

[0 0 0 1 1 1 0 1 1 0]]

[[1. 0.57735027 0.40824829 0.4472136]

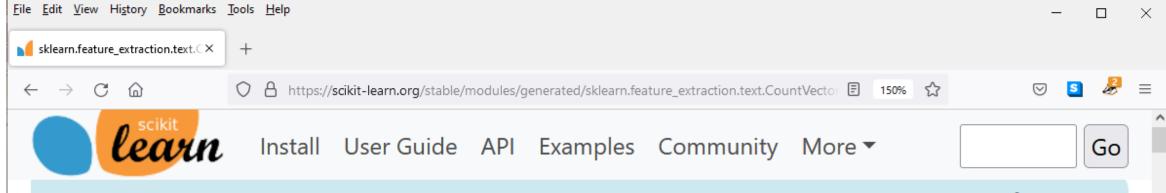
[0.57735027 1. 0.47140452 0.51639778]

[0.40824829 0.47140452 1. 0.54772256]

[0.4472136 0.51639778 0.54772256 1. ]]
```

Cosine Similarity is Normalized Intersection

- Dice coefficient: Dice (A, B) = $|A \cap B|/((|A| + |B|)/2)$
 - Intersection size divided by the arithmetic mean of the sizes of the two sets
- Cosine similarity: |A ∩ B||A|^{-1/2}|B|^{-1/2}
 - Intersection size divided by the geometric mean of the sizes of the two sets
 - $0.57735027 = (2)4^{-1/2} 3^{-1/2}$
- There are other means of two numbers.
 - Harmonic mean: $|A \cap B|(|A|^{-1} + |B|^{-1})$



sklearn.feature_extraction.text.CountVectorizer

class sklearn.feature_extraction.text.CountVectorizer(*, input='content', encoding='utf-8', decode_error='strict', strip_accents=None, lowercase=True, preprocessor=None, tokenizer=None, stop_words=None, token_pattern='(?u)\b\w\w+\b', ngram_range=(1, 1), analyzer='word', max_df=1.0, $min_df=1$, $max_features=None$, vocabulary=None, binary=False, dtype=<class 'numpy.int64'>) [source]

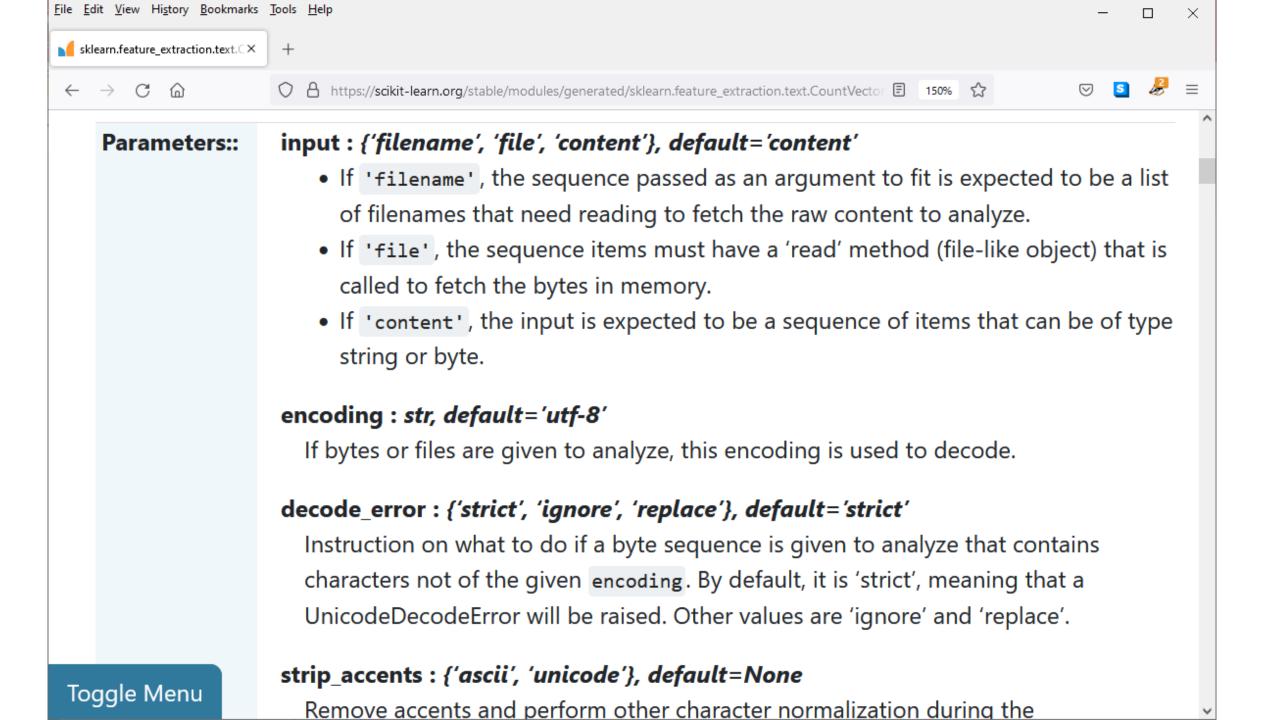
Convert a collection of text documents to a matrix of token counts.

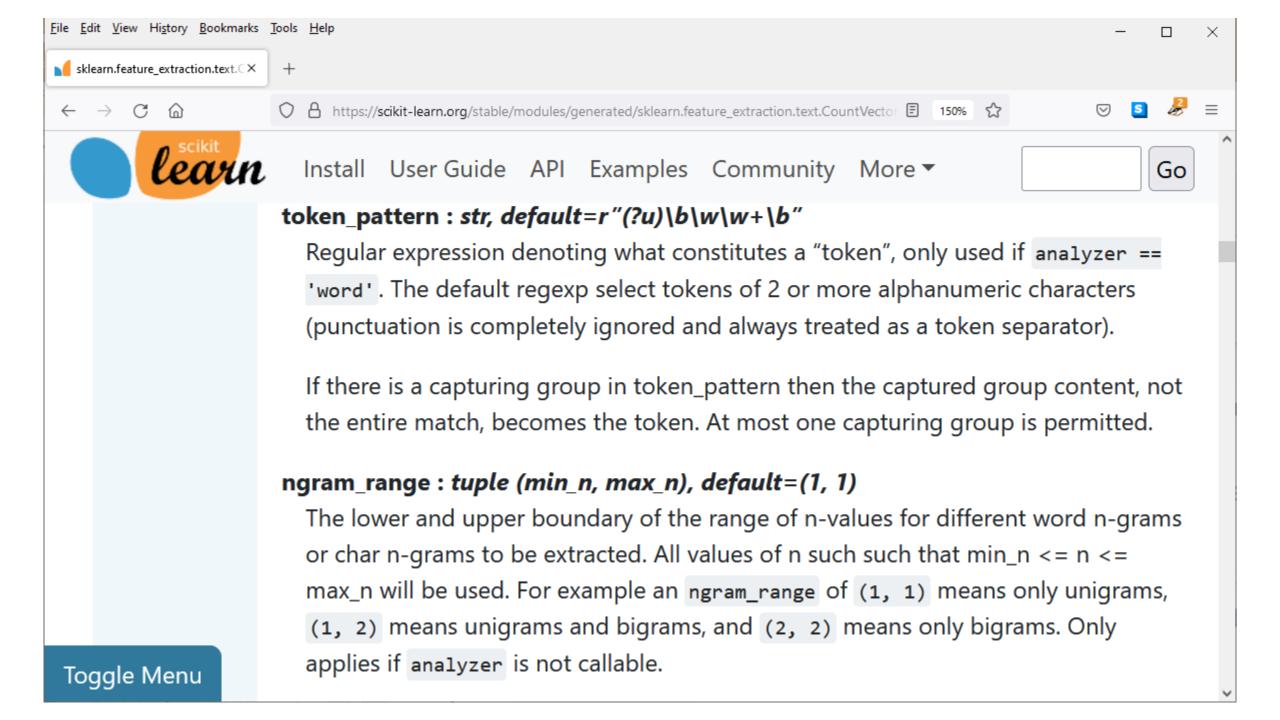
This implementation produces a sparse representation of the counts using scipy.sparse.csr_matrix.

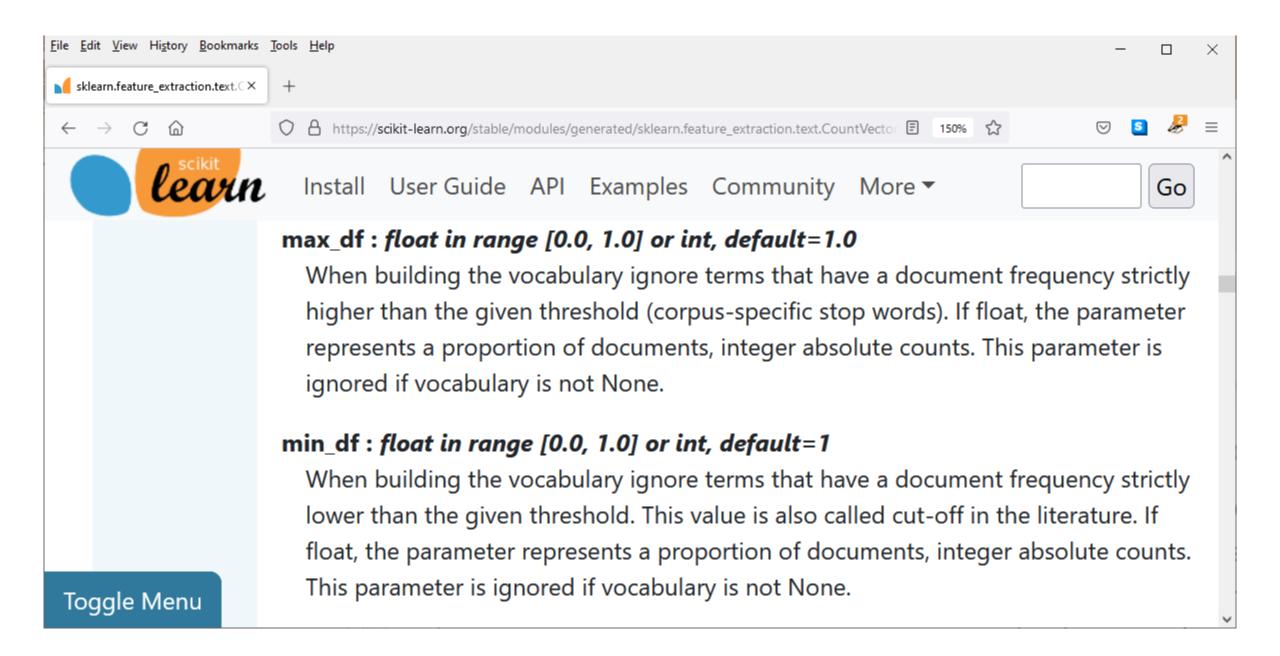
If you do not provide an a-priori dictionary and you do not use an analyzer that does some kind of feature selection then the number of features will be equal to the vocabulary size found by analyzing the data.

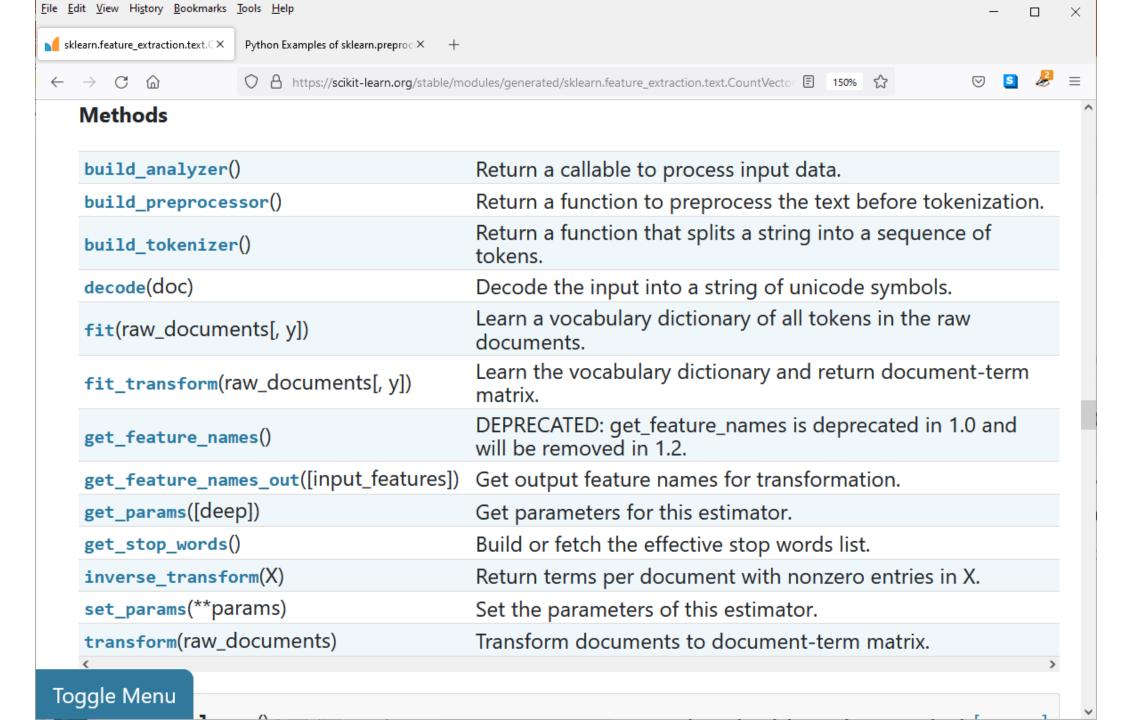
Toggle Menu

n the User Guide









```
# IR6B.py CS5154/6054 cheng 2022
# Usage: python IR6B.py
import re
import numpy as np
from sklearn.feature_extraction.text import CountVectorizer
from sklearn.metrics.pairwise import cosine_similarity
f = open("gutprotocol.txt", "r", encoding="utf8")
docs = f.readlines()
f.close()
cv = CountVectorizer()
cv.fit(docs)
print(cv.get_feature_names())
vectors = cv.transform(docs)
print(vectors)
```

C:\classes\6054>python IR6B.py '000', '000g', '10', '100', '101', '102', '103', '104', '105', '106', '107', '108', '109', '11', '110', '111', '112', 113', '114', '115', '116', '117', '118', '119', '12', '120', '13', '14', '15', '150', '16', '17', '18', '19', '20', '200 ', '21', '22', '23', '24', '25', '26', '27', '28', '29', '30', '300', '31', '32', '33', '34', '35', '36', '37', '38', ,'40','400g','41','42','43','44','45','450','46','47','48','488','49','50','500','500g','51','52', 53', '54', '55', '56', '57', '58', '59', '60', '600', '61', '62', '63', '64', '65', '650', '66', '67', '71', '72', '73', '74', '75', '76', '77', '78', '79', '80', '81', '82', '83', '84', '85', '86', '87', '88', '89', '900', '91', '92', '93', '94', '95', '96', '97', '98', '99', 'acceptable', 'accommodate', 'according', 'achieve', 'add 'adding', 'addition', 'additional', 'adhered', 'after', 'again', 'against', 'agar', 'air', 'alcohol', uots', 'all', 'allow', 'allowing', 'already', 'also', 'alternatively', 'aluminum', 'amount', 'amounts', 'an', 'anaerobic ', 'anaerobically', 'and', 'another', 'antifade', 'any', 'apical', 'appropriate', 'are', 'as', 'aside', 'aspirate', 'asp irating', 'aspiration', 'aspirator', 'assess', 'at', 'avoid', 'away', 'back', 'background', 'bacteria', 'bacterial', 'ba g', 'base', 'basolateral', 'bath', 'be', 'because', 'become', 'been', 'before', 'behavior', 'bend', 'bent', 'biosafety' 'block', 'blockaid', 'blue', 'both', 'bottom', 'break', 'bright', 'bring', 'bucket', 'buffer', 'but', 'by', 'cabinet', calculate', 'calculated', 'calculations', 'can', 'cap', 'capacity', 'carefully', 'case', 'cases', 'cause', 'cell', 'cel' ls', 'center', 'centrifugation', 'centrifuge', 'cfu', 'chamber', 'change', 'check', 'co2', 'coated', 'coating', 'cocultu re', 'cold', 'collagen', 'collect', 'collected', 'collection', 'colon', 'colonies', 'colony', 'comparing', 'completely' component', 'concentration', 'confluency', 'conical', 'connect', 'connecting', 'connects', 'containing', 'contains', content', 'continue', 'cool', 'cooling', 'corresponding', 'count', 'counted', 'countess', 'counting', 'cover', 'covered 'coverslip', 'critical', 'crs', 'cryotube', 'cryovial', 'culture', 'cup', 'currently', 'curve', 'cut', 'cycles', 'dapi 'data', 'day', 'density', 'depending', 'depends', 'described', 'desired', 'determine', 'diameter', 'did', 'differenti ation', 'dilute', 'diluted', 'diluting', 'dilution', 'dilutions', 'discard', 'dish', 'disinfect', 'disinfectant', 'dislo dge', 'dispense', 'disposable', 'disrupting', 'dissociate', 'dissociation', 'dissolved', 'disturbing', 'divide', 'dividi ng', 'donor', 'down', 'dpbs', 'drawing', 'dried', 'drop', 'droplet', 'droplets', 'dry', 'during', 'each', 'easily', 'edg 'edta', 'eight', 'end', 'endohm', 'ends', 'ensure', 'epithelial', 'equivalent', 'estimate', 'ethanol', 'evaluate', evaluating', 'evaporate', 'every', 'example', 'excessive', 'eye', 'factors', 'field', 'fig', 'fill', 'finally', 'firm', 'firmly', 'first', 'fit', 'fixative', 'flat', 'flip', 'foil', 'following', 'follows', 'for', 'forceps', 'formation', 'fo rming', 'formula', 'fragment', 'fragmentation', 'fragmented', 'fragments', 'fresh', 'friday', 'fridays', 'fridge', 'from , 'full', 'fully', 'further', 'gelation', 'generally', 'generate', 'generated', 'gentle', 'gently', 'get', 'getting

×

```
X
Command Prompt
trypan', 'trypsin', 'tube', 'tubes', 'turn', 'turned', 'tweezer', 'tweezers', 'two', 'typical', 'typically', 'under',
unit', 'unstable', 'until', 'up', 'use', 'used', 'using', 'vacuum', 'value', 'values', 'varies', 'vary', 'via', 'viabili
ty', 'vol', 'volume', 'wait', 'warm', 'was', 'wash', 'washing', 'water', 'we', 'well', 'wells', 'when', 'which', 'whole'
  'wide', 'will', 'wire', 'wires', 'wish', 'with', 'withdraw', 'workstation', 'ycfa', 'you', 'yourself', 'μg', 'μl', 'μm
  (0, 28)
  (0, 125)
  (0, 153)
  (0, 214)
  (0, 236)
 (0, 244)
 (0, 296)
  (0, 447)
  (0, 607)
 (0, 668)
  (0, 688)
  (0, 701)
  (0, 713)
 (1, 93)
  (1, 153)
  (1, 186)
 (1, 199)
  (1, 284)
  (1, 317)
 (1, 529)
  (1, 624)
  (1, 639)
 (1, 716)
                1
 (1, 724)
  (2, 195)
```

```
Command Prompt
                                                                                                                  ×
 (2, 195)
 (121, 668)
 (121, 689)
 (122, 25)
 (122, 28)
  (122, 142)
 (122, 198)
 (122, 251)
  (122, 253)
 (122, 303)
 (122, 307)
 (122, 365)
 (122, 385)
 (122, 442)
 (122, 445)
 (122, 483)
 (122, 488)
  (122, 519)
 (122, 543)
  (122, 595)
 (122, 599)
                2
 (122, 600)
  (122, 621)
 (122, 668)
 (122, 688)
 (122, 726)
C:\classes\6054>_
```

Count Matrix with Term Frequencies (TFs)

	Anthony	Julius	The	Hamlet	Othello	Macbeth	
	and	Caesar	Tempest				
	Cleopatra						
Anthony	157	73	0	0	0	1	
Brutus	4	157	0	2	0	0	
Caesar	232	227	0	2	1	0	
Calpurnia	0	10	0	0	0	0	
CLEOPATRA	57	0	0	0	0	0	
MERCY	2	0	3	8	5	8	
WORSER	2	0	1	1	1	5	

Each document is now represented as a count vector $\in \mathbb{N}^{|V|}$.

Count Vector Representation of Documents

	Anthony	Julius	The	Hamlet	Othello	Macbeth	
	and	Caesar	Tempest				
	Cleopatra						
Anthony	157	73	0	0	0	1	
Brutus	4	157	0	2	0	0	
Caesar	232	227	0	2	1	0	
Calpurnia	0	10	0	0	0	0	
CLEOPATRA	57	0	0	0	0	0	
MERCY	2	0	3	8	5	8	
WORSER	2	0	1	1	1	5	

. . .

Each document is now represented as a count vector $\in \mathbb{N}^{|V|}$.

To compensate for the effect of document length, the standard way of quantifying the similarity between two documents d_1 and d_2 is to compute the *cosine similarity* of their vector representations $\vec{V}(d_1)$ and $\vec{V}(d_2)$

 $sim(d_1, d_2) = \frac{\vec{V}(d_1) \cdot \vec{V}(d_2)}{|\vec{V}(d_1)||\vec{V}(d_2)|},$

COSINE SIMILARITY

DOT PRODUCT

EUCLIDEAN LENGTH

LENGTH-NORMALIZATION where the numerator represents the *dot product* (also known as the *inner product*) of the vectors $\vec{V}(d_1)$ and $\vec{V}(d_2)$, while the denominator is the product of their *Euclidean lengths*. The dot product $\vec{x} \cdot \vec{y}$ of two vectors is defined as $\sum_{i=1}^{M} x_i y_i$. Let $\vec{V}(d)$ denote the document vector for d, with M components $\vec{V}_1(d) \dots \vec{V}_M(d)$. The Euclidean length of d is defined to be $\sqrt{\sum_{i=1}^{M} \vec{V}_i^2(d)}$.

The effect of the denominator of Equation (6.10) is thus to length-normalize the vectors $\vec{V}(d_1)$ and $\vec{V}(d_2)$ to unit vectors $\vec{v}(d_1) = \vec{V}(d_1)/|\vec{V}(d_1)|$ and

 $\vec{v}(d_2) = \vec{V}(d_2)/|\vec{V}(d_2)|$. We can then rewrite (6.10) as

(6.11)
$$\sin(d_1, d_2) = \vec{v}(d_1) \cdot \vec{v}(d_2).$$

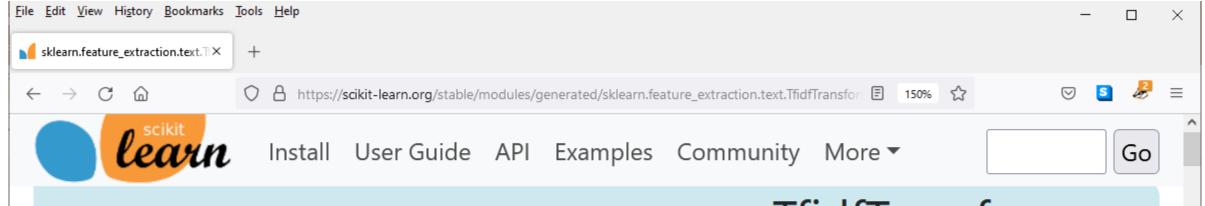
Example 6.2: Consider the documents in Figure 6.9. We now apply Euclidean normalization to the tf values from the table, for each of the three documents in the table. The quantity $\sqrt{\sum_{i=1}^{M} \vec{V}_{i}^{2}(d)}$ has the values 30.56, 46.84 and 41.30 respectively for Doc1, Doc2 and Doc3. The resulting Euclidean normalized tf values for these documents are shown in Figure 6.11.

	Doc1	Doc2	Doc3
car	27	4	24
auto	3	33	0
insurance	0	33	29
best	14	0	17

► Figure 6.9 Table of tf values for Exercise 6.10.

	Doc1	Doc2	Doc3
car	0.88	0.09	0.58
auto	0.10	0.71	0
insurance	0	0.71	0.70
best	0.46	0	0.41

▶ Figure 6.11 Euclidean normalized tf values for documents in Figure 6.9.



sklearn.feature_extraction.text.TfidfTransformer

class sklearn.feature_extraction.text.TfidfTransformer(*, norm='l2', use_idf=True,
smooth_idf=True, sublinear_tf=False)

Transform a count matrix to a normalized tf or tf-idf representation.

Tf means term-frequency while tf-idf means term-frequency times inverse document-frequency. This is a common term weighting scheme in information retrieval, that has also found good use in document classification.

[source]

The goal of using tf-idf instead of the raw frequencies of occurrence of a token in a given document is

to color down the impact of tokens that occur very frequently in a given corpus and that are hence

Toggle Menu ess informative than features that occur in a small fraction of the training corpus.



sklearn.feature_extraction.text.TfidfVectorizer

class sklearn.feature_extraction.text.**TfidfVectorizer**(*, input='content', encoding='utf-8', decode_error='strict', strip_accents=None, lowercase=True, preprocessor=None, tokenizer=None, analyzer='word', stop_words=None, token_pattern='(?u)\b\w\w+\b', ngram_range=(1, 1), max_df=1.0, min_df=1, max_features=None, vocabulary=None, binary=False, dtype=<class 'numpy.float64'>, norm='l2', use_idf=True, smooth_idf=True, sublinear_tf=False) [source]

Convert a collection of raw documents to a matrix of TF-IDF features.

Equivalent to CountVectorizer followed by TfidfTransformer.

n the User Guide.

```
# IR6C.py CS5154/6054 cheng 2022
# Usage: python IR6C.py
import re
import numpy as np
from sklearn.feature_extraction.text import TfidfVectorizer
from sklearn.metrics.pairwise import cosine_similarity
f = open("gutprotocol.txt", "r", encoding="utf8")
docs = f.readlines()
f.close()
tv = TfidfVectorizer(max_df=0.4, min_df=3)
tv.fit(docs)
print(tv.get_feature_names())
vectors = tv.transform(docs)
print(vectors)
```

(0, 67)

0.3651628007763991

C:\classes\6054>python IR6C.py '000', '000g', '10', '100', '102', '105', '12', '15', '20', '200', '24', '37', '45', '46', '50', '500', '60', '6 ', '84', '91', '96', '99', 'add', 'additional', 'after', 'again', 'agar', 'aliquot', 'aliquots', 'all', 'allow', 'alter natively', 'aluminum', 'an', 'anaerobic', 'apical', 'appropriate', 'are', 'as', 'aspirate', 'aspirator', 'at', 'avoid', 'back', 'bacteria', 'bacterial', 'base', 'basolateral', 'bath', 'be', 'before', 'biosafety', 'block', 'both', 'bottom', 'bring', 'bucket', 'by', 'cabinet', 'calculate', 'can', 'cap', 'carefully', 'cell', 'cells', 'centrifugation', 'centrifu ge', 'cfu', 'chamber', 'check', 'co2', 'coating', 'coculture', 'collagen', 'colon', 'completely', 'conical', 'containing ', 'contains', 'continue', 'cover', 'crs', 'cryovial', 'culture', 'curve', 'day', 'density', 'described', 'desired', 'de termine', 'dilution', 'dish', 'disinfectant', 'disposable', 'dissociation', 'disturbing', 'down', 'dpbs', 'droplet', oplets', 'during', 'each', 'edta', 'end', 'endohm', 'ethanol', 'every', 'example', 'fill', 'first', 'from', 'full', 'gen tly', 'glass', 'growth', 'have', 'ice', 'if', 'in', 'incubate', 'incubation', 'incubator', 'insert', 'inside', 'inspect' 'into', 'inverted', 'is', 'it', 'keep', 'least', 'let', 'make', 'matrigel', 'measurement', 'medium', 'membrane', 'micr oscope', 'min', 'mix', 'ml', 'monolayer', 'monolayers', 'needed', 'new', 'next', 'number', 'obtain', 'obtained', 'od600' 'ohmmeter', 'on', 'once', 'one', 'onto', 'or', 'organoid', 'organoids', 'original', 'outer', 'overnight', 'passaging' 'pasteur', 'pbs', 'pellet', 'per', 'pipette', 'pipetting', 'place', 'plate', 'plates', 'preempt', 'preparation', 'prepa re', 'prepared', 'prereduced', 'prewarmed', 'proceed', 'put', 'ratio', 'ready', 'record', 'remove', 'repeat', 'required' 'residual', 'respectively', 'resuspend', 'rinse', 'room', 'seed', 'seeding', 'set', 'should', 'side', 'sides', 'single 'size', 'small', 'solution', 'spray', 'staining', 'standard', 'step', 'steps', 'sterile', 'sterilize', 'supernatant' 'supplementary', 'surface', 'suspension', 'table', 'take', 'teer', 'temperature', 'that', 'thaw', 'then', 'there', 'the ', 'this', 'thoroughly', 'time', 'times', 'tip', 'tissue', 'top', 'transfer', 'transwell', 'transwells', 'trypsin', 'tu pe', 'tubes', 'tweezers', 'under', 'until', 'up', 'use', 'using', 'vacuum', 'values', 'via', 'vol', 'volume', 'washing' 'water', 'we', 'well', 'wells', 'when', 'which', 'will', 'wire', 'with', 'workstation', 'ycfa', 'µl'] (0, 237)0.3651628007763991 (0, 233)0.41104229322535957 (0, 193)0.3932449402525009 (0, 141)0.21306422155313334 (0, 97)0.43282449285216673 (0, 77)0.3255832481767333

×

Weight Matrix

	Anthony	Julius	The	Hamlet	Othello	Macbeth	
	and	Caesar	Tempest				
	Cleopatra						
Anthony	5.25	3.18	0.0	0.0	0.0	0.35	
Brutus	1.21	6.10	0.0	1.0	0.0	0.0	
Caesar	8.59	2.54	0.0	1.51	0.25	0.0	
Calpurnia	0.0	1.54	0.0	0.0	0.0	0.0	
CLEOPATRA	2.85	0.0	0.0	0.0	0.0	0.0	
MERCY	1.51	0.0	1.90	0.12	5.25	0.88	
WORSER	1.37	0.0	0.11	4.15	0.25	1.95	

. . .

Each document is now represented as a real-valued vector of tf-idf weights $\in \mathbb{R}^{|V|}$.

Weight Matrix

	Anthony	Julius	The	Hamlet	Othello	Macbeth	
	and	Caesar	Tempest				
	Cleopatra						
Anthony	5.25	3.18	0.0	0.0	0.0	0.35	
Brutus	1.21	6.10	0.0	1.0	0.0	0.0	
Caesar	8.59	2.54	0.0	1.51	0.25	0.0	
Calpurnia	0.0	1.54	0.0	0.0	0.0	0.0	
CLEOPATRA	2.85	0.0	0.0	0.0	0.0	0.0	
MERCY	1.51	0.0	1.90	0.12	5.25	0.88	
WORSER	1.37	0.0	0.11	4.15	0.25	1.95	

. . .

Each document is now represented as a real-valued vector of tf-idf weights $\in \mathbb{R}^{|V|}$.

```
COSINESCORE(q)

1 float Scores[N] = 0

2 Initialize Length[N]

3 for each query term t

4 do calculate w_{t,q} and fetch postings list for t

5 for each pair(d, tf_{t,d}) in postings list

6 do Scores[d] += wf_{t,d} \times w_{t,q}

7 Read the array Length[d]

8 for each d

9 do Scores[d] = Scores[d] / Length[d]

10 return Top K components of Scores[]
```

▶ Figure 6.14 The basic algorithm for computing vector space scores.