## BIST8130 - Final Project Report

 Mengfan Luo (ml<br/>4701) Yushan Wang (yw<br/>3772) Jing Lyu (jl<br/>6049) Yiqun Jin (yj<br/>2686) Mingkuan Xu (mx<br/>2262)

## Abstract

In this project, we aim to build regression models based on a set of demographic variables to estimate county-level crime rates. After an exploratory analysis of the variables on their distributions and correlations, we derived more meaningful variables by manipulating the existing ones, removed outlier values, and implemented several variable selection methods. Using the selected variables, we trained a linear regression model, elaborated on the model by adding several interactive terms, and did cross-validations. All 3 resulting models have achieved a good estimation of the training set. We selected the third model (adjusted R-square: 0.542, RMSE: 16.46, RMSPE: 11.90) as the final model, as it has the best prediction on testing set. Further studies can be done on correcting the dataset using external data sources, as well as using more sophisticated non-linear models.

## Introduction

Over the last three decades, crime has become a major public concern in the US arousing massive political discussion and public expenditure[1]. Crime rates in major cities experienced a general rise from the 1960s to 1990s, with two peaks observed in 1980 and in early 1990s[2]. Despite extensive attention across the nation, factors influencing crime trends were not yet made clear[1]. In this project, we examined crime rate and potential factors that affect the crime rate in "County Demoraphic Information" (CDI), and constructed multiple linear regression model to predict crime rate.

## Methods

## **Data Description**

We analyzed data from the "County Demographic Information" (CDI) data set, which contains characteristics of 440 counties in the United States collected from 1990-1992. The primary goal of this investigation is to develop insight relevant to predicting the crime rate in counties.

**Data Preprocessing** Transform vairables in order to extract interpretable information.

**Exploratory Analysis** Calculate the pairwise correlations between variables and ist all correlations between the crime rate (our interest) and other variables.

#### Statistical Methods

**Training/Testing Set Split:** Randomly split the dataset into training (90%) and testing sets (10%) to avoid overfitting.

Remove Outliers and High Leverage Points: Use percentile to detect potential outliers and high leverage points. Remove rows containing the smallest and largest 0.2% for each variable given the size of the dataset.

Variable Selection: Select key variables using stepwise regression and criteria based procedure and conduct interaction analysis,

**Model Construction:** Build linear regression models using selected variables, interaction terms (p-value < 0.2). Attempt model transformations.

Cross Validation: Use 5-fold cross validation on each model to estimate model performances.

**Model Assessment:** Assess the models and choose a final model used for future prediction. Compare the models based on three criteria: the R-square values, the root mean square error (RMSE), and the root mean square prediction error (RMSPE).

## Results

#### Descriptive Analysis

We noticed that crimes, physicians, and hospital beds in the original dataset are given as numbers, while other info are given as proportions. We therefore computed the number of crimes, physicians, and hospital beds per 1000 people. Population density could be a key factor to crime rate. Thus, we also derived a new variable, density, which is population divided by area.

We drew boxplots and histogram to visualize continuous variables, a categorical variable, and the dependent variable crime rate (Figure 1,2,3). We identified several extreme values that can be

treated as potential outliers to be removed in further analysis.

From the pairwise plots (see .Rmd for details), we did not recognize any relationship between each variable. We further investigated pairwise correlations (Figure 4). Correlation analysis suggested that the derived variable density is a more meaningful variable with a stronger association to the crime rate compared to area and population.

After a preliminary analysis of the data, we identified several variables that might be relevant to the crime rate (Table 1).

## **Data Preprocessing**

We randomly sampled 10% from the dataset as a testing set (n = 44) and put the rest into a training set (n = 396). We then removed 19 rows with outliers and high leverage points from a total of 396 training data.

#### Variable Selection

Both stepwise and backward procedures gave the same set of variables (Table 2): pop, pop18, bagrad, poverty, pcincome, totalinc, region, beds\_rate\_1000.

The output of criteria based procedure (Figure 5) suggested that the number of variables should be above 12 (region was converted into 3 dummy variables) because  $C_p \leq p$ . We therefore also put unemp and density into candidate list. In addition, We removed totaline, because it can be replaced with totaline = peincome \* pop.

### Interaction Analysis

poverty & income. We divided poverty into two categories: higher and lower than the national poverty rate in 1990 [4]. We observed an intersection of the two lines (Figure 6), suggesting that the association between crime rate and per capita income is modified by poverty status.

pcincome & bagrad. We divided bagrad into two categories: higher and lower than the national bachelor's degree percentage [4]. We observed that the association between crime rate and per

capita income is modified by percent bachelor's degrees status (Figure 7).

### **Model Construction**

By adding interation terms to the model built with selected variables, we resulted in the following three models:

**Model 1** was built using the following terms: pop, pop18, bagrad, poverty, unemp, pcincome, pcincome\*pop, region, beds\_rate\_1000, density.

**Model 2** was built using the following terms: pop, pop18, bagrad, poverty, unemp, pcincome, pcincome\*pop, region, beds\_rate\_1000, poverty\*pcincome

**Model 3** was built using the following terms: pop, pop18, bagrad, poverty, unemp, pcincome, pcincome\*pop, region, beds\_rate\_1000, density, pcincome\*bagrad

## Model Diagnosis and Transformation

Using Variable Inflation Factor (VIF), we determined if each model had a high collinearity. The 3 models all have passed the collinearity test (See .Rmd for details).

We then drew diagnostic plots for each model to see how the residuals behaved. In all three models, residuals followed a normal distribution ( $\mu = 0$ ) with no influential points (See .Rmd for details).

In addition, we drew boxcox plots to see if each model needed transformation. The peak of all three boxcox plots fell between 0.5 and 1 (see .Rmd for details). As such, we tried  $\sqrt{y}$  transformation for each model. Since the residuals were more unevenly distributed in all three transformed models, we kept the three untransformed models (Table 3).

#### Model Assessment

We performed cross validation on each model and got the RMSE average and R-square values. We further assessed the models in the testing set by RMSPE (Table 4).

## Conclusion and Discussion

According to table 5, evaluated in terms of accuracy in estimating the training set, model 2 has the best performance with its leading R square and the smallest RMSE, followed by model 3 and model 1. In terms of predicting values outside the training set, model 3 has the best performance with the smallest RMSPE on the testing set. Such an inconsistency of model performance may be explained by model overfitting of the training data. Above all, although model 2 have achieved a good estimation of the training set, we will choose model 3 as the final model, given its fair RMSE and R-square values, plus excellent testing set performance. By using model 3, we can predict the crime rate by the following parameters.

Overall, our project has several strengths. First, we did feature engineering before training the model by transforming variables using our domain knowledge to the ones more relevant to the predicted variable. For example, while area and population are not directly related to the crime rate, population density (population/area) can be more relevant. Second, we did analysis of correlation and collinearity to reduce potential bias. Third, we did interactive analysis and involved multiple interactive terms in our model, which to some extents represented the possible non-linear relations between the parameters and the predicted value. Finally, we separated a testing set from the dataset at the very beginning, on which we evaluated the performance of several models, addressing the potential predicting errors caused by model overfitting.

Meanwhile, the project also has its limitations. Essentially, we identified several wrong data points in the original dataset: for example, the population of Los Angles, an outstandingly large number, is not consistent with the number found on Wikipedia. Given that some of the data are mistaken, further works can be done on correcting the dataset using external data sources. Furthermore, our regression model considered only linear and interactive terms, while some parameters could be better fitted using polynomials or exponentials. More sophisticated models can be used in the future to better estimate the data.

## Reference and Documentation

- [1] Committee on Law and Justice, et al. *Understanding Crime Trends: Workshop Report*. Edited by Arthur S. Goldberger and Richard Rosenfeld, National Academies Press, 2009. Accessed 11 December 2021.
- [2] Rosenfeld, R., Vogel, M. & McCuddy, T. Crime and Inflation in U. S. Cities. *J Quant Criminol* 35, 195–210 (2019). https://doi.org/10.1007/s10940-018-9377-x
- [3] U.S. Department of Commerce Economics and Statistics Administration, Bureau of the Census. Current Population Reports. Poverty in the United States: 1990. Series P-60, No.175
- [4] Bureau of the Census. We asked... You told us. Census Questionnaire Content, 1990 CQC-13
- [5] Friedman, Jerome, Trevor Hastie, and Robert Tibshirani. The elements of statistical learning.Vol. 1. No. 10. New York: Springer series in statistics, 2001.

As Numerous new questions emerging during our discussion, our group explored materials below to solve them.

- Question: Do we still need a test set when using k-fold cross-validation? Source: https://stats.stackexchange.com/questions/225949/do-we-need-a-test-set-when-using-k-fold-cross-validation https://datascience.stackexchange.com/questions/80310/is-a-test-set-necessary-after-cross-validation-on-training-set
- 2. Question: How to achieve build test set & predict Source: https://www.ritchieng.com/machine-learning-evaluate-linear-regression-model/ https://campus.datacamp.com/courses/machine-learning-with-caret-in-r/regression-models-fitting-them-and-evaluating-their-performance?ex=8
- 3. Question: How to evaluate continuous by continuous interactions Source: Continuous by Continuous Interactions, Joel S Steele http://web.pdx.edu/~joel8/resources/ConceptualPresentationResources/ContinuousByContinuousInteractions\_walkthrough\_v2.

  pdf

# Appendix

Table 1: Potential Variables Relevant to the Crime Rate

Variable	Meaning					
area	Land area					
density	Population Density					
pop	Esimate 1990 population					
pop18	Percent of population aged 18-34					
pop65	Percent of population aged 65+					
$docs_rate_1000$	Number of active physicians per 1000 people					
beds_rate_1000	Number of hospital beds per 1000 people					
$crime\_rate\_1000$	Number of serious crimes per 1000 people					
hsgrad	Percent high school graduates					
bagrad	Percent bachelor's degrees					
poverty	Percent below poverty level					
unemp	Percent unemployment					
pcincome	Per capita income					
totalinc	Total personal income					
region	Geographic region (1=Northeast, 2=North Central, 3=South, 4=West)					

Table 2: Vairable selected from stepwise regression

backward	stepwise	
pop	pop	_
pop18	pop18	
bagrad	bagrad	
poverty	poverty	
pcincome	pcincome	

Table 4: Model 3 Parameters

Parameters	Meaning
pop	Esimate 1990 population
pop18	Percent of total population in age range from 18-34
beds_rate_1000	Total number of hospital beds, cribs and bassinets during 1990 per 1000 people
bagrad	Percent of person 25 years old or older with bachelor's degrees
poverty	Percent of 1990 total population with income below poverty level
unemp	Percent of labor force that is unemployed
pcincome	Income (in dollars) per person among those in 1990 population
region	Geographic region
pcincome*pop	Per capita income * Total Population
pcincome*bagrad	Per capita income * Percent bachelor's degrees

backward	stepwise					
totalinc	totalinc					
region2	region2					
region3	region3					
region4	region4					
beds_rate_1000	beds_rate_1000					

Table 3: Model assessment table

Model	R Square	RMSE	RMSPE
1	0.534	16.60	12.06
2	0.561	16.20	12.32
3	0.542	16.46	11.90

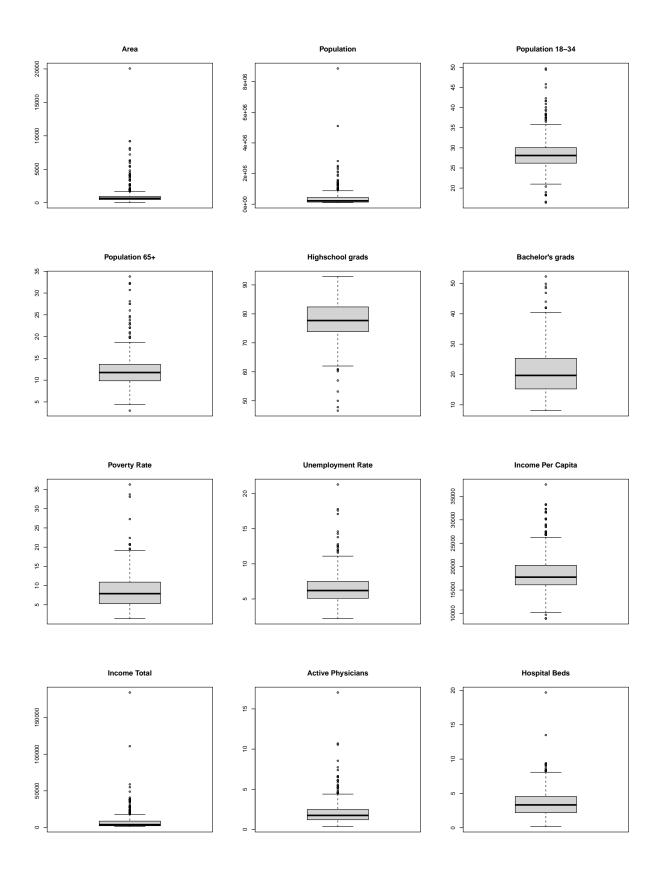


Figure 1: boxplot of continuous variables distribution

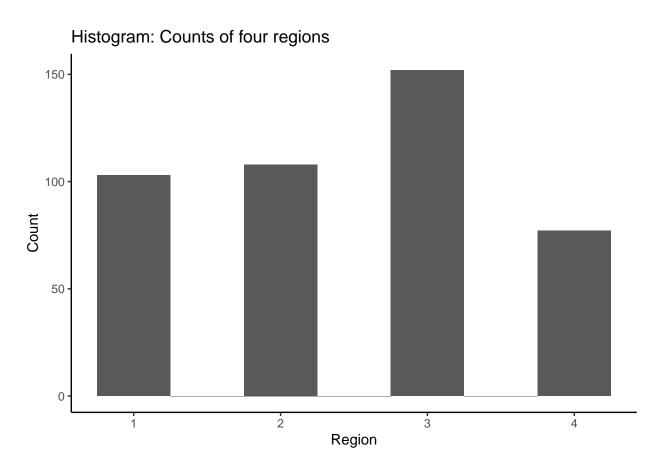


Figure 2: Histogram of catagorical variable:region distribution

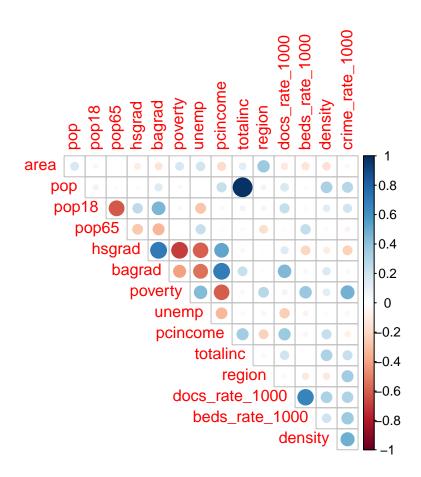


Figure 3: Correlation heatmap

## **Crime Rate**

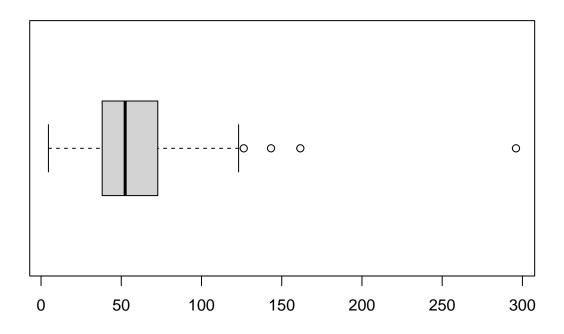


Figure 4: boxplot of dependent variable: crime rate

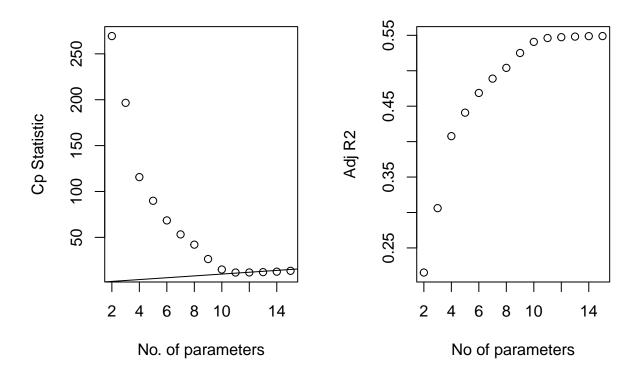


Figure 5: Subset selection for best parameter numbers

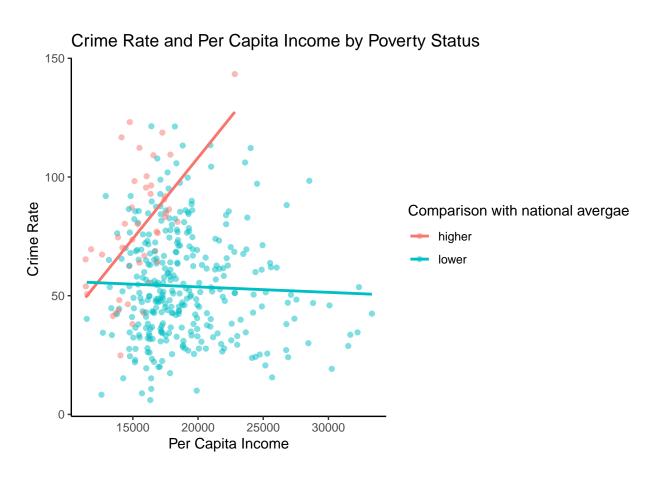


Figure 6: Interaction plot of Income Per Capita and Poverty

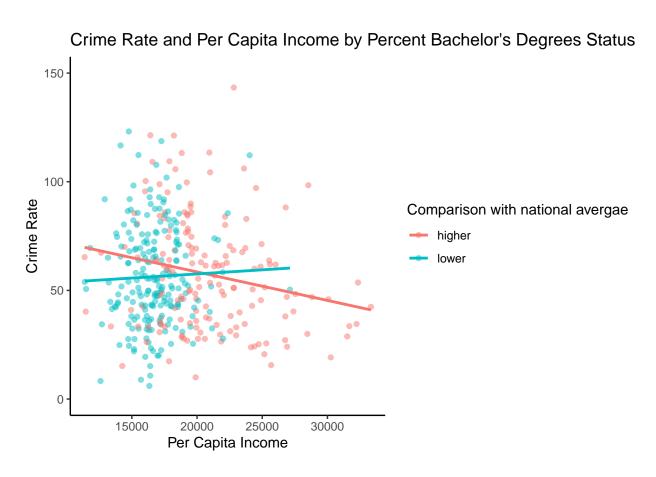


Figure 7: Interaction plot of Income Per Capita and Bachelor's Degree Status

Table 3: Models summary

	Model 1					141	odel 2		Model 3			
Coeffcient	Estimates	std. Error	Conf. Int (95%)	P-Value	Estimates	std. Error	Conf. Int (95%)	P-Value	Estimates	std. Error	Conf. Int (95%)	P-Value
Intercept	-83.18	15.49	-113.63 – -52.72	<0.001	-41.43	15.68	-72.27 – -10.59	0.009	-114.11	19.63	-152.72 – -75.51	<0.001
Total population	0.00	0.00	0.00 - 00.0	<0.001	0.00	0.00	- 00.0 0.00	<0.001	0.00	0.00	- 00.0 0.00	<0.001
Percent of population aged 18-34	1.25	0.32	0.62 – 1.88	<0.001	0.93	0.23	0.47 - 1.38	<0.001	1.05	0.33	0.40 - 1.69	0.002
Bachelors proportion	-0.37	0.25	-0.86 – 0.13	0.145					1.25	0.69	-0.10 – 2.60	0.069
Percent below poverty level	1.66	0.39	0.90 – 2.43	<0.001	-2.78	1.09	-4.93 – -0.62	0.012	1.91	0.40	1.12 - 2.69	<0.001
Percent unemployment	0.75	0.53	-0.30 – 1.79	0.160	0.94	0.48	-0.01 – 1.90	0.052	0.90	0.53	-0.14 – 1.94	0.091
Per Capita income	0.00	0.00	0.00 - 00.0	<0.001	0.00	0.00	-0.00 – 0.00	0.112	0.01	0.00	0.00 - 0.01	<0.001
Region-North Central	12.03	2.62	6.88 – 17.18	<0.001	10.79	2.57	5.73 – 15.85	<0.001	12.44	2.60	7.32 – 17.56	<0.001
Region-South	29.67	2.68	24.40 - 34.95	<0.001	27.69	2.64	22.50 - 32.89	<0.001	29.79	2.66	24.55 – 35.02	<0.001
Region-West	24.63	3.13	18.47 - 30.78	<0.001	21.32	3.03	15.35 – 27.28	<0.001	24.32	3.11	18.21 - 30.43	<0.001
Number of hospital beds per 1000 person	3.09	0.69	1.74 – 4.44	<0.001	1.99	0.72	0.56 – 3.41	0.006	2.74	0.69	1.37 – 4.11	<0.001
Density	0.00	0.00	-0.00 – 0.00	0.199					0.00	0.00	-0.00 – 0.00	0.134
Total Population*income per capita	-0.00	0.00	-0.00 – -0.00	<0.001	-0.00	0.00	-0.00 – -0.00	<0.001	-0.00	0.00	-0.00 – -0.00	<0.001
Poverty*income per capita					0.00	0.00	- 00.0 0.00	<0.001				
Bachelors proportion*income per capita									-0.00	0.00	-0.00 – -0.00	0.012
Observations	367				367				367			
R2 / R2 adjusted	0.563 / 0.	548			0.580 / 0	.567			0.571 / 0.	555		