Algorithms 2018







Consider the following 4 x 4 array.

	0	1	2	3
0	3	-3	-2	-1
1	2	6	-5	1
2	-3	-5	2	4
3	2	4	0	-2

• The sum of numbers in the following gray rectangle becomes 2 (=6-5-5+2+4+0).

3	-3	-2	- 1
2	6	-5	1
-3	-5	2	4
2	4	0	-2

• The sum of numbers in the following gray rectangle becomes 5 (=1+4).

3	-3	- 2	-1
2	6	- 5	1
- 3	- 5	2	4
2	4	0	- 2

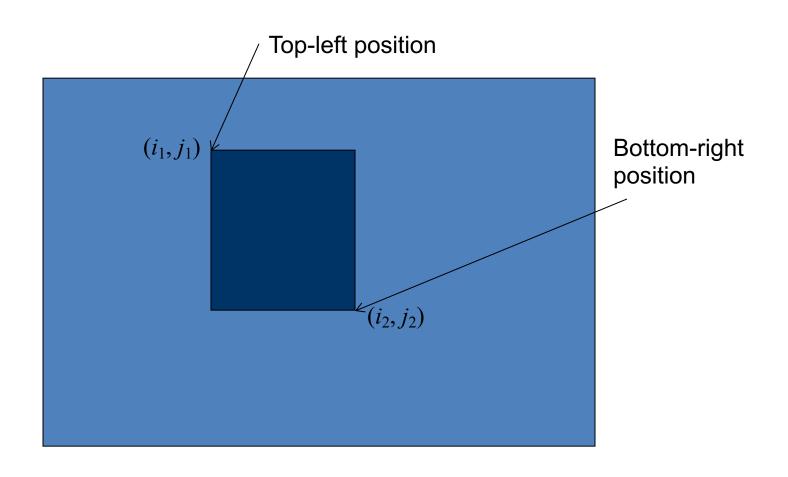
• The sum of numbers in the following gray rectangle becomes 8 (=2+6).

3	-3	-2	- 1
2	6	-5	1
-3	-5	2	4
2	4	0	-2

• The sum of numbers in the following gray rectangle becomes -8 (=-3-5).

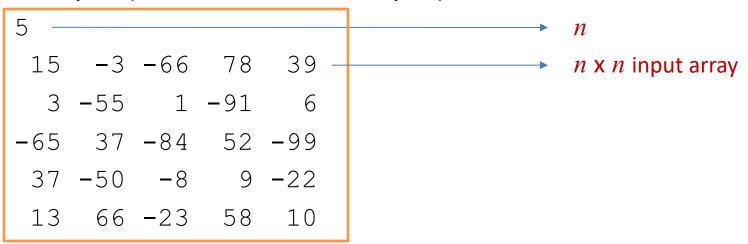
3	-3	-2	- 1
2	6	-5	1
-3	-5	2	4
2	4	0	-2

- Given an n x n integer array, your program should find a rectangle such that the sum of numbers in the rectangle is maximized/minimized.
- Your program should output the maximum/minimum summation value in the first line, and in the next line, the top-left and bottom-right positions of the rectangle that gives the maximum/minimum summation value.
- Note that n is less than or equal to <u>1,000</u>.



Examples (1/4)

Input (standard/console input)





Examples (2/4)

- Input (standard/console input)
 - testcase100.txt



Examples (3/4)

- Input (standard/console input)
 - testcase500.txt



Examples (4/4)

- Input (standard/console input)
 - testcase1000.txt



Naïve Method

• $O(n^6)$ -time algorithm

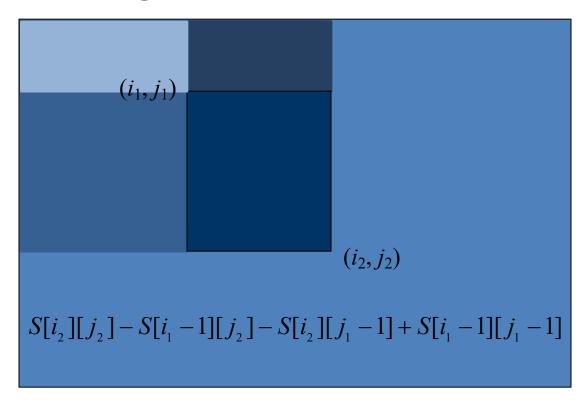
$$(i_{1}, j_{1})$$

$$(i_{2}, j_{2})$$

$$\sum_{r=i_{1}}^{i_{2}} \sum_{c=j_{1}}^{j_{2}} A[r][c]$$

Better Method

• $O(n^4)$ -time algorithm



Your Method

- Design $O(n^3)$ -time algorithm
 - Dynamic Programming

 Cf. Section 2.6 and Problem 2.f of the auxiliary textbook.

Due Date

Soft deadline: May 13, 2018

Hard deadline: May 20, 2018

But, will be deducted 10% per one day from your original

score

Submission Date	Deduction Rate
May 14	10%
May 15	20%
May 16	30%
May 17	40%
May 18	50%
May 19	60%
May 20	70%
May 21	100%

Notice (cont'd)

- You should observe the format of input & output exactly.
- You should submit a compressed file (HW2_your-ID.zip) containing the following three files to the "u-campus" web-site (http://info.kw.ac.kr).
 - HW2_your-ID.hwp/doc // report document
 - HW2_your-ID.cpp/cc (or .java) // source code
 - HW2_your-ID.exe // executable file

Notice (cont'd)

Source code

- It should be compiled in
 - C/C++ Language: Visual Studio 2010 or higher, or g++
 - Java Language: not restricted
 - You should note your environment in your report.
- Your name and student ID should be noted at the top of your source files in the form of comment.

Report

- Free format.
- But, it must include several examples for testing your program and your own discussion.
- It will be an important factor for getting a good score.
- Mention your programming language together with compiler.