BACS2063 Data Structures and Algorithms

Array Implementations of Collection ADTs

Chapter 4

Learning Outcomes

At the end of this chapter, you should be able to

- Implement the ADTs list, stack and queue using arrays.
- Discuss the strengths and weaknesses of using arrays to implement the ADTs.
- Analyze the efficiency of the array implementations of the ADTs

Recall: Creating an ADT

Step 1 Write the ADT specification

Write an ADT specification which describes the characteristics of that data type and the set of operations for manipulating the data. Should not include any implementation or usage details.

Step 2 Implement the ADT

- a. Write a Java interface
 - Include all the operations from the ADT specification
- b. Write a Java class
 - This class implements the Java interface from a.
 - Determine how to represent the data
 - Implement all the operations from the interface

Step 3 Use the ADT in a client program or application

Collection ADTs

- An ADT that can store a collection of objects.
- A <u>linear</u> collection is a collection that stores its entries in a linear sequence, e.g.:
 - List
 - Stack
 - Queue

They differ in the restrictions they place on how these entries may be added, removed, or accessed

Lists





A list provides a way to organize data



Fig. 4-1 A to-do list.

Operations on Lists

- Add new entry at end, or anywhere
- Remove an item
- Replace an entry
- Get an entry at a specified position
- Count how many entries
- Check if list is empty, full

Step 1: Write the ADT specification

- Refer to Appendix 4.1 for List ADT specification
 - Note that in this specification, entries in the list have positions that begin with 1 to be consistent with typical lists used in everyday life.
- Remember that at this point,
 - You should not think about how to represent the list in your program or how to implement its operations.
 - Instead, focus on <u>what</u> are the operations and <u>what</u>
 the operations do, <u>not how</u> they do them.
 - i.e., at this point, the list is an abstract data type.

Design Issues

 When you specify an ADT, you need to decide how to handle special / unusual conditions, and the ADT specification should include details on how the special conditions would be handled by the various operations.

Possible Solutions

- 1. Assume the invalid situations will not occur
- 2. Ignore the invalid situations
- Make reasonable assumptions, act in predictable way
- 4. Return boolean value indicating success or failure of the operation
- 5. Throw an exception

Possible Solutions #1 & 2 - Do Nothing!

- Assume the invalid situations will not occur
- Ignore the invalid situations



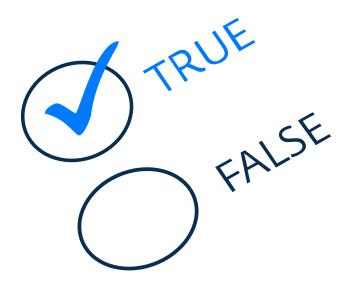
Possible Solutions #3 - Make Assumptions!

Make reasonable assumptions, act in predictable way



Possible Solutions #4 - Return Boolean Value!

 Return boolean value indicating success or failure of the operation



Possible Solutions #5 - Throw Exception!

Throw an exception



Step 2: Implement the List ADT (1)

- Step 2a: Write the Java interface
 - Contains the method declarations of all the operations listed in the List ADT specification.
 - All the methods are abstract methods.
- Refer to Chapter 4\adt\
 - ListInterface.java

Step 2: Implement the List ADT (2)

Step 2b: Write the Java class

- □ Data fields in the Java class:
 - An array to store the elements of the list
 - An integer variable to keep track of the current total number of elements in the list

```
T[] array;  // array of list entries
int numberOfEntries; // current no. of entries in the list
```

Note: **T** represents the data type of the entries in the list. It will be defined as generic type within the class.

Generic Types (1)

- Used in Java interface and classes which implement <u>collection</u> ADTs to specify and constrain the type of objects being stored in the collection.
- The interface name or class name is followed by an identifier enclosed in angle brackets:
 - public interface ListInterface<T>
- The identifier T which can be any identifier but usually is a single capital letter – represents the data type within the class definition.

Generic Types (2)

 When you use the class, you supply an actual type argument to replace T, e.g.:

ListInterface<String> taskList;

- Now, whenever T appears as a data type in the definition of ListInterface, String will be used.
- Note: A generic type <u>must be α reference type</u>, not a primitive type.

Using Generic Type in a Java Interface

```
public interface ListInterface<T> {

   /**
   * Task: Adds a new entry to the end of the list. Entries currently in the
   * list are unaffected. The list's size is increased by 1.
   *
   * @param newEntry the object to be added as a new entry
   * @return true if the addition is successful, or false if the list is full
   */
   public boolean add(T newEntry);
```

Using Generic Type in a Java Class

```
package adt;
import java.io.Serializable;
public class ArrayList<T> implements ListInterface<T>, Serializable {
 private T[] array;
 private int numberOfEntries;
 private static final int DEFAULT_CAPACITY = 5;
 public ArrayList() {
  this(DEFAULT_CAPACITY);
```

How a client creates a reference type variable when the class uses Generic Type T?

```
public class TestArrayList{
  public static void main(String[] args) {
    ListInterface<Customer> custList = new ArrayList<>();
    custList.add(new Customer("123","Amy"));
    custList.add(new Customer("444","Dylan"));
```

Step 2: Implement the List ADT (2)

- Step 2b: Write the Java class (cont'd)
 - Implements the interface ListInterface
 - Operations are implemented as Java methods:
 - Core operations as appears in the list ADT specification and also the interface ListInterface
 - Utility operations to support the core operations. This are implemented as private methods.

Issues to consider for the operations

• add, remove, replace, getEntry work OK when valid position given

 remove, replace and getEntry not meaningful on empty lists

 A list could become full, what happens to add?

Method add(newEntry)

- Adds a new item at the end of the list
 - Assign new value at end
 - Increment length of list

0	1	2	3	4	5	6	length
apple	orange	durian	lemon	plum			5

add(newPosition, newEntry)

- Adds an item in at a specified position
 - Requires a utility method makeRoom() to shift elements ahead

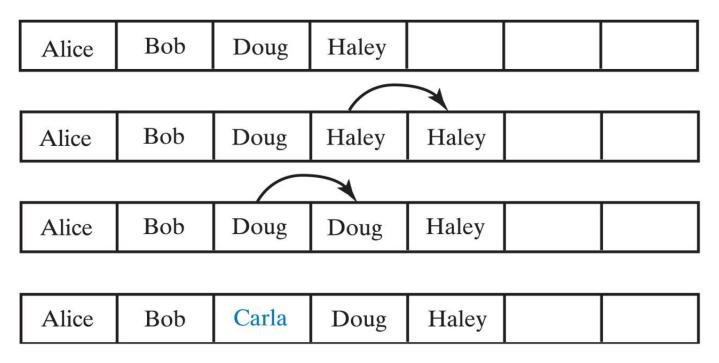
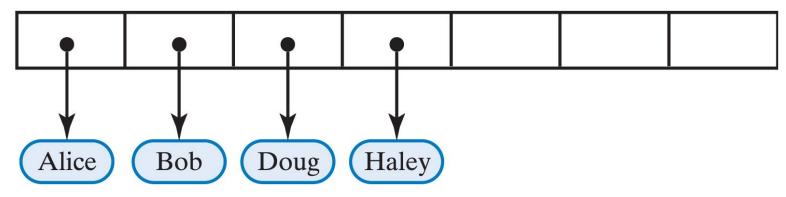


Fig. 5-3 Making room to insert Carla as third entry in an array.

Array of Objects References

 An array of objects actually contain references to those objects



 For simplicity, figures portray arrays as if they actually contained objects

Alice Bob	Doug	Haley			
-----------	------	-------	--	--	--

Method remove(givenPosition)

- Removes the item at the specified position.
- Must shift existing entries to avoid gap in the array – requires the utility method removeGap()
 - Except when removing last entry
- Method must also handle error situations
 - When position specified in the remove is invalid
 - When remove() is called and the list is empty
 - Invalid call returns null value

Removing a List Entry

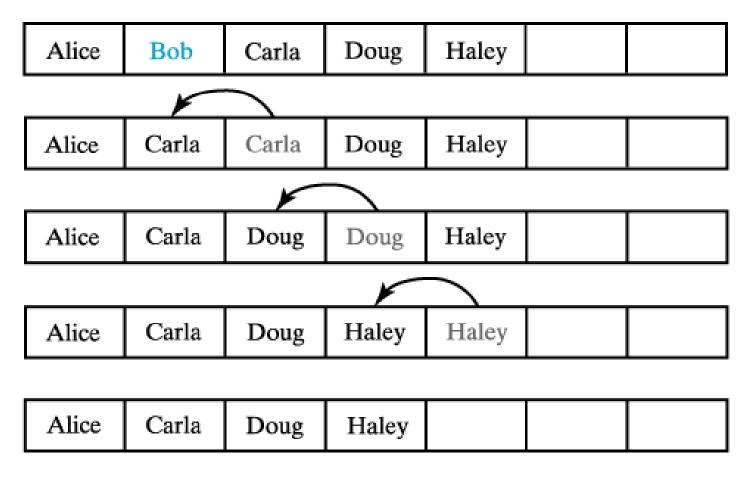


Fig. 5-5 Removing Bob by shifting array entries.

Algorithms for Other Methods?



replace(int, T) Method

```
@Override
public boolean replace(int givenPosition, T newEntry) {
 boolean isSuccessful = true;
 if ((givenPosition >= 1) && (givenPosition <= numberOfEntries)) {
  array[givenPosition - 1] = newEntry;
 } else {
  isSuccessful = false;
 return isSuccessful;
```

getEntry(int) method

```
@Override
public T getEntry(int givenPosition) {
  T result = null;

if ((givenPosition >= 1) && (givenPosition <= numberOfEntries)) {
  result = array[givenPosition - 1];
  }

return result;
}</pre>
```

contains(T) method

```
@Override
public boolean contains(T anEntry) {
   boolean found = false;
   for (int index = 0; !found && (index < numberOfEntries); index++) {
     if (anEntry.equals(array[index])) {
        found = true;
      }
   }
   return found;
}</pre>
```

The Java Implementation

Refer to:

Chapter4\adt\ArrayList.java

Note:

- In the interface ListInterface, each abstract method corresponds to an ADT list operation.
- Since the ArrayList class implements ListInterface,
 ArrayList contains the implementation of each abstract method of ListInterface.

Problem

 What if the array becomes full, i.e. all the array locations are assigned entries?

Expanding an Array (1/4)

- An array has a fixed size
 - If we need a larger list, we are in trouble
- When array becomes full, move its contents to a larger array (dynamic expansion)
 - Copy data from original to new location
 - Manipulate names so new location keeps name of original array
- Need two utility methods for expanding an array:
 - isArrayFull()to determine if the array is already full
 - doubleArray() to expand the array

Expanding an Array (2/4)

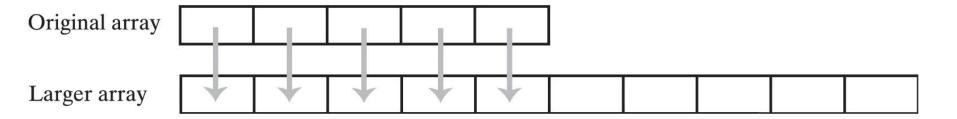


Fig. 5-6 The dynamic expansion of an array copies the array's contents to a larger second array.

Expanding an Array (3/4)

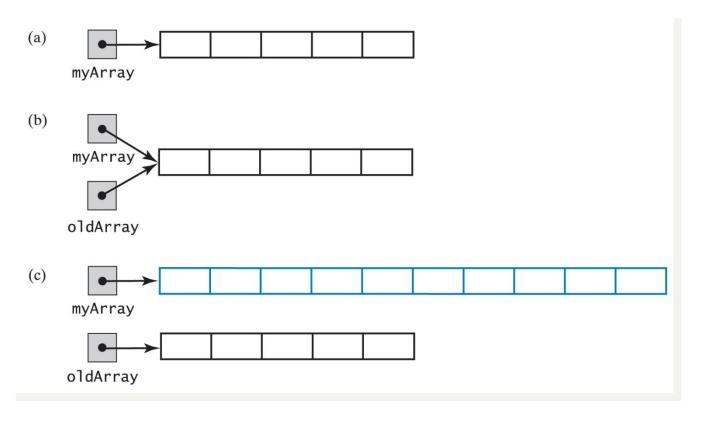


Fig. 5-7 (a) an array;

- (b) the same array with two references;
- (c) the two arrays, reference to original array now referencing a new, larger array

Expanding an Array (4/4)

 Code to accomplish the expansion shown in Fig. 5-7, previous slide

Expandable List Implementation

- Change the isFull to always return false
 - We will expand the array when it becomes full
 - We keep this function so that the original interface does not change
- The add() methods will double the size of the array when it becomes full
- Now declare a private method isArrayFull
 - Called by the add() methods

Pros and Cons of Array Implementation for the ADT List

- ☑ Retrieving an entry is fast
- ☑ Adding an entry at the end of the list is fast

- *Adding or removing an entry that is between other entries requires shifting elements in the array
- Increasing the size of the array requires copying elements

Sample Code

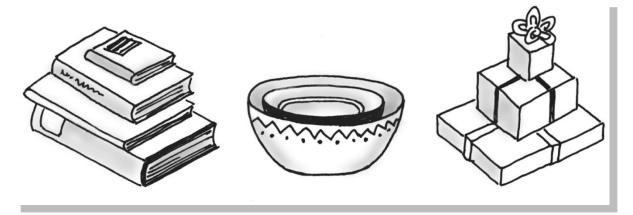
- Chapter4\adt\
 - ListInterface.java
 - ArrayList.java
- Chapter4\entity\
 - Runner.java
- Chapter4\client\
 - Registration.java

Stacks





- New items are added to the top of the stack,
 i.e. the item most recently added is always on
 the top. The most recently added item is
 always the next item to be removed.
- Exhibits LIFO behavior.



ADT Stack's Basic Operations

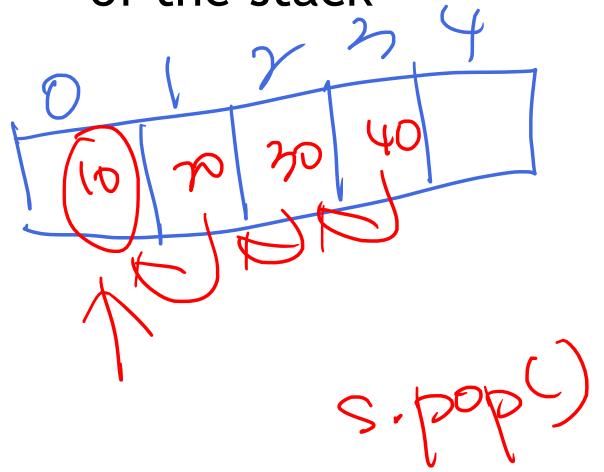
push(newEntry)pop()peek()isEmpty()

clear()

Array Stack Implementation: Consideration

- When using an array to implement a stack
 - The array's first element should represent the bottom of the stack
 - The last occupied location in the array represents the stack's top
- This avoids shifting of elements of the array if it were done the other way around

Using the first element as the top of the stack



Using the last element as the top of the stack 5. push (5

Comparison of 2 approaches

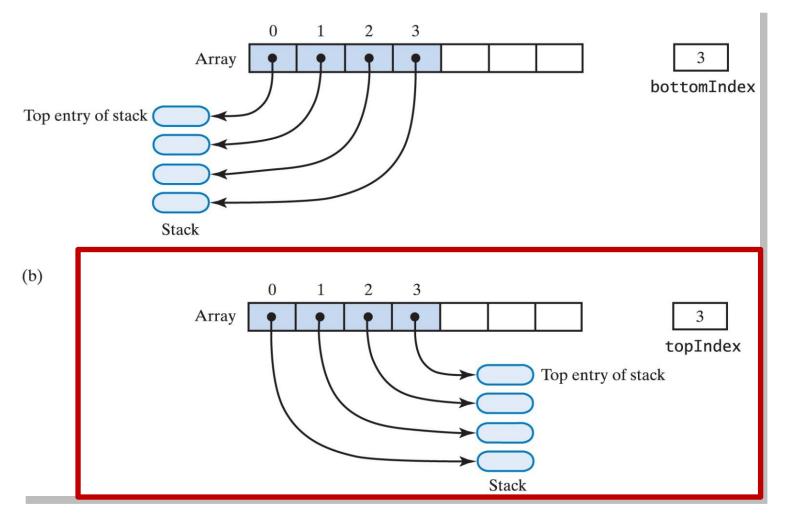


Fig. 22-4 An array that implements a stack; its first location references (a) the top of the stack; (b) the bottom of the stack

Array Stack Implementation

- Java interface: refer to StackInterface.java
- Data fields in the Java class:
 - An array to store the entries of the stack
 - An integer variable represents the array index of the top entry; initialized to -1 to indicate an empty stack

```
T[] array;  // array of stack entries
int topIndex; // index of the top entry
```

Java class: refer to ArrayStack.java

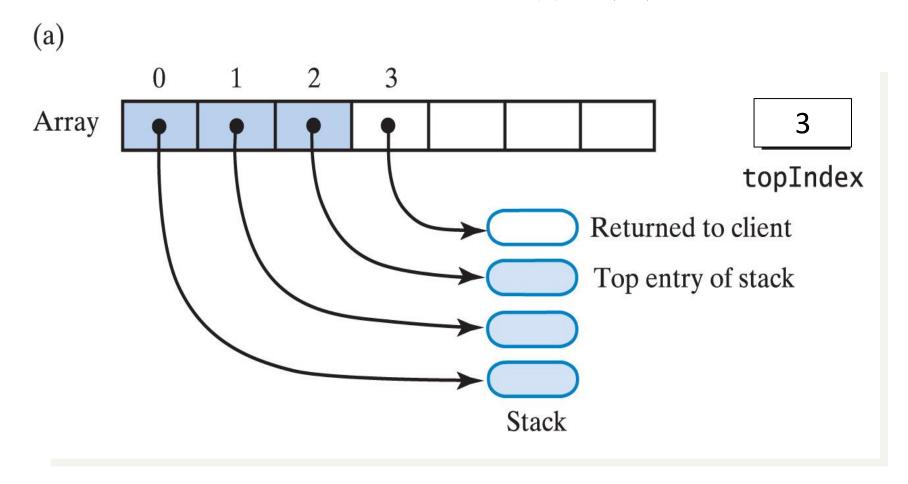
Method push(newEntry)

- Adds a new item at the top of the stack
 - Increment topIndex
 - Assign new value at the array location indicated by topIndex

Method pop() (1)

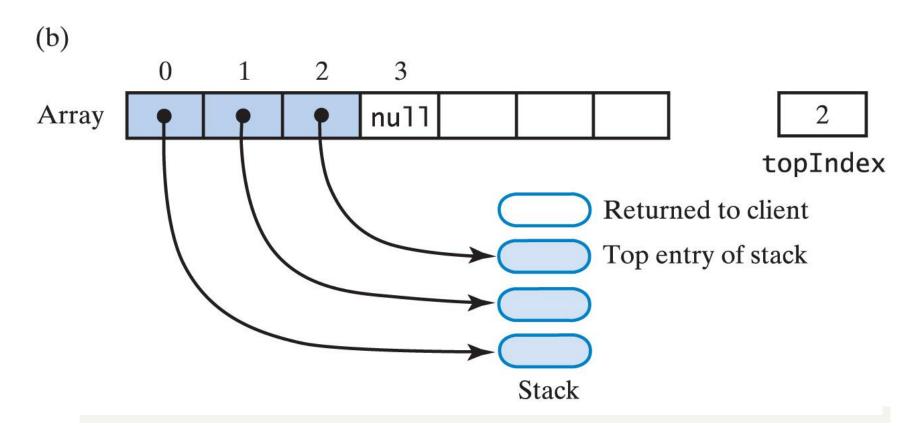
- Removes the entry at the top of the stack
 - Assign the entry at the array location indicated by topIndex to a temporary variable (to be returned)
 - 2. Decrement topIndex

Method pop() (2)



Assign the value at the array location indicated by **topIndex** to a temporary variable to be returned to the calling method

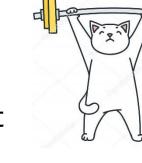
Method pop() (3)



Setting array[topIndex]=null and then decrement topIndex

Exercise 4.1

Write the algorithm for the method **convertNumberToBinary(int number)** to convert the given number to its equivalent binary (base-2) representation and returns the result as a string value.



Hint: use a stack.

- 1. Create a stack of Integers
- 2. while number is not 0
 - 2.1 remainder = number % 2
 - 2.2 push remainder on the stack
 - 2.3 update number i.e., number /= 2
- 3. Declare variable binaryStr as an empty string
- 4. while the stack is not empty
 - 4.1 pop the top value from the stack
 - 4.2 concatenate the top value to binaryStr
- 5. return binaryStr

Exercise 4.1: Example 7

Divide the number repeatedly by 2 until the quotient becomes 0.

```
Remainders
```

- When 7 is divided by 2, the quotient is 3 and the remainder is 1.
- When 3 is divided by 2, the quotient is 1 and the remainder is 1.
- When 1 is divided by 2, the quotient is 0 and the remainder is 1.

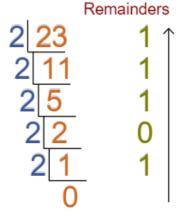
Write the remainders from bottom to top.

The decimal number 7 is 111 in binary form

Exercise 4.1: Example 23

• 1%2 = <mark>1</mark>

Divide the number repeatedly by 2 until the quotient becomes 0.



- When 23 is divided by 2, the quotient is 11 and the remainder is 1.
- When 11 is divided by 2, the quotient is 5 and the remainder is 1.
- When 5 is divided by 2, the quotient is 2 and the remainder is 1.
- When 2 is divided by 2, the quotient is 1 and the remainder is 0.
- When 1 is divided by 2, the quotient is 0 and the remainder is 1.

Write the remainders from bottom to top.

The decimal number 23 is 10111 in Binary Form.

Decimal to Binary Conversion

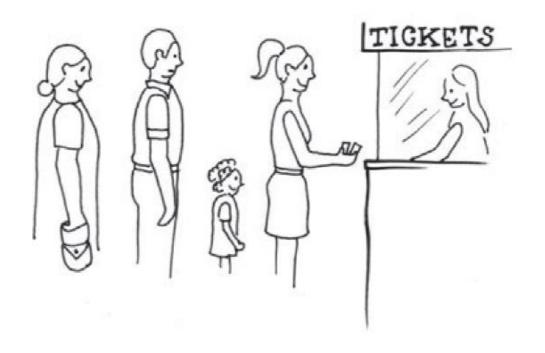
Answers with step-by-step

 https://madformath.com/calculators/basicmath/base-converters/decimal-to-binaryconverter-with-steps/decimal-to-binaryconverter-with-steps

Sample Code

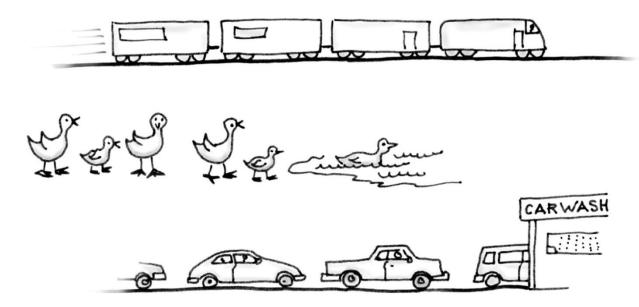
- Chapter4\adt\
 - StackInterface.java
 - ArrayStack.java
- Chapter4\client\
 - StringReversal.java

Queues





- Queue organizes entries according to order of entry - exhibits FIFO behavior
- All additions are at the back of the queue. Front of queue has items added first



ADT Queue's Basic Operations

- enqueue
- dequeue
- getFront
- isEmpty
- clear

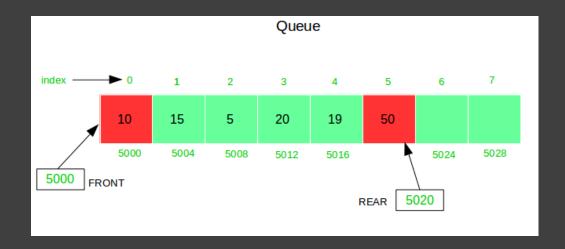
Array Queue Implementation

- Java interface: refer to QueueInterface.java
- Data fields in the Java class:
 - An array to store the entries of the queue
 - Two integer variables to represent
 - the array index of the front of the queue and
 - the array index of the back of the queue

```
T[] array;  // array of queue entries
int frontIndex; // index of the front entry
int backIndex; // index of the back entry
```

Array Queue Implementation: Variations

- 1. Linear array with fixed front
- 2. Linear array with dynamic front
- 3. Circular array



Method 1: Linear Array with Fixed Front

Data Fields

- The front of the queue is fixed to array[0],
 i.e., frontIndex is always 0.
- backIndex initialized to -1 to indicate an empty queue

Method enqueue()

- Increment backIndex
- Assign new value at the array location indicated by backIndex

```
public void enqueue(T newEntry) {
  if (!isArrayFull()) {
    backIndex++;
    array[backIndex] = newEntry;
  }
}
```

Method dequeue()

- Assign the entry at array location 0 to a temporary variable (to be returned)
- Shift entries from array location 1 to backIndex one step towards the front of the array
- 3. Decrement backIndex

Method dequeue()

Method isEmpty()

Method 1: Linear Array Fixed Front

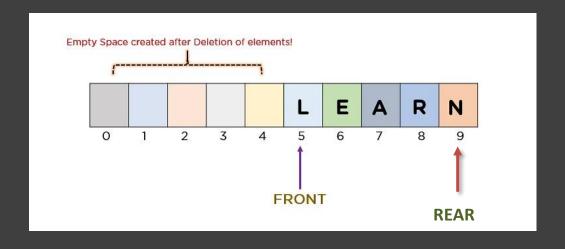
The queue is empty if backIndex is equal to -1

```
public boolean isEmpty() {
  return frontIndex > backIndex;
}
```

Method 1: Linear Array Fixed Front

Strength and Weakness

- Easy to understand as it is similar to how everyone else in a queue moves forward a step
- The dequeue operation is inefficient: there's overhead incurred as must shift entries each time we remove an entry



Method 2: Linear Array with Dynamic Front

Data Fields

Method 2: Linear Array Dynamic Front

- **frontIndex** is *dynamic*, *i.e.*, we instead "move" (i.e. update) **frontIndex**
- backIndex initialized to -1; frontIndex initialized to 0

Method enqueue()

Method 2: Linear Array Dynamic Front

- Increment backIndex
- Assign new value at the array location indicated by backIndex

Method dequeue()

Method 2: Linear Array Dynamic Front

- Assign the entry at array location frontIndex to a temporary variable (to be returned)
- 2. Increment frontIndex

Method 2: Linear Array Dynamic Front

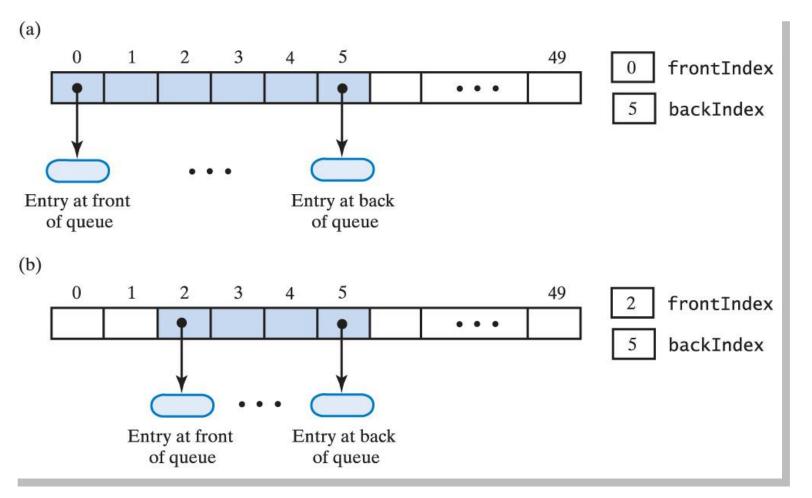


Fig. 24-6 An array that represents a queue without shifting its entries: (a) initially; (b) after removing the front twice;

Method isEmpty()

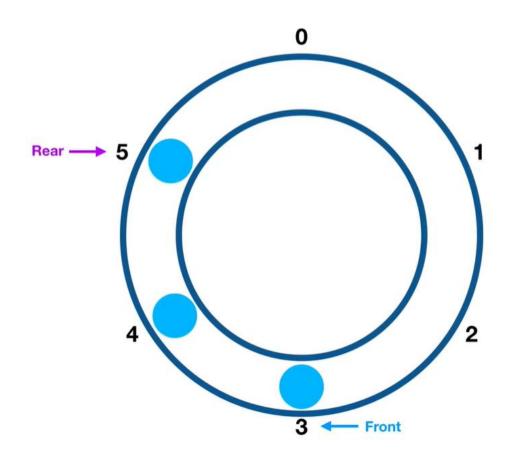
Method 2: Linear Array Dynamic Front

• The queue is empty if backIndex < frontIndex

Method 2: Linear Array Dynamic Front

Strength and Weakness

- Do not have to shift entries after each dequeue operation.
- Problem: Rightward drift, i.e. the array can become "full" when the last array location has been occupied but there are empty locations in the beginning part of the array.
 - How to use the empty locations?



Data Fields

- When queue reaches end of array, add subsequent entries to beginning
- Array behaves as though it were circular
 - First location follows last one
- backIndex initialized to -1; frontIndex initialized to 0
- Use *modulo arithmetic* to update indices:

```
backIndex = (backIndex + 1) % array.length
frontIndex = (frontIndex + 1) % array.length
```

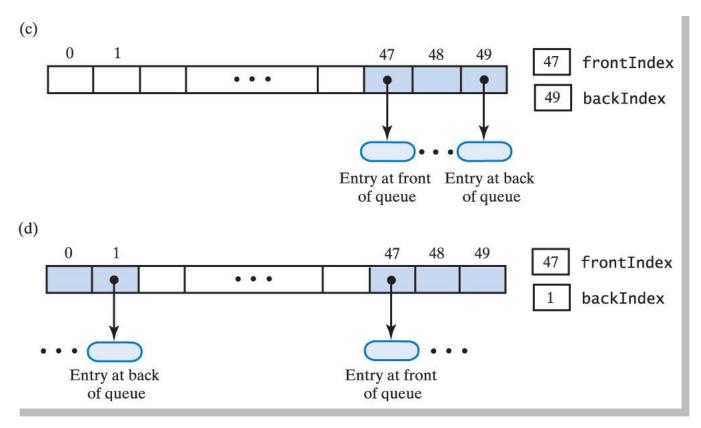


Fig. 24-6 An array that represents a queue without shifting its entries: (c) after several more additions & removals; (d) after two additions that wrap around to the beginning of the array

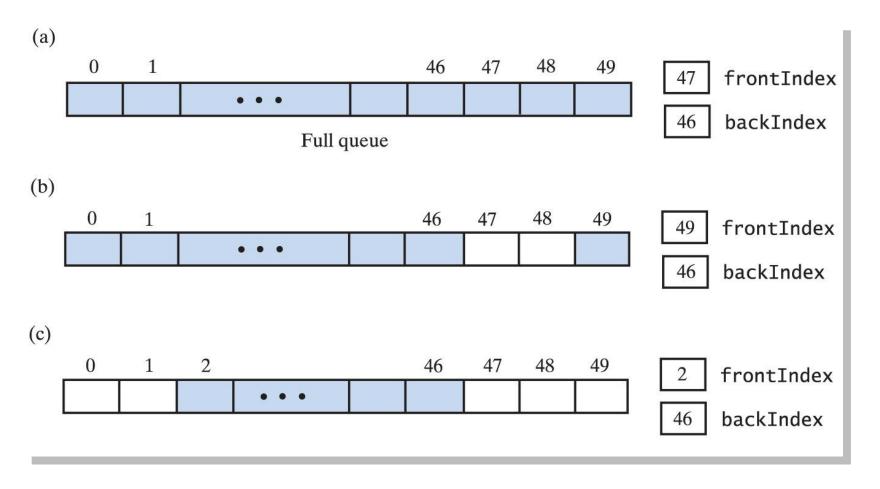


Fig. 24-7 A circular array that represents a queue: (a) when full; (b) after removing 2 entries; (c) after removing 3 more entries;

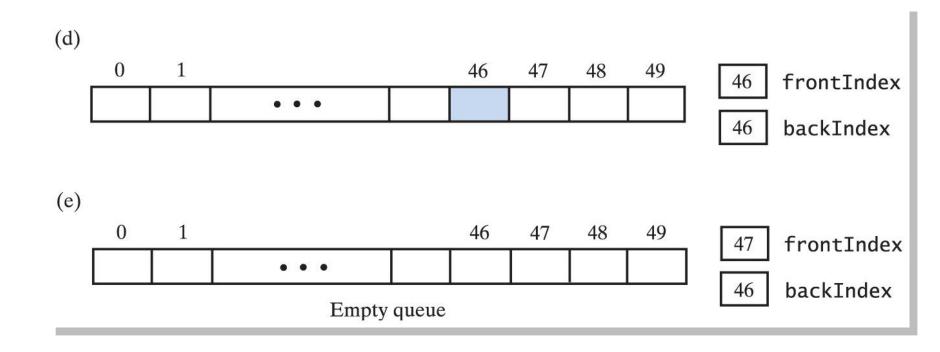


Fig. 24-7 A circular array that represents a queue: (d) after removing all but one entry;

(e) after removing remaining entry.

Method enqueue()

- 1. Update backIndex using modulo arithmetic: backIndex = (backIndex + 1) % array.length
- Assign new value at the array location indicated by backIndex

```
public void enqueue(T newEntry) {
  if (!isArrayFull()) {
    backIndex = (backIndex + 1) % array.length;
    array[backIndex] = newEntry;
  }
}
```

Method dequeue()

- Assign the entry at array location frontIndex to a temporary variable (to be returned)
- 2. Update frontIndex using modulo arithmetic:

```
frontIndex = (frontIndex+1) % array.length
```

```
public T dequeue() {
  T front = null;

if (!isEmpty()) {
  front = array[frontIndex];
  array[frontIndex] = null;
  frontIndex = (frontIndex + 1) % array.length;
 }

return front;
}
```

Circular Array Implementation of a Queue

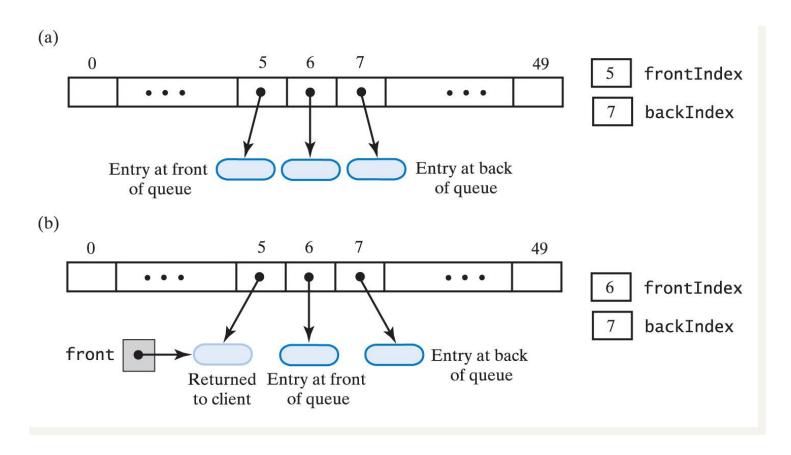


Fig. 24-9 An array-base queue: (a) initially; (b) after removing its front by incrementing **frontIndex**;

Circular Array Implementation of a Queue

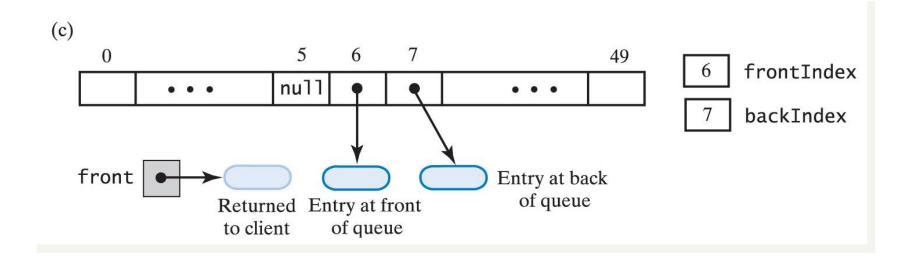
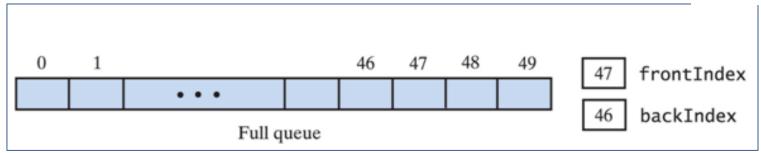


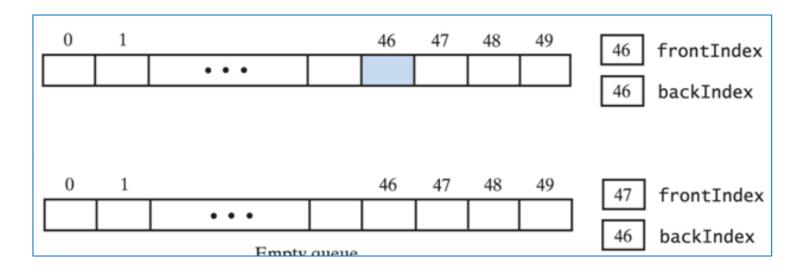
Fig. 24-9 An array-base queue: (c) after removing its front by setting **queue[frontIndex]** to **null**, then incrementing **frontIndex**.

Strength and Weakness

- No rightward drift problem
 - No wasted array locations
 - Do not have to shift entries after the last array location is used
- Problem: How to detect when the queue is empty and when the array is already full?
 - Note: with circular array
 frontIndex == backIndex + 1
 - both when queue is empty and when full



Observe that the relative positions of frontIndex and backIndex are the same for full queue (figure above) and empty queue (figure below).



Solutions to Detect Empty and Full Queues

- 1. Use a counter to keep track of the total entries in the queue
 - Empty queue detected when counter is 0
 - Full queue detected when counter equals array length
- 2. Leave one unused (vacant) location in the array
 - Empty queue detected when frontIndex is one location "in front" of backIndex (remember the wraparound action)
 - Full queue detected when only one vacant array location left.

A Circular Array with One Unused Location

Method 3: Circular Array

Fig. 24-8 A sevenlocation circular array that contains at most six entries of a queue ... continued → (a) 0 frontIndex backIndex Empty queue (b) frontIndex backIndex (c) frontIndex backIndex Full queue (d) 0 frontIndex backIndex (e) 0 2 3 frontIndex backIndex Full queue

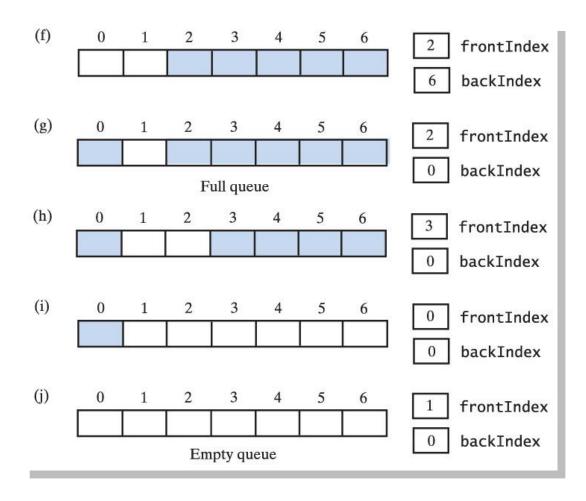
Allows us to distinguish between empty and full queue

A Circular Array with One Unused Location

Method 3: Circular Array

Fig. 24-8 (cont'd.)

A seven-location circular array that contains at most six entries of a queue.



Method isEmpty()

Method 3: Circular Array

•The queue is empty if
 ((backIndex + 1) % array.length) == frontIndex

Checking for full array

•The queue is full if
 ((backIndex + 2) % array.length) == frontIndex

Implementation of method doubleArray() in a circular array

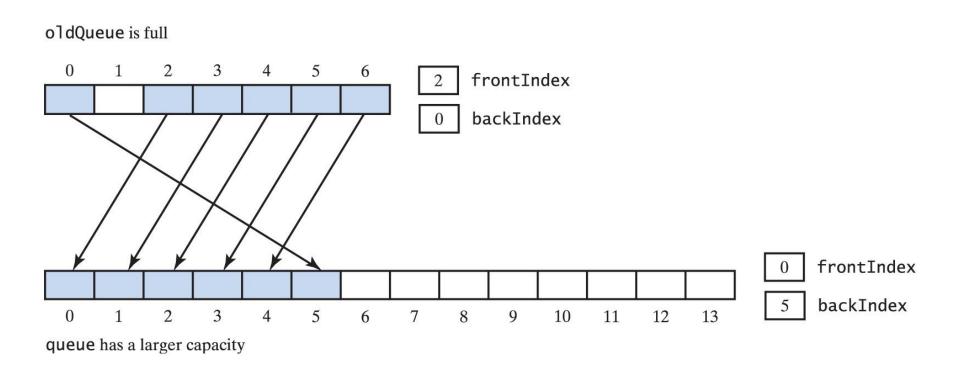


Fig. 24-10 Doubling the size of an array-based queue

Self Recap

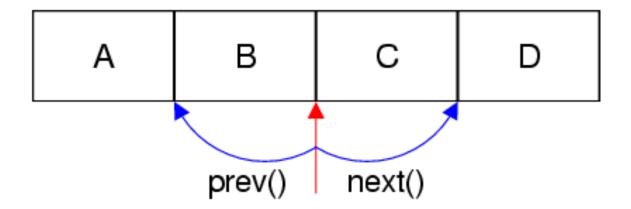
The 3 array implementations covered today:

- Linear array with fixed front
- Linear array with dynamic front
- Circular array

Sample Code

- Chapter4\adt\
 - QueueInterface.java
 - ArrayQueue.java
 - CircularArrayQueue.java
- Chapter4\entity\
 - SharePortfolio.java
 - SharePurchase.java
- Chapter4\client\
 - SharePortfolio Driver.java

java, util. Herator Iterators



Iterators (1)

- What if you need to go through the entries of a collection in order, one at a time?
- An iterator
 - is an object that enables you to traverse a collection of data, beginning with the first entry.
 - acts like a cursor or pointer, moving about on a data structure and locating individual elements for access.
 - is a software design pattern that abstracts the process of scanning through a collection of elements one element at a time.

Iterators (2)

- During one complete iteration, each entry is considered once
- Iterator may be manipulated
 - Check whether next entry exists
 - Asked to advance to next entry
 - Give a reference to current entry
 - Modify the list as you traverse it

Java's Iterator Interfaces

- As iteration is such a common operation, Java provides 2 interfaces for iterators for a uniform way for traversing elements in various types of collections:
 - Iterator
 - ListIterator
- These interfaces provide a uniform way for traversing elements in various types of collections.

(Recall: Collections include list, stack, queue, etc.)

java.util.Iterator

- This interface specifies a generic type for entries
- Includes 3 method headers:

hasNext	Checks if next entry exists.
next	Returns next entry and advances iterator to the next entry. Throws NoSuchElementException if there are no more elements.
remove	Removes the entry that was returned by the last call to next().

<<interface>> java.util.Iterator<T>

```
+hasNext(): boolean
+next(): T
+remove(): void
```

An Inner Class Iterator (1)

The iterator class is defined as an inner class of the collection ADT

Thus, it has direct access to the ADT's data fields.

```
Outer/Enclosing
public class ArrayQueue<T> implements QueueInterface<T> { ←
                                                                           Class
  private T[] array;
  private final static int frontIndex = 0;
  private int backIndex;
                                                                                Inner/Nested
  private class ArrayQueueIterator implements Iterator<T> {
                                                                                Class
     private int nextIndex = 0;
     public boolean hasNext() {
        return nextIndex <= backIndex;</pre>
     public T next() {
        if (hasNext()) {
          T nextEntry = array[nextIndex];
          nextIndex++; // advance iterator
          return nextEntry;
        } else {
          return null;
```

An Inner Class Iterator (2)

Then, provide a public method that returns an iterator to the

 getIterator() includes a call to the inner class iterator's constructor, which enables the client to create an iterator:

Example of How to Use Iterator in Client Program

```
package client;
import adt.QueueInterface;
import adt.ArrayQueue;
import java.util.Iterator;
public class TestIterator2{
  public static void main(String[] args) {
     QueueInterface<Integer> q = new ArrayQueue<>();
                                                         Output - Chapter4 (run)
    q.enqueue(10);
    q.enqueue(20);
                                                             run:
    q.enqueue(50);
                                                             10
    q.enqueue(100);
                                                             20
    q.enqueue(60);
                                                             50
    q.enqueue(35);
                                                             100
    Iterator<Integer> iterator = q.getIterator();
                                                             60
    int count = 0;
                                                             35
    int num = 0;
                                                             No of items with values > 50 is 2
                                                             BUILD SUCCESSFUL (total time: 0 seconds)
     while(iterator.hasNext()){
       num = iterator.next();
       System.out.println(num);
       if(num > 50)
         count++;
```

System.out.println("No of items with values > 50 is " + count);

Sample Code

(a) Chapter4\adt\

- QueueInterface.java
 - Contains the additional abstract method getIterator() which returns an iterator to the queue
- ArrayQueue.java
 - A class that implements the interface QueueInterface.

(b) Chapter4\adt\SharePortfolio.java:

- Contains the additional methods
 - countTotalUnitShares() which returns the current number of units of shares in the portfolio, and
 - getSharePortfolioCapital() which returns the capital value in the portfolio

(b) Chapter4\adt\SharePortfolioDriver.java:

Learning Outcomes

You should now be able to

- Implement the ADTs list, stack and queue using arrays.
- Discuss the strengths and weaknesses of using arrays to implement the ADTs.
- Analyze the efficiency of the array implementations of the ADTs

References

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- Liang, Y.D., 2018. Introduction to Java Programming and Data Structures.11th ed.United Kingdom:Pearson
- Malik DS and Nair PS, 2003, Data Structures using Java, Thomson Course Technology