

Procedural generation of levels for the angry birds videogame using evolutionary computation

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Abstract—In this paper an evolutionary computation-based system is proposed to generate levels for the angry birds video game, the levels themselves are composed of a set of birds that the player can use, a set amount of pigs that must be destroyed in order to progress to the next level and a given number of pieces that conform structures that may or may not protect the pigs from the player, this level generation system can create composites of pieces in order to create structures that can be used in the game this is based on our own interpretation of an open-ended evolutionary algorithm in which the evolution of the elements is not guided towards a single objective but rather is free to evolve and generate novelty or diversity in this case diversity of structures which the system can later select composites from in order to decide what will conform a level, this data is saved in groups that represent a population that can evolve by an evolutionary algorithm in order to create more complex levels. This elements of a population are then evaluated by how complex they become and how different they are from the rest of the group in order to create a variety of possible levels to be played.

Index Terms—genetic algorithm, procedural generated content, open-ended evolution, evolutionary computation

I. INTRODUCTION

Procedural content generation is an interesting subject on the entertainment industry, primarily in the video game development because of the easiness and quickness provided to generate content for different video game projects [ref]. In this paper an evolutionary content generation system is proposed to generate levels for the popular Angry Birds video game [1], taking inspiration in concepts of open-ended evolution.

For this project a procedural generation content system is proposed for the game angry birds, angry birds is a game developed by Rovio Entertainment in which the objective is to destroy structures placed on the map as well as eliminating green pig-like entities in order to obtain the highest score possible, the game uses a gravity and collision system that allows the structures to fall and be destroyed by means of damage as well as the use of three different construction materials *ice*, *wood* and *stone* each one with different resistances ranging from fragile, normal and sturdy in that order, the game mechanic is to use a slingshot to shoot a certain number of birds with different abilities to destroy the structures and the objectives, it is possible to obtain a high score by doing the most destruction as possible with the least birds as you can. [1]

While it is possible to create a evolutionary agent to play the levels and obtain the best score the main objective of this project is to generate the levels that can be played by naive agents or physical players, the levels themselves need to be complex in the sense that interesting structures can be created but it has to be possible to complete in some way [2, 3].

Procedural content generation provides a peculiar case of study because of the way content has to be made for a each particular type of game, in this particular case the restrictions that the game and the competition track have provide an interesting challenge for a evolutionary algorithm because we have to take into account the different pieces that can be used, their interactions with one another because of gravity and the possible effects the trajectory of a shot from a player can affect all of this.

In order to tackle this case of study we proposed to use a genetic algorithm capable of creating content, more specifically levels for the angry birds video game in which the generated levels satisfy the objectives of being *interesting* and *playable*.

After concluding this paper we expect to identify the places where a evolutionary algorithm can be used alongside procedural content generation applied to video games in order to be able to clarify in which areas a evolutionary algorithm can be used to further improve video game development cycles.

As mentioned above in this paper we use procedural content generation (PCG) which denotes the way to automatically generate content by algorithms instead of generating the same content by manual means such as with different personnel.

In the videogame industry many developers use a PCG style software that produces raw images and designs used by other personnel to improve it and use it in order to reduce the development cycles, and the productions cost. PCG as various focus areas that resolve around a video game, however in this paper the main focus is the *Level design* area which as the objective to design the different areas of a game in which a player can interact with, since in the angry birds video game a level is represented by a scene then the system will have to create the entities (birds and pigs) and objects (pieces) in it in order to create a playable level.

And finally we use our own interpretation of an Open-ended evolution (OEE) algorithm which is a variant of genetic evo-

lution algorithm where the objective differs from the regular genetic algorithm one, in this case the final objective is not to reach a final state of the evolution but to continue evolving and creating new types of entities more complex on each new generation, these same entities have the possibility to evolve not only inside the frame of their type but create entirely new groups. [4]

Another explanation provided by T. Taylor et al. [5, 6] defines OEE has a system capable of creating novelty beyond a point where nothing changes on the current group of interest rather than just converging to a stable or quasi-stable state.

For this project OEE is defined simply has a process of genetic evolution that encapsulates a group of similar processes and that is able to increase complexity of the original entities.

Section 2, contains a quick overview of some aspects used by different authors in order to tackle this problem, their design and basic functionality, in Section 3 the description of the current state of the project is explained, from the basis of the development, modification to the original proposed method as well as different approaches that were taken to solve the problem. finally in Section 4 we provide our conclusions about the development of this paper as well as improvements that can help to refine the proposed work.

II. OVERVIEW OF EXISTING WORK

In this Section we present some of the different approaches to the procedural generation of content for the angry birds video game.

M. Kaidan et al. [7] propose a model in which the generation of content is controlled by the skill of a player while actively playing the game, the moment the player finishes a certain level the algorithm obtains the score and generates the next level to be played.

J. Renz et al. [8] created an article in which the angry birds level generation contest mechanics of the IEEE Conference on Computational Intelligence and Games are based on, it explains some of the solving methods proposed by previous competitors.

Y. Jiang et al. [9] proposed the use of predefined letter style patterns and combined to create a small pool of words and letters used to be combined in order to create levels with text on them, the participants would play the game and after that they would be asked if they liked the layout of the levels.

III. APPROACH

In this Section we describe the approaches that were used for this project, first explaining some information of how techniques like OOE were implemented with the paper.

The game contains a total of 11 pieces as shown on figure 1 that cannot be modified, it is not possible to add more or modify the existing ones, with this in mind the purpose is to create composites of this same pieces in different locations and angles in order to create structures that can be used as building blocks for more complex levels.

Since there is no way to *add* a composite to the pool of pieces of the game then a way to combine both groups is

needed, in order to do this first the original 11 pieces of the game will be converted into composites, since the easiest way to read the data to create composites is by using lists then a *composite* of one element will be created for each piece, after this in order to add a composite of pieces as a new component first a group of existing composites is selected and placed in a imaginary enviroment then as a unique group they are measured, an imaginary bounding box is defined by calculating the lengths of all the pieces, finding the borders of said pieces and then finding the points that could define a box around all of them, then use this defined box to calculate the height and width of the new composite and then calculate from the center point of said box the offsets from the center of the group to the center of each respective piece as shown on figure 3, this information is needed in order to add it as a new composite so it can be used to place the pieces in their respective new positions when the files needed for the simulation are being created.

So using the composite generator the order of this sequence of events needs to be done as follows:

- 1) Gnerate composited to add to the pool of options.
- 2) Generate the first generation of the population.
- 3) Run a Simulation.
- 4) Evaluate each member of the population.
- 5) If a member of the population has remaining pieces obtain the location and angle of the pieces, create a composite and add it to the pool.
- 6) Select the parents for the next generation.
- 7) Do the crossover and mutation operations.
- 8) Repeat the cycle.



Fig. 1. List of pieces in the angry birds game.

The Angry Birds level generation track is a competition where the objective is to generate levels that are *fun* and *enjoyable* however they also have to be challenging but impossible however the rules for the competition specify that a configuration file must be used to generate the levels of the game in a limited amount of time, the information on the configuration file is first the number of *different* levels that must be generated, the second value is the different materials *not allowed* to be used, for instance a group of generated levels must not have circles which composition material is ice or stone moreover it does not have to integrate a triangle piece with ice, stone or wood material so this combinations must be removed from the pool of options, the third configuration value is the *number of pigs* that must be placed in a level, and finally the *limit* of time that the system has to create the required amount of levels.

After taking into account this restrictions the structure of our current approach had to be changed, so this section will be

divided in two subsections, the first will explain the approach that was used and after that the second will explain the modifications that had to be made in order to integrate the configuration files for the competition.

A. Original approach

Since the algorithm has to generate more complex structures the remaining pieces of a member of the population have to be used has a starting point, this new

additions to the piece pool are added to the population by the mutation operation, the objective in the first phase of the project is to generate structures that are capable of maintaining their own balance as shown on figure 2, since the objective of open-ended evolution for this project is to add new composites to the pool of options the algorithm will first run a simulation with a group of pieces and after it the ones that were not destroyed by falling because of gravity will be saved and added to the pool of options.

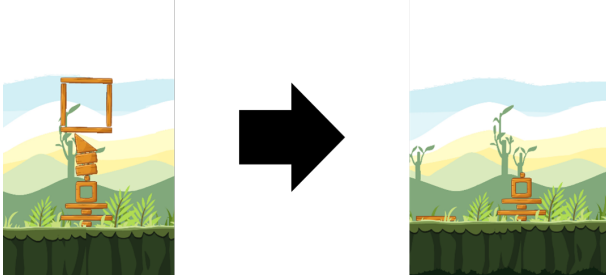


Fig. 2. Structure at beginning and end of a simulation.

The way to represent the elements of a member of the population is by using the id of each piece and the new added ones has a pointer to the respective data that needs to be obtained, this way and individual can be represented as shown on figure 4 where each chromosome represents a certain item in the pool of pieces, the numbers for this elements are assigned in a first come first served basis, the numbers are infinitely incremented and the same pieces can be repeated on each individual of the population.

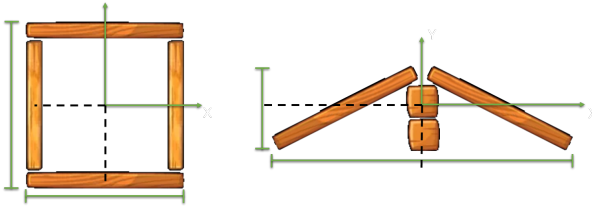


Fig. 3. Bounding box calculation.

Once the pieces have been added and the individuals are ready to be evaluated a simulation on the game environment is scheduled by order in the population, all the individuals have a maximum of ten seconds to maintain balance or reach absolute stability, if absolute stability is reached it means one of two things, first the generated structure is completely stable or second, the tower fell to either side and the pieces were

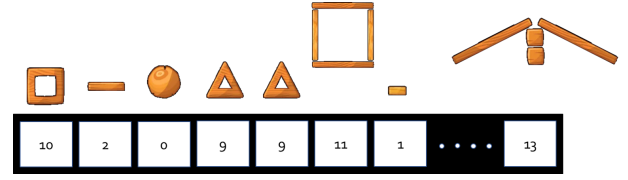


Fig. 4. Chromosome chain of an individual.

destroyed or stopped moving by gravitational pull, when either of this happens by more than two seconds the simulation ends regardless of time remaining and the next individual is simulated.

The evaluation process for this project is still in the development stages, however in order to check that the evolution is working has it should a criteria has been temporarily made as follows, each individual in the population has 100 points so before the simulation starts each of them are viable candidates to be an elite member of the population regardless relative height or complexity, then the remaining of the process is separated in three phases as follows.

First, after each of the individual simulations are over the evaluation process takes place, in this phase the resulting level is checked for pieces, each one of them is counted and then the resulting number is compared to that of the initial quantity of pieces that were originally put in before the simulation in order to calculate the first element of the evaluation process, each piece represents a certain percentage of 100% so the missing pieces are subtracted from the total.

Second, after removing percentage according to the missing pieces an individual remaining pieces are checked for their positions in comparison to the original ones before the simulation, using the formula 1 each piece within the individual is evaluated according to the center point of the piece, if the piece moved more than a certain threshold half the percentage for one piece is removed from the remaining percentage, after this using formula 2 the position of the piece is further checked, this time by the difference in angle from the original one, in case the difference of angles is more than a certain threshold half a piece value is further removed from the total.

$$error_{xy} = \begin{cases} 0.1 & \text{if } 0.08 > d, \\ \frac{100}{length_pieces} * 0.5 & \text{if } 0.08 < d. \end{cases} \quad (1)$$

where : $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$error_r = \begin{cases} 0 & \text{if } -5 \leq r \leq 5, \\ \frac{100}{length_pieces} * 0.5 & \text{if } r < -5 \text{ or } r > 5. \end{cases} \quad (2)$$

where : $r = |rotation_0| - |rotation_f|$

Finally, the total height of the remaining group of pieces is calculated by combining the bounding boxes of all pieces, then the individuals are ordered by the obtained percentage and then further ordered by the total height, this way the most balanced

ones will have the best probability to be selected together for a crossover operation to create the next generation.

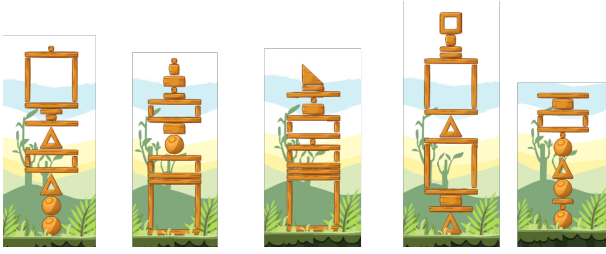


Fig. 5. Result samples of current system.

Since there is a need to create complex structures than can cover a great section of the play map, a method to evaluate the distribution is needed, for this instance we propose using the rule of thirds [10] which is a guideline used while creating images, the purpose is to create aesthetical pleasant images where the focus point or the most important area is at the center of the image as shown on figure 6, using this rule different distribution groups or masks are created has shown on figure 7 in order to use them before the simulation of an individual by placing the pieces in order to distribute them in a way that can cover more area and create more balanced levels instead of using a tower like distribution as shown on figure 5.

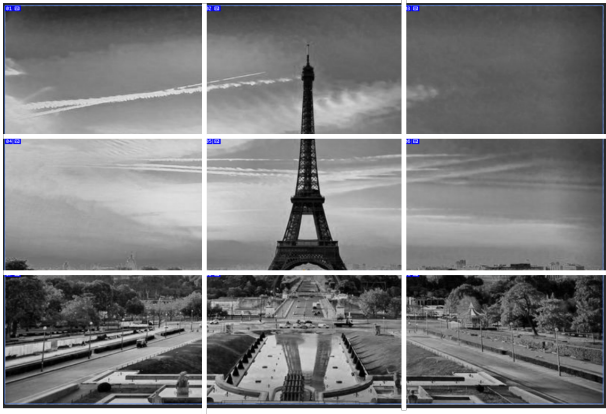


Fig. 6. Rule of thirds example.

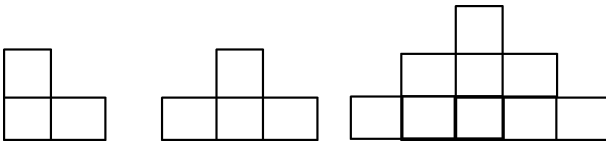


Fig. 7. Masks created using the rule of thirds.

Using this same distribution a new evaluation will be added in which according to how much of the area is filled a score will be given and this score will be used as a new sorting value at the moment of selecting individuals for the crossover operation, since as shown on figure 7 there is a possibility that

a huge mask is given to an individual it can be possible that the amount of pieces will not be able to cover the full area given, so in order to prevent this kind of problem we also proposed to give each mask a value that refers to the minimum amount of pieces and height required to fill the most of the mask, then check the amount of pieces and height before simulation for a single individual and then randomize which mask of the ones that can be used will be assigned to that individual, this way the results shown on figure 9 are obtained, this however gave us a new problem because as shown in the figure and on figure 8 as well, there were instances in which a certain combination of pieces could be too big for the area and this resulted in a level that had structural flaws from the beginning which could provoke the entire structure and immediately nearby others to fall at the beginning of the simulation however this allowed us to realize that predefined composites could provide problems to the generated structures therefore this approach was not the best for this problem.

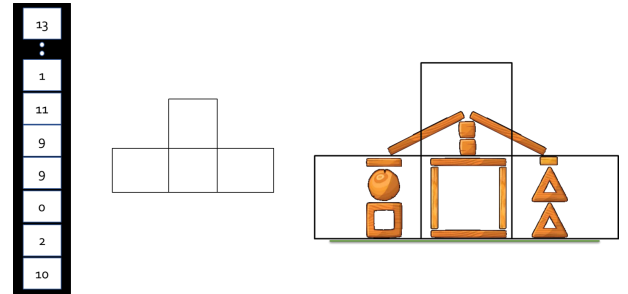


Fig. 8. Rule of thirds applied to an individual.

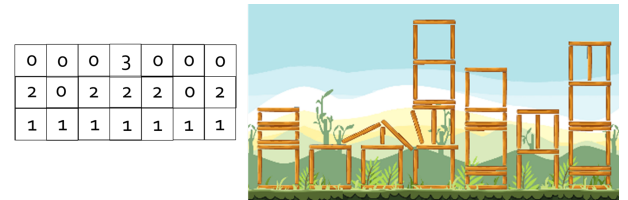


Fig. 9. Results obtained with rule of thirds.

B. New approach

The first difference that the new approach has is that the masks that are assigned to each individual are no longer pre-generated ones, this is because we decided that pre-generating them would not allow the generator to *evolve* because the individuals would be limited to a certain number of possible combinations which will in turn prevent diversity in the population, so in order to prevent this the modification to this section allows the individuals to generate a mask in which a number of columns is defined by default but the amount of pieces in each one is random, however the total of assigned pieces in all columns must be the same as the total pieces allowed in each individual which is a number assigned before beginning the system, an example of this can be seen in figure 10 where the total of pieces in an individual is 18 and this

pieces are distributed on all the columns available. This is further explained in this section.

The competition also requires that a generator follows a certain ruleset this is emulated by providing a file to the system to simulate the ruleset provided at the competition, this *text file* (*parameters.txt*) provides the specifications that must be met in the competition, the parameters in the file are as follows:

- Total required levels.
- Restrictions to pieces or piece-material combinations that cannot be placed or used in the levels, in this case if the file specifies that a *CIRCLE* made out of *ICE* cannot be placed, so the system must be able to verify that said combination is not used.
- Total number of pigs, this value can be a single value or a range of values that represent how many pigs must be placed on a level.
- The amount of time in which the system must give an output.

			0			
4		1	2	6		2
1		5	8	9		3
0	0	4	3	2	4	5

Fig. 10. New chromosome chain.

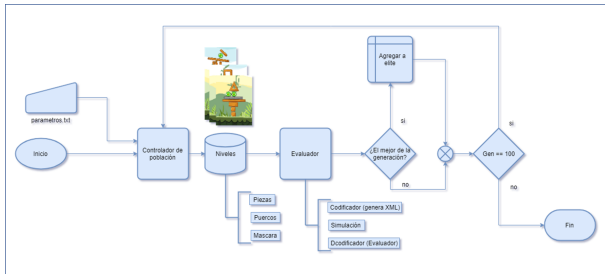


Fig. 11. New system diagram based on the parameter file and the new chromosome representation.

Using this as a base a new system diagram is proposed as shown of figure 11 in which the file with parameters is integrated with the input data the system requires, the way the individuals of the population are further presented and the way the simulation phase is taken, the method to representate the individuals is proposed by dividing the individual on three layers represented as follows:

- Element layer: also known as pieces layer, this layer represents the elements assigned to a particular individual by an array of numbers from 0 to infinite, where each number represents a reference to the class of a piece in the selection pool including the ones generated by the OOE algorithm, the representation of this is was shown in figure 4.
- Mask layer: this layer is represented by a 7 digit array in which the value assigned in each column represents the amount of pieces from the element layer that will be

assigned to said column, a representation of this is shown on figure 12.

- Enemy layer: also known as pig layer, this layer is represented by two elements a single numeric value representing the total amount of pigs assigned to the level and an array of locations for the placement of this same pigs, a representation of it is shown on figure 13.

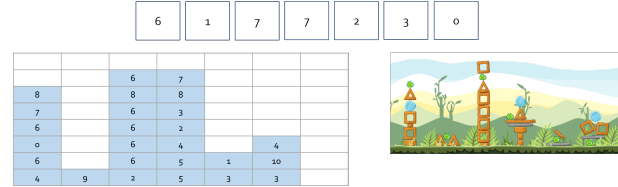


Fig. 12. Mask array with column and phenotype representation.

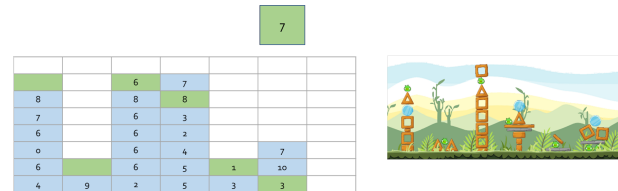


Fig. 13. Amount of pigs in a level, their location relative to the mask layer (green) and phenotype representation.

In order to select the parents of the next generation the parents are ordered by their fitness, then the system can choose between 2 options for the selection, tournament selection or roulette selection:

- Tournament selection: in order to select the parent by this method the system checks the amount of crossovers assigned, then calculates the ammount of parent required to compete in pairs, then by doing a descendent selection the slots for the tournament are filled and the winners are calculated in each group.
- Roulette selection: this method of selection was first decided to be used directly by giving a proportional amount of chances to be selected according to the fitness of a individual, however since one of the objectives is to obtain variety of levels the roulette must first be ranked in order to ensure that low fitness individuals can be selected as parents.

As for the crossover operations the system currently uses two types, single point crossover and double point crossover, however this crossover operation is not only applied to the piece array of an individual, but it is also applied to the mask of said individual, this way the mask can ensure that some pieces of some childs in the population are now placed in the level, this can bring the possibility that a mask that uses less pieces that it normally as can obtain a better fitness than one that uses all of them. An example of this two crossover types can be seen in figure 14 in which the mask of an individual is combined with another and the resulting mask for the childs have different amount of pieces to be placed.

The diagram illustrates the inheritance of two traits, A and B, from two parents to two children. The parents' genotypes are Parent1 (3, 2, 1, 1, 5, 9) and Parent2 (5, 2, 7, 0, 1, 6). The alleles for trait A (3, 5) and trait B (2, 7) are shown in green boxes, while the alleles for trait C (1, 0) and trait D (5, 6) are shown in blue boxes. The alleles for trait A and trait B are inherited together from each parent, forming the gametes (3, 2) and (5, 7) from Parent1, and (5, 2) and (1, 7) from Parent2. The children's genotypes are Child1 (3, 2, 7, 0, 1, 6) and Child2 (5, 2, 1, 1, 5, 9).

Parent	3	2	1	1	5	9
Parent1	3	2	1	1	5	9
Parent2	5	2	7	0	1	6
Child1	3	2	7	0	1	6
Child2	5	2	1	1	5	9

Fig. 14. Single point crossover(up) and double point crossover(bottom) applied to an individual mask.

The mutation operations of the generator work with the pieces layer of an individual, the four types of mutations used are:

- Add or remove elements from the piece list
- Change the piece that is being used in a point of the list
- Change the material a piece is made offsets
- Change the x and y coordinates of a piece

This mutations do not have to be used all at once on a single individual but depending on the probabilities they can happen all at once, since most of the pieces on a individual are mostly the same type of material then at least the material mutation can occur on all or most of the individuals to ensure that all levels will not have all the pieces with the same material which could render a level *"boring"* by the fitness function.

Since this group of mutations further ensures diversity in the populations a different way to evaluate the individuals is needed, by using the previous proposed method as a base a way to evaluate the "*diversity*" and "*uniqueness*" of a individual, for this we first remove the x and y position as well as the *angle* errors in order to add two new evaluation formulas as follows:

- Hamming distance: a simple explanation for the *Hamming distance* is that it is a calculation applied to a pair of strings where the objective is to find the minimum required number of substitutions required in order to convert a string exactly the same as the other, its formula is shown in equation 3, since the formula itself locates the minimum number of substitutions then we compare the individual with the rest of the population trying to find the maximum number of substitutions required effectively using the formula to give a better fitness to those individuals that are different from the group.
- Shannon entropy: the shannon entropy is used in information theory to calculate the disorder or uncertainty, in this case it will be used to determine if a level is

"boring" or *"interesting"* based on the amount of entropy calculated according to the pieces used in a level where a low entropy is boring because if a determined level as a lot of repeated pieces then it will look simple, the formula used is shown in equation 4 where the elements calculated are the pieces of a level and their appearance probability against all others.

$$d = \min \{ d(x, y) : x, y \in C, \text{if } x \neq y, 1 \text{ else } 0 \} \quad (3)$$

$$S = -\sum_i P_i \log P_i \quad (4)$$

Finally figure 15 and figure 16 represent the way all the layers of an individual are combined to create a level after all the selection, combination and mutation operations, first in figure 15 the composites layer is obtained from an individual, by a background process the width and height of all composites are obtained, then using the mask from the same individual the composites are placed in the order they are in their respective list (left to right in the level) in case a mask is not able to accommodate all the composites the remaining ones are not placed nor taken into account on the evaluation process, in the opposite case that there are not enough composites to fill a mask then the remaining areas are not taken into account as well, then in figure 16 the previous combination of layers is evaluated by checking which placed composites can hold a pig in the center or on the top of it, then the pigs are placed in the same order the composites are placed (left to right) in the locations where one is able to be placed.

Composites layer

8	7	6	0	6	4	9	6	8	6	6	6	6	2	7	8	3	2	4	5	5	1	3	4	10	3
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	----	---

Mask layer

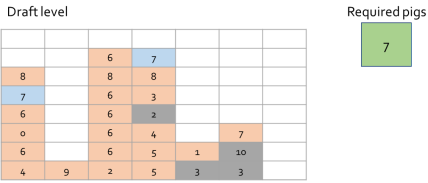
6	1	7	7	2	3	0
---	---	---	---	---	---	---

Resulting level

		6	7			
8		8	8			
7		6	3			
6		6	2			
0		6	4		7	
6		6	5	1	10	
4	9	2	5	3	3	

Fig. 15. Combination of composites layer and mask layer.

Using all this configurations the system is capable of creating levels, some of them playable as shown in figure 17 however the levels that can be generated are far from optimized to be played on, this is an issue that must be changed in future instances but the generator itself is able to be used as a base for a more complex one, and as shown in the future work section this issues can be solved by different means.



Final level and phenotype representation

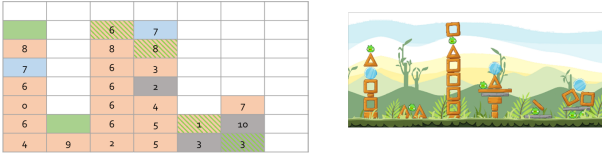


Fig. 16. Combination of figure 15 layers with pig layer.



Fig. 17. Example of resulting level with current system.

IV. CONCLUSIONS AND FUTURE WORK

The system as been able to generate levels that fulfill the requirements provided by the parameters file, however a way to evaluate that the levels generated are indeed "fun" or "interesting" is still needed, at this point we have two was to evaluate the results:

- User survey, in case a survey is used as an evaluation tool then first the system has to generate the levels and a group of people must participate by playing the levels and answering a set of questions afterwards, the questions themselves must try to capture the feeling of a person towards the game like questioning if a level was too easy or too difficult to solve, if the generated structures look interesting or if the level required them to strategize how to use the provided birds to solve the level, the survey must be applied to a equal quantity of people of three different game skill levels, "non video game players", "casual video game players" and "avid video game players", this way we can evaluate a level or the entire system by knowing if all skill levels did not enjoyed a level because it was too simple or easy.
- By using a naive agent, if a naive agent is used to play the levels we can obtain data of how the agent solves the levels placed before them, and the way to evaluate if the level is or not "interesting" will be by checking how easily the aggent is able to solve a level, the point here is to have a level that cannot be solved by a single movement but to have one that a human player has to think a while to solve tryingto place the difficulty of

a level just at the middle point between easy and hard difficulty levels.

Other aspects that the system need to improve is in the processing time required, since the current way to calculate the fitness and create the next generations of a population the system requires the system to execute simulations of the levels on every generation that passes therefore increasing the time it takes to complete an entire cycle of execution, so in order to change this we require to create a way to evaluate a level using only the information of the pieces, locations and pigs locations and using this data to predict the way a level will behave when placed in a real simulation environment therefore drastically reducing execution times.

Finally a different method to evaluate the individuals must be created, this is because the current evaluation method allows us to generate playable levels, this levels are far from ideal in the way that they only use a certain range of items present in the game therefore reducing the potential of a level, we expect to make the current fitness function work the most efficient that it can but another possible solution is found a good combination of formulas to generate the fitness function.

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