

COMP105 Lecture 21

Parameterised Custom Types

Outline

Today

- ▶ Parameterized custom types
- ▶ The `Maybe` type
- ▶ The `Either` type
- ▶ `case` expressions

Relevant book chapters

- ▶ Programming In Haskell Chapter 8
- ▶ Learn You a Haskell Chapter 8

Recap: Custom Types

```
data Point = Point Int Int deriving (Show, Read, Eq)
```

```
ghci> Point 1 2  
Point 1 2
```

```
ghci> Point 1 2 /= Point 3 4  
True
```

```
ghci> read "Point 1 1" :: Point  
Point 1 1
```

Type Variables in Custom Types

We can use **type variables** in custom types

```
data Point a = Point a a
```

```
ghci> :t Point (1::Int) (2::Int)  
Point Int
```

```
ghci> :t Point "hello" "there"  
Point [Char]
```

Type Variables in Custom Types

We can use **multiple** variables in the same type

```
data Things a b c = Things a b c    deriving(Show)
```

```
ghci> Things "string" 1 True
Things "string" 1 True
```

```
ghci> Things [] 1.5 'a'
Things [] 1.5 'a'
```

Type Variables in Custom Types

We can write **functions** using these types

```
first_thing (Things x _ _) = x
```

```
ghci> first_thing (Things 1 2 3)  
1
```

```
ghci> :t first_thing  
first_thing :: Things a b c -> a
```

The Maybe type

```
data Maybe a = Just a | Nothing
```

```
ghci> :t Just "hello"  
Maybe [Char]
```

```
ghci> :t Just False  
Maybe Bool
```

```
ghci> :t Nothing  
Maybe a
```

The Maybe type

The Maybe type is used in pure functional code **that might fail**

```
safe_head [] = Nothing
safe_head (x:_) = Just x
```

```
ghci> safe_head [1,2,3]
Just 1
```

```
ghci> safe_head []
Nothing
```


Case expressions

`case` expressions can do pattern matching **in functions**

```
head_or_zero list =  
  let  
    h = safe_head list  
  in  
    case h of Just x  -> x  
             Nothing -> 0
```

```
ghci> head_or_zero [1,2,3]  
1
```

Case expressions

The **syntax** for a case expression is

```
case [expression] of [pattern 1] -> [expression]
                    [pattern 2] -> [expression]
                    ...
                    [pattern k] -> [expression]
```

You can use `_` (the wildcard) as a catch-all

Case expressions

You can write all the patterns on **one line**

```
case h of {Just x  -> x; Nothing -> 0}
```

Case is an **expression**

```
ghci> (case 1 of 1 -> 1) + (case 2 of 2 -> 1)  
2
```

Maybe example

```
safe_get_heads list =  
  let  
    mapped = map safe_head list  
    filtered = filter (/=Nothing) mapped  
    unjust = (\ x -> case x of Just a -> a)  
  in  
    map unjust filtered
```

```
ghci> safe_get_heads [[], [1], [2,3]]  
[1,2]
```

Exercise

What do these functions do?

```
mystery x 0 = Nothing  
mystery x y = Just (div x y)
```

```
mystery2 x = case x of Just _ -> False  
                  Nothing -> True
```

```
mystery3 (Just x) (Just y) = Just (x+y)  
mystery3 _ _ = Nothing
```

Exceptions in Haskell

Haskell does include support for **exceptions**

```
ghci> head []
```

```
*** Exception: Prelude.head: empty list
```

Exceptions are **not** pure functional

- ▶ Every function returns exactly one value
- ▶ You can't catch exceptions in pure functional code
- ▶ Exceptions are mostly used in IO code

Exceptions in Haskell

The **Maybe** type provides a way to do **exception-like** behaviour in pure functional code

Can this function fail for some inputs?

- ▶ use the **Maybe** type

Exceptions should only be used in **IO** code

- ▶ File not found, could not connect to server, etc.
- ▶ These are unpredictable events

The Either type

```
data Either' a b = Left a | Right b
```

```
ghci> :t Left 'a'  
Either Char b
```

```
ghci> :t Right 'b'  
Either a Char
```


The Either type

The either type is useful if you want to store **different types** in the same list

```
ghci> let list = [Left "one", Right 2,  
                  Left "three", Right 4]
```

```
is_left (Left _) = True  
is_left _       = False
```

```
ghci> map is_left list  
[True,False,True,False]
```

The Either type

```
get_lefts list =  
  let  
    filtered = filter is_left list  
    unleft = (\ (Left x) -> x)  
  in  
    map unleft filtered
```

```
ghci> get_lefts list  
["one", "three"]
```

Example: squaring mixed number types

```
ghci> let nums = [Left pi, Right (4::Int), Left 2.7182]
```

```
square (Left x)  = Left (x ** 2)
```

```
square (Right x) = Right (x ^ 2)
```

```
ghci> map square nums
```

```
[Left 9.86,Right 16,Left 7.38]
```

Meaningful error messages

Either can be used to give **detailed errors**

```
safe_head_either []      = Right "empty list"
safe_head_either (x:_) = Left x
```

```
ghci> safe_head_either []
Right "empty list"
```

```
ghci> safe_head_either [1,2,3]
Left 1
```

Exercise

What are the **types** of these functions?

```
is_nothing x = case x of Just _  -> False
                  Nothing -> True
```

```
second_thing (Things _ y _) = y
```

```
half (Left x)  = Left  (x / 2)
half (Right x) = Right (x `div` 2)
```

Exercises

1. Create a type `FourThings` that has a single constructor with four parameters, each of which can be any type.
2. Write a function `middle_two` that takes one input of type `FourThings` and returns a tuple containing the middle two elements.
3. Write a type annotation for `middle_two`. Check that it compiles. Comment out your annotation, and use the `:t` command in `ghci` to see if your annotation was the most general.
4. Create a type `ThreeSameThings` that has a single constructor with three parameters, each of which has the same type.

Exercises

5. Write a function `safe_tail :: [a] -> Maybe [a]` that returns the tail of the list if the list is non-empty, and `Nothing` otherwise.
6. Write a function `safe_tails :: [[a]] -> [Maybe [a]]` that takes a list of lists, and returns a list containing the output of `safe_tail` for each element of the input list.
7. Use `safe_tails` to write a function `tails :: Eq a => [[a]] -> [[a]]`, which returns the tail of each non-empty list from the input.

Exercises

8. Use a case expression to write a function `second_head :: [a] -> a` that returns the second element of a list
9. Use a case expression and `safe_tail` to write a function `is_empty :: [a] -> Bool` that returns True if the input list is empty.
10. Write a function `one_over :: [Float] -> Maybe Float` which computes the sum of $1/x$ for every element x in the input list. But, if there is a zero in the input list, the function should return `Nothing`

Summary

- ▶ Parameterized custom types
- ▶ The `Maybe` type
- ▶ The `Either` type
- ▶ `case` expressions

Next time: Recursive custom types