## Problem 1

(a) The MATLAB code can be written as below:

```
1 \% Q = 2^{-1} [-4:2]
2 %constant
  wc = 2*pi*1000;
  Q = 2.^(-4:2);
  N = length(Q);
  B = [0 \ 0 \ 1];
  for i = 1:N
       A = [1 1/(wc*Q(i)) 1/(wc^2)];
       [H,W] = freqs(B,A);
10
       subplot(2,1,1);
11
       loglog(W, abs(H));
12
       xlabel 'Frequency (rad/s)', ylabel 'Magnitude'
13
       legend('-1','-3','-2','-1','0','1','2');
14
       hold all;
15
       subplot(2,1,2);
16
       semilogx(W, angle(H));
17
       xlabel 'Frequency (rad/s)', ylabel 'Phase (degrees)'
18
       legend('-1','-3','-2','-1','0','1','2');
       hold all;
20
21
  end
```

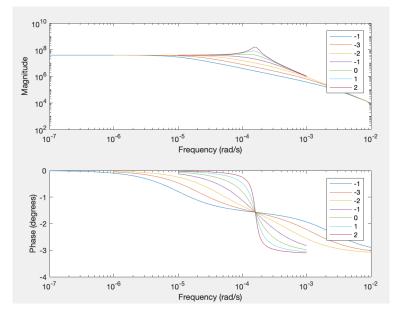


Figure 1:  $Q = 2^{[-4:2]}$ 

```
1 clear all;
2 close all;
  %constant
s wc = 2*pi*1000*2.^{(-2:2)};
6 Q = 2;
  N = length(wc);
  B = 1;
  for i = 1:N
       A = [1/(wc(i)^2) 1/(wc(i)*Q) 1];
11
       [H,W] = freqs(B,A);
       subplot (2, 1, 1);
13
       loglog(W, (abs(H)/max(abs(H))));
       xlabel ('Frequency (rad/s)'), ylabel ('Magnitude');
15
       ylim([-20 20]);
16
       legend('-2','-1','0','1','2');
17
       hold all;
18
       subplot(2,1,2);
19
       semilogx(W, angle(H));
20
       xlabel ('Frequency (rad/s)'), ylabel ('Phase (degrees)');
^{21}
       legend('-2','-1','0','1','2');
22
       hold all;
24 end
```

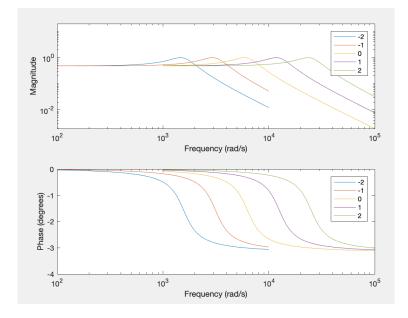


Figure 2:  $wc = 2*pi*1000*2^{[-2:2]}$ 

The following figure shows the varying Q:

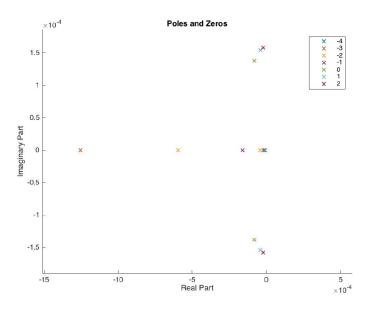


Figure 3: varying Q

The following figure shows the varying wc:

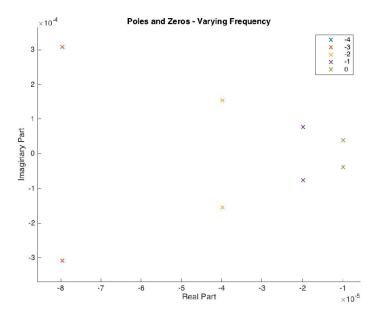


Figure 4: varying cut-off frequency

(b) By using bilinear transform, our analog filter into a digital representation can be obtained:

$$H(s) = \frac{1}{(\frac{s}{w})^2 + \frac{1}{Q}\frac{s}{w} + 1}$$

```
We let s = \frac{2}{T} \frac{1-z^{-1}}{1+z^{-1}} H(s) = \frac{1}{(\frac{s}{w})^2 + \frac{1}{O} \frac{s}{w} + 1}
```

Then the C++ code can be written as:

Figure 5: Low pass filter in s domain

Figure 6: Low pass filter in z domain by applying Bilinear Transform

## Problem 2

(a) So as to make the filter smoothly varying over time, the user controls will be tracked using leaky integrators.

Figure 7: Code for SlewedParameter class

(b) Implement a low-frequency oscillator (LFO) with sine of a phase counter:

Figure 8: Code for LFO class