Week 1: Descriptive Analytics

- An Operational Decision Problem
- Forecasting with Past Historical Data
- Moving Averages
- Exponential Smoothing

Thinking about Trends and Seasonality

- Forecasting for New Products
- Fitting distributions

Session 4

New Product Problem

- ◆ In the case of new products or new designs in the market, there is limited demand data.
- ♦ How to Forecast in such cases?
 - Subjective techniques...

Subjective Forecasting Methods

- ◆ Composites
 - Sales Force Composites: Aggregation of sales personnel estimates.
- Customer Surveys
- ◆ Jury of Executive Opinion
- The Delphi Method
 - Individual opinions are compiled and reconsidered. Repeat until overall group consensus is (hopefully) reached.

Forecasting Demand: An Application

- ◆ An outdoor wear company (Andes) has a new product: A new men's hiking shoe design.
- ◆ Andes Inc. has sold this particular design called *Drifter* for one season only. In the past season, they
 - made a forecast of 1200 units
 - produced Q=1500 units, and
 - sold 1397 units.
- As you can see, not much demand data is available.
- How can Andes think about descriptive statistics for *Drifter*?

Fitting a Distribution by Tracking Errors

- ◆ If there is limited demand data for new products...
 - We start with subjective forecasts.
 - However, we can do better with more data.
- Often, there is additional demand data from other products that you forecast in the past.
 - This is informative of how forecasts in your firm deviated from demand.
- We will learn one approach on how to fit a Normal distribution to such available data.
- We can use similar approaches for other distributions.

Andes Inc: Men's Shoes

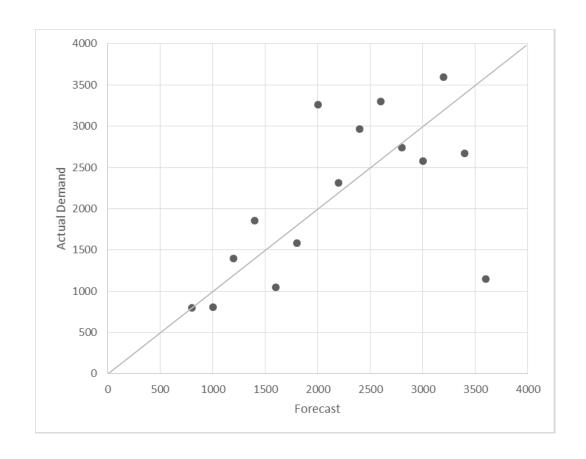
| Product | Forecast | Produced | Sales | Actual Demand |
|---------------|----------|----------|-------|---------------|
| | | | | |
| Tale | 800 | 1000 | 796 | 796 |
| Lancic | 1000 | 1250 | 805 | 805 |
| Drifter | 1200 | 1500 | 1397 | 1397 |
| Manas | 1400 | 1750 | 1750 | 1857 |
| Tsake | 1600 | 2000 | 1049 | 1049 |
| Screen | 1800 | 2250 | 1585 | 1585 |
| Ayers | 2000 | 2500 | 2500 | 3265 |
| Pau | 2200 | 2750 | 2314 | 2314 |
| Omega | 2400 | 3000 | 2967 | 2967 |
| Nomad | 2600 | 3250 | 3250 | 3299 |
| Snake | 2800 | 2500 | 2500 | 2739 |
| Maui | 3000 | 3750 | 2578 | 2578 |
| Rainier | 3200 | 4000 | 3598 | 3598 |
| Carbon | 3400 | 4250 | 2672 | 2672 |
| Bear lake | 3600 | 4500 | 1148 | 1148 |
| | | | | |
| Average | 2200 | | | 2138 |
| Std Deviation | 894 | | | 963 |

- ◆ The subjective forecast for Drifter for next season is 1000 pairs.
- What demand model should Andes use for the Drifter?

Sales vs. Demand: A note

- Note there is a difference between Sales and Demand
 - Sales is censored demand.
 - E.g. If your demand was 1000 units, but you have only 800 units on shelf, the sales is only 800 units.
 - Examples: Popular music players, gaming consoles are often sold out.
- ◆ For most operational problems, such as the Newsvendor problem, we need demand distribution data.

Forecast Performance at Andes



◆ Some demands exceed forecasts, and some demands are lower than forecasts.

Measuring Forecast Performance

| Product | Forecast | Produced | Sales | Actual Demand | A/F ratio |
|---------------|----------|----------|-------|---------------|-----------|
| | | | | | |
| Tale | 800 | 1000 | 796 | 796 | 1.00 |
| Lancic | 1000 | 1250 | 805 | 805 | 0.81 |
| Drifter | 1200 | 1500 | 1397 | 1397 | 1.16 |
| Manas | 1400 | 1750 | 1750 | 1857 | 1.33 |
| Tsake | 1600 | 2000 | 1049 | 1049 | 0.66 |
| Screen | 1800 | 2250 | 1585 | 1585 | 0.88 |
| Ayers | 2000 | 2500 | 2500 | 3265 | 1.63 |
| Pau | 2200 | 2750 | 2314 | 2314 | 1.05 |
| Omega | 2400 | 3000 | 2967 | 2967 | 1.24 |
| Nomad | 2600 | 3250 | 3250 | 3299 | 1.27 |
| Snake | 2800 | 2500 | 2500 | 2739 | 0.98 |
| Maui | 3000 | 3750 | 2578 | 2578 | 0.86 |
| Rainier | 3200 | 4000 | 3598 | 3598 | 1.12 |
| Carbon | 3400 | 4250 | 2672 | 2672 | 0.79 |
| Bear lake | 3600 | 4500 | 1148 | 1148 | 0.32 |
| | | | | | |
| Average | 2200 | | | 2138 | 1.01 |
| Std Deviation | 894 | | | 963 | 0.31 |

 We measure forecast vs actual demands, by calculating a ratio of actual demand to the forecast.

Empirical distribution function of forecast accuracy

A / F Ratio =
$$\frac{\text{Actual Demand}}{\text{Forecast}}$$

- ◆ Start by evaluating the actual demand to forecast ratio (the A/F ratios) from the *N* past observations.
- A/F ratios measure how much the actual demands deviated from past forecasts.
- ... which helps us pin down uncertainty around current forecast.

Choosing a normal demand distribution

- Start with an initial forecast generated from subjective methods (hunches, guesses, etc).
 - Let's assume that the Initial Forecast = 1000 units.
- Evaluate the A/F ratios of the historical data:

$$A/F$$
 ratio = $\frac{Actual\ demand}{Forecast}$

Set the mean of the normal distribution to

Expected actual demand = $Expected\ A/F\ ratio \times Forecast$

◆ Set the standard deviation of the normal distribution to Standard deviation of actual demand = Standard deviation of A/F ratios × Forecast

Normal distribution forecast

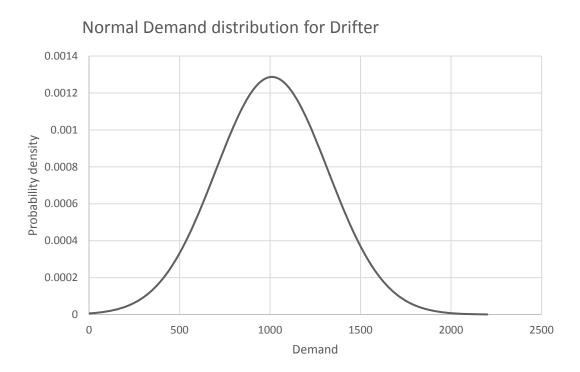
Expected actual demand =
$$1.01 \times 1000 = 1010$$

Standard deviation of actual demand = $0.31 \times 1000 = 310$

- Descriptive Data: normal distribution with mean 1010 and standard deviation 310 to represent demand.
- Note for predictive purposes, we update the distribution to Normal with mean and standard deviation as follows:

$$\mu = 1010$$
 $\sigma = 390$.

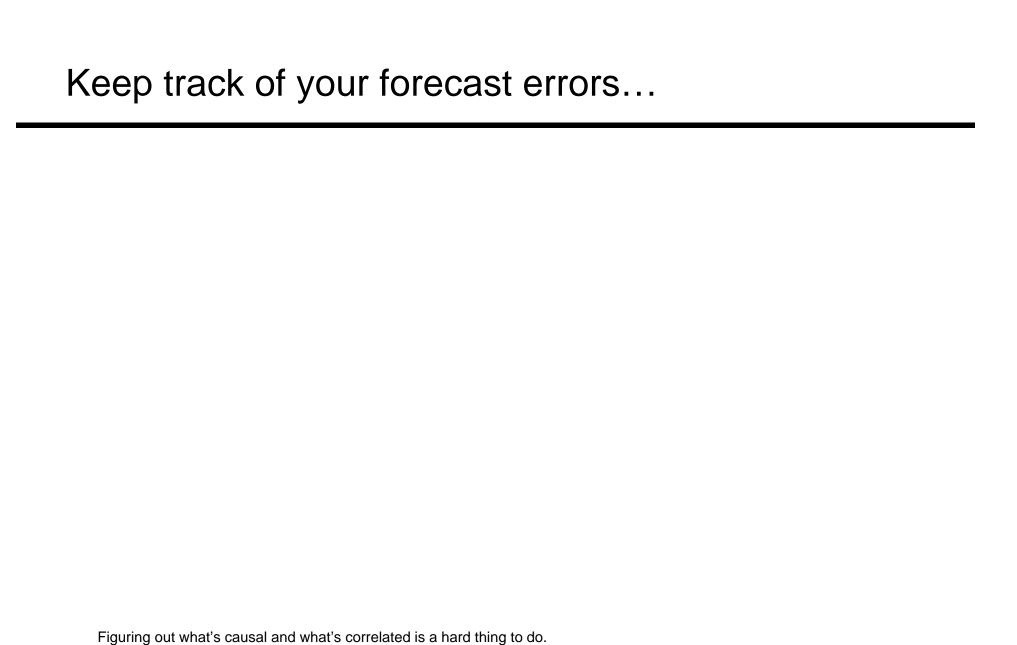
Descriptive Statistics: Normal Demand model



 Drifter Descriptive Stats: Normal Demand distribution with mean 1010 and Standard deviation 310.

Our techniques broadly applicable...

- Can be used for understanding GDP forecasts and actual observations:
 - See Nate Silver's book: The Signal and the Noise: Drowning in 3 feet of water. Chapter 6.
- Forecasting process used at Sport Obermeyer.
 - Reducing the Cost of Demand Uncertainty through Accurate Response to Early Sales. Fisher and Raman. Operations Research 1996. vol. 44 -99.(1), 87



- Jan Hatzius, Chief Economist, Goldman Sachs.

Week 1: Descriptive Analytics Recap

- Newsvendor Problem
- Random Variables and Demand Distributions
- Forecasting with Past Historical Data
 - Errors and Biases
- Moving Averages
- Exponential Smoothing
- Descriptive Statistics
- Trends and Seasonality
- Forecasting for New Products
- Fitting Demand distributions

Conclusion

- ◆ That's it for Descriptive Analytics.
- ◆ We will cover more tools in the weeks to come -
- ◆ We will continue on to prescriptive and predictive analytics.