파이썬 입문

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PyTorch - 로지스틱회귀 (Logistic Regression)

두 개의 선택지 중에서 정답을 고르는 문제: 이진 분류 (Binary Classification)

예) 제조 부품 테스트에서 점수 60점 이상이면 정상, 미만이면 불량 판정

0.6 Falsé

1.0

8.0

w : 경사 b : 좌우이동

임계값 (threshold) **True**

시그모이드 함수 (Sigmoid function)

$$H(x) = rac{1}{1 + e^{-(wx+b)}} = sigmoid(wx+b) = \sigma(wx+b)$$

e : 자연상수(exponential), 2.718281...

w : 가중치, weight

b : 편향, bias

- 선형회귀, 다중선형회귀
- 로지스틱회귀, 다중로지스틱회귀
- 소프트맥스회귀

import torch import matplotlib.pyplot as plt

```
def sigmoid(x):
   return 1 / (1 + torch.exp(-x))
```

x = torch.arange(-5.0, 5.0, 0.1)y1 = sigmoid(0.5 * x)

v2 = sigmoid(x)

v3 = sigmoid(2 * x)

y4 = sigmoid(10 * x)

import torch import matplotlib.pyplot as plt def sigmoid(x): return 1 / (1 + torch.exp(-x))

x = torch.arange(-5.0, 5.0, 0.1)

y1 = sigmoid(x + 0.5)

y2 = sigmoid(x)

Sigmoid Function

y3 = sigmoid(x + 1.0)

v4 = sigmoid(x + 2.0)

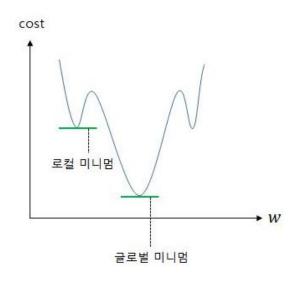
plt.plot(x, y1, 'r', linestyle='--') plt.plot(x, y2, 'g') plt.plot(x, y3, 'b', linestyle='--') plt.plot(x, y4, 'black', linestyle='--') plt.plot([0,0],[1.0,0.0], ':') plt.title('Sigmoid Function') plt.show()

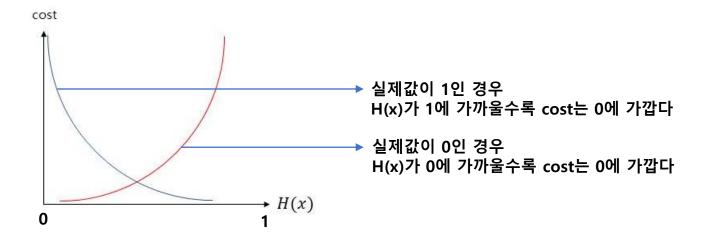
PyTorch - 로지스틱회귀 (Logistic Regression)

비용함수 (Cost Function), 또는 손실함수 (Loss Function)

• 선형회귀, 다중선형회귀 : MSE(Mean Squared Error)

이진 크로스 엔트로피 (Binary Cross Entropy)





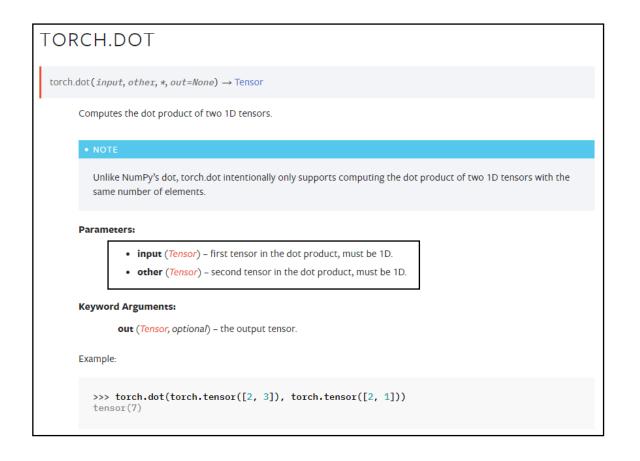
$$cost(W) = -rac{1}{n} \sum_{i=1}^{n} [y^{(i)} log H(x^{(i)}) + (1-y^{(i)}) log (1-H(x^{(i)}))]$$

$$W := W - lpha rac{\partial}{\partial W} cost(W)$$

구현

```
epochs = 1000
import torch
                                                                         for epoch in range(epochs + 1):
import torch.nn as nn
import torch.nn.functional as F
import torch.optim as optim
                                                                              # cost
                                                                              hypothesis = torch.sigmoid(W * x data + b)
torch.manual_seed(1)
                                                                              # hypothesis = torch.sigmoid(x data.matmul(W) + b)
                                                                              cost = -(y train * torch.log(hypothesis) + (1 - y train) *
x_data = [[1], [2], [3], [4], [5], [6]] # 로지스틱회귀
                                                                                    torch.log(1 - hypothesis)).mean()
# x_data = [[1, 2], [2, 3], [3, 1], [4, 3], [5, 3], [6, 2]] #다중로지스틱회귀
y data = [[0], [0], [0], [1], [1], [1]]
                                                                              optimizer.zero_grad()
x train = torch.FloatTensor(x data)
                                                                              cost.backward()
y train = torch.FloatTensor(y data)
                                                                              optimizer.step()
                                                                              if epoch % 100 == 0:
# Model 가중치, 편향 초기화
                                                                                    print('Epoch {:4d}/{} Cost: {:.6f}'.format(
W = torch.zeros((1, 1), requires grad=True)
                                                                                         epoch, epochs, cost.item() ))
# W = torch.zeros((2, 1), requires grad=True)
b = torch.zeros(1, requires grad=True)
                                                                         prediction = hypothesis >= torch.FloatTensor([0.5]) # 임계값 (threshold)
                                                                         print(prediction)
# Optimizer 설정
optimizer = optim.SGD([W, b], lr=1)
                                                                         print(W)
                                                                         print(b)
```

numpy, torch dot product



numpy dot product는 다차원 x 다차원 가능 torch dot product는 1차원 x 1차원만 가능 해결책

- 1. torch.matmul 사용
- 2. numpy.ndarray로 계산 후 tensor로 변경
 - tensor_data.numpy() # numpy.ndarray로 변환
 - a = numpy.dot(x, w) # dot product계산
 - torch.Tensor(a) # tensor로 변환
 - requires_grad = True인 경우, False로 변경 -> 수행 -> True로 변경

https://pytorch.org/docs/stable/generated/torch.dot.html

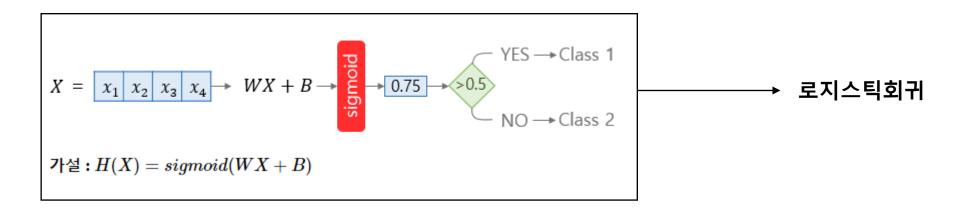
```
nn.Module로 구현 (nn.Linear, nn.Sigmoid) - refactoring
```

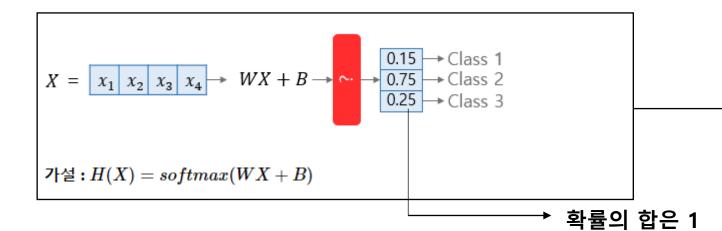
```
import torch
import torch.nn as nn
import torch.nn.functional as F
import torch.optim as optim
torch.manual seed(1)
x_data = [[1, 2], [2, 3], [3, 1], [4, 3], [5, 3], [6, 2]] #다중로지스틱회귀
#x_data = [[1], [2], [3], [4], [5], [6]] # 로지스틱회귀
y data = [[0], [0], [0], [1], [1], [1]]
x train = torch.FloatTensor(x data)
y_train = torch.FloatTensor(y data)
model = nn.Sequential(
     nn.Linear(2, 1), # 다중로지스틱회귀
     # nn.Linear(1, 1), # 로지스틱회귀
     # nn.Linear(1, 1, bias=False), # 편향 사용 여부
     nn.Sigmoid()
model(x train)
```

```
optimizer = optim.SGD(model.parameters(), lr=0.1)
epochs = 5000
for epoch in range(epochs + 1):
     hypothesis = model(x train)
     cost = F.binary cross entropy(hypothesis, y train)
     # cost = F.mse loss(hypothesis, y train) # 선형회귀
     optimizer.zero grad()
     cost.backward()
     optimizer.step()
     if epoch \% 10 == 0:
          prediction = hypothesis >= torch.FloatTensor([0.5])
          correct prediction = prediction.float() == y train
          accuracy = correct prediction.sum().item() / len(correct prediction)
          print('Epoch {:4d}/{} Cost: {:.6f} Accuracy {:2.2f}%'.format(
               epoch, epochs, cost.item(), accuracy * 100, ))
model(x train)
print(list(model.parameters()))
```

```
class로 구현 - refactoring
                                                                         optimizer = optim.SGD(model.parameters(), lr=0.1)
import torch
                                                                         epochs = 5000
import torch.nn as nn
import torch.nn.functional as F
                                                                         for epoch in range(epochs + 1):
import torch.optim as optim
                                                                              hypothesis = model(x train)
                                                                              cost = F.binary_cross_entropy(hypothesis, y train)
torch.manual seed(1)
                                                                              optimizer.zero grad()
                                                                              cost.backward()
                                                                              optimizer.step()
x_data = [[1, 2], [2, 3], [3, 1], [4, 3], [5, 3], [6, 2]] #다중로지스틱회귀
#x_data = [[1], [2], [3], [4], [5], [6]] # 로지스틱회귀
                                                                              if epoch \% 10 == 0:
y data = [[0], [0], [0], [1], [1], [1]]
                                                                                   prediction = hypothesis >= torch.FloatTensor([0.5])
x train = torch.FloatTensor(x data)
                                                                                   correct prediction = prediction.float() == y train
y train = torch.FloatTensor(y data)
                                                                                   accuracy = correct prediction.sum().item() / len(correct prediction)
                                                                                   print('Epoch {:4d}/{} Cost: {:.6f} Accuracy {:2.2f}%'.format(
class BinaryClassifier(nn.Module):
                                                                                         epoch, epochs, cost.item(), accuracy * 100, ))
     def init (self):
                                                                         model(x train)
                                                                         print(list(model.parameters()))
          super(). init ()
          self.linear = nn.Linear(2, 1) # 다중로지스틱회귀
          # self.linear = nn.Linear(1, 1) # 로지스틱회귀
          self.sigmoid = nn.Sigmoid()
                           # forward propagation
     def forward(self, x):
          return self.sigmoid(self.linear(x))
                                                                         • init ()
                                                                         forward()
model = BinaryClassifier()
```

다중 클래스 분류 (Multi-class Classification)





소프트맥스회귀

- 2개 이상의 class 분류
- 활성화함수(activation function)가 다르다

다중 클래스 분류 (Multi-class Classification)

소프트맥스 함수

$$p_i = rac{e^{z_i}}{\sum_{j=1}^k e^{z_j}} \; ext{ for } i=1,2,\dots k$$

입력: k차원의 벡터 z

비용 함수 : 크로스 엔트로피 (cross entropy, categorical cross entropy)

$$cost(W) = -rac{1}{n} \sum_{i=1}^{n} \sum_{j=1}^{k} y_{j}^{(i)} \ log(p_{j}^{(i)})$$

print(y train.shape)

다중 클래스 분류 (Multi-class Classification) # 모델 초기화 W = torch.zeros((4, 3), requires grad=True) 구현 b = torch.zeros((1, 3), requires_grad=True) # optimizer 설정 import torch optimizer = optim.SGD([W, b], Ir=0.1) import torch.nn as nn epochs = 1000import torch.nn.functional as F for epoch in range(epochs + 1): import torch.optim as optim z = x train.matmul(W) + bcost = F.cross_entropy(z, y_train) # 비용함수에 소프트맥스함수가 포함 torch.manual seed(1) optimizer.zero grad() cost.backward() x train = [[1, 2, 1, 1],optimizer.step() [2, 1, 3, 2], if epoch % 100 == 0: [3, 1, 3, 4], print('Epoch {:4d}/{} Cost: {:.6f}'.format(epoch, epochs, cost.item())) [4, 1, 5, 5], [1, 7, 5, 5], 크로스 엔트로피 [1, 2, 5, 6], print(z) 가장 큰 값이 예측결과 (cost가 0일 때, 모두 더하면 0) [1, 6, 6, 6], [1, 7, 7, 7]] y train = [2, 2, 2, 1, 1, 1, 0, 0]-3.0665, 0.6256, 2.5122], x train = torch.FloatTensor(x train) [-7.2341, <u>3.7583</u>, 4.7448], y train = torch.LongTensor(y train) 4.4897, 3.0981, 1.4420, -2.1420], 0.6266, 3.8136, -3.9867], 2.1208, print(x_train.shape)

[2.7828, 2.3761, -4.5870],

2.8725, -6.3362]], grad fn=<AddmmBackward0>

```
# 모델 초기화
nn.Module로 구현 - refactoring
                                                                model = nn.Linear(4, 3)
                                                                # optimizer 설정
                                                                optimizer = optim.SGD(model.parameters(), lr=0.1)
import torch
import torch.nn as nn
                                                                epochs = 1000
import torch.nn.functional as F
                                                                for epoch in range(epochs + 1):
import torch.optim as optim
                                                                     prediction = model(x_train)
                                                                                                                           # softmax
                                                                     cost = F.cross entropy(prediction, y train)
torch.manual seed(1)
                                                                     # cost = F.binary cross entropy(prediction, y train)
                                                                                                                           # logistic
                                                                     # cost = F.mse loss(prediction, y train)
                                                                                                                           # linear
x train = [[1, 2, 1, 1],
                                                                     optimizer.zero grad()
             [2, 1, 3, 2],
                                                                     cost.backward()
             [3, 1, 3, 4],
                                                                     optimizer.step()
             [4, 1, 5, 5],
                                                                     if epoch % 100 == 0: print('Epoch {:4d}/{} Cost: {:.6f}'.format(
             [1, 7, 5, 5],
                                                                          epoch, epochs, cost.item() ))
             [1, 2, 5, 6],
             [1, 6, 6, 6],
                                                                print(prediction)
             [1, 7, 7, 7]]
y train = [2, 2, 2, 1, 1, 1, 0, 0]
                                                                  tensor([[-4.3709, -0.3246,
                                                                                           4.5068],
x train = torch.FloatTensor(x train)
                                                                          [-3.0665, 0.6256, 2.5122],
y train = torch.LongTensor(y train)
                                                                          [-7.2341, 3.7583, 4.7448],
                                                                          [-6.3326, 4.4897, 3.0981],
print(x train.shape)
                                                                           0.6266, 1.4420, -2.1420],
                                                                          2.1208, 3.8136, -3.9867],
print(y train.shape)
                                                                          [ 2.7828, 2.3761, -4.5870],
                                                                          4.1330, 2.8725, -6.3362]], grad fn=<AddmmBackward0>)
```

class로 구현 - refactoring

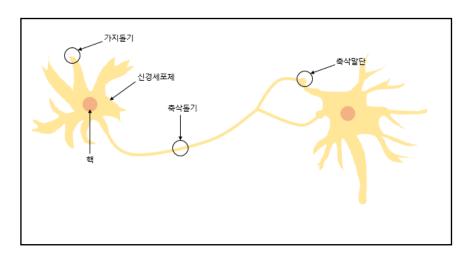
```
class SoftmaxClassifierModel(nn.Module):
    def __init__(self):
        super().__init__()
        self.linear = nn.Linear(4, 3) # Output<sup>0</sup>| 3!
    def forward(self, x):
        return self.linear(x)
model = SoftmaxClassifierModel()
```

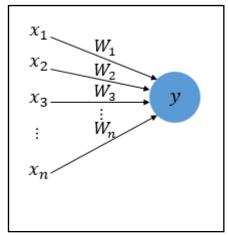
```
optimizer = optim.SGD(model.parameters(), lr=0.1)
epochs = 1000
for epoch in range(epochs + 1):
    prediction = model(x_train)
    cost = F.cross_entropy(prediction, y_train)
    optimizer.zero_grad()
    cost.backward()
    optimizer.step()
    if epoch % 100 == 0:
        print('Epoch {:4d}/{} Cost: {:.6f}'.format(epoch, epochs, cost.item() ))
```

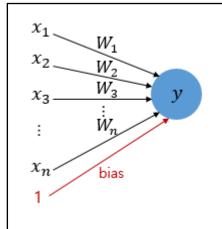
print(prediction)

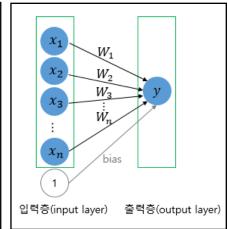
PyTorch - 단층 퍼셉트론 (Single-Layer Perceptron)

퍼셉트론(Perceptron): 초기 인공신경망 모델









인공신경망(퍼셉트론)

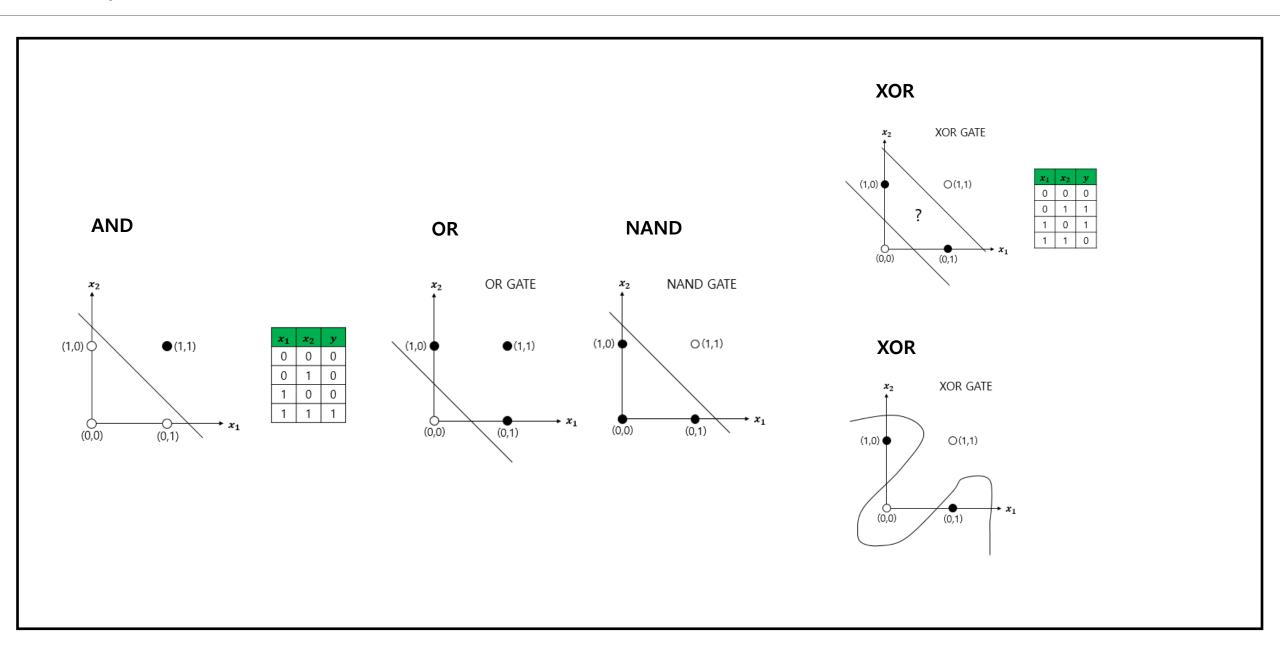
활성화함수(계단함수)

$$f(\sum_{i}^{n} W_{i} x_{i} + b)$$

PyTorch - 단층 퍼셉트론 (Single-Layer Perceptron)

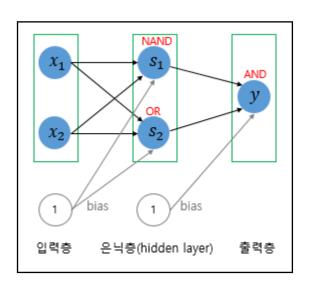
```
퍼셉트론(Perceptron): 초기 인공신경망 모델
                                                                   hypothesis = model(X)
                                                                   predicted = (hypothesis > 0.5).float()
                                                                   accuracy = (predicted == Y).float().mean() * 100
                                                                   print('모델의 출력값(Hypothesis): ', hypothesis)
import torch
                                                                   print('모델의 예측값(Predicted): ', predicted)
import torch.nn as nn
X = torch.FloatTensor([[0, 0], [0, 1], [1, 0], [1, 1]])
                                                                   print('실제값(Y): ', Y)
Y = torch.FloatTensor([[0], [1], [1], [0]])
                                                                   print('정확도(Accuracy): ', accuracy.item())
linear = nn.Linear(2, 1, bias=True)
sigmoid = nn.Sigmoid()
model = nn.Sequential(linear, sigmoid)
criterion = torch.nn.BCELoss()
optimizer = torch.optim.SGD(model.parameters(), lr=1)
                                                                   단층 퍼셉트론은 XOR문제를 풀 수 없다
for step in range(10001):
     optimizer.zero_grad()
                                                                   XOR
     hypothesis = model(X)
                                                                   x1 x2 y
     cost = criterion(hypothesis, Y)
     cost.backward()
     optimizer.step()
     if step % 100 == 0:
          print(step, cost.item())
```

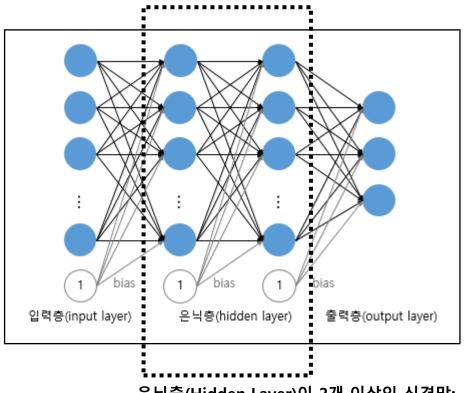
PyTorch - 단층 퍼셉트론 (Single-Layer Perceptron)



PyTorch - 다층 퍼셉트론 (MLP, Multi-Layer Perceptron)

다층 퍼셉트론(MLP, Multi-Layer Perceptron)





은닉층(Hidden Layer)이 2개 이상인 신경망: 심층 신경망(DNN, Deep Neural Network)

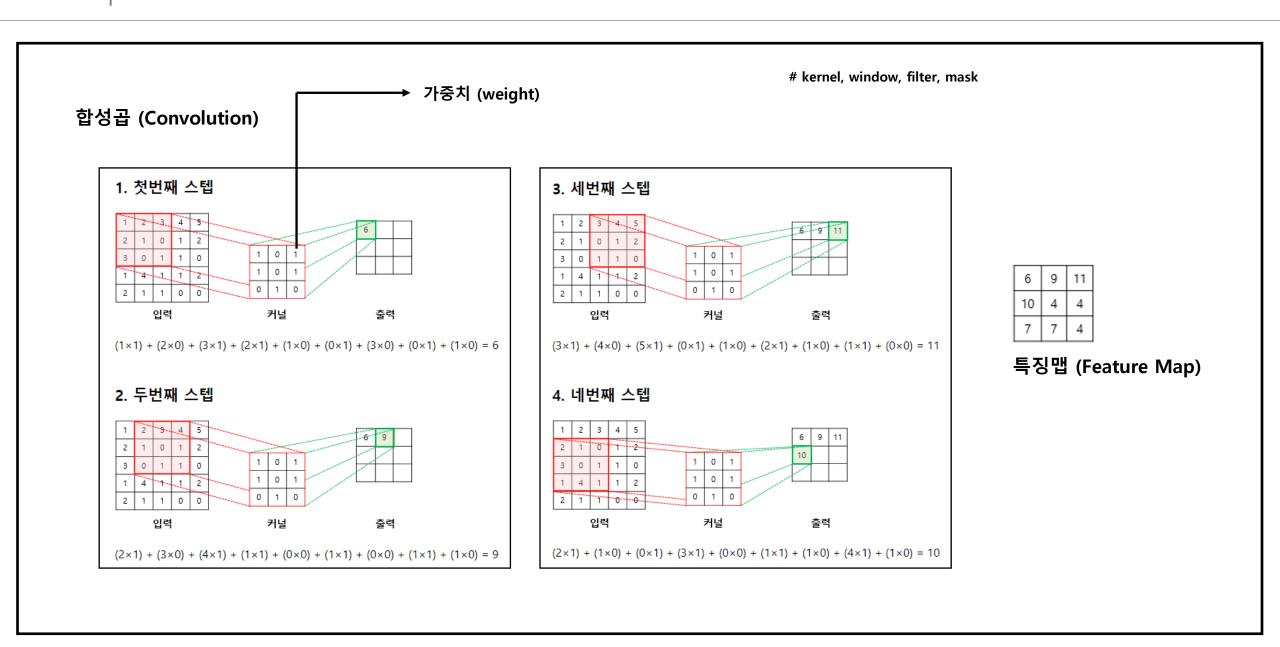
심층 신경망 학습: 딥러닝(Deep Learning)

PyTorch - 다층 퍼셉트론 (MLP, Multi-Layer Perceptron)

```
import torch
import torch.nn as nn
X = torch.FloatTensor([[0, 0], [0, 1], [1, 0], [1, 1]])
Y = torch.FloatTensor([[0], [1], [1], [0]])
model = nn.Sequential(
     nn.Linear(2, 10, bias=True), # input layer=2, hidden layer1=10
     nn.Sigmoid(),
     nn.Linear(10, 10, bias=True), # hidden layer1=10, hidden layer2=10
     nn.Sigmoid(),
     nn.Linear(10, 10, bias=True), # hidden layer2=10, hidden layer3=10
     nn.Sigmoid(),
     nn.Linear(10, 1, bias=True), # hidden layer3=10, output layer=1
     nn.Sigmoid()
criterion = torch.nn.BCELoss()
optimizer = torch.optim.SGD(model.parameters(), lr=1)
for epoch in range(10001):
     optimizer.zero_grad() # forward 연산
     hypothesis = model(X) # 비용 함수
     cost = criterion(hypothesis, Y)
     cost.backward()
     optimizer.step()
     if epoch % 100 == 0:
          print(epoch, cost.item())
```

hypothesis = model(X)
predicted = (hypothesis > 0.5).float() # threshold 0.5
accuracy = (predicted == Y).float().mean() * 100
print('모델의 출력값(Hypothesis): ', hypothesis)
print('모델의 예측값(Predicted): ', predicted)
print('실제값(Y): ', Y)
print('정확도(Accuracy): ', accuracy.item())

다층 퍼셉트론은 XOR문제를 풀 수 있다



합성곱 (Convolution)

import torch

```
import torch.nn as nn
# batch size × channel × height × width의 Tensor 선언
x = torch.full((1, 1, 5), 2.)
print(x)

# in_channels, out_channels, kernel_size, padding, stride
conv = nn.Conv1d(1, 1, 3, padding=0, stride=1)
nn.init.uniform_(conv.weight, 1,1)
# nn.init.constant_(conv.weight, 1,1)
nn.init.uniform_(conv.bias, 3,3)
print(conv.weight, conv.bias)

print(conv(x))
```

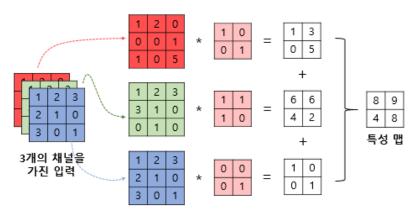
```
import torch
import torch.nn as nn
# batch size × channel × height × width의 Tensor 선언
x = torch.full((1, 1, 5, 5), 2.)
print(x)

# in_channels out_channels, kernel_size, padding, stride
conv = nn.Conv2d(1, 1, 3, padding=0, stride=1)
nn.init.uniform_(conv.weight, 1,1)
nn.init.uniform_(conv.bias, 3,3)
print(conv.weight, conv.bias)
```

1D Convolution

2D Convolution

합성곱 (Convolution)



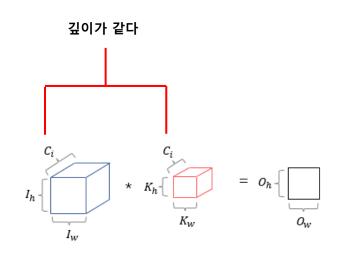
채널 간 합성곱 연산

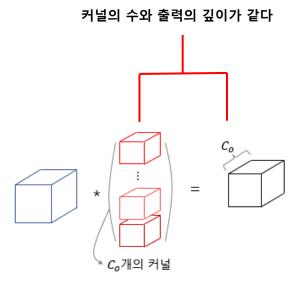
입력의 깊이(depth)와 필터의 깊이(depth)는 같아야 한다

입력: 3 x 3 x 3 필터: 3 x 2 x 2 출력: 1 x 2 x 2

예) 흑백 이미지: 256 x 256 x 1

컬러 이미지: 256 x 256 x 3





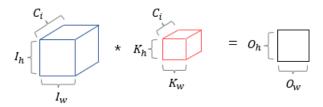
패딩 전					패딩 후							
2	1	1	0	0		0	0	0	0	0	0	0
1	4	1	1	2		0	2	1	1	0	0	0
3	0	1	1	0		0	1	4	1	1	2	0
2	1	0	1	2		0	3	0	1	1	0	0
<u> </u>	2	3	4	5		0	2	1	0	1	2	0
				_	1	0	1	2	3	4	5	0
						0	0	0	0	0	0	0

합성곱 (Convolution)

```
import torch
import torch.nn as nn
# batch size × channel × height × width의 Tensor 선언
x = torch.full((1, 3, 5, 5), 2.)
print(x)
```

in_channels, out_channels, kernel_size, padding, stride conv = nn.Conv2d(3, 1, 3, padding=0, stride=1) nn.init.uniform_(conv.weight, 1,1) nn.init.uniform_(conv.bias, 3,3) print(conv.weight, conv.bias)

print(conv(x))

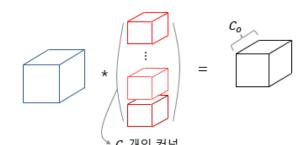


2D convolution

import torch import torch.nn as nn # batch size × channel × height × width의 Tensor 선언 x = torch.full((1, 3, 5, 5), 2.) print(x)

in_channels, out_channels, kernel_size, padding, stride conv = nn.Conv2d(3, 3, 3, padding=0, stride=1) nn.init.uniform_(conv.weight, 1,1) nn.init.uniform_(conv.bias, 3,3) print(conv.weight, conv.bias)

print(conv(x))



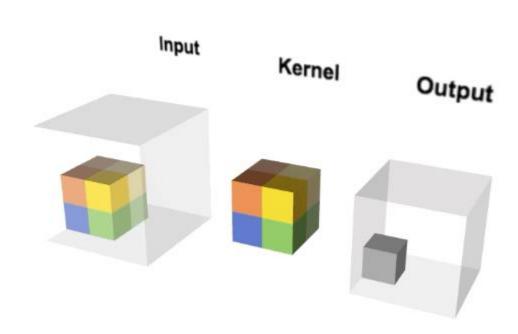
2D convolution

합성곱 (Convolution)

```
import torch
import torch.nn as nn
# batch size × channel × height × width의 Tensor 선언
x = torch.full((1, 1, 5, 5, 5), 2.)
print(x)
```

in_channels, out_channels, kernel_size, padding, stride
conv = nn.Conv3d(1, 1, 3, padding=0, stride=1)
nn.init.uniform_(conv.weight, 1,1)
nn.init.uniform_(conv.bias, 3,3)
print(conv.weight, conv.bias)

print(conv(x))



3D Convolution

```
합성곱 (Convolution)
model = nn.Conv2D(1, 1, 5) # in_channels, out_channels, kernel_size
print(list(model.parameters()))
# 가중치(weight), 편향(bias) 초기화
nn.init.uniform_(model.weight, 0, 5)
# nn.init.constant_(model.weight, 2)
# nn.init.ones_(model.weight)
# nn.init.zeros (model.weight)
# nn.init.eye (model.weight)
# nn.init.normal_(model.weight)
# nn.init.xavier_uniform_(model.weight, gain=1.0)
# nn.init.xavier_normal_(model.weight, gain=1.0)
# nn.init.kaiming_uniform_(model.weight, mode='fan_in', nonlinearity='relu')
# nn.init.kaiming_normal_(model.weight, mode='fan_out', nonlinearity='relu')
# model.weight.data = nn.Parameter(torch.Tensor([ [ [ [1,1,1,1,1],
                                                      [1,1,1,1,1],
                                                      [1,1,1,1,1],
                                                      [1,1,1,1,1],
                                                      [1,1,1,1,1]]]]))
# model.bias.data = nn.Parameter(torch.Tensor([ [ [ [0.5] ] ] ] ]))
```

```
import torch
import matplotlib.pyplot as plt
import numpy as np

tensor = torch.empty(100)
torch.nn.init.uniform_(tensor, 1, 10)
# torch.nn.init.uniform_(tensor)

# graph
plt.plot(range(len(tensor)),tensor)
plt.show()

# histogram
plt.hist(np.sort(tensor))
plt.show()
print("uniform")
```

풀링 (Pooling) : 다운샘플링 (Down Sampling)

노이즈를 제거하고, 효율적으로 특징추출

Parameter를 줄여, computation이 줄고, hardware resource를 절약하고, 학습속도를 높인다. 과적합(Overfitting) 억제 효과가 있다.

Max Pooling, Average Pooling, Global Average Pooling

	5	2	3	4			
	2	1	0_	1_	 최대값	 	
Γ	3	7	9	5	최대값 출력	5	4
	1	4	1	8	 	 . 7	9

Max Pooling : [5, 4, 7, 9]

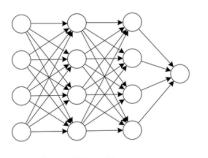
Average Pooling : [2.5, 2, 3.75, 5.75]

Global Average Pooling: [3.5]

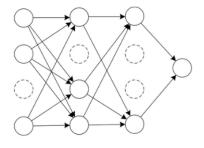
과(대)적합 (Overfitting) ←→ 과소적합(Underfitting)

- 1. 데이터 양 늘리기 (데이터 증강, Data Augmentation)
- 2. 모델의 복잡도 줄이기
- 3. 가중치 규제(Regularization) 적용하기
- 4. 드롭아웃(DropOut) 적용하기

Dropout = 0.5, 랜덤으로 절반의 뉴런만 사용하여 학습 (추론시에는 모든 뉴런 사용)







(b) Network after Dropout

Optimizer

- 1. SGD (Stochastic Gradient Descent)
- 2. Adam (Adaptive Moment Estimation)
- 3. AdaGrad (Adaptive Gradient)
- 4. AdaDelta (Adaptive Delta
- 5. Momentum
- 6. RMSProp
- 7. NAG (Nesterov Accelerated Gradient)

momentum

$$V_{t} = m \times V_{t-1} - \eta \nabla_{\omega} J(\omega_{t})$$

$$\omega_{t+1} = \omega_t + V_t$$