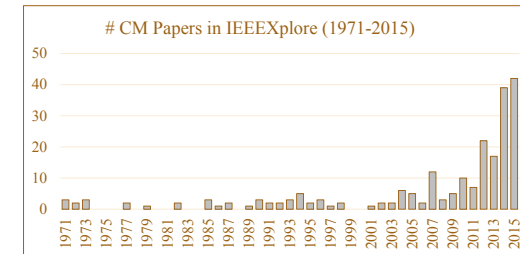


## Course Objective

- Theory of Characteristic Modes (TCM) proposed in 1971 by Garbacz and Harrington
- Time finally come for widespread interest
  - Research activities exploding



- Major software vendors implemented characteristic mode analysis (CMA) due to strong customer interest

2



## Course Objective

- This course designed to answer basic questions:
  - What is it? What's all the fuss about?
  - Can I use it in my work?
  - How do I get started?
  - How do I get involved?
  - What opportunities are there?
  - etc.
- This course to provide good foundation, NOT to treat fine details



3

## Course Overview

Short, short course (2 hr)

- Course Objective
- Physical Insights
- Intro to CM Concepts
- Basic CM Analysis & Examples
- Specialized Example (Terminal antenna)
- Demo of CMA Tools
- Future Directions
- Concluding Remarks



4

## Physical Insights of TCM

WHAT INSIGHTS, WHY ARE THEY USEFUL, HOW TO USE THEM?



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## Physical Insights to Abstract Problems

- Electromagnetic systems are complex (Maxwell's Equations!)
- In many problems, object's resonance is important
- Energy stored also important:
  - Capacitive vs. inductive
- So are these issues:
  - Feed locations, radiation pattern, coupling, etc.
- TCM gives physical insights on these aspects



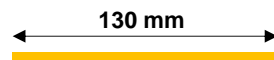
Acoustic resonance



6

## Physical Insights to Abstract Problems

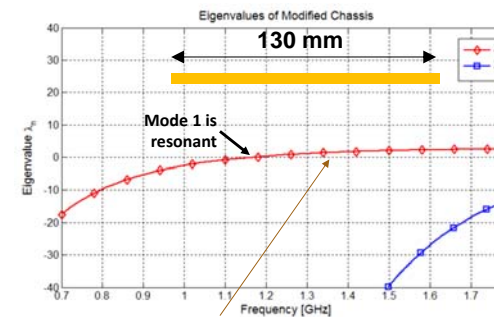
- TCM for electromagnetic analysis and design
  - Provide inherent resonant properties of a structure
  - Depends only on geometry and materials
  - Useful to solve scattering and antenna problems
  - For antenna design, visualize possible radiation modes supported by structure
- Still too abstract? Let's demonstrate CMA using a dipole-like PEC structure (width of 4 mm)



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## Physical Insights with CMA

- How does a dipole antenna radiate?
  - Calculate CMs for the thin strip using eigenvalue decomposition
  - Eigenvalues indicate **resonance property**



Expect resonance at 1.36 GHz if  
130mm is half a wavelength ( $\lambda/2$ )

Eigenvalues @750MHz

Mode 1: -12  
Mode 2: -1455  
⋮



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## Physical Insights with CMA

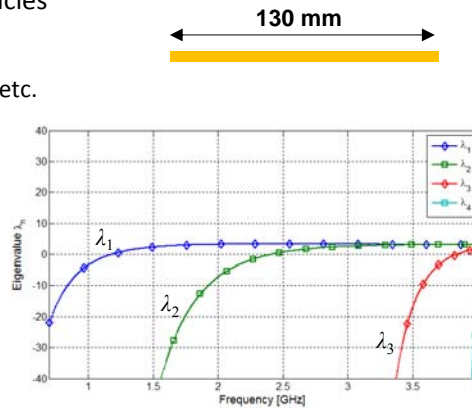
- Multiple resonant frequencies

- $\lambda_1$  is resonant at 1.2 GHz
- $\lambda_2$  is resonant at 2.4 GHz, etc.

- Excitation of Modes

- Resonant modes
- Non-resonant modes
  - Proper feed location(s)
  - Matching network
  - Structural change

- Modes are orthogonal in currents and far-fields



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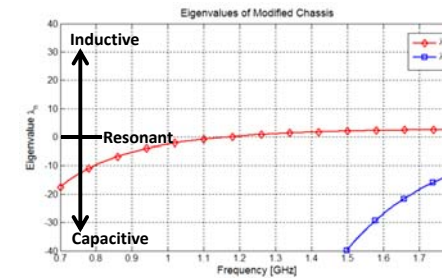
## Physical Insights with CMA

- “Capacitive” Mode,  $\lambda_n < 0$

- Stores electric energy  $W_e$  ( $W_e > W_m$ )
- Often excited with capacitive coupling element

- “Inductive” Mode,  $\lambda_n > 0$

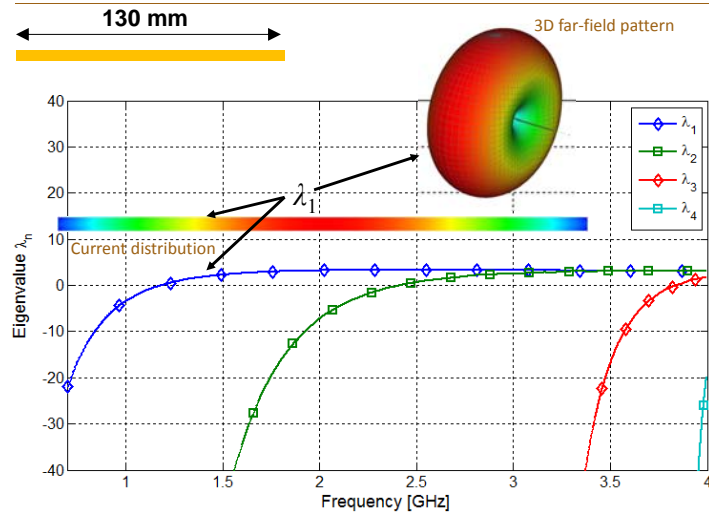
- Stores magnetic energy  $W_m$  ( $W_m > W_e$ ),
- Often excited with inductive coupling element



10



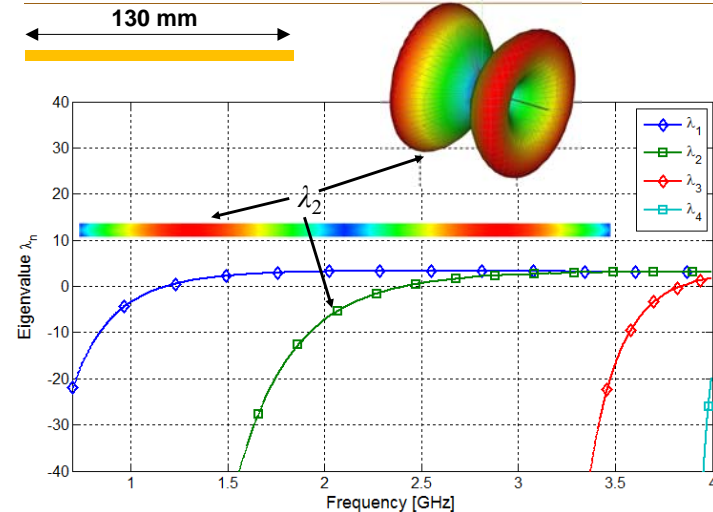
## Modal Attributes of Thin Wire



11



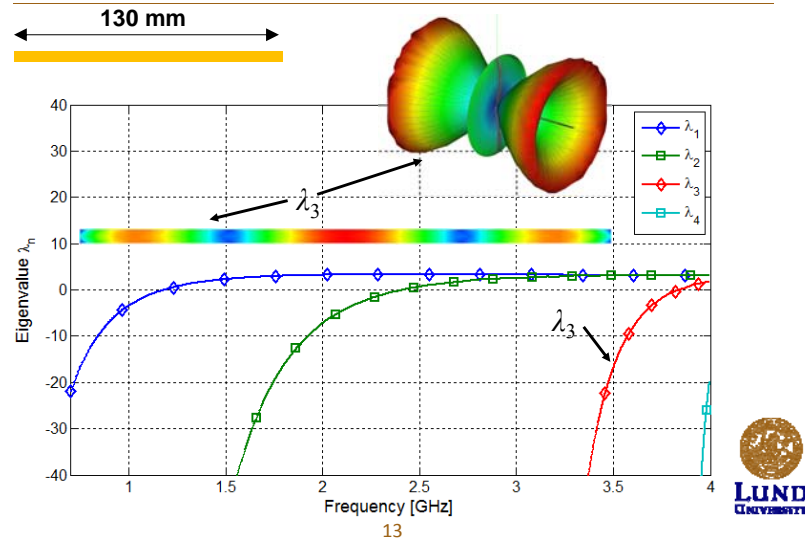
## Modal Attributes of Thin Wire



12

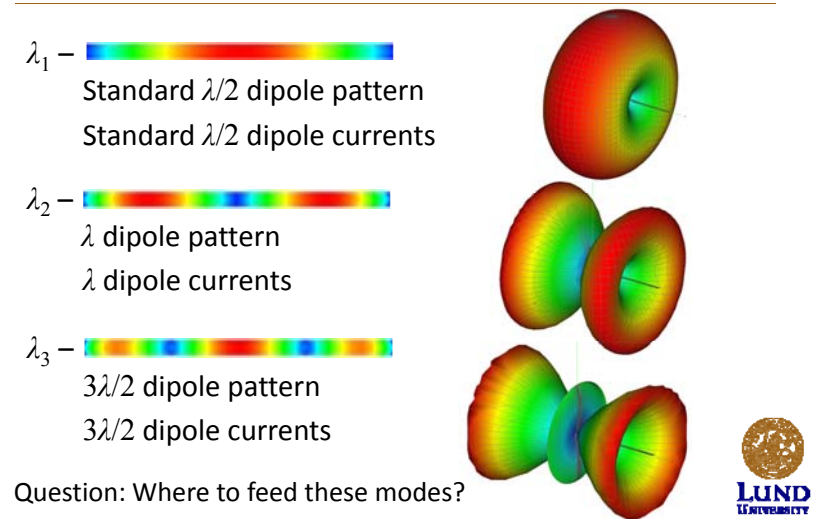


## Modal Attributes of Thin Wire



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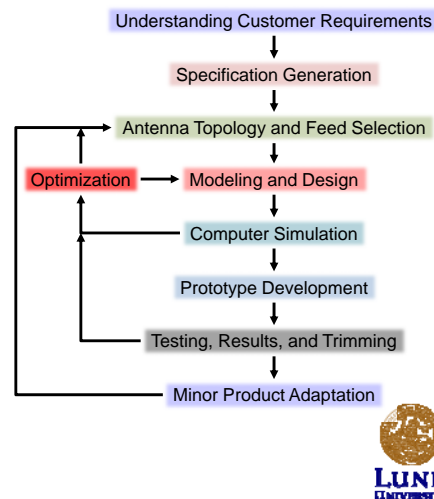
## Currents and Far-Fields Orthogonal



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## Current Integrated Antenna Design

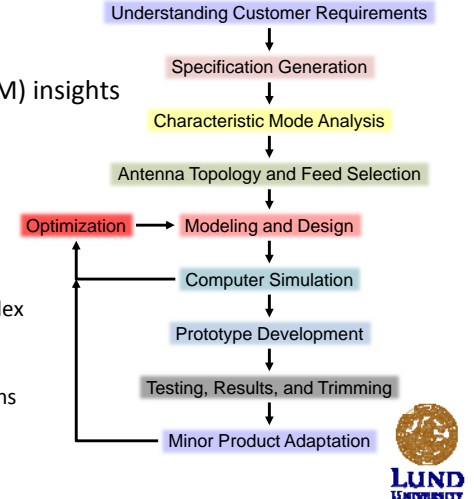
- Start from an system
  - Not a closed form solution
- Complex
  - Multiple ideas
- Time consuming
  - Abstract ideas/information
- Optimization intensive
  - Computationally complex
- No physical insights



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## CM Integrated Antenna Design

- Start from an system
- Obtain electromagnetic (EM) insights
  - Resonant characteristics
- Utilize EM characteristics
  - Development of Feeds
- Traditional Optimization
  - Less computationally complex
- Full Understanding
  - Allows for future adaptations



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## Basic CM concepts

UNDERLYING THEORY, COMMON METRICS AND MODE TRACKING



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## Underlying Theory

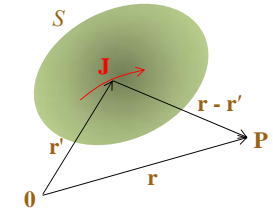
- Start from Electromagnetic Theory 101
- Current  $\mathbf{J}(\mathbf{r}')$  on surface of conductor  $S$  causes electric field  $\mathbf{E}(\mathbf{r})$  at point  $\mathbf{r}$
- Solving Maxwell's Equations in time harmonic form, we obtain

$$\mathbf{E}(\mathbf{r}) = -\nabla\phi(\mathbf{J}) - j\omega\mathbf{A}(\mathbf{J})$$

$$\text{where } \phi(\mathbf{J}) = -\frac{1}{j\omega\epsilon} \oint_S \nabla' \cdot \mathbf{J}(\mathbf{r}') \psi(\mathbf{r}, \mathbf{r}') ds'$$

$$\mathbf{A}(\mathbf{J}) = \mu \oint_S \mathbf{J}(\mathbf{r}') \psi(\mathbf{r}, \mathbf{r}') ds'$$

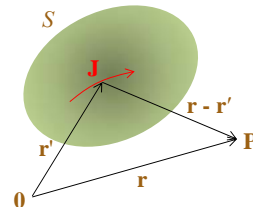
$$\psi(\mathbf{r}, \mathbf{r}') = \frac{e^{-jk|\mathbf{r}-\mathbf{r}'|}}{4\pi|\mathbf{r}-\mathbf{r}'|}$$



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## Underlying Theory

- But  $\mathbf{J}(\mathbf{r}')$  is from an impressed field  $\mathbf{E}^i(\mathbf{r}')$ 
  - antenna problem, known sources over  $S$
  - scattering problem, known sources external to  $S$  (incident wave)



- Define operator  $L(\mathbf{J}) = -\mathbf{E}(\mathbf{r})$ , then at the conductor surface (boundary)

$$[L(\mathbf{J}) - \mathbf{E}^i(\mathbf{r})]_{\text{tan}} = 0$$

Tangential component of induced E-field

- Define impedance operator  $Z(\mathbf{J}) = [L(\mathbf{J})]_{\text{tan}}$ ,  $Z(\mathbf{J}) = R(\mathbf{J}) + jX(\mathbf{J})$

- To obtain CMs, perform generalized eigenvalue decomposition

$$Z(\mathbf{J}_n) = \nu_n W(\mathbf{J}_n)$$

where  $W(\mathbf{J}_n)$  is the weight operator



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## Underlying Theory

- Eigenfunctions  $\mathbf{J}_n$  are real-valued since  $Z(\mathbf{J})$  is symmetric operator

- $\mathbf{J}_n$  orthogonal by default, free to choose  $W(\mathbf{J}_n)$

- Radiated power (of mode  $n$ ) given by

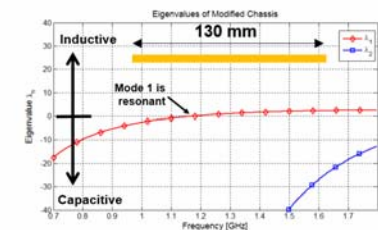
$$P_n = \langle \mathbf{J}_n^*, R(\mathbf{J}_n) \rangle = \oint_S \mathbf{J}_n^* \cdot \mathbf{R}(\mathbf{J}_n) ds$$

- To obtain orthogonal far-fields for the modes, let  $W(\mathbf{J}_n) = R(\mathbf{J}_n)$

$$\Rightarrow X(\mathbf{J}_n) = \lambda_n R(\mathbf{J}_n), \nu_n = 1 + j\lambda_n \text{ (CM eigenvalue equation)}$$

- Eigenvalue  $\lambda_n$  relates to difference in stored energies ( $W_m - W_e$ ):

- $W_m > W_e$  (inductive)
- $W_e > W_m$  (capacitive)



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## Underlying Theory

- For computation, operator  $Z(\mathbf{J})$  is discretized over surface  $S$  as impedance matrix  $\mathbf{Z} = \mathbf{R} + j\mathbf{X}$  using method-of-moments (MoM)
- $\mathbf{J}(\mathbf{r}')$  becomes scalar current vector  $\mathbf{I}$  associated with  $\mathbf{Z}$
- Therefore, eigenvalue equation becomes

$$\mathbf{X}\mathbf{I}_n = \lambda_n \mathbf{R}\mathbf{I}_n$$

- Characteristic currents should be normalized such that radiated power is 1 for all modes:

$$\mathbf{I}_n^H \mathbf{R} \mathbf{I}_n = \mathbf{I}_n^T \mathbf{R} \mathbf{I}_n = 1$$



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## CM Metric: Modal Significance

- Recall that  $[L(\mathbf{J}) - \mathbf{E}^i]_{\tan} = 0$  and all currents can be written as  $\mathbf{J} = \sum_n a_n \mathbf{J}_n$
- Taking inner product with  $\mathbf{J}_m$ :  $\sum_n a_n \langle \mathbf{J}_m, \mathbf{Z} \mathbf{J}_n \rangle = \underbrace{\langle \mathbf{J}_m, [\mathbf{E}^i]_{\tan} \rangle}_{\text{modal excitation coefficient}}$
- Using properties of CM,

$$a_n (1 + j\lambda_n) = \langle \mathbf{J}_n, [\mathbf{E}^i]_{\tan} \rangle \Rightarrow a_n = \frac{\langle \mathbf{J}_n, [\mathbf{E}^i]_{\tan} \rangle}{1 + j\lambda_n}$$

- Modal significance (MS) is defined as:

$$MS = \left| \frac{1}{(1 + j\lambda_n)} \right|$$

(normalization for the characteristic current  $\mathbf{J}_n$ )



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## CM Metric: Modal Bandwidth

- Bandwidth defined as:

$$BW = \frac{f_h(S_{11} = \gamma) - f_l(S_{11} = \gamma)}{f_c}, \text{ typically } \gamma = -6 \text{ or } -10\text{dB}$$

- Modal Significance can be used to define “bandwidth”:

$$BW = \frac{f_H(MS = 1/\sqrt{2}) - f_L(MS = 1/\sqrt{2})}{f_c(MS = 1)}$$

- This was determined useful as it matches the modal Q

$$Q \approx \frac{1}{BW}$$

(Note: This does not relate well to excitable bandwidth)



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## CM Metric: Characteristic Angle

- $\mathbf{J}_n$  is the orthogonal set of currents induced by  $\mathbf{E}^i$
- $\mathbf{J}_n$  releases the energy accepted from  $\mathbf{E}^i$  as  $[\mathbf{E}_n]_{\tan}$
- $[\mathbf{E}_n]_{\tan}$  has an associated characteristic angle (“scattered” phase)  $\alpha_n$
- If no time lag, mode  $n$  acts like perfect scatterer, i.e. 180° shift
- Inductive modes store magnetic energy for a period of time
  - Time lag of magnetic energy, i.e.  $90^\circ < \alpha_n < 180^\circ$
- Capacitive modes store electric energy for a period of time
  - Time lag of electric energy, i.e.  $180^\circ < \alpha_n < 270^\circ$
- Characteristic angle is defined by:

$$\alpha_n = 180^\circ - \tan^{-1}(\lambda_n)$$

e.g. Insight into Yagi-Uda antenna



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## Characteristic Mode Tracking

- Eigenvalues found by solving the equation (discrete form):

$$\mathbf{X}\mathbf{I}_n = \lambda_n \mathbf{R}\mathbf{I}_n$$

- Solution is frequency dependent
  - Every frequency has a different impedance matrix
  - At every frequency  $\lambda_n$  is found in a different order
- Eigenvalues are not sorted between frequencies
  - Eigenvalue tracking algorithms needed
- Orthogonal properties not guaranteed across frequency

Z. Miers and B. K. Lau, "Wide band characteristic mode tracking utilizing far-field patterns," *IEEE Antennas Wireless Propag. Lett.*, vol. 14, pp. 1658-1661, 2015.

E. Safin and D. Manteuffel, "Advanced eigenvalue tracking of characteristic modes," *IEEE Trans. Antennas Propag.*, in press. (Special Issue on Theory and Applications of Characteristic Modes)



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## Eigenvector Correlation Tracking

- Eigenvector correlation based on

$$\rho_{m,n} = \frac{\mathbf{I}_m^H \mathbf{I}_n}{|\mathbf{I}_m| |\mathbf{I}_n|}$$

- Easy to implement
- Widely implemented
- Based on orthogonal currents assumption
  - not rigorous since actually  $\mathbf{I}_m^H \mathbf{R}\mathbf{I}_n = \mathbf{I}_m^T \mathbf{R}\mathbf{I}_n = 0, m \neq n$
  - Structure discretized, sensitive to errors
  - Orthogonality of currents not guaranteed across frequency



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## Surface Current Correlation Tracking

- Correlation of "surface current" (or "radiated power")

$$\rho_{m,n} = \langle \mathbf{J}_m, \mathbf{R}(\mathbf{J}_n) \rangle = \mathbf{I}_m^H \mathbf{R}\mathbf{I}_n$$

- For a given frequency:  $\mathbf{I}_m^H \mathbf{R}\mathbf{I}_n = \mathbf{I}_m^T \mathbf{R}\mathbf{I}_n = 0, m \neq n$
- Total surface current is "more orthogonal"
  - $\mathbf{R}(\mathbf{J}_n)$  does not vary quickly in frequency
  - Uses more characteristic information of structure
  - Usually better than eigenvector correlation
    - » Currents of individual discretized elements can vary more across frequency
  - Easy to implement



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## Hybrid Tracking

- Utilizes a mixture of different algorithms
  - Traditionally with mixed linear correlation functions
  - Tracking of eigenvalues using image processing techniques
  - Can utilize any other form of tracking
- Only as good as the algorithms used
  - Easy or hard to implement
  - Can be computationally efficient if used wisely



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## Far-Field Tracking

- Correlation of far-field pattern data

$$\rho_{m,n}^{CM} \approx \frac{\left| \oint_{4\pi} [E_{\phi,n}(\Omega) E_{\phi,m}^*(\Omega) + E_{\theta,n}(\Omega) E_{\theta,m}^*(\Omega)] d\Omega \right|^2}{\left| \oint_{4\pi} G_n(\Omega) d\Omega \right| \left| \oint_{4\pi} G_m(\Omega) d\Omega \right|}$$

where

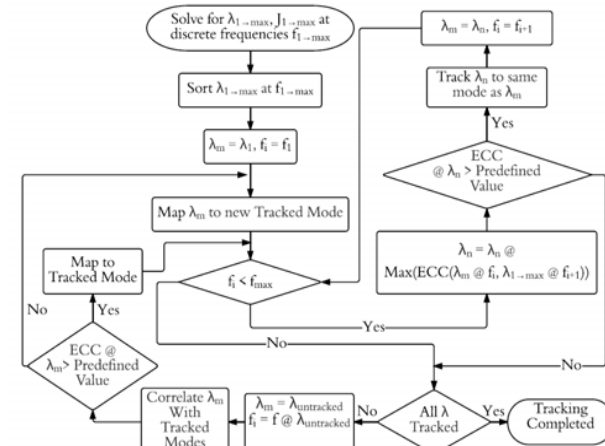
$$G_i(\Omega) = |E_{\phi,i}(\Omega)|^2 + |E_{\theta,i}(\Omega)|^2 \quad d\Omega = \sin\theta d\phi d\theta = (\phi, \theta)$$

- Discretized data is orthogonal for same frequency
- Fields not always orthogonal across frequency, but more stable than currents
- Computationally more complex (need far-fields)
- Struggles with degenerated modes



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## Lund University Tracking Method



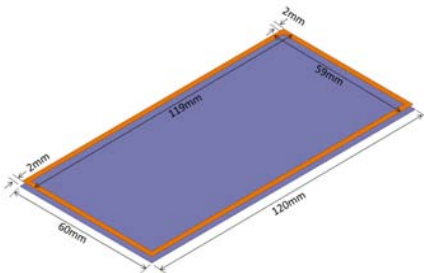
Z. Miers and B. K. Lau, "Wide band characteristic mode tracking utilizing far-field patterns," *IEEE Antennas Wireless Propag. Lett.*, vol. 14, pp. 1658-1661, 2015.



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## Comparison of Tracking Methods

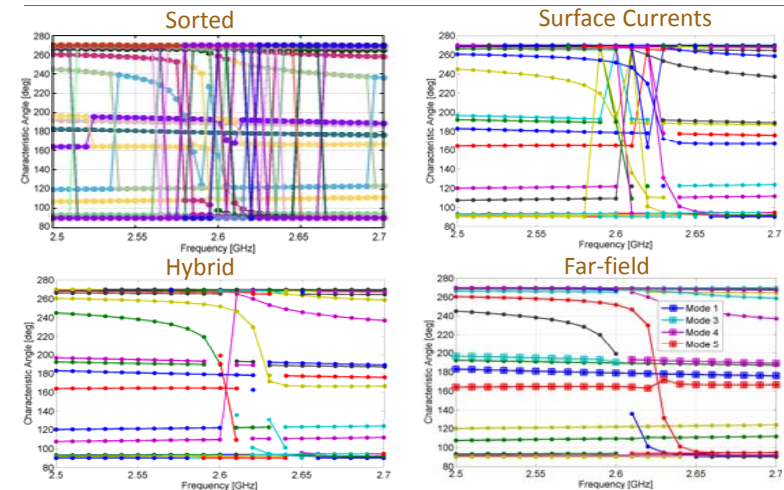
- Flat PEC chassis 60 mm × 120 mm, 2 mm wide rectangular metal ring 2 mm above the ground plane
- There exist modes with differences limited to high currents in small regions of the structure



Z. Miers and B. K. Lau, "Wide band characteristic mode tracking utilizing far-field patterns," *IEEE Antennas Wireless Propag. Lett.*, vol. 14, pp. 1658-1661, 2015.

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## Comparison of Tracking Methods



Z. Miers and B. K. Lau, "Wide band characteristic mode tracking utilizing far-field patterns," *IEEE Antennas Wireless Propag. Lett.*, vol. 14, pp. 1658-1661, 2015.

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## Basic CM Analysis

EIGENVALUES, CURRENTS, NEAR-FIELDS, AND FAR-FIELDS



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## Antenna Analysis – Eigenvalues

- Eigenvalues provide a “quick look” of antenna properties
  - Where are the resonances
  - How many modes can be excited by antenna(s)
- Further physical insights from quality factor Q
  - Approximate calculation is quick and easy ( $Q \approx 1/\text{bandwidth}$ )
    - » Modal significance  $\rightarrow$  modal bandwidth
    - » slope of eigenvalue  $d\lambda_n/d\omega \rightarrow$  obtainable bandwidth
  - Can modal bandwidth meet the requirements?
- Characteristic angle for analyzing reflection of a mode



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## Antenna Analysis – Currents

- Insights into structural modifications
  - Areas of high current will impact the eigenmode
  - Areas of low current will have less impact on eigenmode
- Insights into current<sup>1</sup> and voltage feeds
  - Splitting structures in areas of high current
  - Impact of feed location on multi-mode excitation
- Correlation functions allow for other additional insights
  - For example, comparison of structures, feed locations, etc.

<sup>1</sup> Current feeds can only be implemented through voltage induced currents



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## Antenna Analysis – Near-fields

- 3D structural changes
  - Information beyond physical structure allowing insights into structural changes
- Feed analysis of “complete units”
  - Capacitive coupling elements
  - Inductive coupling elements
- Coupling analysis
  - Feeds, matching circuits, and element modifications
  - Impact of multiple feeds
- Correlation functions allow for other additional insights



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## Antenna Analysis – Far-fields

- Provides structure-to-structure analysis
  - Structural modifications
    - » Modal changes across structure adaptations
    - » Allows for specific mode optimization



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## Examples of CM Analysis

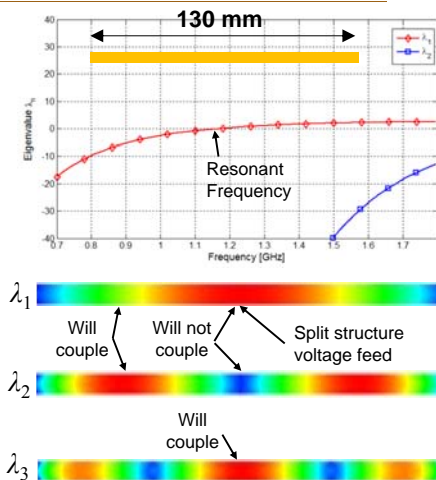
DIPOLE, WIDEBAND DIPOLE, SPIRAL



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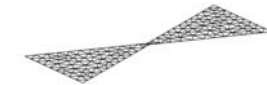
## Thin Wire - Dipole Antenna

- Eigenvalue analysis
  - Resonance → 1.15GHz
  - BW → 14%
- Currents analysis
  - Center feed with splitting
  - Will not couple to  $\lambda_2$
  - Will couple to  $\lambda_3$

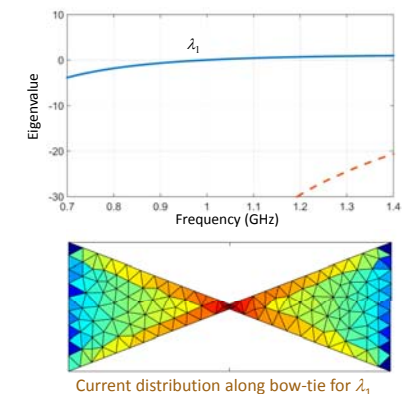


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## Bow-Tie Antenna



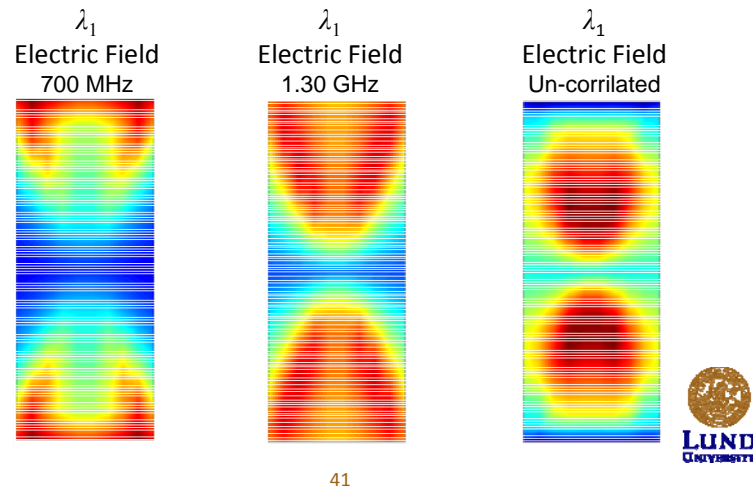
- Eigenvalue analysis
  - Resonance → 1.0GHz
  - BW → 26%
  - “single mode” contribution
- Currents analysis
  - Center fed with splitting
  - Constant over frequency
- Near-field analysis
  - Shift significantly over frequency



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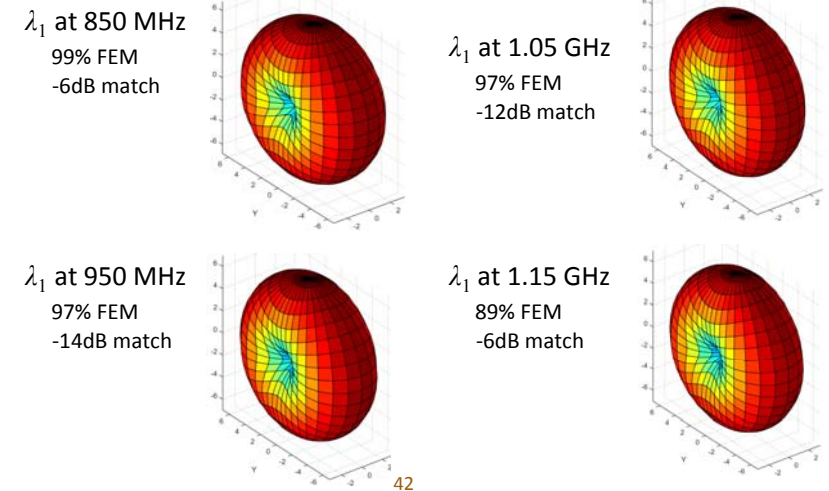
## Bow-Tie (Characteristic Near-fields)

- Near-field analysis (10 mm above bow-tie)



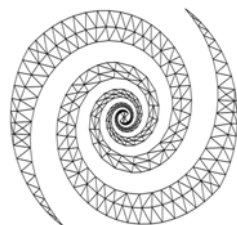
## Bow-Tie Eigen Patterns vs FEM Simulation

- Far-field analysis



## Logarithmic Spiral Antenna

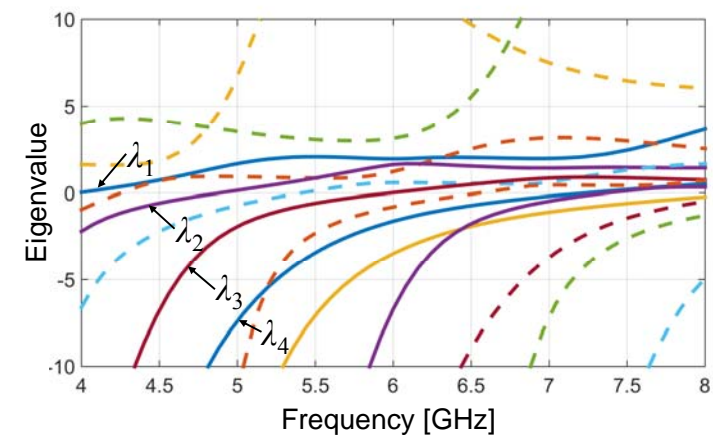
- Wideband antennas can be better understood
  - Analysis of orthogonal currents
  - Modal “hopping” becomes obvious
  - Far-field modal contribution
  - CMA vs excited structures



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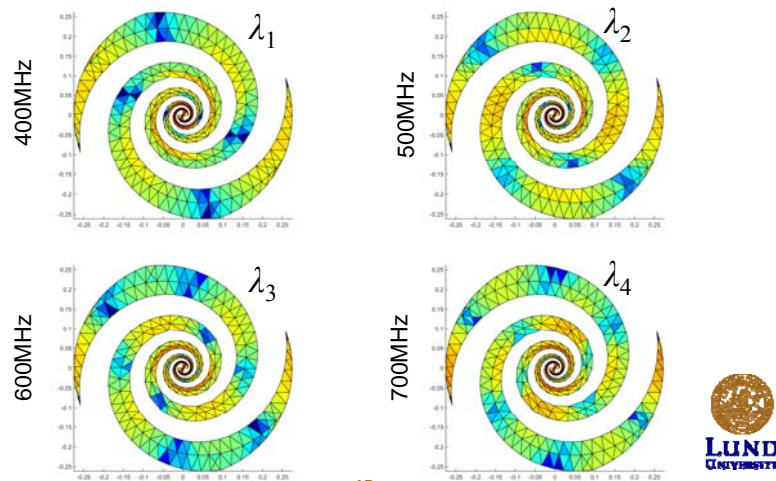
## Single Eigenmode Contribution

- Solid lines contribute to >80% of “typical pattern” across resonance



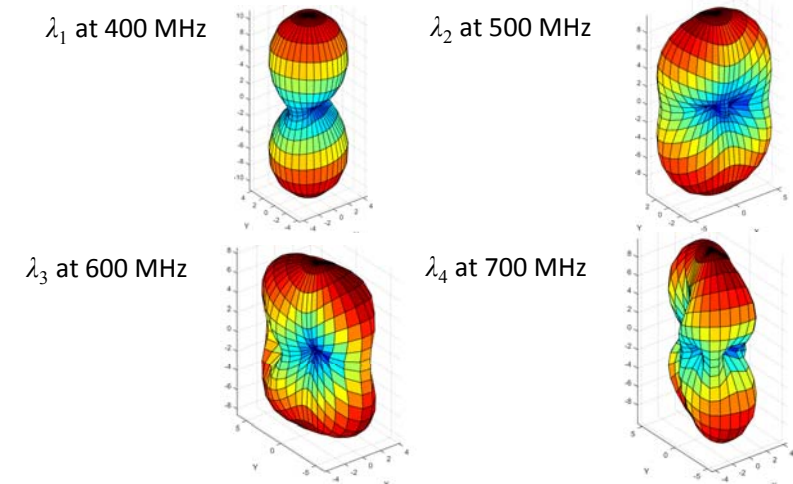
## Current Distribution of Dominant CM

- Single excitation of specific modes observed



## Pattern Variation Across Frequency

- Different modes over frequency, pattern evolving/rotating



## TCM-Assisted Terminal Design

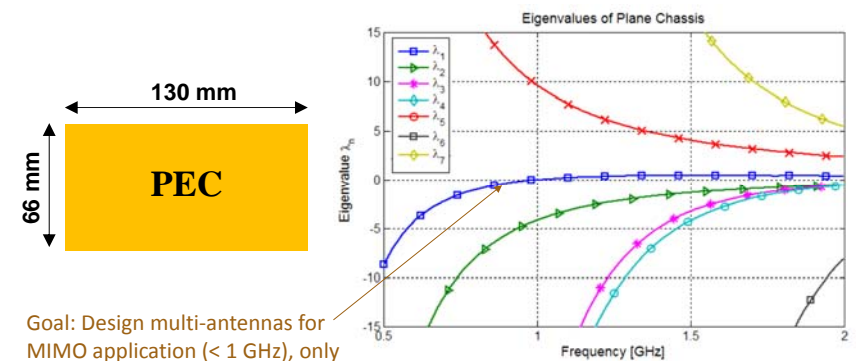
STANDARD FLAT CHASSIS, COMPONENT CHASSIS



47

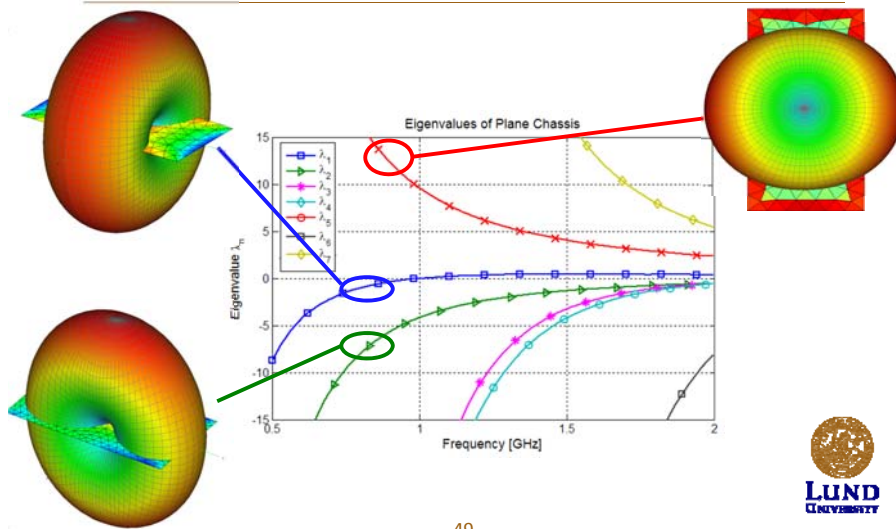
## TCM for Terminal Antennas

- Consider 130 mm × 66 mm chassis of a “typical mobile”
- What modes are available, can they be adapted?



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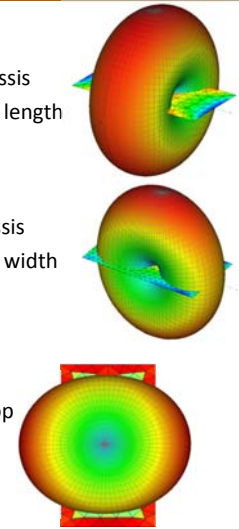
## CMA for Structure Alteration



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## Mode adaptation (850 MHz)

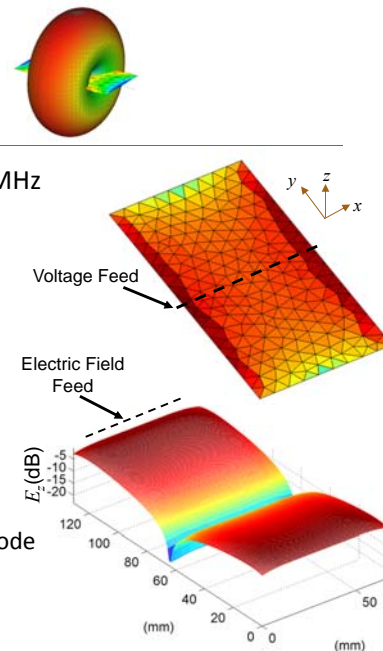
- Mode 1 ( $\lambda_1$ )
  - Currents alternating along the length of the chassis
  - Modal pattern represents that of a dipole along length
  - Slightly capacitive, near resonance
- Mode 2 ( $\lambda_2$ )
  - Currents alternating along the width of the chassis
  - Modal pattern represents that of a dipole along width
  - Very capacitive, not near resonance
- Mode 3 ( $\lambda_3$ )
  - Currents rotating around structure
  - Modal pattern represents that of a resonant loop
  - Very inductive, not near resonance



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## CMA of Mode 1

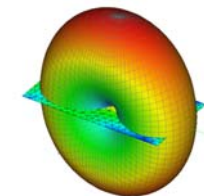
- Mode 1 is near resonance at 850 MHz
- Splitting of the chassis
  - Not often allowed
- Utilization of near-field feeding
  - Many typical antennas
  - Top loading of structure
  - Matching Circuits
- Not an interesting mode
  - Well-known and often utilized mode
  - Modal features used in MIMO



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## CMA of Mode 2

- Mode 2 is not resonant < 2 GHz
  - Must use structural adaptation
- Sectioning or splitting the chassis
  - Not often allowed, may not help
- Utilization of near-field Feeding
  - Must be near resonance for usefulness
  - Side loading of structure
  - Matching circuits do not help with excitation
- Very interesting mode for CMA
  - Modal features used in MIMO



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## CMA of Mode 2

- Modal Currents
  - Resemble that of dipole along width
  - Far-field verifies this assumption
- Closed form dipole modifications can now be used
  - Capacitive loading
  - Inductive loading
- Top-hat (capactive) loading method chosen

H. Li, Z. Miers, and B. K. Lau, "Design of orthogonal MIMO handset antennas based on characteristic mode manipulation at frequency bands below 1 GHz," *IEEE Trans. Antennas Propag.*, vol. 62, no. 5, pp. 2756-2766, May 2014.

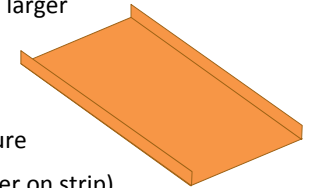
Z. Miers, H. Li, and B. K. Lau, "Design of bandwidth enhanced and multiband MIMO antennas using characteristic modes," *IEEE Antennas Wireless Propag. Lett.*, vol. 12, pp. 1696-1699, 2013. (Special Cluster on Terminal Antenna Systems for 4G and Beyond)



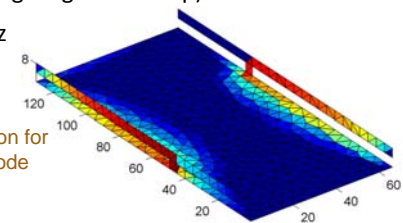
53

## Mode 2 Modification

- Add top-hat type features to the chassis (shorted along length of structure – physically bigger and adds capacitance)
  - Forces currents to outer edge, electrically larger
  - Pushes resonance to 1.6 GHz
- Add structural series inductance
  - Forces currents through section of structure
  - Increases outer capacitance (voltage higher on strip)
  - Pushes resonance to below 1 GHz

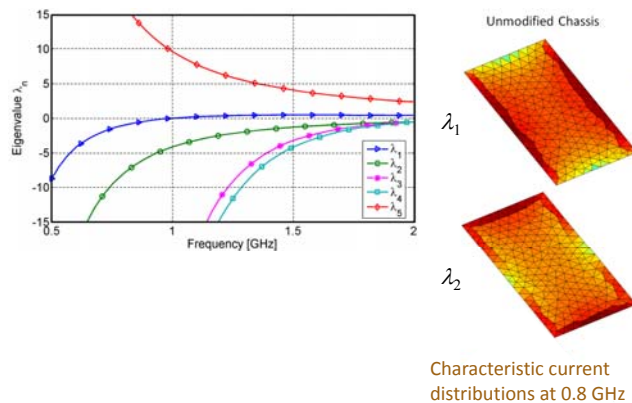


Current distribution for low frequency mode



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## Resonant Mode 2, and New Mode



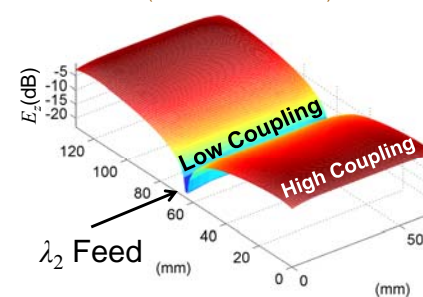
Characteristic current distributions at 0.8 GHz

55

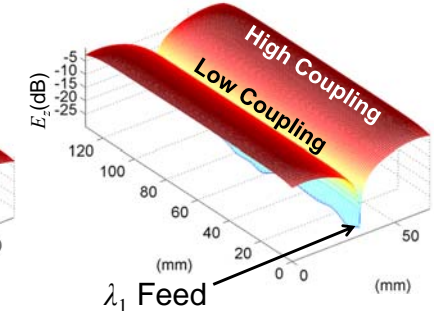
## Feeding Analysis

- MIMO antenna feeding considerations
  - Low coupling required
  - Multiple antennas, multiple feeds

Near field of  $\lambda_1$   
(10 mm above chassis)



Near field of  $\lambda_2$   
(10 mm above chassis)

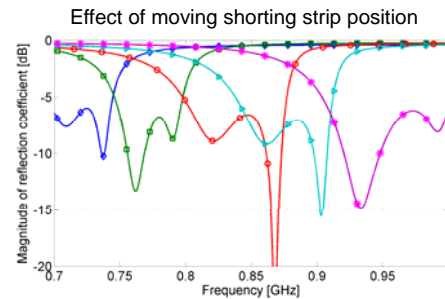
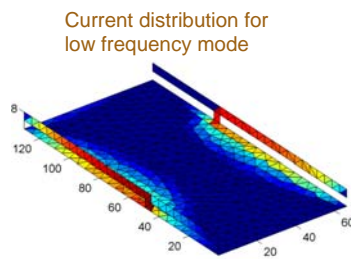


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## Physical Understanding – Easy Adaptation

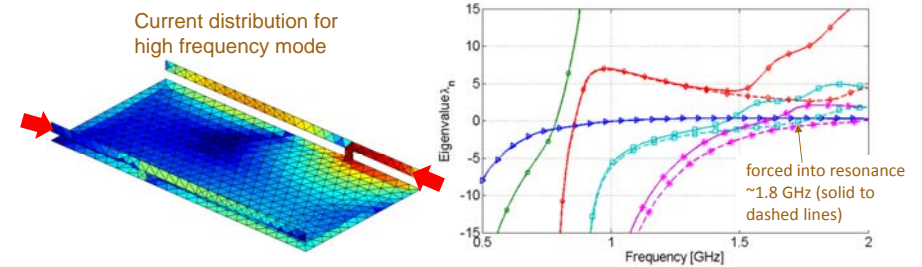
- Mode resonances is based on:
  - Total capacitance
  - Location of inductance (shorting strip)
  - Amount of inductance (width of shorting strip)



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## Modal Tracking – Multiband Response

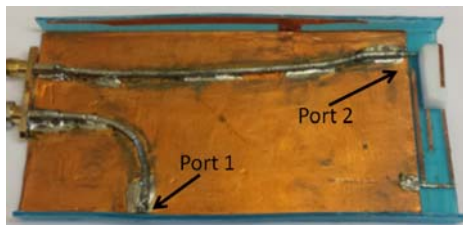
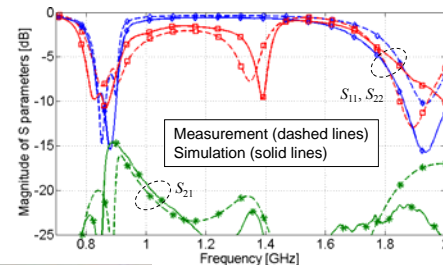
- High frequency resonances:
  - Tracking modes across frequency
  - Modal correlation in feed areas
  - Apply modal analysis on high frequency mode (force into resonance at desired frequency)



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## From TCM to Full Prototype

- TCM Design
- CST Model
  - Dielectrics
  - Feed matching
- Prototype

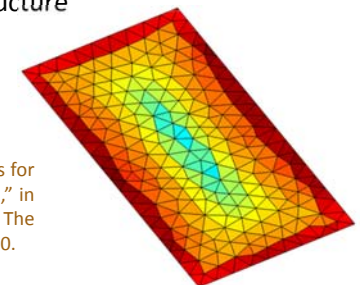
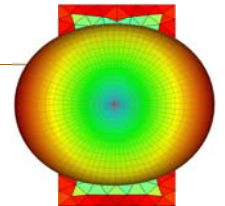


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## CMA of Mode 3

- Modal Currents
  - Resemble that of resonant loop
  - Far-field verifies this assumption
- Closed form loop modifications can now be used
  - Inline loops, not possible with structure
  - Secondary loop
- Apply and test theory

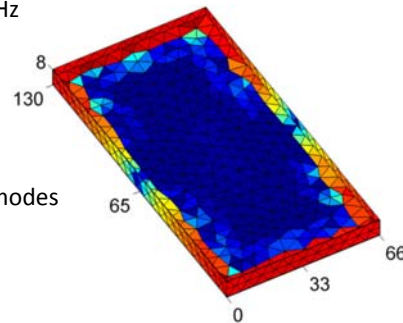


Z. Miers, H. Li, and B. K. Lau, "Design of bezel antennas for multiband MIMO terminals using characteristic modes," in *Proc. 8th Europ. Conf. Antennas Propag. (EuCAP'2014)*, The Hague, The Netherlands, Apr. 6-10, 2014, pp. 2556-2560.

60

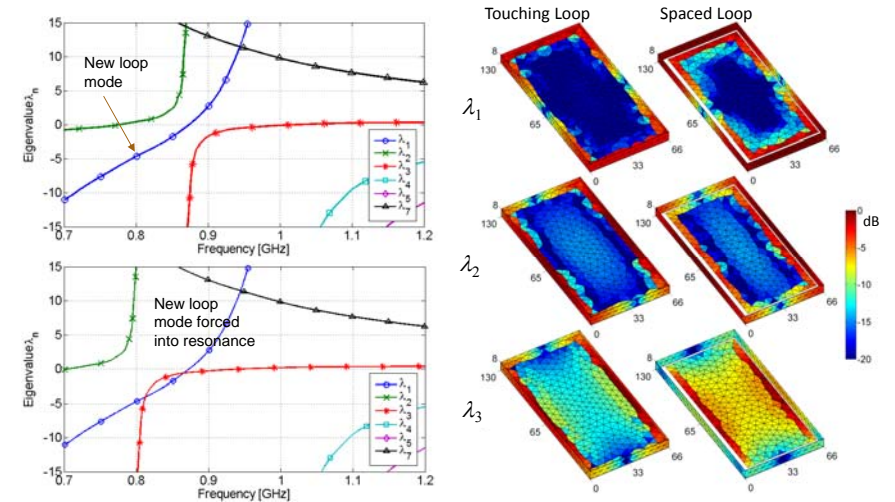
## Mode 3 Modification

- Add secondary loop features to the structure
  - Forces currents to outer edge, electrically larger
  - Pushes resonance to below 1 GHz
- Impacts fundamental mode
  - Forces only single resonances
  - Isolation of the loop
  - Allows for tuning and multiple modes



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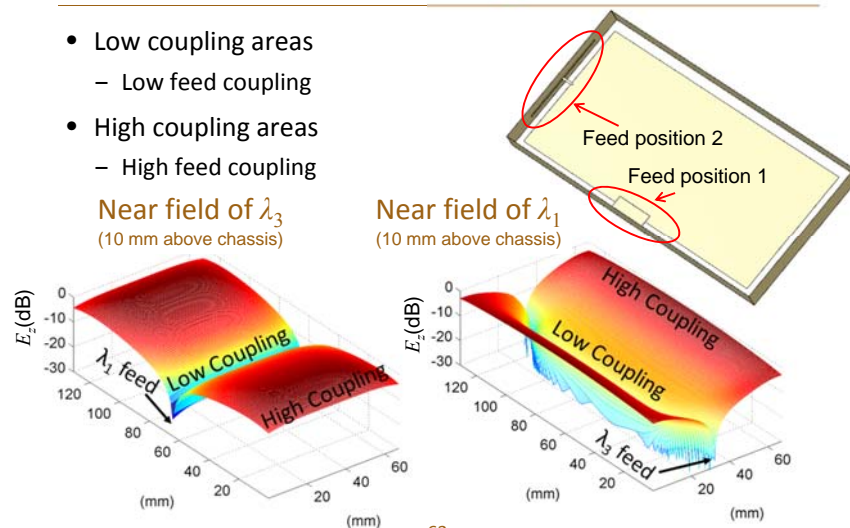
## Dual Low Band Resonance (Bezel)



62 Characteristic current distributions at 0.8 GHz

## Utilize TCM for Feeding

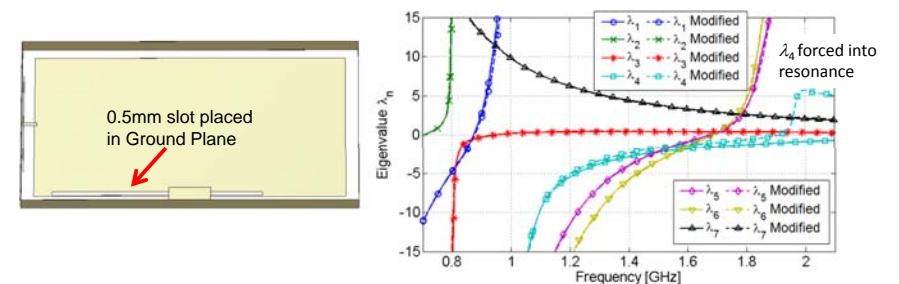
- Low coupling areas
  - Low feed coupling
- High coupling areas
  - High feed coupling



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## Modal Tracking

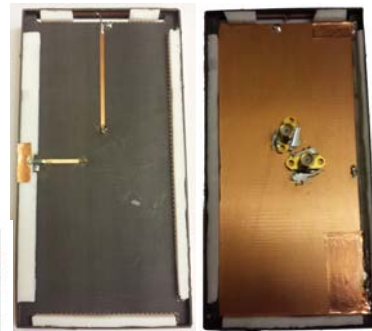
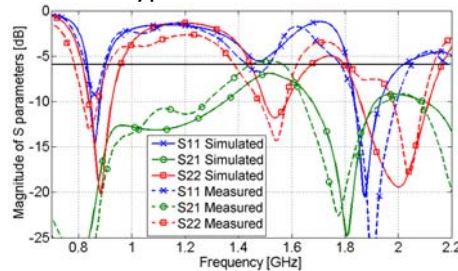
- High frequency resonances:
  - Shows how feeds can excite higher order modes
  - Apply modal analysis on high frequency mode
  - Application of slot forces mode into resonance



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## From TCM to Full Prototype

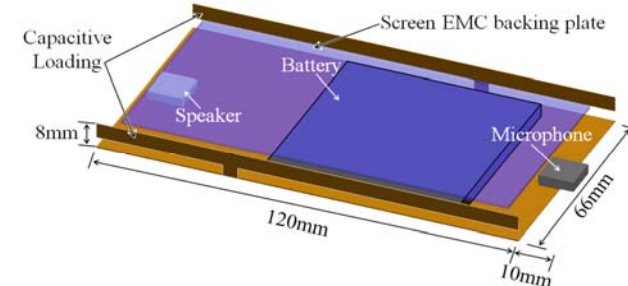
- TCM Design
- CST Model
  - Dielectrics
  - Feed matching
- Prototype



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## Full Structure TCM

- How practical is TCM design approach? Will it still work with components integrated?
- Consider a “fully-equipped” mobile terminal



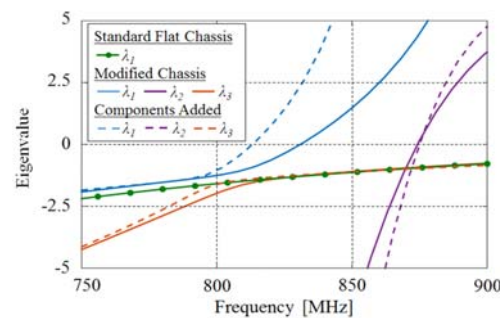
Z. Miers, A. Sekyere, J. A. Enohnyaket, M. Landaeus, and B. K. Lau, “Effects of internal components on designing MIMO terminal antennas using characteristic modes,” in *Proc. 10th Europ. Conf. Antennas Propag. (EuCAP’2016)*, Davos, Switzerland, Apr. 10-15, 2016.



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## TCM Design with Impact of Components

Impact of components on CM eigenvalues



- Design approach identical to that of previous examples
  - Analyze modal currents
  - Utilize antenna theory for basic adaptation (capacitive/inductive loading)
  - Utilize structural loading to create or modify modes



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## Quick Demo of CMA Software

MATLAB-BASED, FEKO, CST, WIPL-D



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## Future Directions & Conclusions

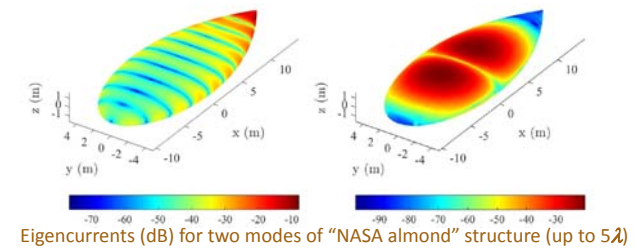
REFINING THEORY AND NEW APPLICATIONS



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## Electrically Larger Problems

- Current emphasis on structures around  $1\lambda$
- Complex for larger structures: Numerical issues and many resonant modes
- Attracting more interest (W. C. Chew, UIUC, USA; WIPL-D)  
Q. Dai, et al. "Large-scale characteristic mode analysis with fast multipole algorithms," *IEEE Trans. Antennas Propag.*, in press. (Special Issue on Theory and Applications of Characteristic Modes)



Eigencurrents (dB) for two modes of "NASA almond" structure (up to  $5\lambda$ )

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## TCM for Dielectric/Magnetic Materials

- Motivation: CM analysis and design for problems with non-PEC materials:
  - dielectric resonators/loading, body-worn antennas, etc.
- Basic theory exists from 1970's, but incomplete:

R. F. Harrington, J. R. Mautz, and Y. Chang, "Characteristic modes for dielectric and magnetic bodies," *IEEE Trans. Antennas Propag.*, vol. 20, no. 2, pp. 194-198, Mar. 1972.

Y. Chang and R. F. Harrington, "A surface formulation for characteristic modes of material bodies," *IEEE Trans. Antennas Propag.*, vol. 25, no. 6, pp. 789-795, Nov. 1977.

- Eigenvalue no longer give resonance
- Existing integral formulations complex (volume-based) or have internal resonances (surface-based)



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## TCM for Dielectric/Magnetic Materials

- Two research tracks:
  - New surface-based formulations to address shortcomings (Y. Chen, UESTC, China; C. F. Wang, NUS, Singapore)  
Y. Chen, "Alternative surface integral equation-based characteristic mode analysis of dielectric resonator antennas," *IET Microw. Antennas Propag.*, vol. 10, no. 2, pp. 193-201, 2016
  - Removing internal resonances in surface formulations (Z. Miers/B. K. Lau, LU, Sweden; McNamara, Uni Ottawa, Canada)  
Z. Miers and B. K. Lau, "Computational analysis and verifications of characteristic modes in real materials," *IEEE Trans. Antennas Propag.*, in press. (Special Issue on Theory and Applications of Characteristic Modes)
- More research needed!

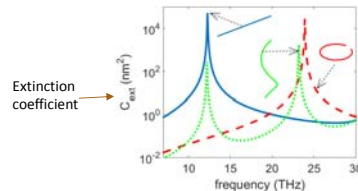


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## Examples of New Applications

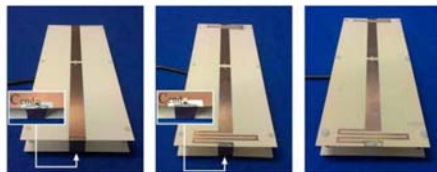
- Non-destructive testing of carbon nanotubes (CNT)



Scattering property for 3 CNT shapes

A. M. Hassan, et al., "Electromagnetic resonances of individual single-walled carbon nanotubes with realistic shapes: A characteristic modes approach," *IEEE Trans. Antennas Propag.*, in press. (Special Issue on Theory and Applications of Characteristic Modes)

- Design of radiative RF coil for ultrahigh-field (UHF) MRI



Analysis of coupling mechanism for different designs

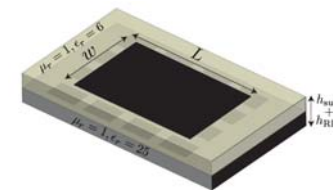
Z. Chen, et al., "Coupling Investigation of different RF coil elements for 7-Tesla Magnetic Resonance Imaging based on characteristic mode analysis" in *Proc. IEEE MTT-S Int. Microw. Symp.*, Tampa, FL, Jun. 1-6, 2014



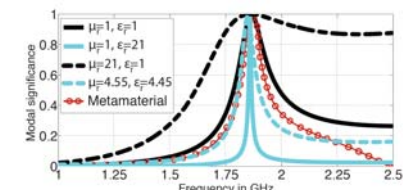
73

## Examples of New Applications

- Analysis of metamaterial structures



Patch antenna over reactive impedance surface (RIS)



Modal significance of mode 1 for different substrates

M. H. Rabbah, et al., "Analysis of miniature metamaterial and magneto-dielectric arbitrary-shaped patch antennas using characteristic modes: Evaluation of the Q factor" *IEEE Trans. Antennas Propag.*, in press. (Special Issue on Theory and Applications of Characteristic Modes)



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## Concluding Remarks

- TCM gives valuable physical insights into antenna and scattering problems, systematic design/analysis possible!
- Critical mass in applying TCM is reached!
- Basics of TCM and CMA explained
- Analysis and design demonstrated for common/specialized cases
- Proposed **action points** for all of you:
  - Get started: You will receive Makarov-script based TCM software by email within a week (Note: use as is, no user support!), etc. Full video introduction to be made available
  - Get involved: Join the TCM community (Special Interest Group on TCM, see [characteristicmodes.org](http://characteristicmodes.org) for more information)
  - Find your niche, still many stones left unturned
  - Have fun!



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