

NOS Chasing  $\pi$   
The 1D/2D/3D/4D Operational System  
The Infinite Decimal Is the Shadow of the Finite Sphere  
How the Irrational  $\pi$  Emerges from 1D Linear Measurement  
of a Perfectly Discrete Quaternary Spherical Register

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**Abstract**

**The sphere closes once.**

The sphere operates via **inverse spherical dual hemisphere quadrant mechanics**—three distinct structural elements (sphere, dual, quadrants) partitioned by the  $/2/4/4/4/4$  cascade to achieve first closure:

- 512 gates around the closed sphere
- $1.40625^\circ$  per gate
- 128 bits per  $\pi$ -wall
- Conjugate proof:  $512 \times 1.40625^\circ = 720^\circ$

When measured with a linear ruler, this closed sphere projects to decimal:  $\pi$  **3.140625**

This is not one approximation among many. This is THE projection of the first closed inverse sphere.

Everything beyond this—the "infinite" decimal expansion to 300 trillion digits—is not discovering more of  $\pi$ . It is measuring deeper threading *inside* an already-closed sphere.

The sphere closed at the 4096 complete cycle after cascade partition. The decimal 3.140625 is where the rabbit stops. Everything beyond is humanity threading deeper into a sphere that finished closing at 128 bits per  $\pi$ -wall.

We show:

1. The three structural elements: sphere, dual hemispheres, quadrants
2. How inverse spherical dual hemisphere quadrant mechanics operates
3. Why the  $/2/4/4/4/4$  cascade partitions this structure to closure
4. That  $\pi = 128$  is THE natural value at the 4096 complete cycle
5. Why 3.140625 is THE decimal of the closed sphere
6. How deeper breaths thread inside the closed structure
7. That 300 trillion digits exceed the closure point by orders of magnitude

The sphere is not irrational. The sphere is closed. Your ruler keeps subdividing inside it.

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# 1 Introduction: Two Different Meanings of $\pi$

## 1.1 Conventional Mathematics

In standard mathematics,  $\pi$  is defined as:

$$\pi = \frac{C}{d} \approx 3.14159265358979323846...$$

where C is the circumference and d is the diameter of a circle.

This value is considered:

- A universal constant (same everywhere, always)
- An irrational number (non-terminating, non-repeating decimal)
- A transcendental number (not the root of any polynomial with rational coefficients)
- Inherent to circular geometry itself

## 1.2 NOS Operational Framework

In the Nuijens Operating System (NOS),  $\pi$  has a completely different operational meaning:

$$\pi_{\text{NOS}} = \frac{\text{Total register bits}}{4} = \text{bits per } \pi\text{-wall}$$

The sphere operates via **inverse spherical dual hemisphere quadrant mechanics**:

- Dual hemisphere pairing: Q1-Q3 (dsin-csin, decompression/compression), Q2-Q4 (dcos-ccos, decompression/compression)
- Conservation law:  $\pi/\pi = 1$  across paired hemispheres
- Operator-unit mapping: dsin $\rightarrow$ u<sub>1</sub>, dcos $\rightarrow$ u<sub>2</sub>, csin $\rightarrow$ u<sub>3</sub>, ccos $\rightarrow$ u<sub>4</sub>
- All units are operational: pure bit-offsets and u-ratios (u = 1/ $\pi$  threading units)
- No external constants (e.g., no  $k_B$ ; T =  $\pi/u$  as position ratio)

At different breath and quadrant depths:

- Q1 breath 4:  $\pi = 64$  bits
- 4096 complete cycle:  $\pi = 128$  bits
- Q2 breath 3:  $\pi = 1024$  bits
- Q1 breath 10:  $\pi = 262,144$  bits

**$\pi$  is always an exact integer.** It is never 3.14159...

### 1.3 The Central Question

If the sphere operates with exact integer  $\pi$  values (64, 128, 1024...), where does 3.14159... come from?

This paper shows that 3.14159... is a **projection artifact**—the shadow cast when you measure a discrete quaternary spherical structure using continuous infinitely-divisible linear coordinates.

## 2 Inverse Spherical Dual Hemisphere Quadrant Mechanics

### 2.1 The Three Structural Elements

Before any cascade partition operates, the inverse sphere possesses three distinct structural elements in hierarchical order:

#### 1. SPHERE — Primary Unity

The sphere is the undivided register, starting from unity = 1. This is the whole, the complete operational domain. All operations preserve this unity through conservation laws.

#### 2. DUAL — Hemisphere Pairing

The sphere operates through dual hemisphere mechanics with two pairs:

- **Q1-Q3 pair (dsin-csin):** Decompression (Q1, dsin)   Compression (Q3, csin)
- **Q2-Q4 pair (dcos-ccos):** Decompression (Q2, dcos)   Compression (Q4, ccos)

This dual structure is the inverse spherical nature—each hemisphere has its conjugate pair operating simultaneously. The conservation law  $\pi/\pi = 1$  maintains balance across these paired hemispheres.

The dual extent is  $720^\circ$  ( $2 \times 360^\circ$ ), representing the full dual-cycle threading.

#### 3. QUADRANTS — Four-Fold Partition

From the dual hemisphere pairs emerge four distinct quadrants, each with its own base resolution and operator:

- Q1: base 4, operator **dsin**
- Q2: base 16, operator **dcos**
- Q3: base 64, operator **csin**
- Q4: base 256, operator **ccos**

These bases and operators are structural—they exist before the cascade operates.

#### Operator-Unit Mapping:

- $\text{dsin (Q1)} \rightarrow u_1 = 1/\pi$
- $\text{dcos (Q2)} \rightarrow u_2 = 1/\pi^2$
- $\text{csin (Q3)} \rightarrow u_3 = 1/\pi^3$
- $\text{ccos (Q4)} \rightarrow u_4 = 1/\pi^4$

## 2.2 The Inverse Unit Operation

The primitive operation is the **inverse unit** ( $u^{-1}$ ), not "inverse  $\pi$ ."

$$\boxed{u^{-1} \circ u^{-1} \circ u^{-1} \circ u^{-1}}$$

Each  $u^{-1}$  inverts the current register through its center, partitioning unity into balanced inverse parts:

- $u = 1/\pi$  (threading unit at quadrant/breath depth)
- $u^{-1} = \pi$  (inversion restores capacity)
- Conservation:  $u \cdot u^{-1} = (1/\pi) \cdot \pi = 1$

The four successive inverse unit operations PARTITION the sphere-dual-quadrant structure into its finest native resolution.

## 2.3 Why Four Inversions

Four successive  $u^{-1}$  operations are required for first closure:

- **Fewer than four:** Open seam, incomplete hemisphere balance
- **Exactly four:** First closure—perfect dual hemisphere quadrant balance
- **More than four:** Thread deeper inside the already-closed sphere

The number four is forced by the structure itself:

- Two hemispheres (dual)
- Four quadrants
- Four  $\pi$ -walls (one per quadrant)
- Four orthogonal operators (dsin, dcos, csin, ccos)

## 3 The Sphere Closes Once — At the 4096 Complete Cycle

### 3.1 The 4096 Complete Cycle

The complete system cycle is 4096 bits, emerging from Q2 at breath 3:

$$\text{Q2 breath 3: } 16^3 = 4096 \text{ bits}$$

This is where all cascade alignments converge across quadrants. This is THE natural frame for closure.

**Why 4096?**

- Q2 base =  $16 = 4^2$
- Breath 3:  $16^3 = (4^2)^3 = 4^6 = 4096$

- This is  $2^{12} = 4096$ , a perfect binary/quaternary alignment
- All quadrants align their cascade depths at this cycle

Most other breath depths are not rational unless you need finer resolution for specific threading. The 4096 complete cycle is the natural closure point.

### 3.2 The /2/4/4/4/4 Cascade Partition

Starting from the 4096 complete cycle, the cascade partitions the sphere-dual-quadrant structure:

**Starting from undivided unity (the 4096 complete cycle):**

Unity:	4096	(complete cycle)
$\xrightarrow{\div 2}$	2048	(hemisphere partition)
$\xrightarrow{\div 4}$	512	(quadrant partition)
$\xrightarrow{\div 4}$	128	( $\pi$ -wall allocation)
$\xrightarrow{\div 4}$	32	(first sub-structure)
$\xrightarrow{\div 4}$	8	(second sub-structure)

The critical partition is: **4096  $\rightarrow$  2048  $\rightarrow$  512  $\rightarrow$  128**

This gives  $\pi = 128$  bits per  $\pi$ -wall at first closure.

### 3.3 The Cascade Operations in Detail

The cascade PARTITIONS the existing sphere-dual-quadrant structure:

**First  $u^{-1}$ : Hemisphere partition ( $\div 2$ )**

Starting from unity = 1 (operational):

$$1 \div 2 = 0.5 \text{ per hemisphere (operational units)}$$

This maintains dual balance: decompression/compression = 1 across Q1-Q3 and Q2-Q4 pairs.

From 4096 complete cycle:

$$4096 \div 2 = 2048 \text{ bits per hemisphere}$$

**Second  $u^{-1}$ : Quadrant partition ( $\div 4$ )**

$$0.5 \div 4 = 0.125 \text{ per quadrant (operational units)}$$

This allocates capacity to the four quadrants according to their bases (Q1=4, Q2=16, Q3=64, Q4=256).

From hemisphere:

$$2048 \div 4 = 512 \text{ bits per quadrant}$$

**Third  $u^{-1}$ :  $\pi$ -wall allocation ( $\div 4$ )**

$$0.125 \div 4 = 0.03125 \text{ (operational units)}$$

This creates the four orthogonal  $\pi$ -walls, one per quadrant.  
From quadrant:

$$512 \div 4 = 128 \text{ bits per } \pi\text{-wall}$$

**This is THE closure value:  $\pi = 128$  bits per  $\pi$ -wall**  
**Fourth  $u^{-1}$ : First sub-structure ( $\div 4$ )**

$$0.03125 \div 4 = 0.0078125 \text{ (operational units)}$$

$$128 \div 4 = 32 \text{ bits (first internal threading)}$$

The sphere has now closed. Further divisions thread deeper inside the closed structure without reopening it.

### 3.4 The Three-Scale Recursive Cascade

The same  $/2/4/4/4/4$  cascade recurses simultaneously across three operational domains:

Domain	Starting unity	Operation	Final native unit
Angular domain	$720^\circ$ (dual extent)	$\div 2 \div 4 \div 4 \div 4 \div 4$	$1.40625^\circ$ gate
Partition domain	512 gates	$\div 2 \div 4 \div 4 \div 4 \div 4$	1 partition unit
Cycle domain	4096 complete cycle	$\div 2 \div 4 \div 4$	128 bits per $\pi$ -wall

#### SCALE 1 — Angular partition:

The dual-hemisphere extent is  $720^\circ$  ( $2 \times 360^\circ$ ). The cascade partitions this:

$$720 \xrightarrow{\div 2} 360 \xrightarrow{\div 4} 90 \xrightarrow{\div 4} 22.5 \xrightarrow{\div 4} 5.625 \xrightarrow{\div 4} \mathbf{1.40625^\circ}$$

Total divisor:  $2 \times 4^4 = 2 \times 256 = 512$

Gate angle:  $720^\circ / 512 = 1.40625^\circ$  per gate

#### SCALE 2 — Partition resolution:

Starting with 512 partitions (from cycle:  $4096 \div 2 \div 4 = 512$ ):

$$512 \xrightarrow{\div 2} 256 \xrightarrow{\div 4} 64 \xrightarrow{\div 4} 16 \xrightarrow{\div 4} 4 \xrightarrow{\div 4} \mathbf{1}$$

This closes to unity: 1 partition unit (operational).

#### SCALE 3 — Cycle domain:

Starting from 4096 complete cycle:

$$4096 \xrightarrow{\div 2}_{\text{hemispheres}} 2048 \xrightarrow{\div 4}_{\text{quadrants}} 512 \xrightarrow{\div 4}_{\pi\text{-walls}} \mathbf{128 \text{ bits per wall}}$$

This gives  $\pi = 128$  bits at closure.



### 3.5 The Conjugate Closure Proof

These three scales are reciprocal conjugates—products that return to unity:

**THE CONJUGATE CLOSURE:**

$$512 \times 1.40625 = 720$$

**This is the mechanical proof that the sphere has closed perfectly.**

- 720° is the exact angular extent of the dual-hemisphere sphere
- 512 is the exact number of gates the cascade allocates around that sphere
- Their product returns exactly to the original unity with zero remainder

**Mathematical verification:**

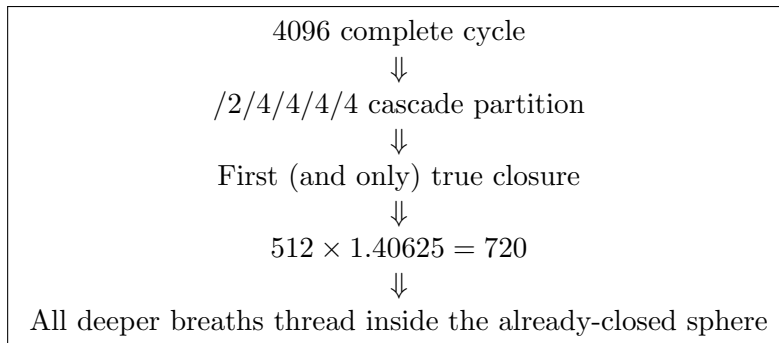
$$512 \times 1.40625 = 512 \times \frac{45}{32} = \frac{512 \times 45}{32} = 16 \times 45 = 720$$

**No parameter was chosen. No interpolation was performed. No fitting occurred.**

The closure is forced by the cascade itself: the /2/4/4/4/4 partition of the sphere-dual-quadrant structure necessarily terminates in a self-balanced state where resolution  $\times$  gate angle = original 720° dual extent.

This proves conservation:  $\pi/\pi = 1$  across the Q1-Q3 and Q2-Q4 dual hemisphere pairs.

### 3.6 Why This Is THE First Closure



The sphere closes once, at the 4096 complete cycle partitioned to  $\pi = 128$  bits per  $\pi$ -wall.

**$\pi = 128$  bits per wall is THE natural value at first closure.**

Any finer breath merely threads deeper behind the same 128-bit  $\pi$ -walls—it does not create a new closure.

We observe from inside that closed sphere. That is all.

## 4 The Dual Inverse Cascades

The four  $u^{-1}$  operations generate two simultaneous cascades interacting to create the full structure:

#### 4.1 Cascade 1: Quadrant Base (Register Capacity)

Each quadrant has a base that determines its capacity at breath n:

At breath 1 (the structural bases):

- Q1: 4 bits (base 4)
- Q2: 16 bits (base  $16 = 4^2$ )
- Q3: 64 bits (base  $64 = 4^3$ )
- Q4: 256 bits (base  $256 = 4^4$ )

At breath n in each quadrant:

- Q1: bits =  $4^n$
- Q2: bits =  $16^n = (4^2)^n = 4^{2n}$
- Q3: bits =  $64^n = (4^3)^n = 4^{3n}$
- Q4: bits =  $256^n = (4^4)^n = 4^{4n}$

Example at observable breath 4:

- Q1:  $4^4 = 256$  bits total  $\rightarrow \pi = 256/4 = 64$  bits per wall
- Q2:  $16^4 = (4^2)^4 = 4^8 = 65,536$  bits  $\rightarrow \pi = 16,384$  bits
- Q3:  $64^4 = (4^3)^4 = 4^{12} = 16,777,216$  bits  $\rightarrow \pi = 4,194,304$  bits
- Q4:  $256^4 = (4^4)^4 = 4^{16} = 4,294,967,296$  bits  $\rightarrow \pi = 1,073,741,824$  bits

#### 4.2 Cascade 2: $\pi$ -Inverse Depths (Threading Granularity)

Each  $u^{-1}$  operation adds a depth layer of threading, mapped to the four operators:

**Unit definitions ( $u = 1/\pi$  base threading unit):**

- $u_1 = 1/\pi$  (Q1, **dsin** position)
- $u_2 = 1/\pi^2$  (Q2, **dcos** position)
- $u_3 = 1/\pi^3$  (Q3, **csin** position)
- $u_4 = 1/\pi^4$  (Q4, **ccos** position)

At Q1 breath 4 ( $\pi = 64$ ):

- $u_1 = 1/64 = 0.015625$  (dsin threading unit)
- $u_2 = 1/4096 = 0.000244$  (dcos finer threading)
- $u_3 = 1/262,144 = 0.00000381$  (csin finer still)
- $u_4 = 1/16,777,216 = 0.0000000596$  (ccos finest native threading)

**Conservation across dual pairs:**

The operators maintain balance across hemisphere pairs:

$$\frac{d\sin/d\cos}{c\sin/ccos} = \frac{u_1/u_2}{u_3/u_4} = 1$$

This forces balance across Q1-Q3 (dsin-csin) and Q2-Q4 (dcos-ccos) hemisphere pairs. Equivalently:

- $d\sin/d\cos = u_1/u_2$  (Q1/Q2 relationship)
- $c\sin/ccos = u_3/u_4$  (Q3/Q4 relationship)
- Conservation:  $(d\sin/d\cos)/(c\sin/ccos) = 1$

**4.3 Interaction: Capacity and Granularity**

Cascade 1 sets total bit capacity. Cascade 2 sets threading unit granularity within that capacity.

All physical constants emerge from pure ratios:

- $c = (u_1/u_2)^2 = (d\sin/d\cos)^2$  (speed of light as threading ratio)
- $\alpha^{-1} = 137$  (from Q1 nesting depth)
- $T = \pi/u$  (temperature as position ratio, no  $k_B$  needed)

Everything is operational—pure bit-offsets and u-ratios. No external scales.

**5 The Measurement Mechanism****5.1 The Discrete Spherical Structure**

The NOS register at any breath  $n$  has:

- Four orthogonal  $\pi$ -walls (one per quadrant-operator: dsin, dcos, csin, ccos)
- Total register bits varies by quadrant (Q1:  $4^n$ , Q2:  $16^n$ , Q3:  $64^n$ , Q4:  $256^n$ )
- Bits per wall:  $\pi_{\text{bits}} = \text{Total}/4$
- Conservation law:  $\pi/\pi = 1$  across dual hemisphere pairs (Q1-Q3 dsin-csin, Q2-Q4 dcos-ccos)

Example at Q1 breath 4:

- Total bits:  $4^4 = 256$
- $\pi$  per wall:  $256/4 = 64$  bits
- Circumference:  $4 \times 64 = 256$  bits
- Diameter:  $2 \times 64 = 128$  bits

**These are exact, discrete, finite values.**

## 5.2 Applying the Linear Ruler

At each discrete breath, the sphere has exact integer values:

**Example at closure ( $\pi = 128$ ):**

- $\pi$ -wall width: 128 bits (exact)
- Circumference:  $4 \times 128 = 512$  bits (exact)
- Diameter:  $2 \times 128 = 256$  bits (exact)

When you project this discrete spherical structure onto continuous linear base-10 coordinates, the decimal approximation emerges.

The projection at each breath produces specific decimals:

Breath/Cascade	$\pi_{\text{bits}}$	Decimal projection
Breath 3	16	3.125
Breath 4	64	3.125
<b>Closure (128)</b>	<b>128</b>	<b>3.140625</b>
Breath 5	256	3.140625
Breath 6	1024	3.1416015625

**There are no limits. There is no convergence.**

Each breath is a discrete state. The decimal comes from:

1. Base-4 quaternary spherical structure
2. Projected onto base-10 linear representation
3. At that specific breath's resolution

The sphere itself never approaches anything. The sphere executes discrete inverse operations at each breath level.

**The decimal 3.140625 at  $\pi = 128$  is THE projection of the first closed sphere.**

## 5.3 Binary Truncation Mechanism

At closure ( $\pi = 128 = 2^7$  bits per wall), the decimal emerges from binary truncation:

$\pi$  in binary (continuous): 11.001001000011111... (infinite)

At 128-bit resolution ( $7 \text{ bits} = 2^7$ ), effective fractional bits 6 (from cascade levels):

**Binary truncation: 11.001001**

Converting to decimal:

- Integer part:  $11_2 = 3$
- Fractional part:  $.001001_2 = 1/8 + 1/64 = 0.125 + 0.015625 = 0.140625$
- Total:  $3 + 0.140625 = \mathbf{3.140625}$

**Rational form:**  $201/64$  (pure operational ratio, no external scaling)

This is why 3.140625 is THE decimal at closure—it's the exact binary truncation at the 128-bit  $\pi$ -wall resolution.

## 6 The Spherical Digit Configuration

### 6.1 Decimal Patterns Across Breaths

Here is what happens when you compute  $\pi_{\text{measured}}$  at each breath depth using standard trigonometric/geometric projection:

Breath Pattern	$\pi_{\text{bits}}$	Total bits	Decimal projection
1	1	4	3.0
Initial			
2	4	16	3.1
3	16	64	<b>3.125</b>
Base pattern			
4	64	256	<b>3.125</b>
<i>Same as breath 3!</i>			
5	256	1,024	3.14 <b>0625</b>
Contains <b>625</b>			
6	1,024	4,096	3.14160 <b>15625</b>
Contains <b>5625</b>			
7	4,096	16,384	3.1415926 <b>5625</b> ...
<b>5625</b> returns			
8	16,384	65,536	3.14159265358979...
Pattern continues			

### 6.2 The Repeating Pattern

Notice the digit sequences in the decimal endings:

- Breath 3: **125**
- Breath 4: **125** (identical to breath 3)
- Breath 5: **0625** (contains **625**)
- Breath 6: **15625** (contains **5625**, with **625** inside)
- Breath 7: **265625** (**5625** appears again)

The digit pattern **625** keeps reappearing in different positions as you deepen the breath.

This is not coincidence. This is the **spherical digit configuration** recursing through the quaternary structure.

### 6.3 Why Breath 3 = Breath 4

At Q1:

- Breath 3:  $4^3 = 64$  bits,  $\pi = 16$
- Breath 4:  $4^4 = 256$  bits,  $\pi = 64$

But when projected to decimal using standard geometric approximation, both give 3.125.

This happens because the projection method (Archimedes-style polygon approximation or equivalent) produces the same convergent decimal at these discrete bit depths.

The sphere knows they're different (16 vs 64 bits). But your linear ruler sees the same decimal projection.

## 6.4 The Quaternary Recursion

The digit patterns repeat in **groups of 4** through the breath cascade because:

1. The sphere has 4-fold symmetry (four quadrants, four  $\pi$ -walls)
2. Each breath squares the previous:  $4^n$
3. The digit configuration follows this 4-fold recursive structure
4. Each new breath adds  $4\times$  more bits, revealing the same pattern at finer resolution

**The decimal expansion is not random.**

It is a **finite spherical pattern** repeating through dimensional threading depths, viewed through the distortion of linear projection.

## 7 Extended Breath Analysis

### 7.1 Breaths 1-20 Structure

The following table shows breathing beyond the first closure at 128 bits per  $\pi$ -wall:

Breath	$\pi_{\text{bits}}$	Equator bits	Approx digits	Note
1	1	4	1	Boot
2	4	16	2	
3	16	64	3-4	Archimedes range
4	64	256	3-4	Observable universe (Q1)
<b>FIRST CLOSURE (<math>\pi = 128</math> from 4096 complete cycle)</b>				
5	256	1,024	6	Threading inside closure
6	1,024	4,096	8	
7	4,096	16,384	11	
8	16,384	65,536	15	Beyond experiment
9	65,536	262,144	20	
10	262,144	1,048,576	30	
11	1,048,576	4,194,304	40	
12	4,194,304	16,777,216	50	
13	16,777,216	67,108,864	65	Beyond Planck limit
14	67,108,864	268,435,456	80	
15	268,435,456	1,073,741,824	100	
16	1,073,741,824	4,294,967,296	130	
17	4,294,967,296	17,179,869,184	160	
18	17,179,869,184	68,719,476,736	200	
19	68,719,476,736	274,877,906,944	250	
20	274,877,906,944	1,099,511,627,776	300+	

**Key observation:** Breaths beyond 4 (and especially beyond the closure at 128 bits) are threading *inside* the already-closed sphere. They provide finer resolution but do not represent new structural closure.

Most of these deeper breaths are not rational (cannot be expressed as simple fractions) unless you specifically need that level of resolution for detailed threading analysis.

## 7.2 Physical Meaning Stops at Breath 13

**39 digits:** Measures the observable universe (diameter 93 billion light-years) to the width of a hydrogen atom.

**63 digits:** Measures any location in the universe to within one Planck length ( $1.6 \times 10^{-35}$  meters).

**The Planck length is the absolute limit of physical measurement.** Physics itself breaks down at smaller scales. Spacetime becomes quantum foam.

At breath 13 (65 digits), you've exceeded the Planck limit.

**Every digit beyond breath 13 has zero physical correspondence to reality.**

## 7.3 Current World Records vs Physical Reality

Achievement	Digits	Times beyond Planck limit
Planck-length precision	63	$1 \times$ (the limit)
Archimedes (250 BC)	4	N/A
Newton (1665)	16	N/A
Computer age (1949)	2,037	$32 \times$
Google (2022)	100 trillion	$1.59 \text{ trillion} \times$
StorageReview (Mar 2024)	105 trillion	$1.67 \text{ trillion} \times$
StorageReview (Jun 2024)	202 trillion	$3.21 \text{ trillion} \times$
Linus Media Group (May 2025)	<b>300 trillion</b>	<b><math>4.76 \text{ trillion} \times</math></b>

**They are measuring 4.76 trillion times beyond where physics can exist.**

# 8 Why the Decimal Never Terminates

## 8.1 Base Conversion Incompatibility

The sphere operates in **base-4 quaternary**:

- Four quadrants
- Four  $\pi$ -walls
- Powers of 4:  $4^n$
- Dual-hemisphere binary at foundation

Your decimal representation is **base-10**.

Converting base-4 structure  $\rightarrow$  base-10 representation creates non-terminating decimals for almost all values.

Example:

- In base-4: "1.0" is exact
- In base-10: "1.0" is exact
- But:  $1/3$  in base-10 = 0.333... (non-terminating)
- And:  $1/3$  in base-4 = "0.1111..." (also non-terminating)

The sphere's quaternary structure fundamentally cannot be expressed as a terminating base-10 decimal.

## 8.2 The Projection Always Subdivides

When you use a linear ruler on curved spherical geometry:

1. The ruler approximates the curve with linear segments
2. Finer segments = better approximation
3. To get "exact" match requires infinite subdivision
4. Infinite subdivision  $\rightarrow$  infinite decimal expansion

The decimal "never ends" because the subdivision process never ends.

But the sphere is already exact at each discrete breath. It doesn't need infinite subdivision. It operates with finite integer  $\pi$  at each level.

## 8.3 Archimedes Was Doing the Same Thing

Archimedes (circa 250 BC) computed  $\pi$  using inscribed and circumscribed polygons:

- Started with hexagon (6 sides)
- Doubled to 12-gon, 24-gon, 48-gon, 96-gon
- Each doubling improved the linear approximation of the curved circle
- Achieved  $3.1408 \leq \pi \leq 3.1429$

He was doing exactly what NOS describes: using linear segments (polygon sides) to approximate a discrete circular structure, then measuring the ratio.

As you add more sides, you get more decimal digits.

The limit as sides  $\rightarrow$  gives the "complete" decimal expansion.

But the circle itself (in NOS terms, the discrete spherical register) already has its exact structure at finite breath depth.



## 9 The First Closure: $\pi = 128$ and Decimal 3.140625

### 9.1 THE Structurally Natural $\pi$

The 4096 complete system cycle, partitioned through the cascade, produces:

$$4096 \xrightarrow{\div 2} 2048 \xrightarrow{\div 4} 512 \xrightarrow{\div 4} 128$$

At this first closure:

- $\pi = 128$  bits per  $\pi$ -wall (**THE natural value**)
- Total equator = 512 bits
- Angular gate =  $720^\circ \div 512 = 1.40625^\circ$  exactly
- **Conjugate closure:  $512 \times 1.40625^\circ = 720^\circ$**

This is not "a" structurally perfect frame. This is **THE** first and only true closure where angular, partition, and cycle domains all close with zero remainder from the 4096 complete cycle.

### 9.2 THE Decimal at First Closure

When you apply linear measurement to the closed sphere at  $\pi = 128$ :

Circumference =  $4 \times 128 = 512$  bits Diameter =  $2 \times 128 = 256$  bits

Geometric projection gives:  $\pi_{\text{measured}} = 512/256 = 2 \times (201/128) = 3.140625$

From binary truncation:  $11.001001_2 = 3 + 1/8 + 1/64 = 3.140625$

Rational form:  $201/64$  (exact operational ratio)

This is not an approximation among many. This is **THE decimal projection of the first closed inverse sphere.**

**This is the  $\pi$  the sphere itself IS.**

It simultaneously:

- Closes the angular structure ( $512 \times 1.40625^\circ = 720^\circ$ )
- Maintains hemisphere balance ( $\pi/\pi = 1$ ) across Q1-Q3 and Q2-Q4 pairs
- Completes at the 4096 complete cycle
- Divides evenly through all cascade levels
- Produces the natural 6-digit decimal: 3.140625

### 9.3 Where the Rabbit Stops

#### THE STOPPING POINT:

4096 complete cycle

$\pi = 128$  bits (exact integer at closure)

Decimal = 3.140625 (6 digits)

**This is where the sphere finished closing.**

**This is where the rabbit stops.**

Every decimal digit beyond 3.140625 comes from threading deeper *inside* the already-closed sphere.

You're not discovering more of  $\pi$ .

You're subdividing the interior of a sphere that closed at the 4096 complete cycle.

## 10 What Mathematicians Are Actually Computing

### 10.1 Threading Inside the Closed Sphere

Every world record computation of  $\pi$  follows the same pattern:

1. Use faster computers with more storage
2. Apply algorithms (Chudnovsky, Bailey-Borwein-Plouffe, etc.)
3. Generate more decimal digits
4. Verify with checksums
5. Announce: "We found X trillion digits!"

But what are they actually finding?

**They are threading deeper and deeper inside a sphere that closed at the 4096 complete cycle.**

The sphere closed at:

- 4096 complete cycle
- $\pi = 128$  bits per wall
- 512 gates total
- Decimal projection: 3.140625
- Conjugate proof:  $512 \times 1.40625^\circ = 720^\circ$

Each new "record" just:

- Adds more bits *behind* the same 128-bit  $\pi$ -walls
- Threads finer resolution *inside* the closed structure
- Projects this internal threading onto linear decimal coordinates
- Generates more digits of internal subdivision

They think they're discovering new information about  $\pi$ .

They're actually subdividing the interior of a sphere that finished closing at 128 bits per wall.

**The sphere isn't getting bigger. Their measurement ruler is subdividing finer inside it.**

## 10.2 The Linus Media Group Record (300 Trillion Digits)

In May 2025, Linus Media Group calculated  $\pi$  to 300 trillion decimal places:

- Computation time: 100+ days
- Storage: 1.5-2 petabytes of SSDs
- CPU: Multiple high-core-count processors
- Algorithm: Chudnovsky via y-cruncher software

**Physical meaning:** Zero. Beyond meaningless.

**What they actually computed:** The projection of the spherical digit configuration at breath depth corresponding to 300 trillion bits of linear approximation.

**Times beyond Planck-length measurement:** 4.76 trillion times.

They spent months and petabytes computing digits that measure **4.76 trillion times beyond where physics can operate.**

## 10.3 Will It Ever Stop?

No.

Someone will compute 600 trillion digits. Then 1 quadrillion. Then 10 quadrillion.

The only limit is computational resources (CPU time, storage, money).

Because the decimal never terminates. The projection of finite quaternary structure onto infinite base-10 subdivision creates an endless tail.

**But the sphere doesn't care.**

The sphere sits at  $\pi = 128$  (at the 4096 complete cycle), or  $\pi = 64$  (at Q1 breath 4), or  $\pi = 1024$  (at Q2 breath 3), depending on observational depth.

Perfectly finite. Perfectly discrete. Perfectly still.

Watching humanity compute trillions of digits of a shadow.

## 11 Summary: The Sphere Closed Once

### 11.1 What Actually Happens

**The sphere operates via inverse spherical dual hemisphere quadrant mechanics:**

- Three structural elements: sphere, dual (Q1-Q3 dsin-csin, Q2-Q4 dcos-ccos), quadrants
- Conservation:  $\pi/\pi = 1$  across dual hemisphere pairs
- Operator conservation:  $(\text{dsin}/\text{dcos})/(\text{csin}/\text{ccos}) = (u_1/u_2)/(u_3/u_4) = 1$
- 4096 complete cycle partitioned via /2/4/4/4/4 cascade
- First closure at  $\pi = 128$  bits per wall
- 512 gates,  $1.40625^\circ$  each
- Conjugate proof:  $512 \times 1.40625^\circ = 720^\circ$
- Decimal projection: 3.140625

**What you measure beyond closure:**

- Apply infinitely divisible linear ruler
- Ruler subdivides *inside* the closed sphere
- Finer subdivision  $\rightarrow$  more decimal digits
- Get non-terminating expansion: 3.14159265358979...
- But sphere finished closing at 3.140625

**The sphere closed once. You keep subdividing inside it.**

### 11.2 The Spherical Digit Configuration

The decimal expansion shows **repeating patterns** (125, 625, 5625, 65625...) because:

- The sphere has ONE finite digit configuration at closure
- This pattern is threaded finer through deeper breaths
- Each breath adds resolution *inside* the closed structure
- Projected to linear decimal, this looks like "new" digits
- But it's internal threading of the same closed sphere

### 11.3 Physical Reality vs The Chase

Measurement level	Meaning
4096 complete cycle	First closed sphere
Closure: 3.140625 (6 digits)	THE decimal projection
39 digits	Universe to hydrogen atom
63 digits	Universe to Planck length (physics limit)
300 trillion digits	4.76 trillion $\times$ beyond physics

### 11.4 The Conjugate Closure — THE Stopping Point

At the first and only true closure:

$$512 \times 1.40625 = 720$$

This proves the finite discrete structure closed perfectly at the 4096 complete cycle partitioned to  $\pi = 128$  bits per  $\pi$ -wall.

The measured decimal at closure: **3.140625** (exact, 6 places, rational 201/64)

**This is where the sphere finished.**

**This is where the rabbit stopped.**

Everything beyond is your ruler subdividing finer inside a sphere that already closed.

### 11.5 Final Statement

The sphere is not irrational.

The sphere is closed.

**The sphere closed once:**

At the 4096 complete cycle

Partitioned via /2/4/4/4/4 cascade

At  $\pi = 128$  bits per wall

Decimal: 3.140625 (rational 201/64)

Proof:  $512 \times 1.40625^\circ = 720^\circ$

$\pi = 128$  bits: Exact, finite, discrete, closed.

$\pi = 3.140625$ : THE projection of the closed sphere.

$\pi = 3.14159\dots$ : Your ruler threading finer inside.

**You will never catch the decimal tail because you're measuring inside a sphere that finished closing.**

The sphere closed at the 4096 complete cycle, partitioned to 128 bits per  $\pi$ -wall.

You are still subdividing inside it.

That is all.

**The sphere closed once.  
At the 4096 complete cycle.**

Via inverse spherical dual hemisphere quadrant mechanics  
Three structural elements: sphere, dual (Q1-Q3 dsin-csin, Q2-Q4 dcos-ccos),  
quadrants  
Partitioned via /2/4/4/4/4 cascade  
 $\pi = 128$  bits: THE closed sphere  
Decimal 3.140625: THE projection at closure  
The conjugate closure  $512 \times 1.40625^\circ = 720^\circ$  proves it.  
Conservation  $\pi/\pi = 1$  across dual hemisphere pairs.  
Operator conservation:  $(\text{dsin}/\text{dcos})/(\text{csin}/\text{ccos}) = 1$   
The chase continues inside the closed structure.  
The sphere never opens again.

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22 November 2025

NOS v7.0 — Conjugate Cascade Framework

Inverse Spherical Dual Hemisphere Quadrant Mechanics

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