```
SECANT METHOD
import javax.swing.*;
import javax.swing.table.DefaultTableModel;
import java.awt.*;
import java.awt.event.*;
import java.util.*;
import net.objecthunter.exp4j.*;
import net.objecthunter.exp4j.tokenizer.UnknownFunctionOrVariableException;
import org.jfree.chart.*;
import org.jfree.chart.annotations.XYTextAnnotation;
import org.jfree.chart.plot.*;
import org.jfree.chart.renderer.xy.XYLineAndShapeRenderer;
import org.jfree.data.xy.*;
public class SecantMethodSolver extends JFrame {
  private JTextField functionField, x0Field, x1Field, tolField, maxIterField;
  private JTable table;
  private DefaultTableModel tableModel;
  private ArrayList<Double> roots = new ArrayList<>();
  public SecantMethodSolver() {
    setTitle("Secant Method Solver");
    setDefaultCloseOperation(JFrame.EXIT_ON_CLOSE);
    setSize(1300, 700);
    setLocationRelativeTo(null);
    setLayout(new BorderLayout(10, 10));
    // Instructions Panel
```

JTextArea instructions = new JTextArea(

```
"層 Secant Method Solver\n" +
  "Instructions:\n" +
  "- Enter f(x) using standard math syntax (e.g., x^3 - x - 2).\n" +
  "- Supported functions: sin, cos, tan, exp, log, abs, sqrt, etc.\n" +
  "- Use ^ for exponents (e.g., x^3 means x cubed).\n" +
  "- Provide two initial guesses x0 and x1, a tolerance, and max iterations.\n" +
  "- Click 'Compute' to find the roots.\n"
);
instructions.setEditable(false);
instructions.setBackground(new Color(240, 240, 240));
instructions.setBorder(BorderFactory.createTitledBorder("Instructions"));
add(instructions, BorderLayout.NORTH);
// Input Panel
JPanel inputPanel = new JPanel(new GridLayout(6, 2, 8, 8));
inputPanel.setBorder(BorderFactory.createTitledBorder("Input Parameters"));
functionField = createField(inputPanel, "Function f(x):", "x^3 - x - 2");
x0Field = createField(inputPanel, "Initial Guess x0:", "1.0");
x1Field = createField(inputPanel, "Initial Guess x1:", "2.0");
tolField = createField(inputPanel, "Tolerance:", "1e-5");
maxIterField = createField(inputPanel, "Max Iterations:", "20");
JButton computeButton = new JButton("Compute");
JButton helpButton = new JButton("Help");
inputPanel.add(computeButton);
inputPanel.add(helpButton);
add(inputPanel, BorderLayout.WEST);
```

```
// Iteration Table
  String[] columns = {"Iteration", "x", "f(x)", "Error"};
  tableModel = new DefaultTableModel(columns, 0);
  table = new JTable(tableModel);
  JScrollPane tableScroll = new JScrollPane(table);
  tableScroll.setBorder(BorderFactory.createTitledBorder("Iteration Table"));
  add(tableScroll, BorderLayout.CENTER);
  // Actions
  computeButton.addActionListener(e -> runSecantMethod());
  helpButton.addActionListener(e -> showHelpDialog());
  setVisible(true);
}
private JTextField createField(JPanel panel, String label, String defaultText) {
  JLabel lbl = new JLabel(label);
  JTextField field = new JTextField(defaultText);
  panel.add(lbl);
  panel.add(field);
  return field;
}
private void runSecantMethod() {
  tableModel.setRowCount(0);
  roots.clear();
  try {
    String fxExpr = functionField.getText().trim();
    // Warn user if they accidentally use Math.pow
```

```
if (fxExpr.contains("Math.pow")) {
        JOptionPane.showMessageDialog(this,
             " \(\lambda\) Use ^ for exponents, not Math.pow!\nExample: x^3 - x - 2",
             "Syntax Warning", JOptionPane.WARNING_MESSAGE);
        return;
      }
      // Replace ^ with ** for exp4j (it supports ^ for exponents)
      Expression fx = new ExpressionBuilder(fxExpr)
                 .variable("x")
                 .build();
      double x0 = Double.parseDouble(x0Field.getText().trim());
      double x1 = Double.parseDouble(x1Field.getText().trim());
      double tol = Double.parseDouble(tolField.getText().trim());
      int maxIter = Integer.parseInt(maxIterField.getText().trim());
      double error = Double.MAX VALUE;
      int iter = 1;
      while (iter <= maxIter && error > tol) {
        double fx0 = fx.setVariable("x", x0).evaluate();
        double fx1 = fx.setVariable("x", x1).evaluate();
        if (Math.abs(fx1 - fx0) < 1e-12) {
           JOptionPane.showMessageDialog(this, "Error: Division by zero in Secant formula.", "Error",
JOptionPane.ERROR_MESSAGE);
           return;
        }
```

```
double x2 = x1 - fx1 * (x1 - x0) / (fx1 - fx0);
        double fx2 = fx.setVariable("x", x2).evaluate();
        error = Math.abs(x2 - x1);
        tableModel.addRow(new Object[] {
          iter, String.format("%.8f", x2), String.format("%.8f", fx2), String.format("%.8f", error)
        });
        x0 = x1;
        x1 = x2;
        iter++;
      }
      roots.add(x1);
      JOptionPane.showMessageDialog(this, String.format("[OK] Root found at x \approx \%.8f", x1), "Result",
JOptionPane.INFORMATION_MESSAGE);
      showPlot(fx, x1);
    } catch (UnknownFunctionOrVariableException ufve) {
      JOptionPane.showMessageDialog(this, "Error: Unknown function or variable in your
expression.\n" +
          "Use functions like sin(x), cos(x), exp(x), log(x), etc.", "Error", JOptionPane.ERROR_MESSAGE);
    } catch (Exception ex) {
      JOptionPane.showMessageDialog(this, "Error: " + ex.getMessage(), "Error",
JOptionPane.ERROR_MESSAGE);
    }
  }
```

```
private void showPlot(Expression fx, double xApprox) {
  XYSeries seriesF = new XYSeries("f(x)");
  double xMin = xApprox - 5, xMax = xApprox + 5;
  for (double x = xMin; x \le xMax; x += 0.01) {
    seriesF.add(x, fx.setVariable("x", x).evaluate());
  }
  XYSeriesCollection dataset = new XYSeriesCollection(seriesF);
  JFreeChart chart = ChartFactory.createXYLineChart(
    "Secant Method: Root Finding",
    "x",
    "f(x)",
    dataset,
    PlotOrientation.VERTICAL,
    true,
    true,
    false
  );
  XYPlot plot = chart.getXYPlot();
  plot.setDomainGridlinesVisible(true);
  plot.setRangeGridlinesVisible(true);
  XYLineAndShapeRenderer renderer = new XYLineAndShapeRenderer(true, false);
  renderer.setSeriesPaint(0, Color.BLUE);
  plot.setRenderer(renderer);
  for (double root : roots) {
```

```
XYSeries rootPoint = new XYSeries("Root");
    rootPoint.add(root, 0);
    XYSeriesCollection rootDataset = new XYSeriesCollection(rootPoint);
    XYLineAndShapeRenderer rootRenderer = new XYLineAndShapeRenderer(false, true);
    rootRenderer.setSeriesPaint(0, Color.RED);
    rootRenderer.setSeriesShape(0, new java.awt.geom.Ellipse2D.Double(-5, -5, 10, 10));
    int datasetIndex = plot.getDatasetCount();
    plot.setDataset(datasetIndex, rootDataset);
    plot.setRenderer(datasetIndex, rootRenderer);
    XYTextAnnotation annotation = new XYTextAnnotation(String.format("%.5f", root), root, 0.05);
    annotation.setFont(new Font("SansSerif", Font.BOLD, 12));
    annotation.setPaint(Color.RED);
    plot.addAnnotation(annotation);
 }
  SwingUtilities.invokeLater(() -> {
    JFrame plotFrame = new JFrame("Secant Method Plot");
    plotFrame.setSize(900, 600);
    plotFrame.add(new ChartPanel(chart));
    plotFrame.setLocationRelativeTo(null);
    plotFrame.setVisible(true);
 });
private void showHelpDialog() {
  String message = """
```

}

}

}

}

```
- The Secant Method is an iterative technique for finding roots of nonlinear equations.
```

```
- Formula: x_{n+1} = x_n - f(x_n) * (x_n - x_{n-1}) / (f(x_n) - f(x_{n-1}))
```

- Provide two initial guesses (x0, x1), tolerance, and max iterations.

```
Function Syntax:
      - Use standard math functions: x^3 - x - 2
      - Supported functions: sin(x), cos(x), tan(x), exp(x), log(x), abs(x), sqrt(x), etc.
      - Use ^ for exponents (e.g., x^3 for x cubed).
      Function: x^3 - x - 2
      x0: 1.0
      x1: 2.0
      Tolerance: 1e-5
      Max Iterations: 20
    JOptionPane.showMessageDialog(this, message, "Secant Method Help",
JOptionPane.INFORMATION_MESSAGE);
  public static void main(String[] args) {
    SwingUtilities.invokeLater(SecantMethodSolver::new);
```

```
GRAPHICAL METHOD
import javax.swing.*;
import java.awt.*;
import java.awt.event.*;
import java.util.ArrayList;
import java.util.List;
import net.objecthunter.exp4j.Expression;
import net.objecthunter.exp4j.ExpressionBuilder;
import org.jfree.chart.*;
import org.jfree.chart.plot.XYPlot;
import org.jfree.chart.annotations.XYTextAnnotation;
import org.jfree.chart.renderer.xy.XYSplineRenderer;
import org.jfree.data.xy.*;
public class GraphicalMethodApp extends JFrame {
  private JTextField funcField, iterField;
  private JTable table;
  public GraphicalMethodApp() {
    setTitle("Graphical Method Root Finder");
    setSize(900, 700);
    setDefaultCloseOperation(EXIT ON CLOSE);
    setLocationRelativeTo(null);
    setLayout(new BorderLayout());
    // === Input Panel ===
    JPanel inputPanel = new JPanel(new GridLayout(3, 2, 10, 10));
    inputPanel.setBorder(BorderFactory.createTitledBorder("Enter Inputs"));
```

```
funcField = new JTextField("");
iterField = new JTextField("");
inputPanel.add(new JLabel("Enter function f(x):"));
inputPanel.add(funcField);
inputPanel.add(new JLabel("Max Iterations:"));
inputPanel.add(iterField);
JButton enterButton = new JButton("ENTER");
JButton aboutButton = new JButton("ABOUT");
inputPanel.add(enterButton);
inputPanel.add(aboutButton);
// === Table Panel ===
table = new JTable();
JScrollPane tableScroll = new JScrollPane(table);
tableScroll.setBorder(BorderFactory.createTitledBorder("Result Table"));
tableScroll.setPreferredSize(new Dimension(850, 300));
add(inputPanel, BorderLayout.NORTH);
add(tableScroll, BorderLayout.CENTER);
// === Actions ===
enterButton.addActionListener(e -> process());
aboutButton.addActionListener(e -> showAboutDialog());
setVisible(true);
```

}

```
private void process() {
    try {
      String input = funcField.getText().trim();
      input = input.replaceAll("@\\(x\\)", ""); // Remove @(x)
      input = input.replaceAll("\\.\\^", "\\^"); // Replace .^ with ^
      input = input.replaceAll("\\.\\*", "*"); // Replace .* with *
      input = input.replaceAll("\\./", "/"); // Replace ./ with /
      int maxIter = Integer.parseInt(iterField.getText().trim());
      if (maxIter <= 0) {
        JOptionPane.showMessageDialog(this, "Max iterations must be positive.", "Input Error",
JOptionPane.ERROR_MESSAGE);
         return;
      }
      double a = -10; // Fixed interval for simplicity
      double b = 10;
      double h = (b - a) / maxIter;
       Expression exp = new ExpressionBuilder(input).variable("x").build();
      List<Double> xVals = new ArrayList<>();
      List<Double> yVals = new ArrayList<>();
      List<Double> roots = new ArrayList<>();
      for (int i = 0; i <= maxIter; i++) {
        double x = a + i * h;
        double y = exp.setVariable("x", x).evaluate();
        xVals.add(x);
        yVals.add(y);
```

```
}
      double tol = 1e-5;
      for (int i = 1; i < yVals.size(); i++) {
         if (yVals.get(i - 1) * yVals.get(i) <= 0) {
           double root = refineRoot(exp, xVals.get(i - 1), xVals.get(i), tol);
           if (roots.stream().noneMatch(r -> Math.abs(r - root) < tol)) {</pre>
             roots.add(root);
           }
        }
      }
      // Populate table
      String[][] data = new String[xVals.size()][2];
      for (int i = 0; i < xVals.size(); i++) {
         data[i][0] = String.format("%.5f", xVals.get(i));
         data[i][1] = String.format("%.7f", yVals.get(i));
      }
      table.setModel(new javax.swing.table.DefaultTableModel(data, new String[]{"x", "f(x)"}));
      // Plot the function
       plotGraph(input, xVals, yVals, roots);
    } catch (NumberFormatException e) {
      JOptionPane.showMessageDialog(this, "Please enter a valid number for max iterations.", "Input
Error", JOptionPane.ERROR_MESSAGE);
    } catch (Exception ex) {
      JOptionPane.showMessageDialog(this, "Error: " + ex.getMessage(), "Input Error",
JOptionPane.ERROR_MESSAGE);
```

```
}
  }
  private double refineRoot(Expression exp, double x1, double x2, double tol) {
    double mid;
    while ((x2 - x1) > tol) {
      mid = (x1 + x2) / 2;
      double f1 = exp.setVariable("x", x1).evaluate();
      double fmid = exp.setVariable("x", mid).evaluate();
      if (f1 * fmid \le 0) x2 = mid;
      else x1 = mid;
    }
    return (x1 + x2) / 2;
  }
  private void plotGraph(String func, List<Double> xVals, List<Double> yVals, List<Double> roots) {
    XYSeries series = new XYSeries("f(x)");
    for (int i = 0; i < xVals.size(); i++) {
      series.add(xVals.get(i), yVals.get(i));
    }
    XYSeriesCollection dataset = new XYSeriesCollection(series);
    JFreeChart chart = ChartFactory.createXYLineChart("Graphical Method", "x", "f(x)", dataset);
    XYPlot plot = chart.getXYPlot();
    plot.setRenderer(new XYSplineRenderer());
    // Add X-axis marker at y=0
    plot.addRangeMarker(new org.jfree.chart.plot.ValueMarker(0.0, Color.BLACK, new
BasicStroke(1.5f)));
```

```
// Mark roots with red dots
XYSeries rootSeries = new XYSeries("Roots");
for (double root : roots) {
  rootSeries.add(root, 0.0);
}
dataset.addSeries(rootSeries);
XYSplineRenderer renderer = new XYSplineRenderer();
renderer.setSeriesPaint(0, Color.BLUE); // Function line
renderer.setSeriesPaint(1, Color.RED); // Root dots
renderer.setSeriesShapesVisible(1, true);
renderer.setSeriesLinesVisible(1, false);
renderer.setSeriesShape(1, new java.awt.geom.Ellipse2D.Double(-4, -4, 8, 8));
plot.setRenderer(renderer);
// Text annotations for roots
for (int i = 0; i < roots.size(); i++) {
  double root = roots.get(i);
  XYTextAnnotation ann = new XYTextAnnotation("Root " + (i + 1), root, 0);
  ann.setPaint(Color.RED);
  ann.setFont(new Font("Arial", Font.BOLD, 12));
  plot.addAnnotation(ann);
}
// Display graph
JFrame frame = new JFrame("Graphical Method");
frame.setDefaultCloseOperation(JFrame.DISPOSE_ON_CLOSE);
frame.setSize(850, 650);
```

```
frame.add(new ChartPanel(chart));
    frame.setVisible(true);
  }
  private void showAboutDialog() {
    String message = """
        === Graphical Method Root Finder ===
        Instructions:
        1. Enter the function using JavaScript-like syntax.
          Example: 2*x^2 - 5*x + 3
        2. Enter the maximum number of iterations.
          (More iterations give better graph resolution)
        3. The program scans the interval [-10, 10].
        4. The function is plotted, and roots (where sign changes) are marked in red.
        Note: Use element-wise operators:
            ^ for power, * for multiplication, / for division.
    JOptionPane.showMessageDialog(this, message, "About - Graphical Method",
JOptionPane.INFORMATION_MESSAGE);
 }
  public static void main(String[] args) {
    try {
      for (UIManager.LookAndFeelInfo info: UIManager.getInstalledLookAndFeels())
        if ("Nimbus".equals(info.getName())) UIManager.setLookAndFeel(info.getClassName());
    } catch (Exception ignored) {}
```

```
SwingUtilities.invokeLater(GraphicalMethodApp::new);
}
```

```
BISECTION METHOD
import javax.swing.*;
import javax.swing.table.DefaultTableModel;
import java.awt.*;
import java.awt.event.*;
import java.util.ArrayList;
import net.objecthunter.exp4j.*;
import org.jfree.chart.*;
import org.jfree.chart.plot.*;
import org.jfree.chart.renderer.xy.XYLineAndShapeRenderer;
import org.jfree.data.xy.*;
public class BisectionMethodSolver extends JFrame {
  private JTextField functionField, aField, bField, tolField, iterField;
  private JTable iterationTable;
  private DefaultTableModel tableModel;
  private ArrayList<Double> roots = new ArrayList<>();
  private String equation;
  public BisectionMethodSolver() {
    setTitle("Bisection Method Solver - Enhanced Version");
    setDefaultCloseOperation(JFrame.EXIT ON CLOSE);
    setSize(1200, 700);
    setLocationRelativeTo(null);
    setLayout(new BorderLayout(10, 10));
    // ♦ Instructions Panel
    JTextArea instructions = new JTextArea(
      "層 Bisection Method Solver\n" +
```

```
"Instructions:\n" +
  "1. Enter a valid equation in terms of x (e.g., x^3 - x - 2).\n" +
  "2. Enter an interval [a, b] such that f(a)*f(b) < 0.\n" +
  "3. Enter the tolerance (e.g., 1e-5) and max iterations.\n" +
  "4. Click 'Compute' to find the root, view the table, and plot.\n"
);
instructions.setEditable(false);
instructions.setBackground(new Color(240, 240, 240));
instructions.setBorder(BorderFactory.createTitledBorder("How to Use"));
add(instructions, BorderLayout.NORTH);
// Input Panel
JPanel inputPanel = new JPanel(new GridLayout(6, 2, 8, 8));
inputPanel.setBorder(BorderFactory.createTitledBorder("Input Parameters"));
functionField = createField(inputPanel, "Function f(x):", "x^3 - x - 2");
aField = createField(inputPanel, "Interval Start (a):", "1");
bField = createField(inputPanel, "Interval End (b):", "2");
tolField = createField(inputPanel, "Tolerance:", "1e-5");
iterField = createField(inputPanel, "Max Iterations:", "100");
JButton computeButton = new JButton("Compute");
inputPanel.add(computeButton);
add(inputPanel, BorderLayout.WEST);
// Table for Iteration Log
String[] columnNames = {"Iter", "xl", "xr", "xu", "f(xl)", "f(xr)", "Error", "f(xl)*f(xr)", "Remarks"};
tableModel = new DefaultTableModel(columnNames, 0);
iterationTable = new JTable(tableModel);
JScrollPane tableScroll = new JScrollPane(iterationTable);
```

```
tableScroll.setBorder(BorderFactory.createTitledBorder("Bisection Iteration Table"));
  add(tableScroll, BorderLayout.CENTER);
  // ♦ Compute Button Action
  computeButton.addActionListener(e -> runBisection());
  setVisible(true);
}
private JTextField createField(JPanel panel, String label, String defaultText) {
  JLabel lbl = new JLabel(label);
  JTextField field = new JTextField(defaultText);
  panel.add(lbl);
  panel.add(field);
  return field;
}
private double evaluate(double x) throws Exception {
  Expression expr = new ExpressionBuilder(equation).variable("x").build().setVariable("x", x);
  return expr.evaluate();
}
private void runBisection() {
  tableModel.setRowCount(0);
  roots.clear();
  try {
    equation = functionField.getText().trim();
    double xl = Double.parseDouble(aField.getText().trim());
    double xr = Double.parseDouble(bField.getText().trim());
```

```
double tol = Double.parseDouble(tolField.getText().trim());
       int maxIter = Integer.parseInt(iterField.getText().trim());
       double fxl = evaluate(xl);
       double fxr = evaluate(xr);
       if (fxl * fxr >= 0) {
         JOptionPane.showMessageDialog(this, "Error: f(a) * f(b) must be negative.", "Error",
JOptionPane.ERROR_MESSAGE);
         return;
      }
       double xu = 0, fxu, error;
       for (int iter = 1; iter <= maxIter; iter++) {
         xu = (xI + xr) / 2;
         fxu = evaluate(xu);
         error = Math.abs(xr - xl) / 2;
         double product = fxl * fxu;
         String remarks = "";
         if (Math.abs(fxu) < tol | | error < tol) {
           remarks = "Converged ";
         } else {
           remarks = (product < 0) ? "Root in [xl,xu]" : "Root in [xu,xr]";
         }
         roots.add(xu);
         tableModel.addRow(new Object[]{
           iter, xl, xr, xu, fxl, fxr, error, product, remarks
         });
```

```
if (Math.abs(fxu) < tol | | error < tol) break;
         if (product < 0) {
           xr = xu;
           fxr = fxu;
         } else {
           xI = xu;
           fxI = fxu;
        }
      }
      showPlot(Double.parseDouble(aField.getText().trim()),
Double.parseDouble(bField.getText().trim()));
    } catch (Exception ex) {
      JOptionPane.showMessageDialog(this, "Error: " + ex.getMessage(), "Error",
JOptionPane.ERROR_MESSAGE);
    }
  }
  private void showPlot(double a, double b) {
  XYSeries seriesF = new XYSeries("f(x)");
  XYSeries seriesRoots = new XYSeries("Root Approximations");
  for (double x = a - 0.1 * Math.abs(b - a); x \le b + 0.1 * Math.abs(b - a); x += (b - a) / 200.0) {
    try {
      seriesF.add(x, evaluate(x));
    } catch (Exception ignored) {}
  }
```

```
for (double root : roots) {
  seriesRoots.add(root, 0);
}
XYSeriesCollection dataset = new XYSeriesCollection();
dataset.addSeries(seriesF);
dataset.addSeries(seriesRoots);
JFreeChart chart = ChartFactory.createXYLineChart(
  "Bisection Method - Root Finding",
  "x",
  "f(x)",
  dataset,
  PlotOrientation.VERTICAL,
  true,
  true,
  false
);
XYPlot plot = chart.getXYPlot();
plot.setDomainGridlinesVisible(true);
plot.setRangeGridlinesVisible(true);
XYLineAndShapeRenderer renderer = new XYLineAndShapeRenderer();
renderer.setSeriesLinesVisible(0, true); // f(x) line
renderer.setSeriesShapesVisible(0, false);
renderer.setSeriesLinesVisible(1, false); // Dots for roots only
renderer.setSeriesShapesVisible(1, true);
```

```
renderer.setSeriesShape(1, new java.awt.geom.Ellipse2D.Double(-4, -4, 8, 8));
  renderer.setSeriesPaint(0, Color.BLUE);
  renderer.setSeriesPaint(1, Color.RED);
  plot.setRenderer(renderer);
  SwingUtilities.invokeLater(() -> {
    JFrame plotFrame = new JFrame("Bisection Plot");
    plotFrame.setSize(800, 600);
    plotFrame.add(new ChartPanel(chart));
    plotFrame.setLocationRelativeTo(null);
    plotFrame.setVisible(true);
 });
}
  public static void main(String[] args) {
    SwingUtilities.invokeLater(BisectionMethodSolver::new);
  }
}
```

```
INCREMENTAL METHOD
import javax.swing.*;
import javax.swing.table.DefaultTableModel;
import java.awt.*;
import java.util.ArrayList;
import net.objecthunter.exp4j.*;
import org.jfree.chart.*;
import org.jfree.chart.annotations.XYTextAnnotation;
import org.jfree.chart.plot.*;
import org.jfree.chart.renderer.xy.XYLineAndShapeRenderer;
import org.jfree.data.xy.*;
public class IncrementalMethodSolver extends JFrame {
  private JTextField functionField, aField, bField, hField;
  private JTable table;
  private DefaultTableModel tableModel;
  private ArrayList<Double> roots = new ArrayList<>();
  private String equation;
  public IncrementalMethodSolver() {
    setTitle("Incremental Method Root Finder");
    setDefaultCloseOperation(JFrame.EXIT ON CLOSE);
    setSize(1300, 700);
    setLocationRelativeTo(null);
    setLayout(new BorderLayout(10, 10));
    // Instructions Panel
    JTextArea instructions = new JTextArea(
      " Incremental Method Solver\n" +
```

```
"Instructions:\n" +
  "1. Enter a valid equation in terms of x (e.g., x^3 - x - 2).\n" +
  "2. Enter an interval [a, b] such that a < b.\n" +
  "3. Enter a small positive step size h (e.g., 0.1).\n" +
  "4. Click 'Compute' to estimate roots.\n"
);
instructions.setEditable(false);
instructions.setBackground(new Color(240, 240, 240));
instructions.setBorder(BorderFactory.createTitledBorder("How to Use"));
add(instructions, BorderLayout.NORTH);
// Input Panel
JPanel inputPanel = new JPanel(new GridLayout(5, 2, 8, 8));
inputPanel.setBorder(BorderFactory.createTitledBorder("Input Parameters"));
functionField = createField(inputPanel, "Function f(x):", "x^3 - x - 2");
aField = createField(inputPanel, "Interval Start (a):", "0");
bField = createField(inputPanel, "Interval End (b):", "5");
hField = createField(inputPanel, "Increment h:", "0.1");
JButton computeButton = new JButton("Compute");
JButton helpButton = new JButton("Help");
inputPanel.add(computeButton);
inputPanel.add(helpButton);
add(inputPanel, BorderLayout.WEST);
// Table for Iteration Log (new columns)
String[] columns = {"Iteration", "xl", "deltax", "xu", "f(xl)", "f(xu)*f(xl)", "Remark"};
```

```
tableModel = new DefaultTableModel(columns, 0);
  table = new JTable(tableModel);
  JScrollPane tableScroll = new JScrollPane(table);
  tableScroll.setBorder(BorderFactory.createTitledBorder("Iteration Table"));
  add(tableScroll, BorderLayout.CENTER);
  computeButton.addActionListener(e -> runIncremental());
  helpButton.addActionListener(e -> showHelpDialog());
  setVisible(true);
}
private JTextField createField(JPanel panel, String label, String defaultText) {
  JLabel lbl = new JLabel(label);
  JTextField field = new JTextField(defaultText);
  panel.add(lbl);
  panel.add(field);
  return field;
}
private double evaluate(double x) throws Exception {
  Expression expr = new ExpressionBuilder(equation).variable("x").build().setVariable("x", x);
  return expr.evaluate();
}
private void runIncremental() {
  tableModel.setRowCount(0);
  roots.clear();
```

```
try {
      equation = functionField.getText().trim();
      double a = Double.parseDouble(aField.getText().trim());
      double b = Double.parseDouble(bField.getText().trim());
      double h = Double.parseDouble(hField.getText().trim());
      if (h \le 0 | | a \ge b | | h \ge (b - a)) {
          JOption Pane. show Message Dialog (this, "[!] Invalid input. Ensure: \\ \  \  a < b \\ \  \  h > 0 \\ \  \  h < (b-a).", 
"Input Error", JOptionPane.ERROR_MESSAGE);
         return;
      }
      ArrayList<Double> xValues = new ArrayList<>();
       ArrayList<Double> fxValues = new ArrayList<>();
      // Fill values & table rows for intervals
      int iteration = 1;
       for (double x = a; x <= b; x += h) {
         double fx = evaluate(x);
         xValues.add(x);
         fxValues.add(fx);
      }
      for (int i = 0; i < xValues.size() - 1; i++) {
         double xl = xValues.get(i);
         double xu = xValues.get(i + 1);
         double fx_l = fxValues.get(i);
         double fx_u = fxValues.get(i + 1);
         double prod = fx_l * fx_u;
```

```
String remark = prod <= 0 ? "Root Interval" : "-";
        if (prod <= 0) {
           double approxRoot = (xl + xu) / 2;
           roots.add(approxRoot);
        }
        tableModel.addRow(new Object[]{
           iteration++,
           String.format("%.6f", xI),
           String.format("%.6f", h),
           String.format("%.6f", xu),
           String.format("%.6f", fx_l),
           String.format("%.6f", prod),
           remark
        });
      }
      if (roots.isEmpty()) {
        JOptionPane.showMessageDialog(this, "[!] No root found in the interval.", "Result",
JOptionPane.INFORMATION_MESSAGE);
      } else {
        StringBuilder result = new StringBuilder("[OK] Estimated roots at:\n");
        for (double root : roots) {
           result.append(String.format("Root at x \approx \%.6f\n", root));
        }
        JOptionPane.showMessageDialog(this, result.toString(), "Result",
JOptionPane.INFORMATION_MESSAGE);
      }
```

```
showPlot(a, b, xValues, fxValues);
    } catch (Exception ex) {
      JOptionPane.showMessageDialog(this, "Error: " + ex.getMessage(), "Error",
JOptionPane.ERROR_MESSAGE);
    }
  }
  private void showPlot(double a, double b, ArrayList<Double> xVals, ArrayList<Double> fxVals) {
    // Function series (line only)
    XYSeries seriesF = new XYSeries("f(x)");
    for (int i = 0; i < xVals.size(); i++) {
      seriesF.add(xVals.get(i), fxVals.get(i));
    }
    XYSeriesCollection dataset = new XYSeriesCollection();
    dataset.addSeries(seriesF);
    JFreeChart chart = ChartFactory.createXYLineChart(
      "Incremental Method - Root Finding",
      "x",
      "f(x)",
      dataset,
      PlotOrientation.VERTICAL,
      true,
      true,
      false
    );
```

```
XYPlot plot = chart.getXYPlot();
plot.setDomainGridlinesVisible(true);
plot.setRangeGridlinesVisible(true);
// Renderer for function: line only, blue
XYLineAndShapeRenderer renderer = new XYLineAndShapeRenderer(true, false);
renderer.setSeriesPaint(0, Color.BLUE);
plot.setRenderer(renderer);
// Plot roots as red dots with labels near dots
for (double root : roots) {
  XYSeries rootPoint = new XYSeries("Root");
  rootPoint.add(root, 0);
  XYSeriesCollection rootDataset = new XYSeriesCollection(rootPoint);
  XYLineAndShapeRenderer rootRenderer = new XYLineAndShapeRenderer(false, true);
  rootRenderer.setSeriesPaint(0, Color.RED);
  rootRenderer.setSeriesShape(0, new java.awt.geom.Ellipse2D.Double(-5, -5, 10, 10));
  int datasetIndex = plot.getDatasetCount();
  plot.setDataset(datasetIndex, rootDataset);
  plot.setRenderer(datasetIndex, rootRenderer);
  // Add label near the dot
  XYTextAnnotation annotation = new XYTextAnnotation(
    String.format("%.4f", root),
    root,
    0.02 * (plot.getRangeAxis().getUpperBound() - plot.getRangeAxis().getLowerBound())
  );
```

```
annotation.setFont(new Font("SansSerif", Font.BOLD, 12));
    annotation.setPaint(Color.RED);
    plot.addAnnotation(annotation);
  }
  SwingUtilities.invokeLater(() -> {
    JFrame plotFrame = new JFrame("Incremental Plot");
    plotFrame.setSize(900, 600);
    plotFrame.add(new ChartPanel(chart));
    plotFrame.setLocationRelativeTo(null);
    plotFrame.setVisible(true);
  });
}
private void showHelpDialog() {
  String helpMessage = """
    El Incremental Method Root Finder Help
    Instructions:
    1. Enter a valid equation in terms of x (e.g., x^3 - x - 2).
    2. Enter an interval [a, b] such that a < b.
    3. Enter a small positive step size h (e.g., 0.1).
    4. Click 'Compute' to estimate roots.
    What is the Incremental Method?
```

The Incremental Method is a root-finding technique that evaluates the function at equally spaced points in the given interval [a, b]. It detects roots by checking where the function changes sign between these points.

Uses:

- Simple way to locate approximate root intervals.
- Good for functions where derivatives are hard to compute.
- Helps provide initial guesses for other root-finding methods.

Note: Smaller step sizes (h) yield better root approximations but require more computations.

""";

}

JOptionPane.showMessageDialog(this, helpMessage, "Help - Incremental Method", JOptionPane.INFORMATION_MESSAGE);
}

public static void main(String[] args) {
 SwingUtilities.invokeLater(IncrementalMethodSolver::new);
}

```
NEWTON RAPHSON
import javax.swing.*;
import javax.swing.table.DefaultTableModel;
import java.awt.*;
import java.awt.event.*;
import java.util.*;
import net.objecthunter.exp4j.*;
import org.jfree.chart.*;
import org.jfree.chart.annotations.XYTextAnnotation;
import org.jfree.chart.plot.*;
import org.jfree.chart.renderer.xy.XYLineAndShapeRenderer;
import org.jfree.data.xy.*;
public class NewtonRaphsonSolver extends JFrame {
  private JTextField functionField, derivativeField, x0Field, tolField, maxIterField;
  private JTable table;
  private DefaultTableModel tableModel;
  private ArrayList<Double> roots = new ArrayList<>();
  public NewtonRaphsonSolver() {
    setTitle("Newton-Raphson Method Solver");
    setDefaultCloseOperation(JFrame.EXIT ON CLOSE);
    setSize(1300, 700);
    setLocationRelativeTo(null);
    setLayout(new BorderLayout(10, 10));
    // Instructions Panel
    JTextArea instructions = new JTextArea(
      "層 Newton-Raphson Method Solver\n" +
```

```
"Instructions:\n" +
  "- Enter f(x) and f'(x) using math-like syntax (e.g., x^3 - x - 2).\n" +
  "- Supported functions: \sin(x), \cos(x), \tan(x), \log(x), \ln(x), \exp(x), abs(x), etc.\n" +
  "- For powers, use ^ (e.g., x^3 for x cubed).\n" +
  "- Provide an initial guess x0, a tolerance (e.g., 1e-5), and max iterations.\n" +
  "- Click 'Compute' to find the roots.\n"
);
instructions.setEditable(false);
instructions.setBackground(new Color(240, 240, 240));
instructions. set Border (Border Factory. create Titled Border ("Instructions"));\\
add(instructions, BorderLayout.NORTH);
// Input Panel
JPanel inputPanel = new JPanel(new GridLayout(7, 2, 8, 8));
inputPanel.setBorder(BorderFactory.createTitledBorder("Input Parameters"));
functionField = createField(inputPanel, "Function f(x):", "x^3 - x - 2");
derivativeField = createField(inputPanel, "Derivative f'(x):", "3*x^2 - 1");
xOField = createField(inputPanel, "Initial Guess (x0):", "1.5");
tolField = createField(inputPanel, "Tolerance:", "1e-5");
maxIterField = createField(inputPanel, "Max Iterations:", "20");
JButton computeButton = new JButton("Compute");
JButton helpButton = new JButton("Help");
inputPanel.add(computeButton);
inputPanel.add(helpButton);
add(inputPanel, BorderLayout.WEST);
// Iteration Table
```

```
String[] columns = {"Iteration", "x", "f(x)", "Error"};
  tableModel = new DefaultTableModel(columns, 0);
  table = new JTable(tableModel);
  JScrollPane tableScroll = new JScrollPane(table);
  tableScroll.setBorder(BorderFactory.createTitledBorder("Iteration Table"));
  add(tableScroll, BorderLayout.CENTER);
  computeButton.addActionListener(e -> runNewtonRaphson());
  helpButton.addActionListener(e -> showHelp());
  setVisible(true);
}
private JTextField createField(JPanel panel, String label, String defaultText) {
  JLabel lbl = new JLabel(label);
  JTextField field = new JTextField(defaultText);
  panel.add(lbl);
  panel.add(field);
  return field;
}
private void runNewtonRaphson() {
  tableModel.setRowCount(0);
  roots.clear();
  try {
    String fxExpr = functionField.getText().trim();
    String dfxExpr = derivativeField.getText().trim();
    double x0 = Double.parseDouble(x0Field.getText().trim());
```

```
double tol = Double.parseDouble(tolField.getText().trim());
      int maxIter = Integer.parseInt(maxIterField.getText().trim());
       Expression fx = new ExpressionBuilder(fxExpr).variable("x").build();
       Expression dfx = new ExpressionBuilder(dfxExpr).variable("x").build();
      double x = x0, error = Double.MAX_VALUE;
      int iter = 1;
      while (iter <= maxIter && error > tol) {
        double fxVal = fx.setVariable("x", x).evaluate();
        double dfxVal = dfx.setVariable("x", x).evaluate();
         if (Math.abs(dfxVal) < 1e-12) {
           JOptionPane.showMessageDialog(this, "Derivative too close to zero at x = " + x, "Error",
JOptionPane.ERROR_MESSAGE);
           return;
        }
        double xNext = x - fxVal / dfxVal;
        error = Math.abs(xNext - x);
        tableModel.addRow(new Object[]{
           iter, String.format("%.8f", x), String.format("%.8f", fxVal), String.format("%.8f", error)
        });
        x = xNext;
        iter++;
      }
```

```
roots.add(x);
      JOptionPane.showMessageDialog(this, String.format("[OK] Root found at x \approx \%.8f", x), "Result",
JOptionPane.INFORMATION_MESSAGE);
      showPlot(fx, x0);
    } catch (Exception ex) {
      JOptionPane.showMessageDialog(this, "Error: " + ex.getMessage(), "Error",
JOptionPane.ERROR MESSAGE);
    }
  }
  private void showPlot(Expression fx, double x0) {
    XYSeries seriesF = new XYSeries("f(x)");
    double xMin = x0 - 5, xMax = x0 + 5;
    for (double x = xMin; x \le xMax; x += 0.01) {
      seriesF.add(x, fx.setVariable("x", x).evaluate());
    }
    XYSeriesCollection dataset = new XYSeriesCollection(seriesF);
    JFreeChart chart = ChartFactory.createXYLineChart(
      "Newton-Raphson Method",
      "x",
      "f(x)",
      dataset,
      PlotOrientation.VERTICAL,
      true,
```

```
true,
  false
);
XYPlot plot = chart.getXYPlot();
plot.setDomainGridlinesVisible(true);
plot.setRangeGridlinesVisible(true);
XYLineAndShapeRenderer renderer = new XYLineAndShapeRenderer(true, false);
renderer.setSeriesPaint(0, Color.BLUE);
plot.setRenderer(renderer);
// Add root points and labels
for (double root : roots) {
  XYSeries rootPoint = new XYSeries("Root");
  rootPoint.add(root, 0);
  XYSeriesCollection rootDataset = new XYSeriesCollection(rootPoint);
  XYLineAndShapeRenderer rootRenderer = new XYLineAndShapeRenderer(false, true);
  rootRenderer.setSeriesPaint(0, Color.RED);
  rootRenderer.setSeriesShape(0, new java.awt.geom.Ellipse2D.Double(-5, -5, 10, 10));
  int datasetIndex = plot.getDatasetCount();
  plot.setDataset(datasetIndex, rootDataset);
  plot.setRenderer(datasetIndex, rootRenderer);
  XYTextAnnotation annotation = new XYTextAnnotation(String.format("%.5f", root), root, 0.05);
  annotation.setFont(new Font("SansSerif", Font.BOLD, 12));
  annotation.setPaint(Color.RED);
```

```
plot.addAnnotation(annotation);
}

SwingUtilities.invokeLater(() -> {
    JFrame plotFrame = new JFrame("Newton-Raphson Plot");
    plotFrame.setSize(900, 600);
    plotFrame.add(new ChartPanel(chart));
    plotFrame.setLocationRelativeTo(null);
    plotFrame.setVisible(true);
});
}

private void showHelp() {
    String helpMessage = """
    Newton-Raphson Method
```

The Newton-Raphson method is an iterative technique for finding approximate roots of a real-valued function.

```
Formula:
```

```
x_{n+1} = x_n - f(x_n) / f'(x_n)
```

How to use this solver:

 \blacksquare Enter the function f(x) in math-like syntax. Example: $x^3 - x - 2$

 Σ Enter the derivative f'(x). Example: $3*x^2 - 1$

Provide an initial guess x0 (e.g., 1.5), a tolerance (e.g., 1e-5), and maximum iterations.

⊈Click 'Compute' to see the iteration steps and the root.

☐The plot will show the function and the root(s) found.

```
Supported functions: sin(x), cos(x), tan(x), log(x), ln(x), exp(x), abs(x), sqrt(x), etc.

Use ^ for powers (e.g., x^3 for x cubed).

""";

JOptionPane.showMessageDialog(this, helpMessage, "Help - Newton-Raphson Method", JOptionPane.INFORMATION_MESSAGE);
}

public static void main(String[] args) {

SwingUtilities.invokeLater(NewtonRaphsonSolver::new);
}
```

```
REGULA FALSI
import javax.swing.*;
import javax.swing.table.DefaultTableModel;
import java.awt.*;
import java.util.*;
import net.objecthunter.exp4j.*;
import org.jfree.chart.*;
import org.jfree.chart.plot.*;
import org.jfree.chart.renderer.xy.XYLineAndShapeRenderer;
import org.jfree.data.xy.*;
public class RegulaFalsiMethodSolver extends JFrame {
  private JTextField functionField, aField, bField, tolField, maxIterField;
  private JTable table;
  private DefaultTableModel tableModel;
  private ArrayList<Double> roots = new ArrayList<>();
  public RegulaFalsiMethodSolver() {
    setTitle("Regula Falsi Method Solver");
    setDefaultCloseOperation(JFrame.EXIT ON CLOSE);
    setSize(1300, 700);
    setLocationRelativeTo(null);
    setLayout(new BorderLayout(10, 10));
    // Instructions
```

JTextArea instructions = new JTextArea(

"層 Regula Falsi Method Solver\n" +

"- Enter f(x) using exp4j syntax (e.g., $x^3 - x - 2$).\n" +

"Instructions:\n" +

```
"- Supported functions: sin, cos, exp, log, sqrt, etc.\n" +
  "- Use '^{\prime}' for powers (e.g., x^3).n" +
  "- Provide interval [a, b], tolerance, and max iterations.\n" +
  "- Ensure f(a) * f(b) < 0 (opposite signs).\n"
);
instructions.setEditable(false);
instructions.setBackground(new Color(240, 240, 240));
instructions.setBorder(BorderFactory.createTitledBorder("Instructions"));
add(instructions, BorderLayout.NORTH);
// Input Panel
JPanel inputPanel = new JPanel(new GridLayout(6, 2, 8, 8));
inputPanel.setBorder(BorderFactory.createTitledBorder("Input Parameters"));
functionField = createField(inputPanel, "Function f(x):", "x^3 - x - 2");
aField = createField(inputPanel, "Interval Start a:", "1.0");
bField = createField(inputPanel, "Interval End b:", "2.0");
tolField = createField(inputPanel, "Tolerance:", "1e-5");
maxIterField = createField(inputPanel, "Max Iterations:", "20");
JButton computeButton = new JButton("Compute");
JButton helpButton = new JButton("Help");
inputPanel.add(computeButton);
inputPanel.add(helpButton);
add(inputPanel, BorderLayout.WEST);
// Table
String[] columns = {"Iter", "xl", "xu", "xr", "Error", "f(xl)", "f(xr)", "f(xu)", "f(xl)*f(xu)"};
tableModel = new DefaultTableModel(columns, 0);
```

```
table = new JTable(tableModel);
  JScrollPane tableScroll = new JScrollPane(table);
  tableScroll.setBorder(BorderFactory.createTitledBorder("Iteration Table"));
  add(tableScroll, BorderLayout.CENTER);
  // Actions
  computeButton.addActionListener(e -> runRegulaFalsi());
  helpButton.addActionListener(e -> showHelpDialog());
  setVisible(true);
}
private JTextField createField(JPanel panel, String label, String defaultText) {
  JLabel lbl = new JLabel(label);
  JTextField field = new JTextField(defaultText);
  panel.add(lbl);
  panel.add(field);
  return field;
}
private void runRegulaFalsi() {
  tableModel.setRowCount(0);
  roots.clear();
  try {
    String fxExpr = functionField.getText().trim().replaceAll("^{", "**"}); // Replace ^ with ** for exp4j
    fxExpr = fxExpr.replaceAll("\\*\\*", "^"); // Actually, exp4j uses ^, so keep this!
    double a = Double.parseDouble(aField.getText().trim());
    double b = Double.parseDouble(bField.getText().trim());
```

```
int maxIter = Integer.parseInt(maxIterField.getText().trim());
       Expression fx = new ExpressionBuilder(fxExpr).variable("x").build();
      double fa = fx.setVariable("x", a).evaluate();
      double fb = fx.setVariable("x", b).evaluate();
      if (fa * fb >= 0) {
         JOptionPane.showMessageDialog(this, "Error: f(a) and f(b) must have opposite signs.", "Error",
JOptionPane.ERROR_MESSAGE);
         return;
      }
      int iter = 1;
      double error = Double.MAX_VALUE;
      double xr = 0;
      while (iter <= maxIter && error > tol) {
         fa = fx.setVariable("x", a).evaluate();
         fb = fx.setVariable("x", b).evaluate();
         xr = b - (fb * (a - b)) / (fa - fb);
         double fxr = fx.setVariable("x", xr).evaluate();
         error = Math.abs(fxr);
         double product = fa * fb;
         tableModel.addRow(new Object[]{
           iter, String.format("%.8f", a), String.format("%.8f", b), String.format("%.8f", xr),
           String.format("%.8f", error),
           String.format("%.8f", fa), String.format("%.8f", fxr), String.format("%.8f", fb),
```

double tol = Double.parseDouble(tolField.getText().trim());

```
String.format("%.8f", product)
        });
         if (Math.abs(fxr) < tol) break;
         if (fa * fxr < 0) {
           b = xr;
         } else {
           a = xr;
        }
         iter++;
      }
      roots.add(xr);
      JOptionPane.showMessageDialog(this, String.format("[OK] Root found at x \approx \%.8f", xr), "Result",
JOptionPane.INFORMATION_MESSAGE);
      showPlot(fx, a, b, roots);
    } catch (Exception ex) {
      JOptionPane.showMessageDialog(this, "Error: " + ex.getMessage(), "Error",
JOptionPane.ERROR_MESSAGE);
    }
  }
  private void showPlot(Expression fx, double a, double b, ArrayList<Double> roots) {
    XYSeries seriesF = new XYSeries("f(x)");
    double xMin = a - 2, xMax = b + 2;
```

```
for (double x = xMin; x \le xMax; x += 0.01) {
  try {
    seriesF.add(x, fx.setVariable("x", x).evaluate());
  } catch (Exception e) {
    // Skip invalid evaluations
  }
}
XYSeriesCollection dataset = new XYSeriesCollection(seriesF);
JFreeChart chart = ChartFactory.createXYLineChart(
  "Regula Falsi Method: Root Finding",
  "x",
  "f(x)",
  dataset,
  PlotOrientation.VERTICAL,
  true,
  true,
  false
);
XYPlot plot = chart.getXYPlot();
plot.setDomainGridlinesVisible(true);
plot.setRangeGridlinesVisible(true);
XYLineAndShapeRenderer renderer = new XYLineAndShapeRenderer(true, false);
renderer.setSeriesPaint(0, Color.BLUE);
plot.setRenderer(renderer);
for (double root : roots) {
```

```
XYSeries rootPoint = new XYSeries("Root");
    rootPoint.add(root, 0);
    XYSeriesCollection rootDataset = new XYSeriesCollection(rootPoint);
    XYLineAndShapeRenderer rootRenderer = new XYLineAndShapeRenderer(false, true);
    rootRenderer.setSeriesPaint(0, Color.RED);
    rootRenderer.setSeriesShape(0, new java.awt.geom.Ellipse2D.Double(-5, -5, 10, 10));
    int datasetIndex = plot.getDatasetCount();
    plot.setDataset(datasetIndex, rootDataset);
    plot.setRenderer(datasetIndex, rootRenderer);
  }
  SwingUtilities.invokeLater(() -> {
    JFrame plotFrame = new JFrame("Regula Falsi Plot");
    plotFrame.setSize(900, 600);
    plotFrame.add(new ChartPanel(chart));
    plotFrame.setLocationRelativeTo(null);
    plotFrame.setVisible(true);
 });
private void showHelpDialog() {
  String message = """
    紫 Regula Falsi Method Overview 紫
    - The Regula Falsi Method is a bracketing technique for root finding.
    - Requires initial guesses a and b such that f(a)*f(b) < 0.
    - Formula: xr = b - fb*(a-b)/(fa-fb)
```

}

```
Supported functions: sin, cos, exp, log, sqrt, etc.
      Use '^1' for powers (e.g., x^3).
      Function: x^3 - x - 2
      a: 1.0
      b: 2.0
      Tolerance: 1e-5
      Max Iterations: 20
      """;
    JOptionPane.showMessageDialog(this, message, "Regula Falsi Method Help",
JOptionPane.INFORMATION_MESSAGE);
  }
  public static void main(String[] args) {
    Swing Utilities. invoke Later (Regula Falsi Method Solver::new); \\
 }
}
```