79428

1

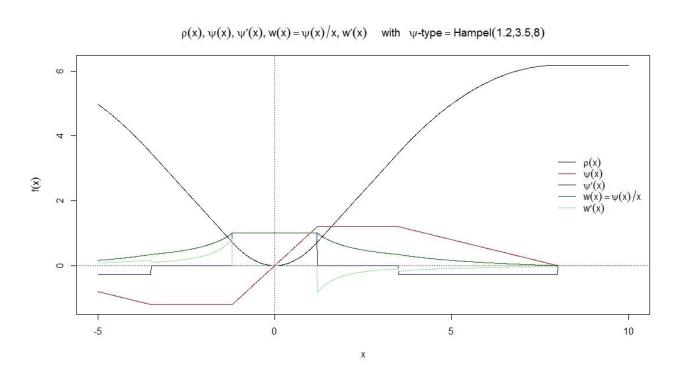
I would use robust statistical methods because they are more resistant to small deviations from the assumptions, in other words robust with respect to outliers and stable with respect to small deviations from the assumed parametric model. It is well known that classical methods behave quite poorly under slight violations of the strict model assumptions. In particular, least squares estimate for regression models are highly sensitive to outliers. If the outlier results from non-normal measurement error or some other violation of standard ordinary least squares assumptions, then it compromises the validity of the regression results if a non-robust regression technique is used. Another instance in which robust estimates should be used is when there is a suspicion of heteroscedasticity.

It is discouraged to screen the data, to remove outliers and then to apply classical inferential methods. This is not a simple and good way to proceed because those outliers might be valid regarding the data generation process. In multivariate or highly structured data, it can be hard to single out outliers or to identify influential points. In place of rejecting an observation, it could be better to down-weight uncertain observations. Rejecting outliers reduces the sample size, could affect the distribution theory, and variances could be underestimated from the cleaned data.

I would use robust methods to compliment and to compare to the classical methods. In other words, I would always make at least two models, one classical and one robust, and see which one fit the data better. This is especially true if I suspect that the data has outliers or influence points. If they give about the same results, I would use the classical method because it is easier to explain to someone not familiar with statistics. However, if the robust method gives a more accurate result, I would definitely use it.

I get the following location estimate

4.58924



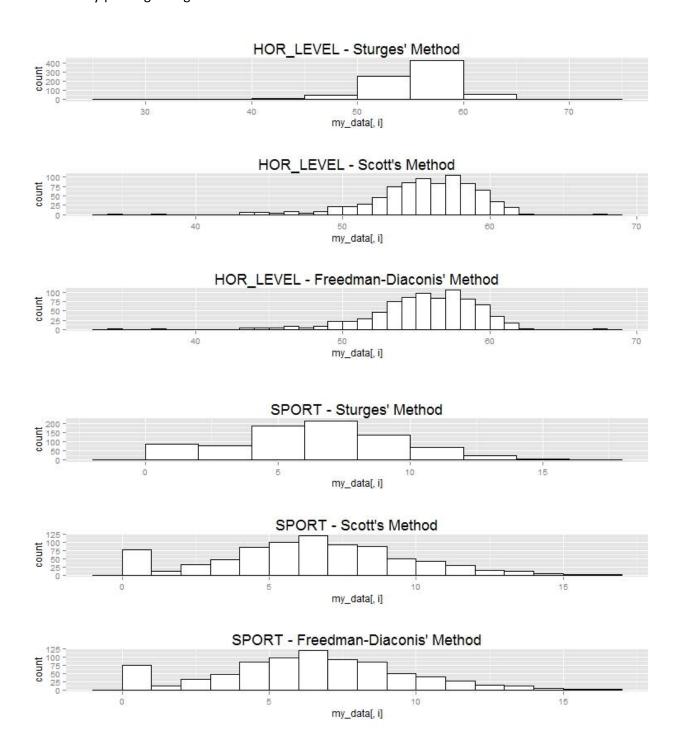
It is a redescender.

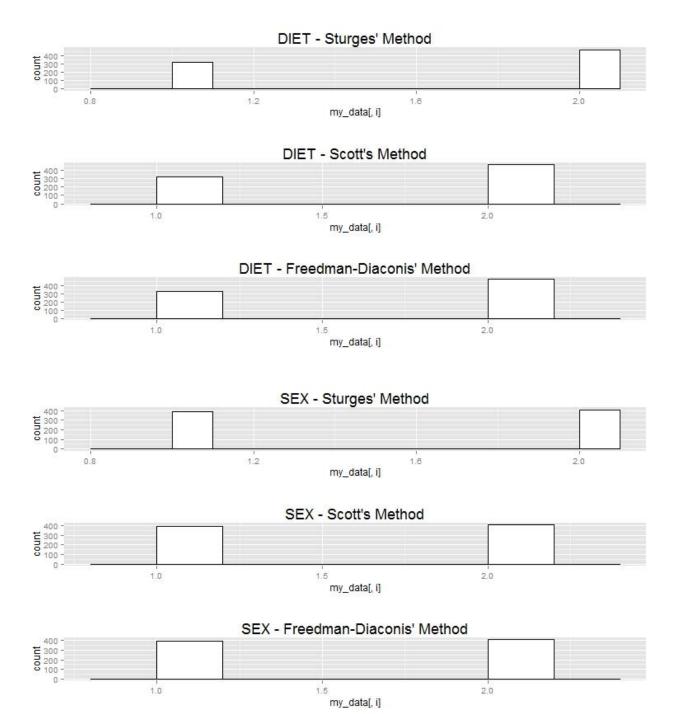
3

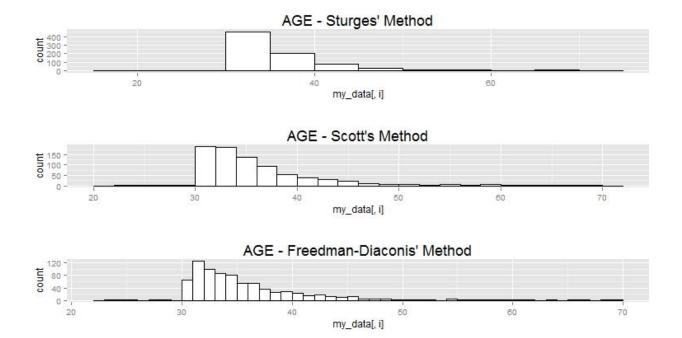
I was unable to complete this one. I have no idea what I was supposed to do in the code.

Data Understanding

I start off by plotting histograms of the attributes with a different number of bins.



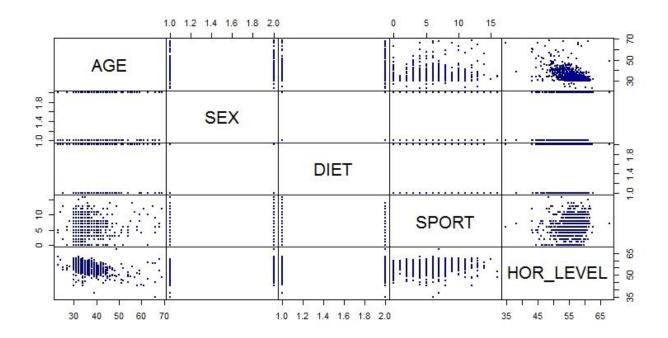


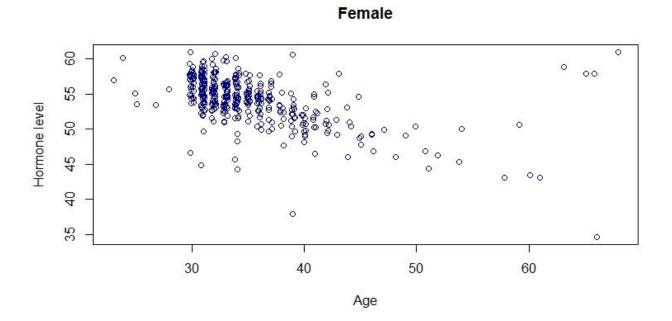


From these histograms we can observe the following things:

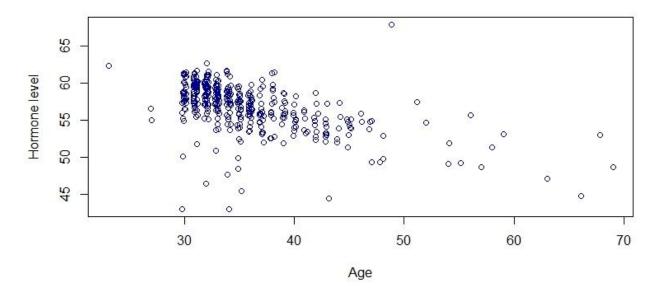
- HOR_LEVEL has a negative skewness and AGE has a positive skewness and a high kurtosis
- HOR_LEVEL and AGE have outliers.
- SPORT could be considered a normal distribution, if it did not have a spike at value zero.
- There are more people with Unhealthy diets.
- There seem to be about an equal amount of men and women.
- The continuous variables have vastly different means and variances.

I have produced a scatter plot of the data. We can see that AGE and HOR_LEVEL are somewhat negatively correlated.



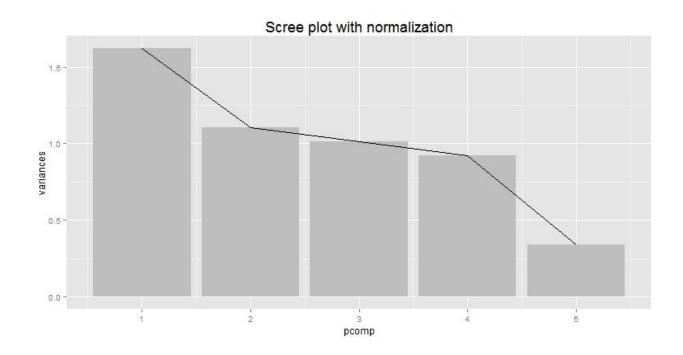


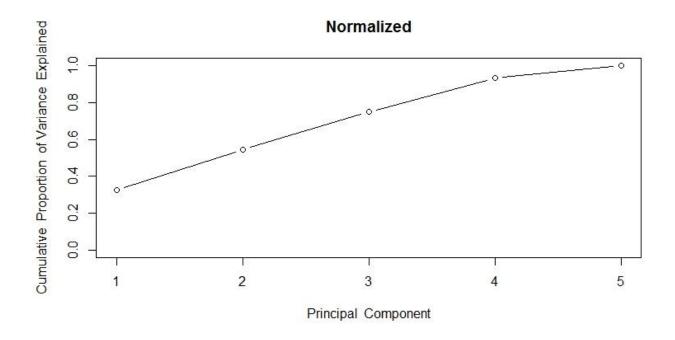
Male



HOR_LEVEL and AGE look negatively correlated for both men and women separately; however there are some interesting values for females with a high age.

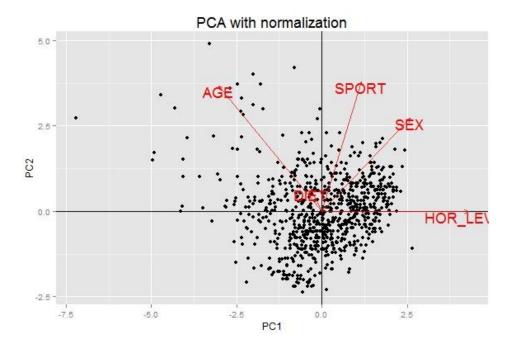
Here are the scree plots of the data:





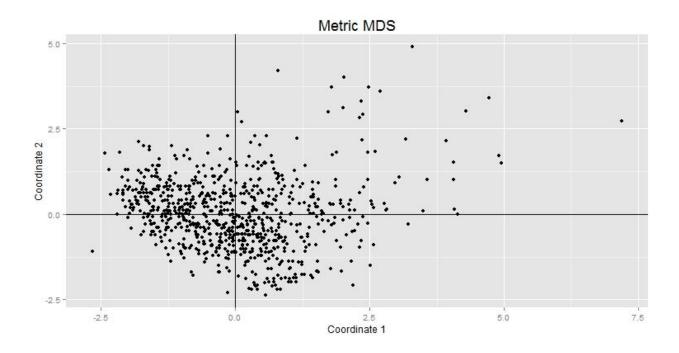
From these plots we can see that the first principle component explains about 35% of the variance and the second principle explains about 20% of the variance. Together they explain about 55%. A scree plot allows a graphical assessment of the relative contribution of the PCs in explaining the variability of the data.

Here's the plot with PC1 on the horizontal axis and PC2 on the vertical axis:



What's interesting about this plot is that judging by the first two principal components; a HOR_LEVEL doesn't seem to be strongly correlated with any variable. In the above plot we can see some points clearly being away from the center of the point cloud. These appear to be in the top left quadrant.

Next I have plotted the 2D MDS chart. Instead of preserving the variance, like in PCA, MDS preserves the Euclidean distance in the data. For this data it looks exactly the same as PCA, we can see some clear outliers.



Correlations:

Kendall's Tau

| | AGE | SPORT | HOR_LEVEL |
|-----------|--------|-------|-----------|
| AGE | 1.000 | 0.035 | -0.342 |
| SPORT | 0.035 | 1.000 | 0.172 |
| HOR_LEVEL | -0.342 | 0.172 | 1.000 |

Pearson's Correlation

| | AGE | SPORT | HOR_LEVEL |
|-----------|--------|-------|-----------|
| AGE | 1.000 | 0.078 | -0.474 |
| SPORT | 0.078 | 1.000 | 0.194 |
| HOR_LEVEL | -0.474 | 0.194 | 1.000 |

Highest absolute correlation is between HOR_LEVEL and AGE, just like was assumed from the visual inspection of the data.

Data Modeling

Next I did some basic models of the data.

```
call:
lm(formula = HOR_LEVEL ~ . - ID, data = DATA.ANA)
Residuals:
                       Median
     Min
                 1Q
                                                Max
-15.7550
           -1.1614
                       0.1098
                                  1.4765
                                           16.1786
Coefficients:
                Estimate Std. Error t value
                63.24287
                                                  < 2e-16
                                                           ***
(Intercept)
                              0.59176 106.873
                                                           ***
                -0.29087
AGE
                              0.01567
                                       -18.567
                                                  < 2e-16
                 2.75557
                                        14.342
SEXmale
                              0.19213
                                                  < 2e-16
                -0.33621
0.23886
                                         -1.722
DIETunhealthy
                              0.19526
                                                   0.0855
                                          7.946
                              0.03006
                                                  6.6e-15
                                                           ***
SPORT
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 2.712 on 795 degrees of freedom
Multiple R-squared: 0.4273, Adjusted R-squared: 0.42
F-statistic: 148.3 on 4 and 795 DF, p-value: < 2.2e-16
```

In this basic model we can see that all variables are statistically significant at the 0.05 level and the model has an adjusted R-squared of 0.42. Age has a negative effect on hormonal level, being male has a higher positive effect on hormonal level than for females, an unhealthy diet has a negative effect on hormonal level when compared to a healthy diet and sport has a positive effect on hormonal level.

Here are the confidence intervals for the predictors:

```
2.5 % 97.5 % (Intercept) 62.0812749 64.40445862 AGE -0.3216241 -0.26011901 SEXmale 2.3784303 3.13270530 DIETunhealthy -0.7194907 0.04707989 SPORT 0.1798514 0.29787304
```

DIETunhealthy is the only one that contains 0 in the confidence interval.

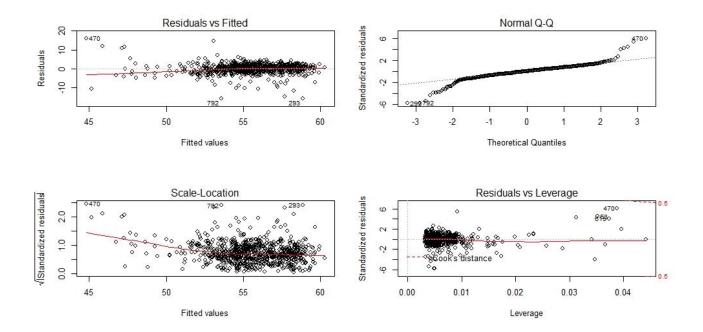
Now that I have a model, I will look for OLS assumption violations for continuous variables (HOR_LEVEL and AGE).

First I check if there a relation between the ith and the i+1th observation, with the following results. (The lag might be larger, i.e. the ith and i+kth observation might be correlated).

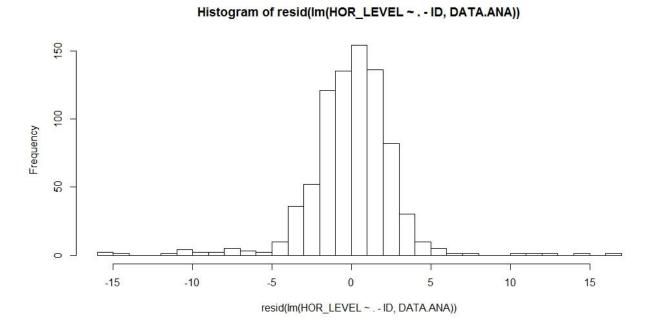
```
> cor(ylag,ynew)
[1] -0.01851628
> cor(cnew,clag)
[1] 0.01502376
```

No correlation, so I assume that the data is generated by an i.i.d process.

Do residuals and yhats correlate? Does explanatory variable correlate with the estimated residuals? Is the relationship linear?



There seems to be no relation between residuals and fitted values so Cov(X'u)=0 is fine. From the QQ-plot we see some departures from the line, which brings doubts about a normal distribution. There are also influential points in the data.



The residuals do not follow a normal distribution, as can be seen from this histogram. Just to make sure I perform a shapiro-wilk test of normality:

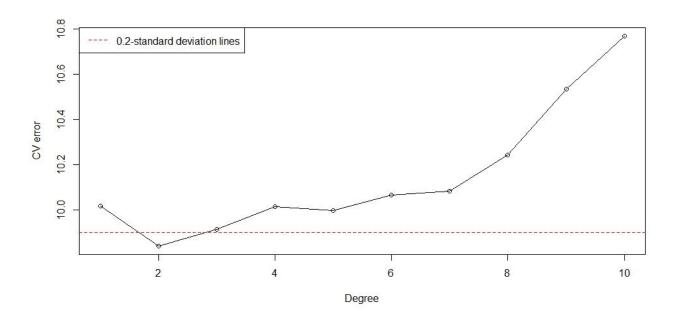
```
Shapiro-Wilk normality test data: resid(lm(HOR_LEVEL ~ . - ID, DATA.ANA)) W = 0.8846, p-value < 2.2e-16 HO(normality) is rejected.
```

I will still try to find the best Im model for the data. I will add interaction terms and check for polynomial degrees.

```
call:
lm(formula = HOR\_LEVEL \sim (AGE + SEX + DIET + SPORT)^2, data = DATA.ANA)
Residuals:
      Min
                        Median
                                                Max
            -1.1708
-15.6216
                                  1.4781
                                            15.9421
                        0.1693
Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
                                                              < 2e-16 ***
                          68.796722
                                        1.529067
                                                   44.993
(Intercept)
                          -0.435247
                                        0.042798
                                                   -10.170
                                                              < 2e-16
AGE
                           1.920351
                                        1.173684
                                                     1.636 0.102202
SEXmale
                                                    -2.112 0.035008 *
-2.597 0.009577 **
DIETunhealthy
                          -2.499084
                                        1.183330
                          -0.426444
                                        0.164201
SPORT
                           0.024985
                                        0.031321
                                                     0.798 0.425282
AGE:SEXmale
                           0.035321
AGE:DIETunhealthy
                                        0.031791
                                                     1.111 0.266893
                                        0.004463
                                                      3.735 0.000201 ***
AGE: SPORT
                           0.016670
                                        0.388322
                                                    0.403 0.687097
-0.261 0.793863
                           0.156473
SEXmale:DIETunhealthy
                           -0.015732
                                        0.060185
SEXmale:SPORT
                           0.140494
                                        0.060647
                                                    2.317 0.020781 *
DIETunhealthy:SPORT
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 2.686 on 789 degrees of freedom
Multiple R-squared: 0.4426, Adjusted R-squared: 0.435
F-statistic: 62.65 on 10 and 789 DF, p-value: < 2.2e-16
                                   Adjusted R-squared: 0.4355
Analysis of Variance Table
Model 1: HOR_LEVEL ~ (ID + AGE + SEX + DIET + SPORT) - ID Model 2: HOR_LEVEL ~ (AGE + SEX + DIET + SPORT)^2 Res.Df RSS Df Sum of Sq F Pr(>F)
      795 5846.8
1
2
      789 5691.2
                   6 155.58 3.5947 0.001598 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The model with interaction terms is better than the basic model.

To see, which polynomial would be best for HOR_LEVEL and AGE, I use 10-fold cross validation. Here are the error results for the polynomial degrees:



As can be seen from the plot, a polynomial degree of two minimizes the error.

Now I can fit a model with interaction terms and AGE with a polynomial.

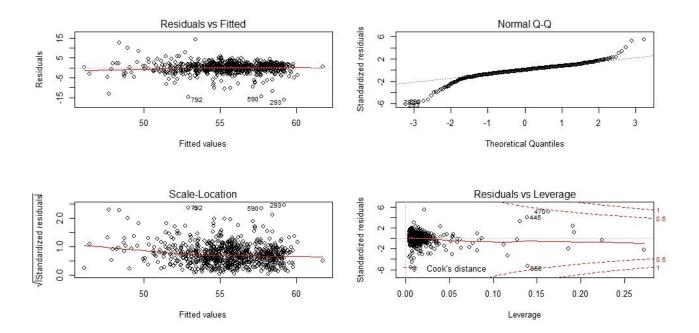
```
call:
lm(formula = HOR\_LEVEL \sim . - ID + I(AGE^2) + (AGE + SEX + DIET + I)
     SPORT)^2, data = DATA.ANA)
Residuals:
                       Median
     Min
                                               Max
-16.1120
           -1.1083
                       0.1356
                                 1.4726
                                          14.4412
Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
                         78.534420
-0.932688
                                                                     ***
(Intercept)
                                                   31.144
                                                           < 2e-16
2.78e-16
                                       2.521653
                                       0.111539
                                                   -8.362
AGE
                          1.739813
                                                             0.1334
SEXmale
                                       1.158109
                                                    1.502
                          -2.850328
                                       1.169290
DIETunhealthy
                                                   -2.438
                                                             0.0150
                                       0.165968
                          -0.251297
SPORT
                                                   -1.514
                                                             0.1304
                                                          1.74e-06 ***
I(AGE^2)
                          0.006136
                                       0.001274
                                                    4.818
AGE:SEXmale
                           0.028536
                                       0.030898
                                                    0.924
                                                             0.3560
                          0.043983
                                                    1.401
AGE:DIETunhealthy
                                       0.031404
                                                             0.1617
AGE: SPORT
                          0.011568
                                       0.004527
                                                    2.555
                                                             0.0108
                          0.256923
                                                    0.670
SEXmale:DIETunhealthy
                                       0.383535
                                                             0.5031
SEXmale:SPORT
                          0.011794
                                       0.059361
                                                    0.199
                                                             0.8426
DIETunhealthy:SPORT
                          0.141793
                                       0.059811
                                                    2.371
                                                             0.0180 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
                                                             0.1 ' ' 1
Residual standard error: 2.649 on 788 degrees of freedom Multiple R-squared: 0.4585, Adjusted R-squared: 0.451
                                   Adjusted R-squared: 0.451
F-statistic: 60.66 on 11 and 788 DF, p-value: < 2.2e-16
```

It is interesting to see that AGE and SEXmale as such a high p-value in this model. There is a marginal increase in the adjusted R-squared compared to the previous model.

Confidence intervals:

| | coef | 2.5 % | 97.5 % |
|-----------------------|--------|--------|--------|
| (Intercept) | 78.534 | 73.584 | 83.484 |
| AGE | | -1.152 | -0.714 |
| SEXmale | 1.740 | -0.534 | 4.013 |
| DIETunhealthy | -2.850 | -5.146 | -0.555 |
| SPORT | -0.251 | -0.577 | 0.074 |
| I(AGE^2) | 0.006 | 0.004 | 0.009 |
| AGE:SEXmale | 0.029 | -0.032 | 0.089 |
| AGE:DIETunhealthy | 0.044 | -0.018 | 0.106 |
| AGE:SPORT | 0.012 | 0.003 | 0.020 |
| SEXmale:DIETunhealthy | 0.257 | -0.496 | 1.010 |
| SEXmale:SPORT | -0.012 | -0.128 | 0.105 |
| DIETunhealthy:SPORT | 0.142 | 0.024 | 0.259 |

Residual plots:



Since not all variables were statistically significant I will test a model that does not have those variables, just to see if there is a significant difference.

```
Call:
lm(formula = HOR_LEVEL ~ . - ID + I(AGE^2) + AGE:SPORT + DIET:SPORT,
    data = DATA.ANA)
Residuals:
                     Median
     Min
                                    3Q
                                            Max
-16.2447
          -1.1119
                     0.1768
                               1.4746
                                        14.9023
Coefficients:
                      Estimate Std. Error
                                            t value Pr(>|t|)
                                                      < 2e-16
(Intercept)
                     76.688997
                                   2.279711
                                              33.640
                      -0.874716
                                              -8.221
                                  0.106399
                                                     8.22e-16
AGE
                                                               ***
SEXmale
                        .835545
                                   0.188039
                                              15.080
                                                      < 2e-16
                                                      0.00277
                      -1.192893
DIETunhealthy
                                   0.397426
                                                .002
SPORT
                      -0.247191
                                   0.164868
                                               1.499
                                                      0.13419
I(AGE^2)
                      0.005967
                                   0.001268
                                               4.704
                                                     3.00e-06
                                                      0.01315
0.01337
AGE: SPORT
                      0.011150
                                  0.004487
                                               2.485
                      0.147169
DIETunhealthy:SPORT
                                  0.059359
                                               2.479
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 2.647 on 792 degrees of freedom
Multiple R-squared: 0.4564, Adjusted R-squared: 0.4516
F-statistic: 94.98 on 7 and 792 DF, p-value: < 2.2e-16
Confidence intervals:
                                 2.5 % 97.5 %
                          coef
                        76.689 72.214 81.164
(Intercept)
                        -0.875
                                -1.084 -0.666
AGE
SEXmale
                         2.836
                                 2.466
                                          3.205
                        -1.193
                                -1.973
DIETunhealthy
                                         -0.413
                                          0.076
                        -0.247
                                -0.571
SPORT
I(AGE^2)
                         0.006
                                 0.003
                                          0.008
AGE: SPORT
                         0.011
                                  0.002
                                          0.020
DIETunhealthy:SPORT
                        0.147
                                  0.031
ANOVA:
Analysis of Variance Table
Model 1: HOR_LEVEL ~ (ID + AGE + SEX + DIET + SPORT) - ID Model 2: HOR_LEVEL ~ (AGE + SEX + DIET + SPORT)^2
Model 3: HOR_LEVEL ~ (ID + AGE + SEX + DIET + SPORT) - ID + I(AGE^2) +
     (AGE + SEX + DIET + SPORT)^2
Model 4: HOR_LEVEL \sim (ID + AGE + SEX + DIET + SPORT) - ID + I(AGE^2) +
    AGE:SPORT + DIET:SPORT
              RSS Df Sum of Sq
  Res.Df
                                      F
                                                Pr(>F)
      795 5846.8
1
23
      789 5691.2
                         155.578 3.6960 0.001249 **
                    6
                         162.862 23.2141 1.739e-06 ***
      788 5528.4
                   1
      792 5550.6 -4
4
                         -22.228 0.7921 0.530451
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
AICS:
> AIC(fit)
[1] 3873.532
  AIC(fit.1)
[1] 3863.956
 AIC(fit.2)
[1] 3842.729
> AIC(fit.3)
[1] 3837.939
The lower the AIC, the better. Fit.3 seems to be the best one here.
```

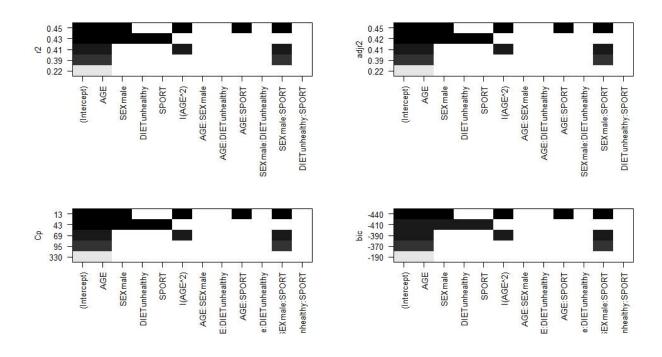
Influence points:

```
cook.d hat
       cov.r
3
      0.91_*
                0.01
                         0.01
53
54
      0.98
                0.14
                         0.13_*
      1.05_*
                0.00
                         0.03
      1.05_*
                         0.04
55
                0.00
      1.09_*
68
                0.01
                         0.08_*
      0.93_*
0.92_*
76
                0.04
                         0.05_*
79
                0.02
                         0.03
      0.98
80
                         0.05_*
                0.02
133
      0.86_*
                0.01
                         0.01
      0.81_*
192
                0.01
                         0.01
     1.12_*
0.84_*
200
                0.02
                         0.11_{-}
229
                0.00
                         0.00
231
      0.99
                0.01
                         0.03
     0.57_*
0.90_*
293
                0.03
                         0.01
308
                0.01
                         0.02
     0.95_*
1.08_*
344
                0.01
                         0.01
348
                         0.08_*
                0.01
```

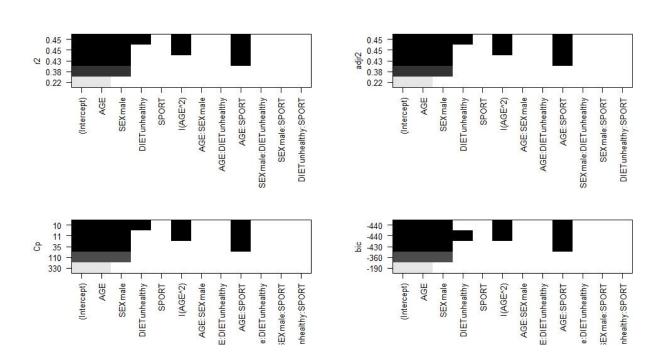
| 374 1 382 1 387 0 418 0 448 0 479 1 483 486 0 494 1 529 1 539 0 567 1 582 1 627 1 629 632 1 627 1 629 632 1 633 647 1 673 7 674 1 775 7 760 0 774 1 774 1 775 7 774 1 775 7 774 1 775 7 776 7 777 7 777 7 777 7 777 7 777 7 777 7 777 7 778 7 779 7 779 7 779 7 779 7 779 7 779 7 779 7 770 7 771 7 772 7 773 7 774 7 775 7 776 7 777 7 778 7 779 779 7 779 | .90_* .05_* .31_* .08_* .95_* | 0.00 0.00 0.00 0.12 0.02 0.22 0.44 0.00 0.02 0.06 0.15 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.01 0.00 0.00 0.01 0.00 0.01 0.00 0.01 0.00 | 0.13_* 0.04 0.05_* 0.12_* 0.04 0.07_* 0.14_* 0.16_* 0.01 0.03 0.02 0.27_* 0.05_* 0.01 0.03 0.19_* 0.03 0.02 0.05_* 0.02 0.05_* 0.02 0.05_* 0.02 0.01 0.19_* 0.02 0.01 0.19_* 0.03 0.01 0.19_* 0.02 0.01 0.19_* 0.03 0.01 0.19_* |
|--|---|--|---|
|--|---|--|---|

Next I will do variable selection based on R-squared, Adjusted R-squared, Mallow's Cp and BIC. Then I will create a robust model.

Forward stepwise selection:



Backward stepwise selection:

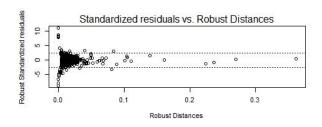


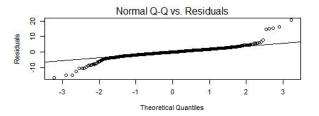
It is interesting to see that all selection criterion would drop the AGE:SEX variable. I will still run a model with all the variables, their synergetic effects and AGE to the power of 2. I chose the setting KS2014 because it is the one suggested to be state of the art in the lecture slides and in the package description of lmrob.

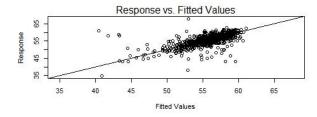
```
Call:
Imrob(formula = HOR_LEVEL ~ . - ID + I(AGE^2) + (AGE + SEX + DIET + SPORT)^2,
    data = DATA.ANA, method = "MM", setting = "KS2014")
    \--> method = "MM"
Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
1.2885500 2.0267760 35.173 < 2e-16
                                                              < 2e-16 ***
                                                     35.173 < 2e-16 ***
-5.957 3.87e-09 ***
                          71.2885500
(Intercept)
                          -0.5544452
                                        0.0930716
AGE
                          -1.3500132
                                        0.9396627
SEXmale
                                                      -1.437
                                                                0.1512
                                        0.9230052
                                                                0.2055
DIETunhealthy
                          -1.1696499
                                                      -1.267
                                        0.1274097
SPORT
                           0.1789987
                                                       1.405
                                                                0.1604
                           0.0012630
                                        0.0011009
I(AGE^2)
                                                       1.147
                                                                 0.2516
                                                       4.641 4.06e-06 ***
AGE:SEXmale
                           0.1181428
                                        0.0254573
                                                                0.9534
AGE:DIETunhealthy
                           0.0014755
                                        0.0252359
                                                       0.058
                                                       0.044
                                                                0.9646
                           0.0001555
                                        0.0035004
AGE: SPORT
SEXmale:DIETunhealthy
                           0.5117789
                                        0.2797045
                                                       1.830
                                                                 0.0677
                                                      -0.231
SEXmale:SPORT
                          -0.0101384
                                        0.0437987
                                                                0.8170
DIETunhealthy:SPORT
                           0.1009363
                                        0.0440880
                                                     2.289
                                                                0.0223 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Robust residual standard error: 1.869
Multiple R-squared:
                        0.6653,
                                  Adjusted R-squared: 0.6607
```

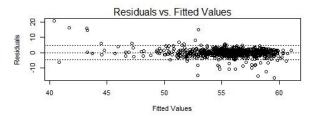
The only statistically significant variables are AGE with a negative effect, AGE:SEXmale with a positive effect when compared to females, SEXmale:DIETunhealthy with a positive effect and DIETunhealthy:SPORT with a positive effect. The adjusted R-Squared is much better here with a value of 0.6607.

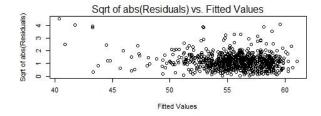
Residuals











Variables 44, 242, 364, 385, 405, 479, 500 and 645 are outliers.

