

Find the dominating set using greedy approach

Algorithm findDominatingSetGreedy
Input: A graph G with n vertices and e edges
Output: A set U , the dominating set of vertices
<pre> 1: $E \leftarrow$ adjacency matrix; $U \leftarrow []$ 2: $coveredV[1 \dots n] \leftarrow$ array used to tell if the vertex is already covered: 1 if covered, 0 otherwise Initialized as 0 for all vertices. 3: $uncovNB[1 \dots n] \leftarrow$ array used to store the number of uncovered neighbors for each vertex. Initialized as the number of neighbors + 1 (itself) 4: while sum($coveredV$) is not n do (<i>meaning there is still vertex(vertices) uncovered</i>) 5: $maxV \leftarrow$ the vertex with largest number of uncovered neighbors 6: add $maxV$ to tail of U 7: $E[maxV][maxV] \leftarrow 0$ 8: if $maxV$ has never been covered 9: $uncovNB[maxV] \leftarrow uncovNB[maxV] - 1$ (<i>minus itself</i>) 10: for i from 1 to n 11: if i is an uncovered neighbor of $maxV$ 12: remove the edge between i and $maxV$ 13: if $maxV$ has never been covered 14: $uncovNB[i] \leftarrow uncovNB[i] - 1$ 15: if i has never been covered 16: $uncovNB[maxV] \leftarrow uncovNB[maxV] - 1$ 17: for j from 1 to n 18: if there is still edge between i and j 19: $uncovNB[j] \leftarrow uncovNB[j] - 1$ 20: if j has been covered before (<i>so now both i and j are covered</i>) 21: remove the edge between i and j 22: mark i as covered 23: mark $maxV$ as covered 24: return U </pre>

p/s: the vertices which have been covered but not yet in the dominating set are still eligible to be picked into the dominating set

Driver code

Sample 1: randomly generated 100x100 adjacency matrix, the number of minimum neighbor (δ) for each vertex is 3.

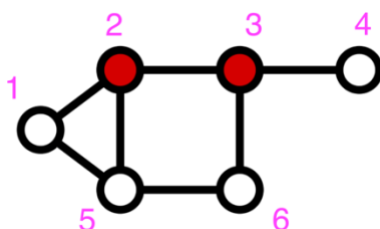
$$n = 100; \quad \delta = 3$$

Sample 2:

$$n = 6; \quad \delta = 1$$

Greedy Approach should be $2 \rightarrow 3$;

output in Python (index from 0): 1 \rightarrow 2



Sample 3:

$n = 10$; $\delta = 3$

Greedy Approach should be $1 \rightarrow 2 \rightarrow 9$;

output in Python (index from 0): $0 \rightarrow 1 \rightarrow 8$

