

Remote Heart Monitoring: A Predictive Modeling Approach for Biomedical Signal Processing

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A Thesis Submitted in Partial Fulfillment
of the Requirements for Degree of
Master of Science
in Electrical Engineering

Northern Arizona University

August 2018

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(ABSTRACT)

Smart healthcare is an emerging field with numerous research projects devoted to design electronic devices, computational methods and networking platforms aiming at facilitate technology-based health service at lower costs. Biomedical signals can directly reflect the information regarding patient health and has therefore been widely investigated by healthcare providers and the research community. The essence of most signal analysis systems is to process a large training dataset and build a reference model to assess the health status of new patients. While the majority of these methods focus on improving classification performance on pooled dataset, the predictive modeling of biomedical signals is rarely emphasized. In this work, we go one step beyond the conventional methods and intend to predict potential upcoming abnormalities before their occurrence. The objective is to build a patient-specific model and identify minor deviations from the normal signal, which can be indicative of potential upcoming significant deviations.

To enable an accurate deviation analysis, two spatial transformation methods are proposed using a controlled nonlinear transformation to reshape the feature space into a more symmetric geometry. We applied the developed algorithms on Electrocardiogram (ECG) signals and the results confirm the effectiveness of the proposed method in predicting upcoming heart abnormalities before their occurrence. For instance, the probability of observing a specific abnormality class increases by 10% after triggering a yellow alarm of the same type. This approach is general and has the potential to be applied to a wide range of physiological signals.

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Chapter 1

Introduction

1.1 Background and Motivation

Heart-related mortality rate has been increasing dramatically due to the aging of population, chronic cardiovascular diseases and increasing life stress and pace of modern life [1]. According [2], cardiac diseases are the most common cause of sudden cardiac death (SCD) with 250 000 to 300 000 mortalities in the U.S. every year accounting for 14.7% of total deaths [2]. As World Health Organization reported, 31% of global deaths are related to cardiovascular diseases (CVDs) [3]. These facts fully reflect that heart diseases are threatening the general health of human beings. Since death from CVD can occur in most cases without prior warning and obvious symptoms, it is of a great importance to enable a timely treatment of heart diseases. For this purpose, prevention principles and guidelines which covers age, family history and other potential risk factors causing CVD are deployed in most clinical modeling methods [4]. However, these methods require complex manual analysis by trained physicians. Taking this issue into consideration, developing a cost-effective automatic analysis for CVD prevention based on computer is a critical need. More specifically, since most

CVDs are accompanied with arrhythmia, accurate and timely recolonization of arrhythmia is a key factor for effective prevention of heart diseases.

Electrocardiogram (ECG) is the most common way of monitoring hearth functionality, which contains abundant physiological and pathological information that reflects the heart rhythm and status of various parts of the heart. ECG signal are recorded for the first time by Waller in 1887 [5]. It records signals generated by electrical activities of heart as a time series. As a noninvasive examination method, it is known to be highly reliable in reflecting functionality of heart. For this reason, ECG has become one of the most conventional technologies (ECG, clinical examination, radiation and ultrasonic inspection) in modern hospitals and clinics, serving as an important reference for doctors' diagnosis of heart diseases [6].

The traditional diagnosis based on ECG analysis are mainly performed by physicians through visual observation and interpretation. However, the approach costly and impractical when continuous monitoring of patients is required (e.g. to recognize CVD conditions). There are tremendous ECG records generated everyday, all demand for timely diagnosis and analysis. Due to the limitations in the access to experienced physicians, automated ECG classification systems have been introduced and became popular soon afterwards to generate real-time analysis result and provide additional information to physicians.

Several computer-based automated classification algorithms has been developed by researchers in the last decades to minimize human intervention or to assist physicians with more accurate diagnosis by reducing human mistakes [7–17]. Moreover, with the emerging application of smart health and smart cities, a constant monitoring and analysis of ECG and other physiological signals with direct experts' intervention deems impossible. Therefore, applying conventional classification algorithms on biomedical signals remains challenging, especially for applications of spontaneous disease detection.

A typical feature of cardiovascular disease is the wide range of causing factors and difficulty of recognizing some implicit symptoms before occurrence [18, 19]. Failing to predict life threatening CVDs is the principal cause of high mortality for patients with heart disease. A timely prediction of hearth abnormalities before their actual occurrences would enable a therapeutic intervention before the condition becomes detrimental, which minimizes the risk of mortality. Nevertheless, the majority of developed conventional ECG classification systems are only able to detect abnormalities when they occur. To the best of our knowledge, no research work is devoted to the prediction of heart abnormalities ahead of time, which is the main focus of this project [20, 21].

Another important property of ECG waveforms is their inherent variability among different individuals and due to different physical and environmental conditions including but not limited to gender, age, body-mass index, elevation and air pressure, humidity, temperature, and etc [22, 23]. Conventional classification algorithms do not easily generalize, when applying to different patients' records [14]. Due to the inter-patient variation in ECG signals and the complexity of cardiac pathological information analysis, most of the existing ECG analysis software only serve as auxiliary devices for physicians. The final results of diagnosis still depend on manual labeling by cardiologists. Recently, several novel patient-specific ECG analysis methods are proposed. Broadly speaking, in these methods systems parameters are adaptable according to individual ECG signal properties [12–17]. Some algorithms combine cardiologist manual annotations with automatically generated labels and train personal classifier with updated labels for each individual [12–14]. This design still requires experts' assistance in order to accurately classify ECG signal. Another design in to train a patient-specific classifier using only the patient's ECG signal. Whereas this method fails when a certain type of abnormal signal is not included in the limited personal ECG signal data.

The automatic analysis of ECG signals includes a wide range of techniques. In this work,

we focus on overcoming the two drawbacks of existing automatic ECG classification systems, namely the failure in capturing patient-specific variability and the lack of predictive power. This research aims at improving the inter-patient classification performance and prediction capability of ECG-based diagnosis methods. Our proposed method can revolutionize the current practice of healthcare service by enabling early detection of heart abnormalities, with applications to high-risk people, senior people, and athletes. It also can significantly reduce the mortality rate of SCD.

1.2 ECG and Arrhythmia

Electrocardiogram is widely used to monitor the electrical activities of heart and assist diagnosing fatal cardiac diseases. In order to design algorithms specifically for ECG analysis, it is important to develop an insightful perception of the functionality of heart and ECG waveforms.

1.2.1 Characteristics of ECG signal

A ECG signal reflects the periodical electric signals generated by a heart. Fig.1.1 demonstrates the typical signal waveform for a cardiac cycle (i.e. a heartbeat), which is usually composed of three main waves including P wave, QRS complexes and T wave. These waves corresponds to different physiological activities of the heart. P waves are generated by atrial depolarization which represents the process of pumping blood to ventricles. QRS complexes as the most significant electric activities are caused by the *Ventricular* contraction, which is the process of pumping blood to lungs and the rest of the human body. Finally, T waves are the result of *Ventricular* repolarization, which is a required recovery process before the

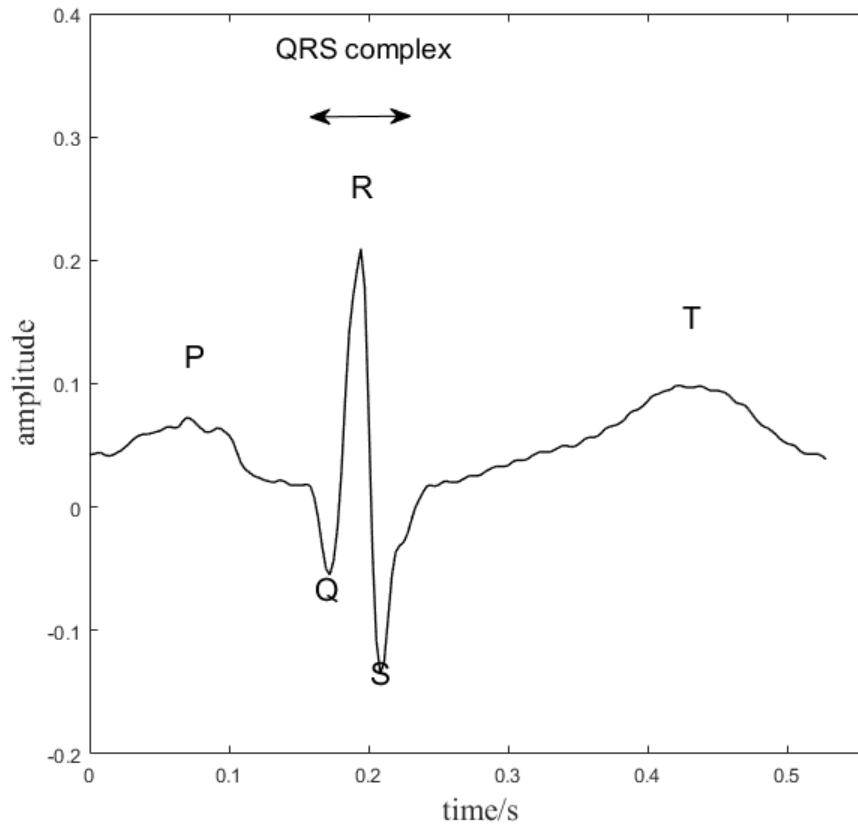


Figure 1.1: A typical cardiac cycle in ECG signal with five characteristic waves.

following cardiac cycle. Accurate detection and segmentation of each wave is necessary for a profound ECG analysis. The waves are usually represented by their peak locations, also called fiducial peaks. By detecting the most significant peak within QRS complexes (e.g. R peak) automatic algorithms are able to discriminate between two adjacent cardiac cycles. The interval between two R peaks is called RR interval, which is also the inverse of heart rate. Fig.1.1 represents a typical cardiac cycle with the aforementioned intervals.

1.2.2 MIT-BIH Arrhythmia Database

Arrhythmia is related to various morbid behaviors of heart. Generally speaking, arrhythmias consist of two main categories: *supraventricular* and *ventricular*. *Ventricular* ectopic beats imply abnormal activities in the ventricles while *supraventricular* ectopic beats are related to the *atria* [24]. Both categories contains fatal abnormal beats, which may lead to death [25]. Therefore, in order to help researchers standardize the evaluation of works on ECG classifiers, Association for the Advancement of Medical Instrumentation (AAMI) has proposed recommendations for reporting ECG classifier performance [26]. According to these recommendations, MIT-BIH Arrhythmia Database (MITDB) is regarded as a standard database to train and test ECG classifiers in the last two decades. MITDB is a public database which is available on Physionet.com [27] since 1997 [28]. There are 48 records collected from 47 individuals in this database. Each record contains two channels of ECG raw signals along with annotations for each cardiac cycle. Annotated labels include 16 types, as shown in Table 1.1. Cardiac cycles are determined by the locations of R peaks. The sampling frequency of MITDB is 360Hz and the signal frequency spans from 0.1 to 100 Hz.

Following the recommendations by AAMI, the original annotations of MITDB are further grouped into 5 major classes: class N(*normal* and *bundle branch block* beat types) class V(*Ventricular* type), class S(*supraventricular* type) and class F(fusion of normal and *Ventricular* types). The class Q which includes unclassified and paced beats are discarded due to the limited number of samples. Table.1.1 summarizes the mapping from 16 original types that include cycles of this type. Therefore, only 4 remaining types (N, V, S, F) are typically used.

Table 1.1: Mapping from 16 original types in annotation to the standard 5 types recommended by AAMI

Standard Types by AAMI	Original Types in MITDB Annotation
N	NOR, LBBB, RBBB, AE, NE
V	PVC, VE, VF
S	APC, AP, BAP, NP
F	VFN
Q	PACE, FPN, UN

1.3 Problem Statement

ECG signals are investigated broadly by researchers to design automated non-invasive diagnosis methods and real-time monitoring systems [17, 29, 30]. As described in the previous section, a majority of current methods suffer from two main challenges: i) failure to capture inter-patient variability and ii) incapability of early detection and prediction.

In conventional classification systems, the training dataset is typically composed of records collected from different patients with experts' annotations per heartbeat. In order to unify the records from different patients, most of the conventional classification algorithm mix heartbeat samples from different individual ECG records and cluster the pooled ECG dataset simply based on the annotations of heartbeats. Since the classification performance is measured based on the comparison between the predicted labels with the annotate (true) labels for each sample, the classifiers are trained to improve the performance on pooled ECG data. While ECG signals shares similar morphologies, the signals from different patients demonstrate considerable variability as shown in Fig.1.2. Ignoring this difference will lead to inconsistent classification performance between patients. Therefore it's of significant importance to adjust classifier configuration according to patient-specific characteristics.

In addition to the inter-patient variability, majority of ECG classification algorithms fail to provide a predictive capability, which refers to the power of triggering corresponding alarms

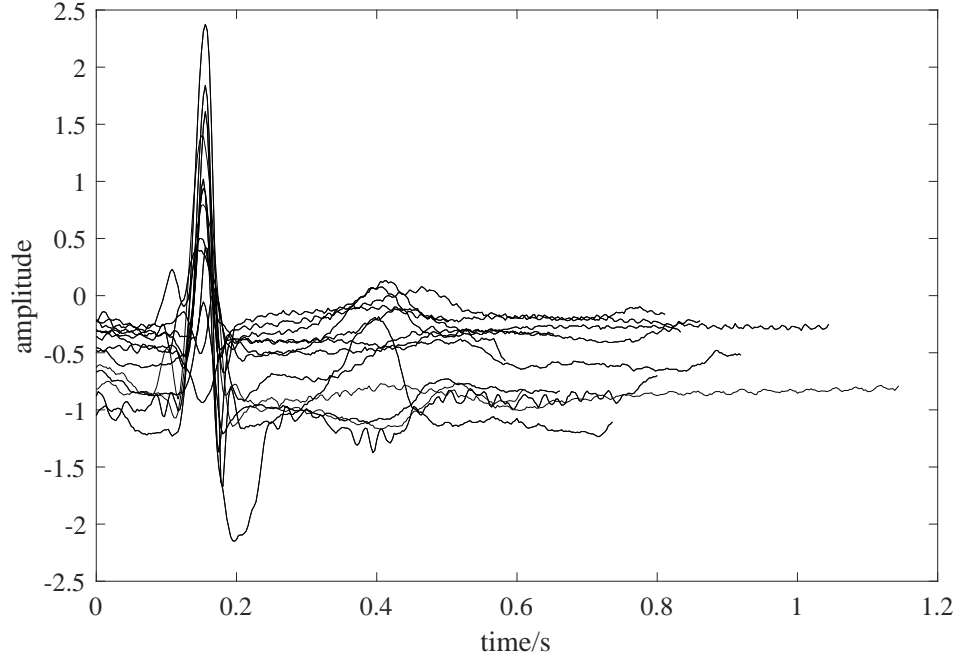


Figure 1.2: ECG signals of normal heartbeat from 15 different records in MIT-BIH reflect the inter-patient variability of ECG signal.

before the occurrence of abnormalities. Typically alarms represent significant distortions in the ECG morphology which reflect a severe heart abnormality. The rest of heartbeats considered as *normal* beats. However, an abnormal beat may include mild distortions that can be indicative of a problem, while it is not severe enough to call a *red alarm*. In this work, we represent these minor deviations with *yellow alarm* and use them to predict real abnormalities as *red alarms*, before their actual occurrence.

Fig.1.3 illustrates this concept, where observation of minor deviations from the patient-specific normal trends (yellow alarms) can be indication of upcoming severe abnormalities (red alarms). Supporting results are provided in Section 3.4 and Section 4.6. Therefore, a method to quantify the level of signal similarity to abnormalities should be incorporated into the ECG classification system.



Figure 1.3: A potential latent abnormal status(yellow alarm) predicts an upcoming abnormality of the same type.

1.4 Literature Review

Automatic analysis of ECG signals refers to the entire process spanning from the acquisition of signals to the classification of samples. This process can be divided into five stages: ECG signal acquisition, preprocessing, fiducial peak detection and segmentation, feature extraction and predictive modeling (Fig. 1.4). Different research works focused on one or multiple stages of the automatic analysis system. Since the main objective of this work is addressing problems in classification algorithms, the literature reviews in this section focuses on studying existing methods proposed for stages before classification, conventional classification algorithms along with patient-specific classification systems.



Figure 1.4: General structure of ECG analysis system.

1.4.1 ECG Signal Preprocessing

During data acquisition, the ECG signal may be affected by different kinds of noise including physiological noise (e.g. myoelectricity noise, breathe interference etc.) and non-physiological noise (e.g. power-frequency interference and electrode impedance interference) [31]. These noises often interfere with the informative signal and thus influence the ECG classification results. Therefore, ECG signal preprocessing mainly focuses on the suppression of noise and interference terms in the ECG signal.

The ECG signal is in millivolt (mV) level with a central frequency ranging from 0 to 40 Hz [32]. Due to the relatively low signal to noise ratio in ECG signals, signal preprocessing is a necessary step before classification. Therefore, various methods are proposed to eliminate noise and other artifacts from the ECG signal [31–38].

Generally speaking, ECG signal preprocessing methods includes finite impulse response (FIR) filtering, adaptive filtering, and modern signal processing filter methods such as wavelet transforms and neural networks [31, 34, 35, 38]. YW Bai *et al.* compared different notch filters and concluded that equiripple notch filter outperforms other methods in terms

of noise reduction and CPU time [34]. Lian *et al.* [33] designed a multiplier-free finite impulse response (FIR) filter to suppress biological and environmental noises with a low power consumption. Sayadi *et al.* proposed a modified extended Kalman filter with estimated hidden state variables to perform denoising and compression at simultaneously [35]. Park *et al.* designed a wavelet-based adaptive filter to reduce S-T segment distortion due to the baseline drift and compared its performance with general adaptive filters [36]. A general conclusion is that the performance of wavelet adaptive filtering is usually higher than generic adaptive filters. In [37], the authors combined wavelet decomposition with Wiener filtering to filter out the noise by thresholding, which is proved to outperform other thresholding denoising methods. Regarding various wavelet basis functions, Singh *et al.* studied an optimal selection of basis functions for ECG signal denoising [31]. By comparing the classification root mean square error using the same classifier and different denoising methods, they concluded that Daubechies filter of order 8 is the best choice for ECG classification system.

1.4.2 Fiducial Peak Detection and Segmentation

Fiducial Peak Detection and cardiac cycle segmentation are the basis for extracting important information from ECG signals, since a ECG record is usually a continuous time signal. This signal can be split into smaller intervals, each of which representing one cardiac cycle. Each cardiac cycle can be viewed as an independent signal and is associated with a separate label to represent the heart function during the corresponding interval. The accuracy and reliability of this stage directly determine the final performance of diagnosis and analysis.

Fiducial peak detection, which is also called ECG signal delineation, aims at localizing five characteristic peaks within one cardiac cycle. The most significant peak is the QRS complex consisting of Q, R and S peaks. The other two fiducial peaks include P wave before the QRS

complex and T wave after the QRS complex. As shown in Fig.1.5, these five characteristic waves along with the onset and offset of the QRS complex are often used to present a cardiac cycle.

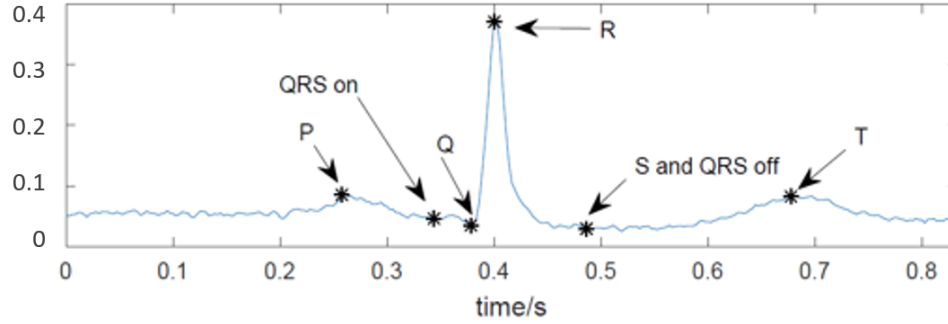


Figure 1.5: Fiducial peaks within one cardiac cycle.

The QRS complex is the most prominent wave and it contains the majority of the information of a ECG signal; therefore, most of the ECG delineation methods detect QRS complex prior to the detection of other peaks. Afonso *et al.* proposed a method using filter banks to detect QRS complexes [39]. In this method, the signal is decomposed to several frequency bands. Fiducial peaks are thus detected using its morphological features in the decomposed signals. Sadhukhan *et al.* proposed a method of detecting R peak by thresholding the double difference signal of ECG data and comparing the relative amplitude within QRS region [40]. The performance of this method is validated using clinical ECG signals and has been proven to be promising. Some advanced machine learning techniques are also deployed to detect QRS complexes. In [41], *Support Vector Machine* (SVM) is used to train a predictive model for QRS complex detection and achieved 99.93% accuracy. Other pattern recognition methods such as *Hidden Markov Models* (HMM) are investigated and proved to be efficient in modeling and detecting characteristic peaks in ECG signals [42]. Wavelet decomposition is also frequently adopted for signal delineation due to the morphological similarity between wavelet basis functions and QRS complexes. As the QRS complex power

spectrum is centered at the range of 5 to 30 Hz, the wavelet coefficients of the corresponding scale levels are frequently used for delineation purpose. In [43], QRS complexes are detected by thresholding wavelet coefficients at scales 1 to 4, then onset, offset and individual waves within QRS complexes are detected using the morphological characters of coefficient at scale 2. T and P waves are detected at scale 3 with a similar method approach. In the literature, some improvements have been proposed to eliminate false detection of R peaks by adding a fixed searching window of 160ms [44].

1.4.3 Feature Extraction and Classification

After localizing the fiducial peaks within a cardiac cycle, we proceed with the next step of extracting informative features of the signal, which collectively convey meaningful information about the signal properties. Since the objective of designing an automatic classification system is to precisely predict types of sample signals, feature selection is usually performed to obtain a better performance and reduce the computation cost [7–11].

As the most significant wave within a ECG signal, the information of QRS complexes are proved to be the most important features for ECG classification systems. Lagerholm *et al.* decompose QRS complexes with a set of Hermite basis functions and the decomposition coefficient are deployed as ECG features to train a Self-Organizing Map (SOM), which achieved an average error rate of 1.5% for 16 ECG types [7]. Prasad *et al.* used discrete wavelet transform (DWT) to extract RR intervals between the current beat and previous or next beats. The two RR-intervals serve as input for training a neural networks, which achieves the average accuracy of 96.77% in classifying 13 different arrhythmia types. De Chazal *et al.* proposed two set of features: morphology and heartbeat interval features. They used different combinations of these features combined with Linear Discriminant Analysis to clas-

sify ECG signal into five arrhythmia types and selected the optimal feature set according to classification performance [9]. The result shows that the sensitivity of detecting two major arrhythmia types can be improved by feature selection. R. Ceylan *et al.* included RR interval as the only ECG feature to train a fuzzy clustering neural network that achieved an average detection rate of 98.35% [10]. Osowski *et al.* proposed two set of features including *Higher Order Statistics* (HOS) and Hermite characterization of QRS complex to classify ECG signals with Support Vector Machine. Their final average error rate is at 1.82% [11].

1.4.4 Patient-Specific ECG Classification

The main drawback of the majority of aforementioned methods mentioned in the last section is the lack of inter-patient model adjustment. In order to generalize the ECG classification system to clinical applications, several methods which are more robust to inter-patient signal variation are proposed to address this issue [12–17].

Hu *et al.* proposed a patient-specific Mixture of Experts (MOE) classifier by incorporating personalized annotations provided cardiologists in the local classifier [12]. The methods achieves patient-adapting capacity but requires further input from human experts. This MOE approach achieved an accuracy of 94.0% for distinguishing *Ventricular* beats from the other non *Ventricular* types. Following the design of MOE, de Chazal and B. Reilly proposed an improved patient-adapting classifier by reducing the requirement of manual annotations to as few as 10 beats for training adaptive local classifier [13]. And Llamedo et al. designed an automatic classification system, which uses experts' assistance, but does not fully depend on the experts and can work independently [14]. By implementing a special block-based neural networks (BbNNs), Jiang et al. achieved accuracies of 98.1% and 96.6% in distinguishing *Ventricular* ectopic beats and *supraventricular* ectopic beats from other types [15].

In [16], particle swarm optimization (PSO) is combined with a neural network to optimize the network structure using patient-specific training data. Based on 1-D convolutional neural networks (CNN), Kiranyaz et al. proposed a flexible algorithm, which adjusts its parameters using information extracted from individual signals [17]. The classifier demonstrates consistent performance over different ECG records achieving an accuracy between 98% and 99% for distinguishing VEBs from non-VEBs. (Acc = 98.9% Sen = 95.9% Spe = 99.4%). While this approach outperforms the aforementioned classification algorithms as it does not require expert further annotations, its performance reduces for some rare abnormal classes.

1.5 Contributions

A crucial drawback of these patient-specific classification systems, recently proposed in the literature, is their failure in predicting abnormalities in advance. These methods aim at improving classification performance by comparing generated labels with a ground truth for each beat and ignore the relationship between the generated labels and upcoming abnormalities. While in many common applications this approach generates satisfying results, it does not meet the needs of SCD prediction.

One of the main objectives of this work is to address the problem of forecasting by proposing the concept of yellow and red alarms and proving the fact that yellow alarms can be indicators of upcoming red alarms. Yellow alarms are defined through a novel deviation analysis which assesses the tendency of deviant normal alarms to one of the red alarm. In order to realize such a deviation analysis, symmetry of different abnormality classes in feature space is desired. We propose a novel controlled nonlinear transformation that maps the original feature space into a new space that presents the desired symmetry. To elaborate more on the symmetry of abnormal classes in the feature space, we assume that there are one nor-

mal class and multiple abnormal classes for a signal while latent states exists for some of the normal samples that represent slight deviations towards abnormalities. By distinguishing latent states, the designed automated system is capable to generating a yellow alarm which indicates a high probability of the presence of some upcoming abnormalities (red alarms) of the same type. Therefore, the contribution of this work can be summarized as:

- Propose a novel self-configuring patient-adaptive framework which incorporates a personal classifier into the predictive modeling;
- Utilize a kernel-based method as a spatial transformation with parameters optimized using multi-objective particle swarm optimization (MOPSO) for the purpose of deviation quantification;
- Design a controlled spatial transformation with deterministic mapping function to optimize cluster topology for predictive analysis
- Propose a deviation quantification method based on cosine similarities, which is capable of generating red alarms for upcoming abnormalities

1.6 Organization of Thesis

In the following chapters, details of the proposed classification framework are presented after reviewing the introductory concepts and related works. Chapter 2 provides a general information about the utilized ECG dataset and the general framework used in proposed classification system. Chapter 3 describes the details of nonlinear transformation with kernel methods and presents the experimental results using kernel transformation. With the concept of nonlinear transformation, chapter 4 introduces an optimized spatial transformation with a

novel deterministic mapping function. The experimental result for the spatial transformation method is presented section 4.6. Finally, the experimental results for the proposed methods in chapter 3 and chapter 4 are studied and compared. More importantly, the predicting capacity of the proposed system is studied and analyzed in this chapter. Based on the experimental results, we introduce some potential directions to further improve the system in terms of classification and predicting accuracy.

Chapter 2

Patient-Adaptable ECG Classification Framework

2.1 Introduction

For decades, automatic ECG signal analysis has been a controversial research topic. Several academic research projects have proved that the design and implementation of automatic ECG analysis methods is beneficial for timely detection and therapeutic intervention of heart diseases. However, some major challenges should to be resolved, and automatic ECG analysis should reach a level of maturity and reliability before getting ready for clinical use. One of the most typical challenges is the inherent inter-patient variation of ECG waveforms, which leads to inconsistent performance of ECG classification systems when applied to different patients under different conditions. In this chapter, the details of the patient-adaptable ECG classification method, as the core of the proposed framework are presented.

The goal of automatic ECG analysis is to determine the arrhythmia types for each signal

sample. Continuous ECG signal is firstly segmented into individual intervals, each of which represents a heartbeat cycle, to be processed by the further stages of the proposed algorithm. Section 2.2 and Section 2.3 in this chapter focus on the data preparation stage, which includes four steps: signal preprocessing, delineation, segmentation, and feature extraction. Following the data preparation, Section 2.4 elaborates on the details of the proposed two-stage hierarchical classifier. The proposed classification system introduces a novel method for patient-adaptation by gradually capturing the normal range for each individual. More specifically, in Section 2.4, the dynamic normal cluster shaping method to achieve rationalization property is discussed. One feature of this method is that the cluster can track a patient’s ECG waveform changes and dynamically adapt to it. In many applications, the physicians need to monitor a long-term real-time heart activity. This dynamic adaptation is able to address the issue of intra-patient temporal signal variation as well.

2.2 Utilized Dataset

Since the quality of ECG signals provided by most of the portable ECG measuring instruments is very unstable and may include transient noises. Signals transmitted through wireless communication systems will exhibit even more unstable waveforms. These transient effects appear in the resulting feature vector and consequently they negatively affect the prediction accuracy of the subsequent ML method. In order to eliminate and smooth out these transient terms, we use the concept of *segmentation* here, where each segment includes multiple cardiac intervals, as shown in Fig. 2.1. *Note that the number of cardiac cycles in each segment is a modeling parameter shown by s_{window} . Also, we can arbitrarily slide segments equivalent to n_{steps} cycles to generate the new feature vector. The parameters s_{window} and n_{steps} can be tuned to improve the overall performance of the method. Based on intensive simulations, we*

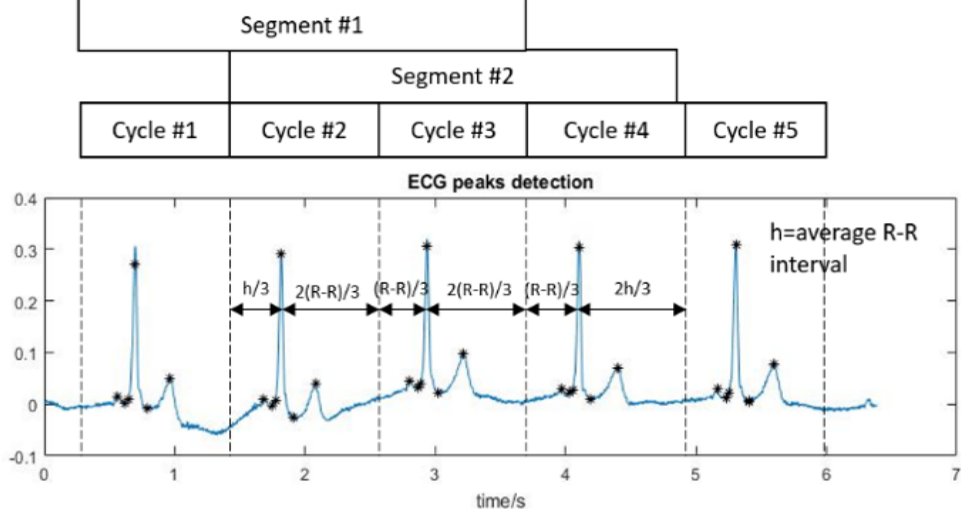


Figure 2.1: Segment samples correspond to three consecutive cardiac cycles.

choose $s_{window} = 3$ and $n_{steps} = 3$, which yield the best classification accuracy. In Fig. 2.1, we have $s_{window} = 3$ and $n_{steps} = 1$.

For the purpose of training and evaluating classifier, MITDB is split into test (DS2) and training (DS1) set by balancing the four classes according to [9].

The ECG signals in MITDB dataset are annotated and labels are provided for each cardiac cycle. However, we define a segment, which may include more than one cycle as a sample. Therefore, we need to translate per-cycle labels into per-segment labels. In this regard, a new label for each segment is generated by integrating all annotations of the beats within the segment. The segment is labeled as *normal*, if all member beats are annotated as N; otherwise, this segment will be labeled as the abnormality type of its member cycles if there is only one abnormality type. If more than one abnormality types are present within the same segment, the segment is excluded. For instance, segments with member cardiac cycles labeled "NNN", "SSS", "NVV", "VVV" are respectively mapped to "N", "S", "V", and "V", and a segment with member label "NVS" is discarded. After segmentation and new annotation, the total number of samples in the training and test set are obtained as

Table 2.1: Training and test datasets in MITDB.

	Number of segments per AAMI class				
Evaluation Dataset	N	V	S	F	Total
DS1:Training	11721	2356	862	256	15195
DS2:Test	12633	2053	550	121	15357
Total	24354	4409	1412	377	30552

summarized in Table 2.1

2.3 ECG Signal Processing

2.3.1 Preprocessing

Biomedical signals, such as ECG signals, are composed of a sequence of signal segments, that can be presented by a set of statistical, morphological, and spectral features. Since the signal properties change over time, the traditional Fourier transform is not suitable for this type of non-stationary signals since it is unable to capture time-varying statistics of the signal. Wavelet decomposition solves this problem by scaling and translating mother wavelet to constitute its basis functions, which capture both spectral and temporal properties of the signal. Given a time series, wavelet decomposition decomposes the signal into linear combinations of basis functions. Thus, basis functions with larger scales are smoother than those with smaller scales and consequently correspond to lower frequency components of the signal. Similarly, the coefficients of the decomposition correspond to higher frequencies when the scale is smaller. Using wavelet decomposition, we extract both time and frequency features of the signal.

In this work, wavelet analysis is applied to ECG signals in MITDB with a sampling frequency of 360 Hz. Daubechies wavelet of order 8 (*db8*) is selected as mother wavelet for denoising stage in this work for its optimal performance [31]. The decomposition coefficients and their

corresponding frequency components are presented in Fig. 2.2.

Low frequency noise or baseline wander between 0.15 to 1 Hz, caused by respiration and body movement, can be removed by deducting the approximation coefficient of level 8 (A_8) from the signal. Since the power of ECG signal is mainly concentrated in the frequency band from 1 to 40 Hz, higher frequency terms are more likely to represent noise terms including electromyogram induced noise and mechanical forces acting on the electrodes. These terms can be removed by discarding the detail coefficient of level 1 (D_1).

2.3.2 Segmentation

Most machine learning (ML) algorithms operate on input vectors and are not directly applicable to continuous-signals. Therefore, biomedical signals are typically converted to a representative vector before incorporating to ML algorithms. We follow the common trend of translating a signal segment into a vector of representative features. In this regard, we first need to split the signal in time domain into smaller segments. To obtain more relevant results, we choose the segments as one or multiple consecutive cardiac samples, noting the fact that each cardiac cycles is associated with a label based on experts observation.

Most existing methods use wavelet analysis to detect the highest peak (R wave) in a cardiac cycle as a reference point and then use signal morphology and typical properties of other waves to determine boundaries between consecutive intervals [20, 44–46]. In this study, we use this common approach. As was mentioned earlier in Section 1.4.2, a cardiac cycle consists of five basic characteristic peaks: P, Q, R, S, and T. Among them, the QRS complex is the most significant peak in one cycle. The energy of ECG signal in one cardiac cycle is mainly concentrated within the QRS complex. The QRS complex also conveys important information that reflects the arrhythmia category [45]. Accurate detection of the QRS complex is

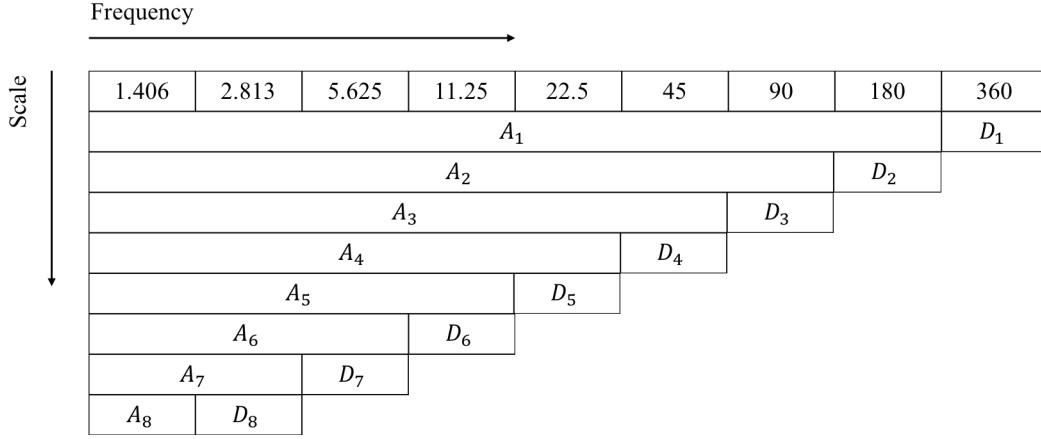


Figure 2.2: Frequency band of wavelet decomposition coefficients for MITDB signals.

of crucial importance for subsequent analysis. The energy of the QRS complex is generally within the range of 5-25 Hz. For ECG signals with sampling frequency of 360Hz, the QRS complex can be extracted from the detail coefficients of level 5 (D_5) and level 6 (D_6)

The mother wavelet *db4* is utilized at this stage due to its morphological similarity to QRS complexes [43]. By superimposing D_5 and D_6 , the QRS complex information in the ECG signal can be characterized in a one-dimensional recombined signal ($QRS_DET = D_5 + D_6$). Other Fiducial peaks (P, QRS onset, Q, S, QRS offset and T waves for each cardiac cycle) are localized according to an algorithm proposed in [45]. The accuracy of peak detection and its coincidence with the true signal are shown in Fig. 2.3.

With the empirical values described in [45], we use 15% of the highest amplitude within the signal as the detection threshold. Since the width of most of the QRS complexes does not exceed 160ms, here we use a sliding window with a width of 160ms to detect the peaks in the QRS_DET . The window step size is set to 200ms, given that the time lag between the two adjacent heartbeat cycles does not exceed 200ms. Fig. 2.4 shows a typical QRS_DET waveform along with the corresponding window of width 160ms. The false peaks are eliminated using a 160ms time window, as seen in Figure.2.4.

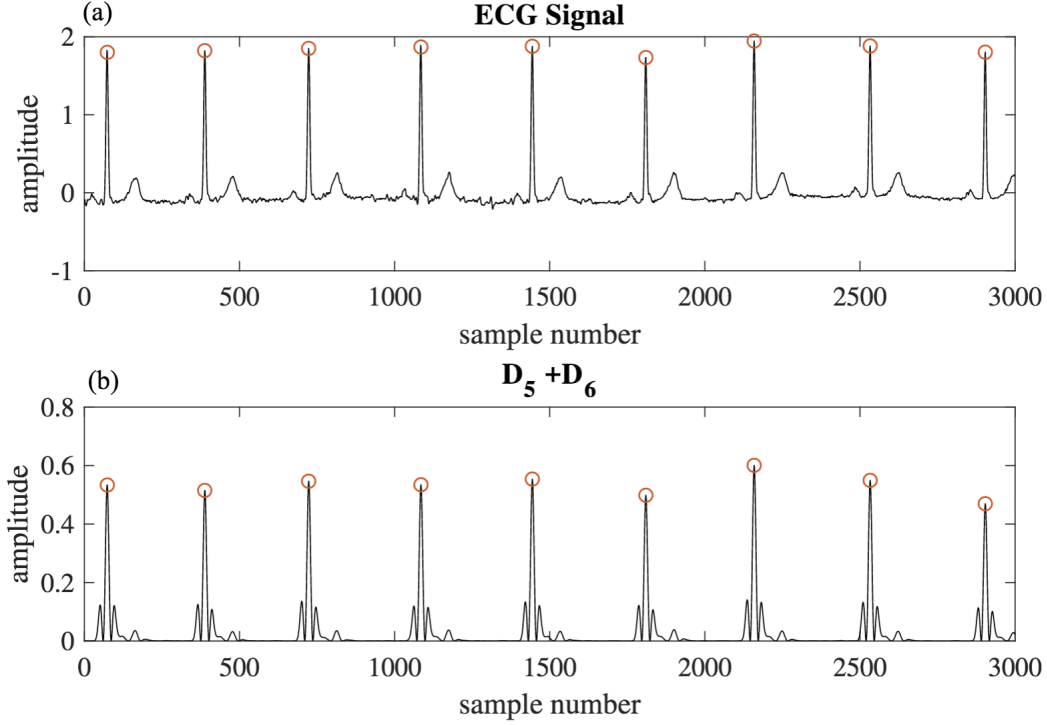


Figure 2.3: (a): the detected R peak location within original ECG signal; (b): corresponding R peak location within the combined signal ($QRS_DET = D_5 + D_6$).

The T and P waves are outside the QRS window. Through scanning the region spanning from the offset of the precedent QRS window to the onset of the current QRS window, the P-wave is located as the highest positive peak in this region. In a similar way, the position of the T wave is obtained by finding the maximum of the signal in the region between the offset of the QRS in the current cardiac interval to the onset of the next cardiac interval. In an alternative way, the two peaks between the two consecutive QRS windows, respectively represent the T and P waves. In short, an ECG signal in one heartbeat segment can be fully described by 7 feature points: P, QRS on, Q, R, S, QRS off and T.

After localizing the fiducial peaks, we can use the location of R peaks to determine the boundaries of a cardiac cycle. By processing a large number of ECG signals, we realize that R peaks approximately split cardiac cycles into two pieces with $1/3$ and $2/3$ of the entire

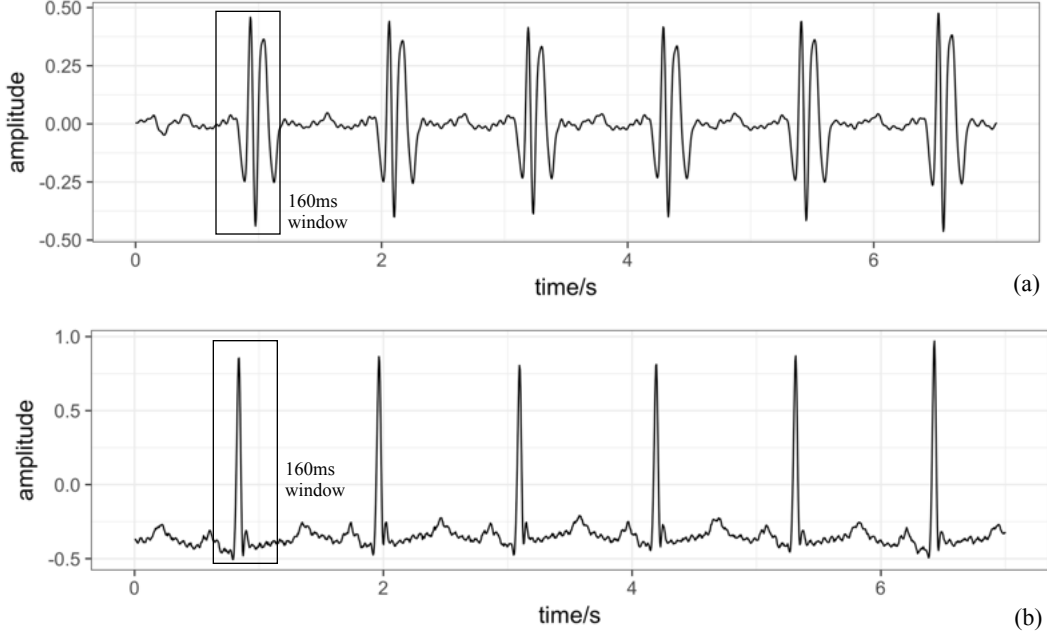


Figure 2.4: Window for detecting R peaks within QRS complexes.

signal [45]. Based on this observation in the morphology of a typical ECG signal, we define the starting point of a cardiac cycle as the point which divides the distance between the two consecutive R waves into two sections, where the length of the first section is half the length of the second section, as depicted in Fig. 2.1. In this figure, the average interval (RR) between the two adjacent R waves is denoted by h , therefore R wave is located in distance $h/3$ with respect to the beginning of the cycle. The advantage of this method is its low computational complexity and easy generalization to different patients, noting that a slight change in cardiac boundaries do not significantly alter the properties of a cardiac cycle as long as T and P waves remain in the correct interval.

2.4 Feature Extraction

The feature extraction step plays a crucial role in the diagnosis of heart disease and has a great influence on the performance of the subsequent automated classification systems. De Chazal et al. have studied the impact of using waveform morphological features on classification results [9]. As discussed in [20], the combination of three types of characteristics (i.e. temporal, morphology, and frequency domain features) can provide a better discriminative power for the classification algorithm to distinguish between different types of arrhythmia.

According to several studies different types of ECG signals mainly differ in the power level of the frequency band ranging from 5 Hz to 15 Hz [43]. Likewise, some other temporal features (such as the duration between the Q wave and the T wave, the P wave to the R wave, etc.) present different levels of correlation with a specific signal classes [9]. Therefore, we choose to use the combination of temporal, morphological and spectral features as detailed in Table 2.2. Moreover, to account for segment-level characteristics as well as cycle-level properties, the extracted features include both cycle-based features (SET 1) and segment-based features (SET 2). SET1 includes the average and standard deviation of the corresponding features of the three cardiac cycles within a segment, and SET2 contains the overall characteristics of the time signal within a segment, so it is calculated only once per segment. Therefore, we have a total of $8 \times 2 + 6 = 22$ features per segment as shown in Table 2.2. Therefore, each feature vector is a 221 vector with zero-mean unit-variance elements after a proper normalization. In Table 2.2, $\text{mean}(R_{i+1} - R_i)$ refers to the mean of the time lag between two adjacent R waves, while $(R_i - R_{avg})$ is the length of each cardiac cycle and the average cardiac cycle duration of the patient.

From Table 2.2, one may notice that these 22 features are not completely independent of each other. Also, some of the features may not be as relevant as the others. Therefore, we

Table 2.2: Features extracted from ECG signal

Feature Type	SET1	SET2
Temporal Features	<ul style="list-style-type: none"> • QRS duration • QT duration • PR duration 	<ul style="list-style-type: none"> • $\text{mean}(R_{i+1} - R_i)$ • $\text{mean}(R_i - R_{avg})$
Morphological Features	<ul style="list-style-type: none"> • max positive peak to second peak ratio 	<ul style="list-style-type: none"> • signal average energy • max positive peak • max negative peak • peak to energy ratio
Frequency Domain Features	<ul style="list-style-type: none"> • signal power level at 7.5Hz, 10Hz, 12.5Hz, 15Hz 	

reduce the number of features to obtain a more robust predictive modeling [9, 14]. We use Principal Component Analysis (PCA) as a commonly used the common dimension reduction method instead of explicit feature selection for its improved performance in biomedical signal processing [47]. We keep the 8 dominant directions of the signal after PCA as the most informative 8 features.

2.5 Classification Framework

In this section, we elaborate on the details of the proposed methodology to perform the classification and prediction tasks using the preprocessed ECG data. Based on our previous study [29] as well as similar prior works on developing patient-specific classifiers [12–14], we propose a two-staged structure which includes a global classifier to capture general properties of different classes followed by a personalized classifier to capture patient-specific properties [12–14, 29]. Moreover, the proposed algorithm incorporates a novel deviation analysis module with details presented in the following sections.

2.5.1 Global Classifier

The flowchart in Figure 2.5 presents the overall operation of the proposed system. The *global classifier* is trained using the whole training dataset as the first classification step. It facilitates the subsequent analysis in the system by identifying samples with severe morbidity. Depending on the application (properties of signals, the utilized labels, and the choice of features), different classification algorithms can be utilized [12, 14]. Two important considerations include the classification accuracy and the computation complexity of the method [14]. Any abnormal label generated by the global classifier is considered as a *red alarm* and does not require further processing. However, samples labeled as *normal* go through the subsequent personalized classification step.

2.5.2 Deviation Detection

Since, one objective of this study is to identify the fuzzy states between normality and abnormalities, the subsequent analysis is focused on processing samples classified as *normal*(N) to check whether or not they show considerable deviations towards one of the abnormality classes. For this purpose, a one-layer classifier is not sufficient due to multiple reasons: i) the numbers of samples in the normal and different morbid classes are not balanced in the training set DS1 as shown in Table 2.1, ii) the patient-specific normal trend is unknown, iii) detecting yellow alarms require a new set of decision rules to determine whether or not the deviations are worthy of calling a yellow alarm. Therefore, a deviation detection module is added after the Global Classifier to identify fuzzy state between normality and abnormalities using patient-specific normal cluster. In order to develop a ground for patient-specific normal functionality and adapt the classifier accordingly, the first 20% of total Normal samples of each patient are selected as the initialization of *personalized dynamic normal cluster* \mathcal{N}_0^k . As

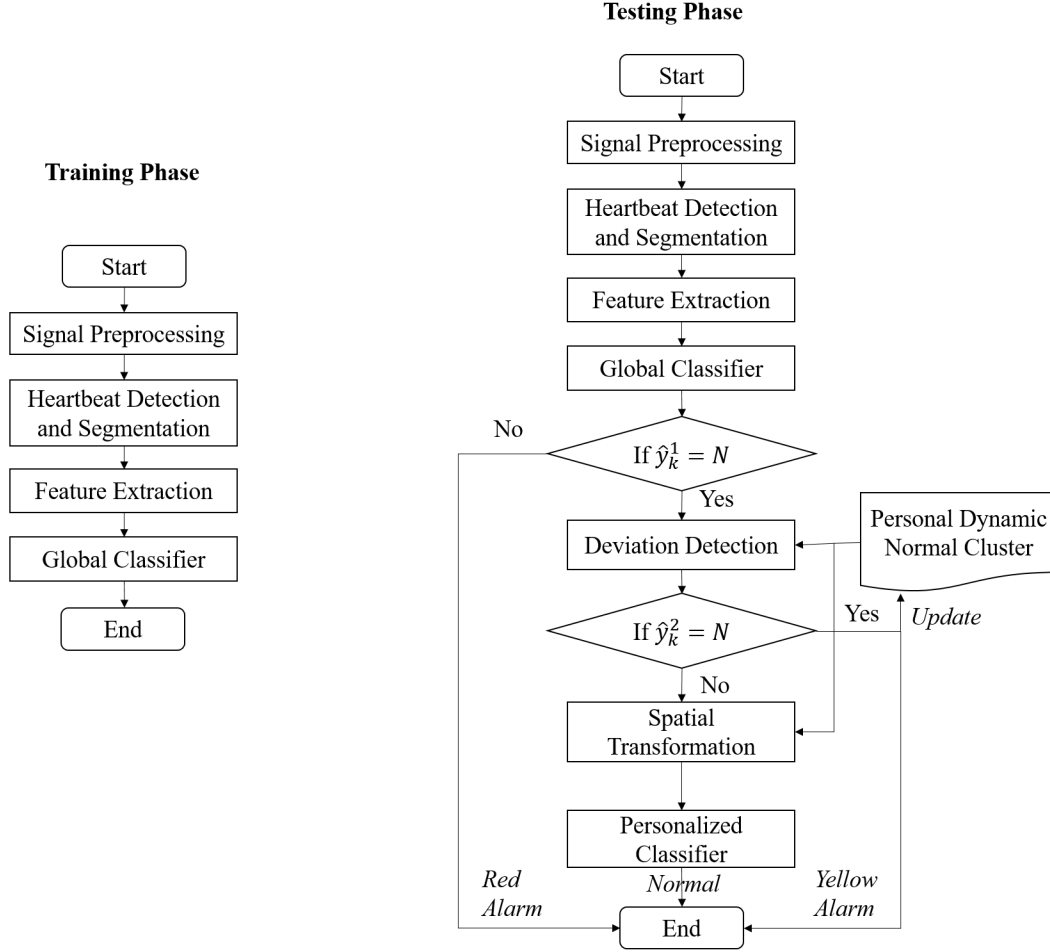


Figure 2.5: The general flowchart of proposed framework.

we collect more samples from the patient, the samples which are newly classified as N class will be used to update the personalized dynamic normal cluster. Therefore, if a sample $\mathbf{x}_k(i)$ is classified as N after deviation detection and the *mahalanobis distance* between $\mathbf{x}_k(i)$ and the centroid of personalized dynamic normal cluster \mathbf{c}_N^k is less than 2, then $\mathbf{x}_k(i)$ is included in the updated \mathcal{N}_i^k . mahalanobis distance quantifies how many the standard deviation away $\mathbf{x}_k(i)$ is from \mathbf{c}_N^k , it can be formulated as follows:

$$d_{\text{mahal}} = \sqrt{(\mathbf{x}_k(i) - \mathbf{c}_N^k)' \mathbf{S}^{-1} (\mathbf{x}_k(i) - \mathbf{c}_N^k)} \quad (2.1)$$

where \mathbf{S}^{-1} stands for the covariance matrix of \mathcal{N}_i^k .

To distinguish between normal state and fuzzy state, we use a binary classification of N versus non-N, where the second includes all abnormal classes. We firstly calculate the following distance metrics:

$$R_i^{\max} = \max_{\mathbf{x}_j \in \mathcal{N}_i^k, \mathbf{x}_k \in \mathcal{N}_i^k} \{\sqrt{(\mathbf{x}_j - \mathbf{x}_k)^2}\}, \quad (2.2)$$

$$D_{\mathcal{X}}(\mathbf{x}_k(i)) = \text{median}_{\mathbf{x} \in \mathcal{X}} \{\sqrt{(\mathbf{x}_k(i) - \mathbf{x})^2}\}, \quad (2.3)$$

$$D_{\mathcal{N}}^{\max}(\mathbf{x}_k(i)) = \max_{\mathbf{x} \in \mathcal{N}_i^k} \{\sqrt{(\mathbf{x}_k(i) - \mathbf{x})^2}\}, \quad (2.4)$$

The following conditions in Eq. 2.5 are then examined to verify if the deviation of a sample is within the range defined by α . Since some rare abnormalities are unlikely to be observed within the limited initialization period, therefore abnormal clusters: $\mathcal{S}, \mathcal{V}, \mathcal{F}$, which include abnormal beats for all patients in DS1, are deployed as the training dataset when [calculating](#) $D_{\mathcal{X}}(\mathbf{x}_k(i))$ in Eq. 2.3

$$\begin{cases} D_{\mathcal{N}}^{\max}(\mathbf{x}_k(i)) \leq \alpha R_i^{\max}, \\ D_{\mathcal{N}}(\mathbf{x}_k(i)) < D_{\mathcal{X}}(\mathbf{x}_k(i)) \quad \text{for } \mathcal{X} \in \{\mathcal{S}, \mathcal{V}, \mathcal{F}\} \end{cases} \quad (2.5)$$

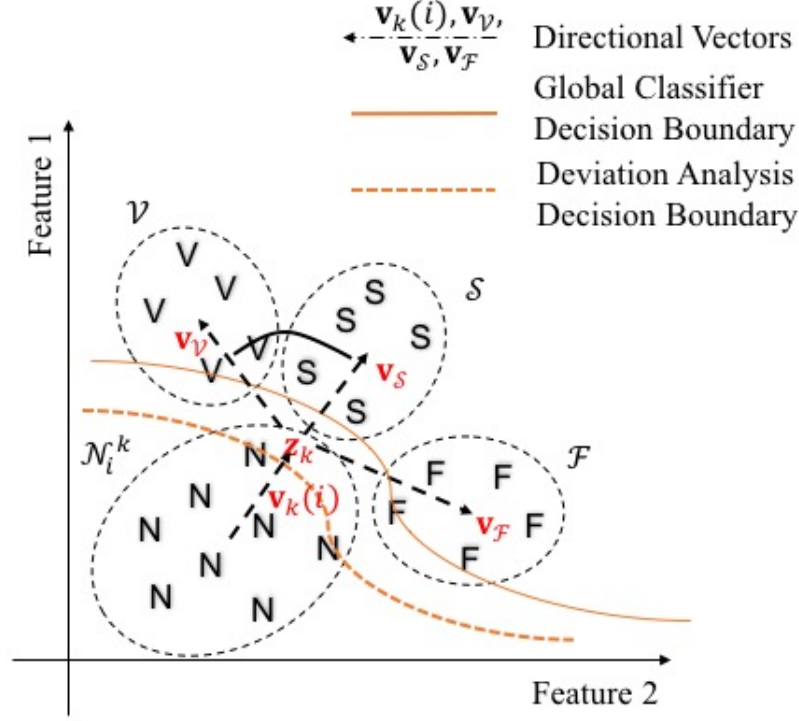


Figure 2.6: The deviation analysis boundary restrict on latent status between normal and abnormal samples compared with the Global Classifier boundary.

If a sample already labeled normal by the global classifier, is again confirmed as N in this module, it will be used to update the \mathcal{N}_i^k as mentioned above. Otherwise, the system assumes that the sample has a considerable deviation towards one of the abnormal clusters and hence will pass it to the subsequent *personalized classifier*. The *personalized classifier* uses controlled transformation with optimized parameters to discern the deviation to different morbid types regardless of the cluster topology within the original feature space, as detailed in Chapters 3 and 4.

After performing both global and personalized classification steps, a given sample $x_k(i)$ of patient i at time k is mapped to label $\hat{y}_k \in \{N, Y_V, Y_S, Y_F, R_V, R_S, R_F\}$, where N stands for normal state, Y_X stands for a yellow alarm of type “X”, and R_X stands for a red alarm of type “X”.

2.6 Personalized Classifier

Here, we provide the core idea behind the design of the personalized classifier, and the details of implementation will be discussed in Chapters 3 and 4. Since the proposed system aims at predicting subsequent abnormalities by analyzing a signal's deviation from the patient's normal functionality of the sample signal, it is vital to quantify the deviations using topological characteristics of the training dataset. For most of the ECG applications, ECG signal is analyzed by its representative feature vectors. A natural choice for deviation analysis in the high-dimensional feature space, is *cosine distance* (as defined in Eq. 2.6) to quantify the distance between two vectors \mathbf{v} and \mathbf{w} .

$$d(\mathbf{v}, \mathbf{w}) = 1 - \frac{\mathbf{v}^T \mathbf{w}}{|\mathbf{v}| |\mathbf{w}|} = 1 - \frac{\mathbf{v}^T \mathbf{w}}{\sqrt{(\mathbf{v}^T \mathbf{v})(\mathbf{w}^T \mathbf{w})}} \quad (2.6)$$

Consequently, relative deviations of a sample from normal cluster(N) to other abnormal clusters (V, S, F) are defined by the cosine distance between the vector $\mathbf{v}_k(i)$ (defined in Eq.2.7) and the three vectors $\mathbf{v}_{\mathcal{X}}(i) = \mathbf{c}_{\mathcal{X}} - \mathbf{x}_k(i)$ where $\mathcal{X} \in \{\mathcal{S}, \mathcal{V}, \mathcal{F}\}$. In this case, a smaller cosine distance represents a higher alignment between the vector from the normal cluster centroid $\mathbf{v}_k(i)$ to the current sample $\mathbf{x}_k(i)$ and the reference vector from the normal cluster centroid to abnormal centroids $\mathbf{c}_{\mathcal{X}}$.

$$\mathbf{v}_k(i) = \mathbf{x}_k(i) - \mathbf{c}_N^k(i) = \mathbf{x}_k(i) - \sum_{\mathbf{x} \in \mathcal{N}_i^k} \mathbf{x} / |\mathcal{N}_i^k|, \quad (2.7)$$

Therefore, the classification result of the Personal Classifier $\hat{y}_k^2(i)$ is determined as follows:

$$\hat{y}_k^2(i) = \underset{\mathcal{X} \in \{S, V, F\}}{\operatorname{argmin}} \{d(\mathbf{v}_k(i), \mathbf{v}_{\mathcal{X}}(i))\} \quad (2.8)$$

The relevance of cosine distance depend on the topology of clusters in the feature space. The topology in feature space, itself is inherited from the feature extraction and feature selection methods. For example, as shown in Fig.2.7, in the original feature space overlaps and alignment of abnormal clusters may lead to inaccurate results of deviation quantification. In order to eliminate the deviation analysis errors that arise from the asymmetry in the topology of clusters, it is desired to transform the original topology into a more symmetric one, where cosine distances directly reflect the amount of deviations.

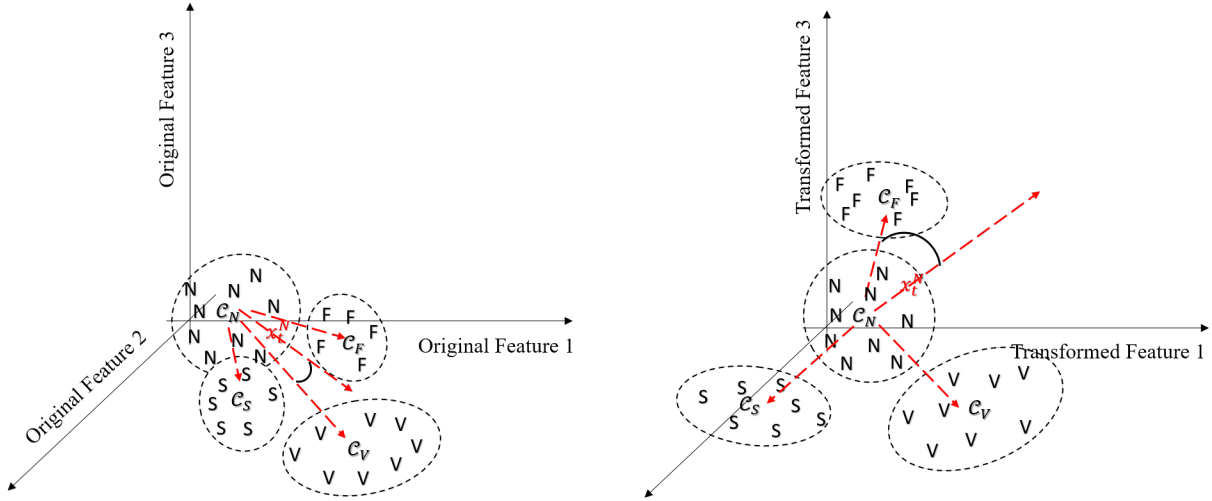


Figure 2.7: Left: illustration of the cluster topology in the original feature space; Right: illustration of the cluster topology in the transformed feature space using a nonlinear mapping function.

For this purpose, two different spatial transformation methods are proposed in the next two chapters.

Chapter 3

Kernels-Based Nonlinear Spatial Transformation

3.1 Introduction

As discussed in Chapter 2, the main objective of the personalized classifier is to reassess the normal samples to identify deviation of seemingly normal samples into any of abnormality types. The original geometry of clusters in the feature space Ω^d depends on the choice of features implied by the feature extraction and feature selection stages $g()$. We noticed that with the resulting features (in this work), the clustering geometry does not exhibit the necessary symmetric property and thus leads to a poor performance and even failure in predicting subsequent abnormalities. Therefore, an optimization method based on spatial transformation is proposed to solve this issue. More specifically, we propose a method to reshape the clusters such that

- The abnormal classes surround the normal class;

- A maximal separation among the abnormal classes are achieved;
- The angles between the vectors connecting the centroid of normal cluster to different abnormal clusters are equalized.

These properties can be achieved through imposing the following conditions:

- Vectors pointing from the normal centroid to different abnormal clusters centroids present maximum mutual cosine distances.
- The overlapping parts among all clusters are minimized.

Given that the clusters in original feature space do not meet these symmetric properties, developing a spatial transformation is unavoidable. In this chapter, a *kernel*-based nonlinear spatial transformation is proposed to reshape the feature space to reach the above-mentioned required symmetric properties. This reshaping process is part of the *personalized classification* stage (as shown in Fig.2.5) of the ECG classification system as described in chapter 2. The nonlinear mapping projects the corresponding feature vector of each sample \mathbf{x}_k in the original space Ω^d onto a new vector \mathbf{z}_k in a higher dimensional space denoted by $\Omega^{d'}$. This is achieved using a nonlinear mapping function $\Phi^{d'} : \Omega^d \rightarrow \Omega^{d'}$. The resulting vectors are used by the personalized classifier to identify the minor yellow alarm type out of $\{\mathcal{N}, \mathcal{S}, \mathcal{V}, \mathcal{F}\}$. The original text was ambiguous. Firstly, set and cluster shapes can be viewed differently, sets are not changes under the transformation although cluster geometry changes. Therefore, since we already used \mathcal{N}, \dots to represent clusters in the original space, you can use \mathcal{N}', \dots for the transformed clusters, unless you mean a set (not a cluster). In this case, sets do not changes under the transformation, and you can omit the definition $\Phi^{d'} = \{\mathcal{N}, \mathcal{S}, \mathcal{V}, \mathcal{F}\}$ to avoid ambiguity. Secondly, you need to distinguish between two functions, one simply maps the vector in original space into a new space, and the second one processes the transformed vector and maps it to a yellow alarm. It is not clear in the text.

3.2 *Kernel Method*

Kernel method has been widely used in machine learning algorithms. For instance, it is the integral part of nonlinear Support Vector Machine (SVM), which has been utilized in numerous applications recently [48]. Nonlinear kernel methods can efficiently improve the classification performance when there exists a nonlinear relationship between the input and output variables. Because of the complexity and diversity of feature vectors used in ECG analysis, the assumption of nonlinear relationship is considered valid in this work. Therefore, incorporating nonlinear kernel methods in the ECG analysis system, can be beneficial.

In kernel SVM, the nonlinearities are introduced to the model through a kernel function, which implicitly maps data points $\mathbf{x}_i \in \mathcal{X}$ in the input space Ω into a Hilbert space Φ via a nonlinear function $\Psi()$ [49]. Then, the algorithm minimizes the expected error $E[L(y, f(x))]$ between the true labels y and the predicted values $f(x)$ for samples in a training dataset, by finding an optimal classification function f , which also depend on the choice of $\Psi()$. Here, $L()$ is an arbitrary loss function, and a popular choice is the least squared errors $\sum_{x_i \in \mathcal{X}} (y_i - f(x_i))^2$ [50]. Other choices for loss function include Hingde loss, absolute loss, hit and miss loss, etc [REF].

If there are m observations in the input space, we use notation \mathbb{N} for index set $1 : m$. Based on the input space $\mathbf{x}_i \in \Omega (i \in \mathbb{N})$ and classification mapping function f , the optimization problem can be written as: better to use n instead of m if it does not conflict with other definitions.

$$\text{minimize } \frac{1}{m} \sum_{i \in \mathbb{N}} L(y_i, f(\mathbf{x}_i)) + \gamma \|f\|^2, \quad (3.1)$$

where $\|f\|^2$ is the squared norm of f here f is a function and norm is defined for vectors.

So add one or two sentences how to calculate it. I think for instance you mean the norm of coefficients of a polynomial function here. and the positive constant γ , also known as the regularization parameter, controls the balance between training error and the model complexity (smoothness).

When optimizing the above objective function, SVM only requires the inner products of the transformed features $\Psi(\mathbf{x})$ in the Hilbert Space Φ . Therefore, a kernel defined as $k(\mathbf{x}_i, \mathbf{x}_j) = \Psi(\mathbf{x}_i)^T \Psi(\mathbf{x}_j)$ can efficiently substitute the inner product calculation and induces the necessary nonlinearities into the model [51].

Different *kernels* represent different nonlinear mapping functions. For machine learning models, the selection of kernel plays a crucial role. Therefore is no straightforward method to choose the best kernel and it is typically chosen by try and error and other heuristic model selection methods. An effective kernel function generally needs to satisfy Mercer conditions, so that the inner products can be replaced by kernel functions, as used in SVM [52]. An exhaustive search for all possible kernels is a computationally expensive and unrealistic task [53]. A more efficient way to resolve this issue would be to search for an optimally weighted combination of a set of base kernels, such as polynomial kernel function and Gaussian kernel function [54]. This method has been proven to be robust and efficient since the base kernels satisfy Mercers condition individually and it can be consistent with different datasets [55].

Polynomial kernel is usually applied on normalized data for its explicit expression and steady performance. However, the degree of freedom in defining a polynomial kernel is relatively high, which requires tuning a large number of parameters. In fact this statement is not so relevant here. Note that a polynomial kernel of order p can be defined as $(1 + v^T w)^p = (1 + v_1 w_1 + v_2 w_2 + \dots)^p$, which has only one free parameter p and all coefficients are automatically determined. However, we are going to use a polynomial function of order p , (i.e. $f(v) = 1 + \alpha_1 v_1 + \alpha_2 v_2 + \dots + \alpha_i v_1^2 + \alpha_j v_1 v_2 + \dots \alpha_k v_N^p$) which obviously required tuning too many

free coefficients α_i .

Gaussian kernel function denoted by XXX for vectors \mathbf{v} and \mathbf{w} is a very classic robust radial function, which has shown a string robustness in the case of noisy datasets [REF XXX]. However, it is equivalent to the inner product of samples after projecting into an infinite dimensional space; therefore it is difficult to visualize the projected observations $\Psi(\mathbf{x})$ and interpret the results.

Considering the above-mentioned facts, in this work, the polynomial kernel is selected for the purpose of validating the proposed method and interpreting the effect of an optimized nonlinear kernel method on feature space reshaping. However, the proposed methodology is general and applicable to other nonlinear kernels.

The mapping function, which is a weighted combination of polynomial kernels can be explicitly written in the following format:

$$\mathbf{z}_k = \Psi_{\mathbf{w}}(\mathbf{x}_k) = \begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_{d'} \end{bmatrix} \circ \begin{bmatrix} \psi_1(\mathbf{x}_k) \\ \psi_2(\mathbf{x}_k) \\ \vdots \\ \psi_{d'}(\mathbf{x}_k) \end{bmatrix}, \quad (3.2)$$

where \mathbf{w} is the vector of normalized coefficients do we have $\|\mathbf{w}\| = 1$. Instead of selecting kernel, the process of spatial geometry optimization is accomplished by adjusting the coefficients of fixed polynomial basis functions $\psi()$. Since the number of free parameters increases exponentially with the order of polynomial function, an exhaustive search is not practical for parameter optimization. Therefore, it is necessary to implement a heuristic optimization algorithm, in which parameters are obtained by maximizing or minimizing an

objective function. More specifically, the nonlinear reshaping module in this chapter aims to adjust mapping coefficients $\mathbf{w} = [w_1, w_2, \dots, w_d]^T$ to achieve the ideal symmetric geometry in the reshaped feature space while maintaining the maximal separation between clusters.

3.3 Multiobjective Optimization

3.3.1 Objective Functions

To elucidate the details of the optimization problem, here we consider an illustrative example, where the original feature space is a 2-dimensional space Ω^2 . **This is not necessarily true, since you can choose any order of power even for a 2-D input vector. Therefore, the mapping base kernel may adopt a second-order polynomial function as follows:** We also assume for simplicity that the order of the polynomial function is 2. Therefore, we have:

$$\begin{aligned} \mathbf{x} &= [x_1 \ x_2]^T, \quad \mathbf{w} = [w_1 \ w_2 \ \dots \ w_5]^T, \quad d = 2, \quad d' = 5, \\ \psi_1(\mathbf{x}) &= x_1, \psi_2(\mathbf{x}) = x_2, \psi_3(\mathbf{x}) = x_1^2, \psi_4(\mathbf{x}) = x_2^2, \psi_5(\mathbf{x}) = x_1 x_2. \end{aligned} \quad (3.3)$$

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Inspired by the way loss functions are used in the SVM methods with a non-linear kernel, we use the following objective functions in order to impose the symmetry and separation of different abnormality classes in the proposed optimization problem: **I think, you mean LDA classification, Fisher discriminant function here where SW/SB is used. I don’t see any**

relation to SVM. Modify this part to be clear and accurate.

$$\begin{aligned} o_1(\mathbf{w}) &= \frac{1}{\min_{c,d=2,\dots,p \text{ and } c \neq d} \{d(\mathbf{v}_{\mathcal{X}_c}, \mathbf{v}_{\mathcal{X}_d})\}} \\ o_2(\mathbf{w}) &= \frac{SW}{SB} = \frac{\sum_{c=1}^C \sum_{\mathbf{z} \in \mathcal{X}_c} (\mathbf{z} - \mathbf{c}_{\mathcal{X}_c})^T (\mathbf{z} - \mathbf{c}_{\mathcal{X}_c})}{\sum_{c=1}^C \sum_{d=1, d \neq c}^C (\mathbf{c}_{\mathcal{X}_c} - \mathbf{c}_{\mathcal{X}_d})^T (\mathbf{c}_{\mathcal{X}_c} - \mathbf{c}_{\mathcal{X}_d})} \end{aligned} \quad (3.4)$$

The maximization of pairwise cosine distance between the vectors $\mathbf{v}_{\mathcal{X}_{c,d}}$ connecting the centroid of the normal cluster to the centroids of abnormal clusters \mathcal{X}_c is achieved by minimizing $o_1(\mathbf{w})$. In fact, this objective functions is deduced from discrimination function of personal classifier in Eq.2.8. Cosine distance is defined by Eq.2.6 and the calculation of $\mathbf{v}_{\mathcal{X}_{c,d}}$ can be written as follows:

$$\mathbf{v}_{\mathcal{X}_i} = \mathbf{c}_N^k - \mathbf{c}_{\mathcal{X}_i} \quad (3.5)$$

Since for some patients, the total number of a certain type of abnormal samples are very limited, the abnormal samples in training set DS1 are utilized in calculating the two objective functions. In Eq.3.4, the abnormal cluster centroids are calculated using the abnormal samples in training dataset DS1, while the centroid of the normal cluster is defined by the [preceding normal samples for the same person](#).

On the other hand, $o_2(\mathbf{w})$ represents the ratio of the within-cluster variance to the between-cluster variance and consequently controls the separation between the clusters. By minimizing $o_1(\mathbf{w})$ and $o_2(\mathbf{w})$ jointly, the algorithm eliminates the ambiguity of classification while improving the predictive power of the personalized classifier due to the symmetric geometry

of clusters.

3.3.2 Multi-objective Particle Swarm Optimization

We notice that $o_1(\mathbf{w})$ and $o_2(\mathbf{w})$ are not necessarily independent of each other. Thus, the optimization problem defined above is equivalent to joint minimization of $o_1(\mathbf{w})$ and $o_2(\mathbf{w})$ subject to a constraint condition: $|w|_2 = 1$. This constraint is necessary since the first objective function $o_1(\mathbf{w})$ is inversely proposal to $|w|_2$, whereas the second objective function $o_2(\mathbf{w})$ is scale-invariant.

This problem is a non-convex multi-objective optimization problem. Therefore, neither closed form solutions nor the optimization methods proposed for convex problems are applicable to this case. In this work, we utilize *multi-objective particle swarm optimization* (MOPSO) algorithm to solve this optimization problem and obtain the optimal coefficients [?].

Particle swarm optimization (PSO) is based on heuristic search and has the advantage of fast convergence, and easy implementation [56, 57]. PSO is defined to solve problems with a single objective function, where closed form solutions are not tractable. Several research works are devoted in the past decade to extend this method to multi-objective optimization problems [?]. In the MOPSO framework, the goal is to solve the typical *Pareto optimization problem* based on the evolutionary algorithm used in PSO. In other words, it aims at solving an optimization problem with two or more conflicting objective functions by approximating the *Pareto front*.

In order to compare different set of coefficient in this optimization problem, the concept of Pareto front is briefly introduced in this section. For a multiobjective optimization problem with two objective function, if a solution \mathbf{w}^1 is said to *dominate* another \mathbf{w}^2 when the

following two conditions are satisfied:

1. $o_1(\mathbf{w}^1) \leq o_1(\mathbf{w}^2)$ and $o_2(\mathbf{w}^1) \leq o_2(\mathbf{w}^2)$
2. $o_1(\mathbf{w}^1) < o_1(\mathbf{w}^2)$ or $o_2(\mathbf{w}^1) < o_2(\mathbf{w}^2)$

If a solution is not dominated by any other solutions in the searching space, then this solution is an *optimal* solution for this problem. A Pareto front is defined by the set of Pareto optimal solutions. However, in non-convex optimization, the Pareto front can not be represented explicitly by a deterministic function. Therefore, the majority of algorithms use heuristic searching algorithms to approximate the Pareto front [56].

MOPSO

change subsection title here since it is exactly equal to the section title. You may use: implementation details of MOPSO,

Among different implementations of MOPSO, the algorithm proposed by Coello Coello and Lechug presents a better performance and lower computational complexity in most applications [56]. Therefore, this algorithm is implemented and utilized in this work to solve the multi-objective optimization problem. One special property of this algorithm is the use of external repository, in which all Pareto optimal particles for every swarm is recorded for each iteration. The solution represented by repository members are stored and used as an optimal approximation of the Pareto front because they converge to the actual Pareto front as proved in [56]. You may add a few more sentences here regarding the operation of MOPSO such that it is easily understandable for a general reader.

Fig.3.1 presents the results of joint minimization of objective functions $o_1(\mathbf{w})$ and $o_2(\mathbf{w})$. This figure demonstrates that the repository members are Pareto optimal compared to the

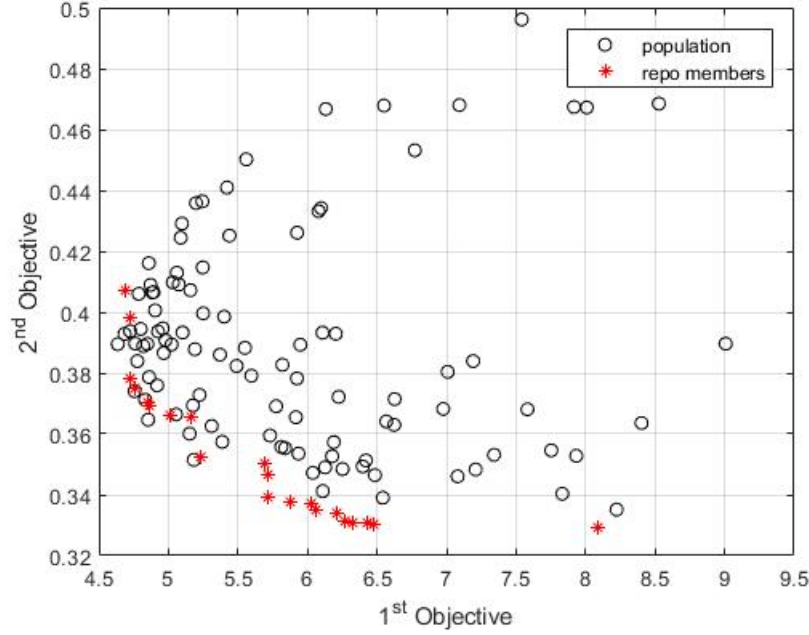


Figure 3.1: Particles stored in external repository approximate the Pareto front. **This figure does not appear for some reason.**

other particles. This figure also confirms that the repository members converge to a uniform Pareto front.

Using the concept of Pareto optimality, we demonstrate the impact of applying kernel functions in this spatial reshaping problem by comparing the [Pareto front of the optimization problem obtained by using MOPSO](#) for two different scenarios including i) the optimized coefficients for the original data sample, (i.e. a linear identity function) and ii) the transformed samples under polynomial kernel whose coefficients are optimized using MOPSO. Therefore, we first optimize the coefficients of the third-order polynomial kernel function, as formulated in Eq.3.3 and then optimize the coefficients of linear features in the origin feature space. The purpose of this comparison is to investigate whether or not the resulting objective functions are fundamentally improved by incorporating nonlinear terms into the feature vectors through the proposed polynomial function.

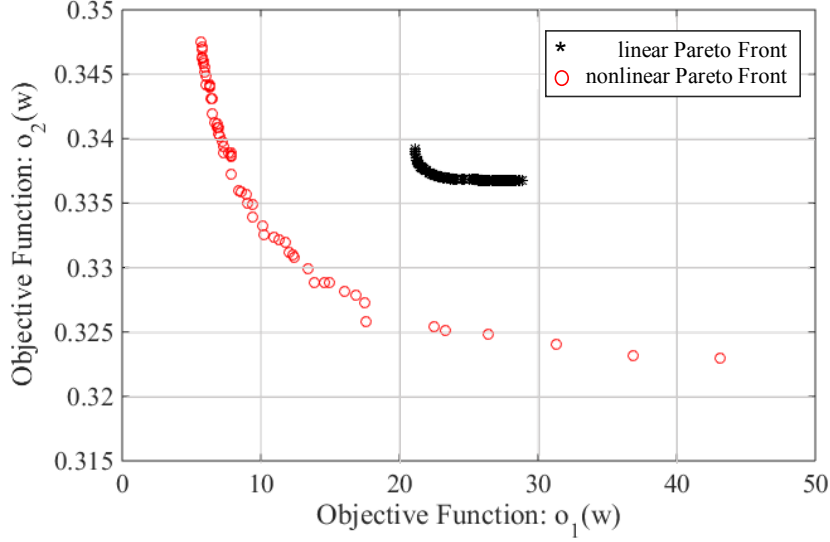


Figure 3.2: The *Pareto front* of the results of MOPSO is significantly shifted when using the transformed feature vectors. This improvement is due to the increase in the degree of freedom provided by additional non-linear dimensions added to the samples.

As shown in Fig. 3.2, the estimated Pareto front of the nonlinear model using the polynomial kernel dominates the Pareto front of the original linear model. This result is expected since the transformed samples exhibit a higher degree of freedom by adding new dimension to the data in the feature space through the nonlinear mapping. A higher degree of freedom enables the MOPSO algorithm to tune the optimization parameters and find better solutions than the best solutions achievable by the original data samples. In other words, the kernel method combined with multi-objective particle swarm optimization algorithm can improve the spatial structure of the clusters quantified by the two objective functions.

3.4 Experimental Results

As mentioned in Section. 2.3 **better to use refs to make sure section numbers are correct.**, a cardiac segment is represented by an 8-dimensional vector $\mathbf{x} = [x_1, x_2, \dots, x_8]$ after the

feature extraction and the PCA-based dimension reduction stages. To specify the nonlinear transformation in (3.2), a polynomial function of order 3 is applied to the feature vectors. The resulting transformed vectors $[x_1, x_2, \dots, x_8, x_1^2, x_2^2, \dots, x_8^2, x_1^3, x_2^3, \dots, x_8^3, x_1x_2, \dots, x_6x_7x_8]$ include XXX terms, 8 of which are the original features. This high dimension may cause the classifier to trap into the overfitting problem. It also significantly increases the computational complexity of the algorithm. To solve these issues, we discard some of the induced terms and include only 8 square terms x_i^2 , 8 cubic terms x_i^3 , and 8 cross terms of power two x_ix_j and 8 cross terms of power three $x_ix_j^2$. We randomly choose these terms after discarding the redundant cross terms. Therefore, the mapped vectors $\mathbf{z}_{32 \times 1}$ include a total of 32 terms as follows:

$$\begin{aligned} \mathbf{z} = & \{x_i^2 | i = 1, 2 \dots 8\} \cup \{x_i^3 | i = 1, 2 \dots 8\} \cup \\ & \{x_ix_j | i, j = 1, 2 \dots 8, i \neq j\} \cup \{x_i^2x_j | i, j = 1, 2 \dots 8, i \neq j\} \end{aligned} \quad (3.6)$$

The performance of the aforementioned kernel-based method is tested on DS2 excluding record 232, for this record has only 7 normal samples $y_k = N$. In total, 21 records are tested. Table 3.1 shows the performance of the proposed method in classifying ECG signal segments. In order to evaluate the consistency as well as the general classification results over all recordings, the median, interquartile range (IQR), mean and standard deviation of accuracy (AC), sensitivity (SE) and specificity (SP) are presented. The results are promising and the median of the classification accuracy for all classes are in the range of 88% – 99%. Sensitivity and specificity of the proposed method exhibit similar ranges. The mean accuracy is at least 86% excluding class V . Therefore, this system is not likely to miss an important alarm or to report false alarms.

Table 3.1: Classification results of the proposed method.

Class N	median(%)	IQR(%)	mean(%)	std (%)
AC	94.8	19.52	86.62	18.55
SE	97.21	17.36	87.47	19.26
class V	median(%)	IQR(%)	mean(%)	std (%)
AC	86.11	27.54	76.41	22.81
SP	99.71	11.22	90.18	18.52
class S	median(%)	IQR(%)	mean(%)	std (%)
AC	99.28	2.24	98.29	2.57
SP	99.64	22.17	97.56	6.06
class F	median(%)	IQR(%)	mean(%)	std (%)
AC	97.91	8.2	93.85	7.84
SP	100.00	0.03	99.12	3.6

More importantly, the predictive capability of the proposed method is worthy of evaluating, since it is unique feature provided by the proposed system. In order to quantify the posterior probability of observing an abnormal signal after a preceding yellow alarm of similar type in (2.8), the number of predicted samples are counted as formulated in Eq 3.7:

$$\begin{aligned}
 P(\hat{y}_{k+i} = X_r | \hat{y}_k = X_y) &= \frac{\# \text{ of } y_{k+i} = X \text{ after } \hat{y}_k = X_y}{\# \text{ of true alarms after } \hat{y}_k = X_y} \\
 P(\hat{y}_{k+i} = X_r) &= \frac{\# \text{ of true alarm of type } X (y_k = X)}{\# \text{ of all true alarms}}
 \end{aligned} \tag{3.7}$$

The summary of results for all 21 test records is presented in Table. 4.4. The values provided under the column *Probability of next abnormality (%)* in Table. 4.4 present the probability of having a subsequent true abnormality of all types after observing a yellow alarm of all types along with the prior probability of observing a certain type regardless of the preceding yellow alarm in the very last column. These results confirm the predictive capability of yellow alarms as well as the scientific fact that yellow alarm are indicative of upcoming red alarms. This conjecture supported by the fact that at least some of the heart problems

Table 3.2: Predictive power of yellow alarms: A yellow alarm increases the chance of observing a red alarm of the same type.

	Count numbers of subsequent abnormality				Probability of subsequent abnormality (%)			
secondary abnormalities	V_y	S_y	F_y	Total	V_y	S_y	F_y	Total
True V	38	23	35	96	75	75	61	67
True S	11	10	8	29	21	29	14	20
True F	2	2	14	18	4	6	25	13

develop over time, although the symptoms may appear suddenly.

For instance, the prior probability of observing a sample segment with abnormal types V , S , and F is respectively $\frac{96}{96+29+18} = 67\%$, $\frac{29}{96+29+18} = 20\%$ and $\frac{18}{96+29+18} = 13\%$, based on their relative frequencies in the dataset. However, the corresponding posterior probabilities after observing a yellow alarm of type Vp are respectively $\frac{38}{38+11+2} = 75\%$, $\frac{11}{38+11+2} = 21\%$ and $\frac{2}{38+11+2} = 4\%$. This means that the probability of observing a real abnormal segment of type V is $75\% - 67\% = 8\%$ higher than its prior probability. The same trend holds for other yellow alarms as well. The results suggest a more in-depth study of the concept of yellow alarms for heart monitoring. We conclude this section by stating that a new methodology provided in Chapter 4 to optimize the nonlinear transformation using an analytical approach, which significantly reduces the computational cost.

3.5 Summary of contributions

It is usual to have a summary of contributions at the end of each chapter. Conclusions and future works should be a separate section [bit 2 or 3 pages is sufficient.

Part of the text here is the repetition of the text before revision. reword this section and

provide a list of contributions and concluding remarks here. The overall conclusions should be provided in a separate section In this chapter, we proposed a novel method which combines kernel-based nonlinear transformation with MOPSO optimization method. Inspired by the concept of kernel method and the loss function utilized in SVM, we implement the method with a weighted combination of base nonlinear kernels to reshape the input feature space by mapping it to a high-dimensional space. The coefficients of kernels are optimized according to two conditions, namely, maximum separation between cluster and maximum cosine similarities between abnormal clusters.

Result shows that approximated Pareto front produced by kernel method in the objective function space is apparently optimal to the one which is produced by the linear combinations of original features. The results verify that the proposed method has a classification accuracy in the range of 88% – 99% for different ECG records in the test set of MIT-BIH database.

Above all, the proposed algorithm demonstrates the potential of providing detailed information about the sample deviations, which indicate the upcoming abnormal sample types. The predictive capacities of the system is verified with ECG signal, but this method is general and not bound to this application. If a biomedical signal has one base class (i.e. normal state) and several abnormal states, the proposed method can be implemented to predict upcoming abnormal types.

Revised up to here

Chapter 4

Controlled Spatial Transformation With Deterministic Mapping Function

4.1 Introduction

In Chapter 2, we elaborate on the details of patient adaptable ECG classification framework. In Chapter 3, the specific spatial topology of normal and abnormal clusters is analyzed in order to identify the fuzzy state of ECG samples between normal and abnormal state. In this chapter, we will introduce another deterministic spatial transformation method to model the fuzzy state of samples.

While the aforementioned method in Chapter 3 demonstrated capacity of predicting upcoming abnormalities, it's challenging to interpret the mechanisms of the systems and thus hindering the generalization of predictive warning to other applications of biomedical signals. Therefore, the main objective of this chapter is developing a deterministic transformation with stronger abnormality predicting power based on spatial topology studied in Chapter

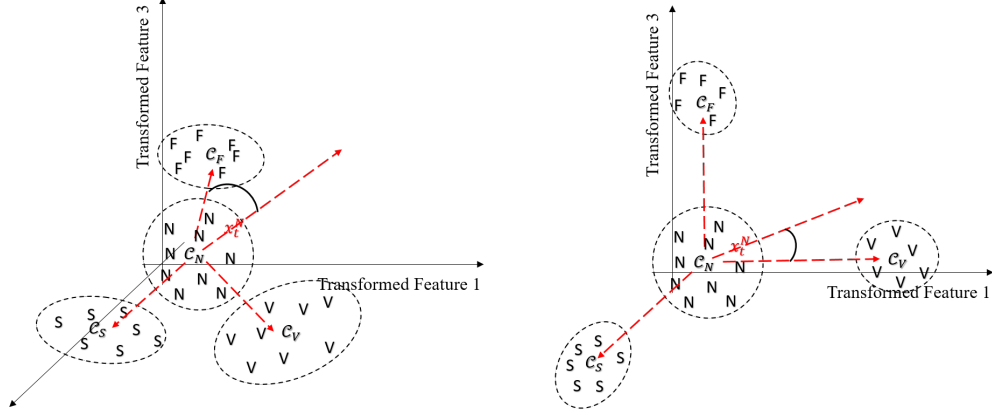


Figure 4.1: Left: illustration of cluster topology in feature space transformed with simple mapping function; Right: illustration of cluster topology in feature space transformed with optimized mapping function.

3. In this method, we further optimize the topology and spatial geometry of clusters in the feature space by reducing the within cluster variance after spatial transformation. As shown in 4.1, through this improvement, the predicting performance of personalized classifier can be further enhanced.

4.2 Hyper-Spherical Coordinates

In the precedent chapter, the spatial transformation module is implemented with kernel function and heuristic optimization algorithm. The system performance has been proven to be promising. However it's difficult to select the appropriate base kernel as spatial mapping function due to the high variety of kernel functions and the limitation of dimensionality.

In order to address this problem, a novel deterministic spatial mapping function is proposed based on *hyper-spherical* coordinates in this chapter. Since hyper-spherical coordinates consists of angles and radius, this information together with the target cluster topology are used to determine the mapping function parameters.

Hyper-spherical coordinates (n-dimensional spherical coordinates) and its mapping to *Cartesian* coordinates are first elaborated in [58]. If \mathbf{x} is a sample vector in n -dimensional feature space, with its Cartesian coordinates $(\xi_1, \xi_2 \dots \xi_n)$, then its corresponding hyper-spherical coordinates can be obtained through Eq.4.1, which is originally derived through its reverse mapping (Eq.4.2) using equation: $\sin(\arccos(x)) = \sqrt{1 - x^2}$.

$$\begin{aligned}
r &= \sqrt{\xi_n^2 + \xi_{n-1}^2 + \dots + \xi_2^2 + \xi_1^2} \\
\theta_1 &= \arccos \frac{\xi_1}{\sqrt{\xi_n^2 + \xi_{n-1}^2 + \dots + \xi_1^2}} \\
\theta_2 &= \arccos \frac{\xi_2}{\sqrt{\xi_n^2 + \xi_{n-1}^2 + \dots + \xi_2^2}} \\
&\vdots \\
\theta_{n-2} &= \arccos \frac{\xi_{n-2}}{\sqrt{\xi_n^2 + \xi_{n-1}^2 + \xi_{n-2}^2}} \\
\theta_{n-1} &= \begin{cases} \arccos \frac{\xi_{n-1}}{\sqrt{\xi_n^2 + \xi_{n-1}^2}} & \xi_n \geq 0 \\ -\arccos \frac{\xi_{n-1}}{\sqrt{\xi_n^2 + \xi_{n-1}^2}} & \xi_n < 0 \end{cases}
\end{aligned} \tag{4.1}$$

$$\begin{aligned}
\xi_1 &= r \cos(\theta_1) \\
\xi_2 &= r \sin(\theta_1) \cos(\theta_2) \\
\xi_3 &= r \sin(\theta_1) \sin(\theta_2) \cos(\theta_3) \\
&\vdots \\
\xi_{n-1} &= r \sin(\theta_1) \dots \sin(\theta_{n-2}) \cos(\theta_{n-1}) \\
\xi_n &= r \sin(\theta_1) \dots \sin(\theta_{n-2}) \sin(\theta_{n-1}).
\end{aligned} \tag{4.2}$$

where $0 \leq \theta_j \leq \pi$, $j = 1, \dots, n-2$; $0 \leq \theta_{n-1} \leq 2\pi$; $0 \leq r < \infty$

4.3 Orthogonalization

To simplify the algorithm, in this chapter, the topology of clusters in feature space is approximated by relative location of cluster centroids: $\mathbf{c}_N^k, \mathbf{c}_V, \mathbf{c}_S, \mathbf{c}_F$. Furthermore, as we assume that the samples with fuzzy state deviate from normality to abnormality, the spatial topology stays unchanged if normal centroid is simply translated to the origin in Cartesian coordinate. The cluster topology in original feature space can be equivalently represented by the following matrix with three row vectors:

$$\mathcal{C} = \begin{bmatrix} \mathbf{c}_V - \mathbf{c}_N^k \\ \mathbf{c}_S - \mathbf{c}_N^k \\ \mathbf{c}_F - \mathbf{c}_N^k \end{bmatrix} = \begin{bmatrix} \mathbf{V}_{VN} \\ \mathbf{V}_{SN} \\ \mathbf{V}_{FN} \end{bmatrix} \quad (4.3)$$

As shown in Fig. 4.1, in order to improve personalized classifier and avoid ambiguity, a topology with maximum separation between three vectors in \mathcal{C} is preferred. To lower computational complexity in high dimension, the algorithm aims at transforming vectors in \mathcal{C} to orthogonal vectors with deterministic functions. Therefore, the method proposed in [59] based on the well known orthogonalization method *Gram-Schmidt* in [60] is deployed. Hence, in the first step of the function, the three row vectors in \mathcal{C} representing the centroids is fed

to the orthogonalization process as follows:

$$\mathcal{C}^\perp = \text{Gram-Schmidt}(\mathcal{C}) = \begin{bmatrix} \mathbf{V}_{\mathcal{V}\mathcal{N}}^\perp \\ \mathbf{V}_{\mathcal{S}\mathcal{N}}^\perp \\ \mathbf{V}_{\mathcal{F}\mathcal{N}}^\perp \end{bmatrix} \quad (4.4)$$

where \mathcal{C}^\perp is the matrix of orthogonalized vectors in Cartesian coordinates. The hyper-spherical coordinates \mathcal{C}_*^\perp of these orthogonalized vectors are calculated subsequently using Eq.4.1. After this step, the orthogonalized vectors in hyper-spherical coordinates are obtained as formulated in Eq. 4.5. The j th angular dimensions are noted as θ_j^\perp and the radius dimension is noted as r^\perp

$$\mathcal{C}_*^\perp = \begin{bmatrix} r_{\mathcal{V}\mathcal{N}}^\perp & \theta_{1_{\mathcal{V}\mathcal{N}}}^\perp & \dots & \theta_{n-1_{\mathcal{V}\mathcal{N}}}^\perp \\ r_{\mathcal{S}\mathcal{N}}^\perp & \theta_{1_{\mathcal{S}\mathcal{N}}}^\perp & \dots & \theta_{n-1_{\mathcal{S}\mathcal{N}}}^\perp \\ r_{\mathcal{F}\mathcal{N}}^\perp & \theta_{1_{\mathcal{F}\mathcal{N}}}^\perp & \dots & \theta_{n-1_{\mathcal{F}\mathcal{N}}}^\perp \end{bmatrix} \quad (4.5)$$

4.4 Spatial Mapping Function

After obtaining the original hyper-spherical coordinates of $[\mathbf{V}_{\mathcal{V}\mathcal{N}}, \mathbf{V}_{\mathcal{S}\mathcal{N}}, \mathbf{V}_{\mathcal{F}\mathcal{N}}]^T$ and orthogonalized hyper-spherical coordinates $[\mathbf{V}_{\mathcal{V}\mathcal{N}}^\perp, \mathbf{V}_{\mathcal{S}\mathcal{N}}^\perp, \mathbf{V}_{\mathcal{F}\mathcal{N}}^\perp]^T$, the goal is to design a mapping function $\mathbf{F} : \mathbf{R}^n \rightarrow \mathbf{R}^n$ from the original coordinates to the orthogonal ones which represent the ideal cluster topology.

In Gram-Schmidt algorithm, the very first vector of the input vector array serves as a reference vector and remains unchanged in the orthogonalized vector array. As a result, $\mathbf{V}_{\mathcal{V}\mathcal{N}} = \mathbf{V}_{\mathcal{V}\mathcal{N}}^\perp$ and \mathbf{F} can be equivalently defined by the following equations:

$$\begin{aligned}
\mathbf{F}(\mathbf{V}_{S\mathcal{N}} - \mathbf{V}_{\mathcal{V}\mathcal{N}}) &= \mathbf{V}_{S\mathcal{N}}^\perp - \mathbf{V}_{\mathcal{V}\mathcal{N}}^\perp = \mathbf{V}_{S\mathcal{N}}^\perp - \mathbf{V}_{\mathcal{V}\mathcal{N}} \\
\mathbf{F}(\mathbf{V}_{\mathcal{F}\mathcal{N}} - \mathbf{V}_{\mathcal{V}\mathcal{N}}) &= \mathbf{V}_{\mathcal{F}\mathcal{N}}^\perp - \mathbf{V}_{\mathcal{V}\mathcal{N}}^\perp = \mathbf{V}_{\mathcal{F}\mathcal{N}}^\perp - \mathbf{V}_{\mathcal{V}\mathcal{N}}
\end{aligned} \tag{4.6}$$

Furthermore, since orthogonality is independent to radius dimension r , we only need to design \mathbf{F} for $n - 1$ dimensions, which includes all angular dimensions $(\theta_1, \dots, \theta_{n-1})$, and coordinate r remains unchanged before and after mapping. Consequently, the determination of \mathbf{F} can be decomposed to the determination of $n - 1$ functions: $f_i : \mathbf{R} \rightarrow \mathbf{R}$, $i = 1 \dots n - 1$ with constraints in Eq.4.6 and boundary constraints of angular dimensions. We note $\mathbf{V}_{S\mathcal{N}} - \mathbf{V}_{\mathcal{V}\mathcal{N}} = \Delta_{S\mathcal{V}}$ and the i th angular dimension of $\Delta_{S\mathcal{V}}$ as $\delta_{i_{S\mathcal{V}}}$. Same notation is applied on $\mathbf{V}_{\mathcal{F}\mathcal{N}} - \mathbf{V}_{\mathcal{V}\mathcal{N}}$. Hence for each angular dimension i , f_i is determined by $(\delta_{i_{S\mathcal{V}}}, \delta_{i_{S\mathcal{V}}}^\perp)$ and $(\delta_{i_{\mathcal{F}\mathcal{V}}}, \delta_{i_{\mathcal{F}\mathcal{V}}}^\perp)$, together with two boundary constraints of angular dimensions.

In order to maintain the simplicity and linearity of the mapping function, f_i needs to be continuous and monotonic. For this purpose, periodicity of angular dimensions is used to determine the boundary constraints and the problem is transformed into a curve fitting one. For example, if linking $(\delta_{i_{S\mathcal{V}}}, \delta_{i_{S\mathcal{V}}}^\perp)$ and $(\delta_{i_{\mathcal{F}\mathcal{V}}}, \delta_{i_{\mathcal{F}\mathcal{V}}}^\perp)$ results in a monotonically decreasing line, the boundary constraints would be $(\pi, 0)$ and $(0, \pi)$. Conversely, if it results in a monotonically increasing line, the boundary constraints would be $(0, 0)$ and (π, π) . Same rules applies on the last angular dimension where period is 2π instead of π . Since $(\delta_{i_{S\mathcal{V}}}, \delta_{i_{S\mathcal{V}}}^\perp)$ and $(\delta_{i_{\mathcal{F}\mathcal{V}}}, \delta_{i_{\mathcal{F}\mathcal{V}}}^\perp)$ represent the orthogonalization process, they are decisive for this process. So we call these two points and the boundary of angular dimension as *target points* in this following sections.

The simplest candidate function for f_i , which connect two boundary points and two target points in the 2-D plane would be a linear spline as shown in Fig.4.2

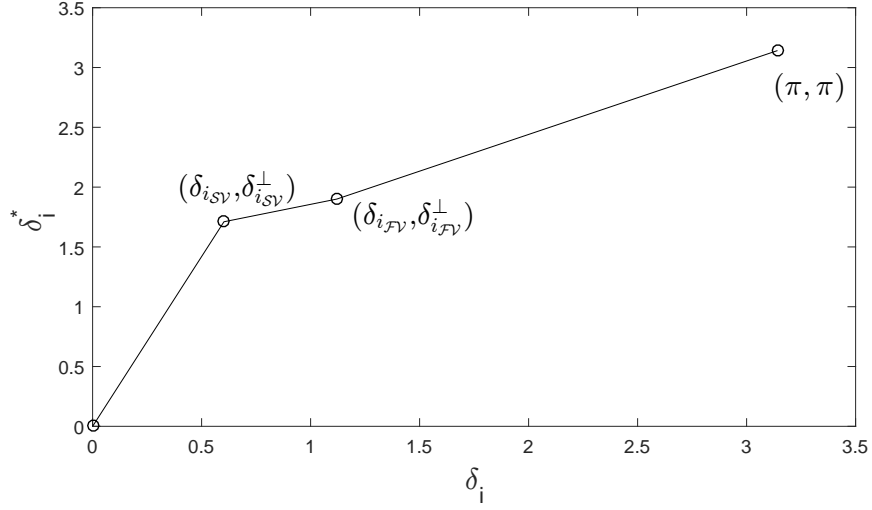


Figure 4.2: The simple mapping function.

4.5 Optimized Mapping Function

The mapping function in Fig.4.2 demonstrates monotonicity and continuity, which is a part of targeted characteristics as an ideal mapping function for f_i . However there exists some drawbacks in the simple mapping function. First of all, the function is not differentiable at two target points $(\delta_{i_{SV}}, \delta_{i_{SV}}^\perp)$ and $(\delta_{i_{FV}}, \delta_{i_{FV}}^\perp)$, which will lead to cluster deformation. Secondly, since the mapping function is applied on the angular dimensions, linearity of each spline in the function will lead to non-convex clusters in Cartesian coordinates after mapping. In order to avoid deformations and preserve within cluster geometry, it is required to assign a region for each cluster within which the function maps the data to a equal or even smaller range in Cartesian coordinates. In other words, the samples close to the centroids has to be close to the same corresponding centroids in the mapped space. In order to avoid deformations, an optimized mapping function is proposed in this section.

To compromise three constrains, a function which satisfies the following mathematical conditions is studies:

- mapping function derivatives around centroids 0 and $\delta_{i_{SV}}$ and $\delta_{i_{FV}}$ are small
- mapping function derivatives between two centroids large
- quasi differentiable at all points

Therefore, we proposed the basis function p , which satisfies the aforementioned conditions. The function p is composed of two parts: $h(x)$ and $g(x)$. The boundaries that each function activates are decided by target points $(\delta_{i_{SV}}, \delta_{i_{SV}}^\perp)$ and $(\delta_{i_{FV}}, \delta_{i_{FV}}^\perp)$ along with the mid-points between the target points. The lower boundary mid points are noted as (γ, γ^\perp) . The upper boundary mid points are noted as $(\epsilon, \epsilon^\perp)$. To ensure the continuity of the mapping function f , the boundaries and target points satisfy:

$$(\epsilon_{i_{SV}}, \epsilon_{i_{SV}}^\perp) = (\gamma_{i_{FV}}, \gamma_{i_{FV}}^\perp) = \left(\frac{\delta_{i_{SV}} + \delta_{i_{FV}}}{2}, \frac{\delta_{i_{SV}}^\perp + \delta_{i_{FV}}^\perp}{2} \right) \quad (4.7)$$

Therefore, the two piecewise functions $h(x)$ and $g(x)$ are defined as follows:

$$K_h = \frac{\epsilon^\perp - \delta^\perp}{e^{\alpha(\epsilon - \delta, 0)^+} - 1} \quad (4.8)$$

$$h(x) = K_h [e^{\alpha(x - \delta, 0)^+} - 1] + \delta^\perp$$

$$K_g = \frac{\gamma^\perp - \delta^\perp}{e^{\alpha(-\gamma + \delta, 0)^+} - 1} \quad (4.9)$$

$$g(x) = K_g [e^{\alpha(\delta - x, 0)^+} - 1] + \delta^\perp$$

To demonstrate this process, we first apply p on two target points $(\delta_{i_{SV}}, \delta_{i_{SV}}^\perp)$ and $(\delta_{i_{FV}}, \delta_{i_{FV}}^\perp)$.

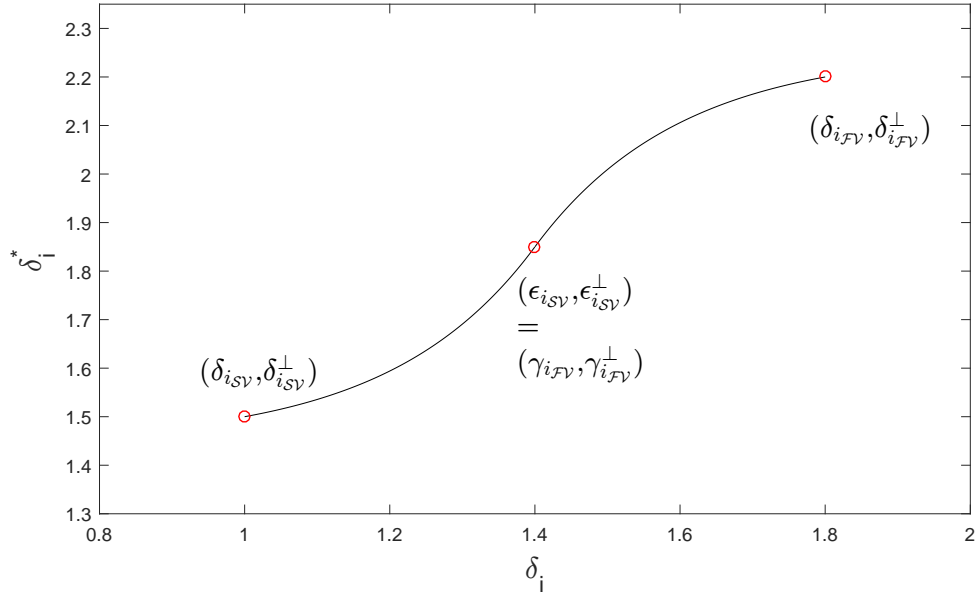


Figure 4.3: Optimized Piecewise Interpolate Function p .

This will result in a smooth curve as shown in Fig.4.3

Therefore, if we apply the piecewise interpolate function p at all four target points: $(\delta_{i_{SV}}, \delta_{i_{SV}}^\perp)$, $(\delta_{i_{FV}}, \delta_{i_{FV}}^\perp)$ and two boundary points of angular dimension, the final result is shown in Fig.4.4

In the training process, abnormal data from DS1 and personalized normal cluster are used to determine the mapping function. In the predicting process, the hyper-spherical coordinate of a new ECG sample is calculated and the mapping function is applied on its hyper-spherical coordinate. After this step, we calculate the Cartesian coordinate of the transformed data. This final result in Cartesian coordinate is then fed into Eq. 2.8 to generate the corresponding type of yellow alarm.

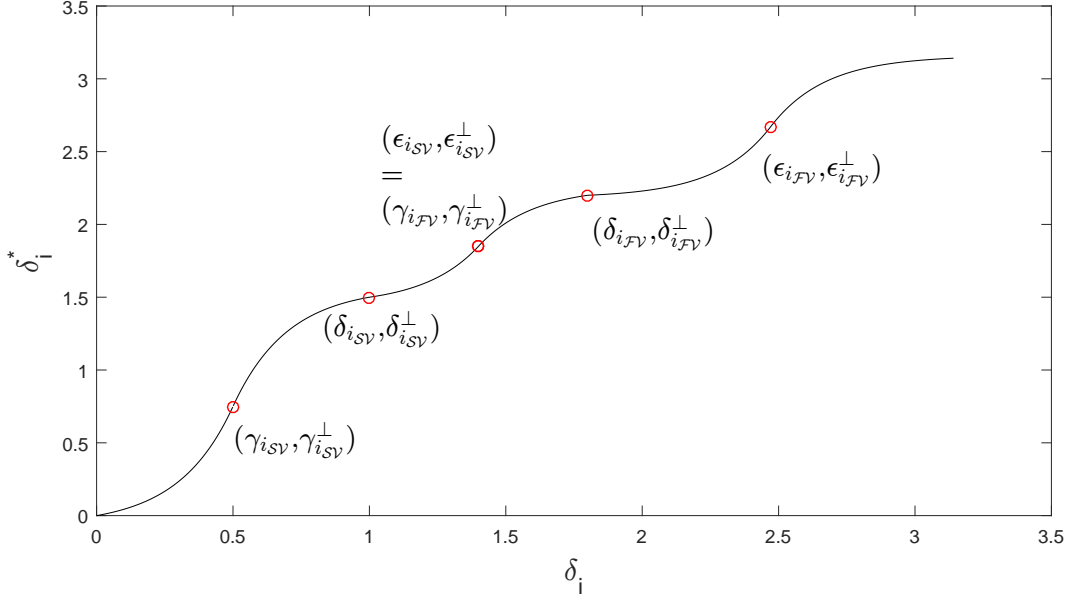


Figure 4.4: Optimized Mapping Function f .

4.6 Experimental Results

In this section, the performance of proposed method is evaluated according to two aspects. We will first analyze the classification performance of the system and demonstrate the comparison with other representative ECG classifiers. Furthermore, the classification results are partitioned into two sets: red alarms generated by global classifier and final results by combining yellow and red alarms. In this way, the impacts of personalized classifier on final results can be revealed. Finally, the prediction performance which is representative in the proposed system is evaluated.

4.6.1 Classification Performance

The experimental results are evaluated with the classification performance of 4 AAMI ECG classes using the test subset of MITBIH Arrhythmia DS2. Originally DS2 contains 15357

Table 4.1: Cumulated Confusion Matrix for All Records in DS2

	Ground Truth				
		N	V	S	F
Result	N	9255(10076)	21(38)	72(90)	1(5)
	V	657(22)	1678(1663)	8(2)	9(7)
	S	71(6)	3(1)	417(416)	0(0)
	F	122(1)	0(0)	11(0)	89(87)

samples after feature extraction. While training Personal Classifier, the first 20% of total normal samples serve as initialization samples for personalized dynamic normal cluster. Therefore, all samples before the last initialization normal sample should be excluded from test set for each records. Consequently, the actual test set contains 12414 samples in total consisting of 10105 type-N, 1702 type-V, 508 type-S and 99 type-F samples.

To present the result, we select weighted k-Nearest Neighbors where $k = 10$ as global classifier because it's comparatively simple and representative among low complexity models. The parameter α in the deviation detection module is set to 1 for test purpose.

Table 4.1 summarized the cumulated confusion matrix for all records in the test set. In order to compare the result of global classifier and combined result, the sample numbers are presented in the following format: *combined(globaled)*. In order to measure classification performance, we adopted three metrics proposed in [12,13,16]: accuracy(Ac), sensitivity(Se), specificity(Sp). All three metrics are calculated based on true positive TP , false positive FP , false negative FN and true negative TN in a binary confusion matrix. Therefore all four metrics are calculated for each class by converting the 4x4 matrix to a 2x2 matrix.

While cumulated classification results are demonstrated in Table 4.1, the robustness of the proposed method should be evaluated based on the performance variation over 22 test records in DS2. Hence medians and IQRs(interquartile range) for each metric and each class are included in Table 4.2 to represent the robustness of proposed methods. The lower variation between performances measured on different tapes, the more robust the system is. In Table

4.2, we observe that among all abnormal classes, the proposed method demonstrates stable performance on class V but less stable on class S and F.

As MITDB is widely used to verify ECG classifier performance, we compared the proposed system with five significant methods proposed in literature. According to AAMI standards, ECG classifier performance should be evaluated over the binary classification performance of *Ventricular (V)* versus *non-V* types and *Supraventricular (S)* versus *non-S* types. For methods proposed in literature, same evaluation metrics are deployed on records from MITDB. To standardize the metrics, we select 11 common ECG records from all 5 methods and compared the median of each classification metrics over these 11 records. The comparison results are demonstrated in Table 4.3. Generally speaking, the proposed method shows higher sensitivity for both V type and S type. Especially for S type, the proposed method has advantage on all three metrics over other five methods in the literature.

4.6.2 Prediction Performance

As an important characteristic of the proposed methods, yellow alarms triggered by personalized classifier after feature space reshaping indicate a higher probability of observing subsequent abnormalities. In order to verify this functionality, all beats following a yellow alarm is investigated for each yellow alarm. Abnormality type which occurs the earliest within the window is recorded. Similar to confusion matrix for classification evaluation, the performance of prediction can be summarized by a confusion matrix with the 3 abnormal

Table 4.2: Classification Performance and Within-Set Variation of Proposed System

statistics	N			V			S			F		
	<i>Ac</i>	<i>Se</i>	<i>Sp</i>	<i>Ac</i>	<i>Se</i>	<i>Sp</i>	<i>Ac</i>	<i>Se</i>	<i>Sp</i>	<i>Ac</i>	<i>Se</i>	<i>Sp</i>
cumulated	92.4	91.59	95.93	94.38	98.59	93.71	98.67	82.09	99.38	98.85	89.9	98.92
median	94.45	92.21	95.42	96.17	99.55	95.71	99.38	80.65	99.84	99.11	90.91	99.11
IQR	6.33	10.08	11.91	5.17	1.64	8.62	1.76	19.35	0.61	1.58	23.33	1.49

Table 4.3: V and S classification performance compared with five algorithms in literature using 11 common records in MITDB

Methods	VEB			SVEB		
	Ac	Se	Sp	Ac	Se	Sp
Proposed	96.6	98.2	92.4	98.63	88.89	99.41
Hu <i>et al.</i> [12]	94.8	78.9	96.8	N/A	N/A	N/A
de Chazal <i>et al.</i> [9]	96.4	77.5	N/A	N/A	N/A	N/A
Jiang and Kong [15]	98.8	78.9	96.8	97.5	74.9	98.8
Ince <i>et al.</i> [16]	97.9	90.3	98.8	96.1	81.8	98.5
Kiranyaz <i>et al.</i> [17]	98.9	95.9	99.4	96.4	68.8	99.5

types. Probabilities of observing an certain type of abnormal beats after a yellow alarm is calculated using the prediction confusion matrix and compared to the prior probability of observing the same type of abnormality. This process is formulated in the following two equations:

$$\begin{aligned}
P(\hat{y}_{k+i} = X_r | \hat{y}_k = X_y) &= \frac{\# \text{ of } y_{k+i} = X \text{ after } \hat{y}_k = X_y}{\# \text{ of true alarms after } \hat{y}_k = X_y} \\
P(\hat{y}_{k+i} = X_r) &= \frac{\# \text{ of true alarm of type } X (y_k = X)}{\# \text{ of all true alarms}}
\end{aligned} \tag{4.10}$$

The capacity of predicting each type of abnormalities is evaluated by comparing $P(\hat{y}_{k+i} = X_r | \hat{y}_k = X_y)$ and $P(\hat{y}_{k+i} = X_r)$. As shown in Table.4.4, the probability of observing a certain type of abnormalities after a yellow alarm are higher than its prior for each type of abnormalities. For example, without knowing the type of a yellow alarm, the probability of observing a type V sample is 71.54% while the probability of observing a type V sample given a type V yellow alarm was triggered is 77.45%. The improvement are consistent among all three types of abnormalities but the system has stronger predicting capacity for type S .

In order to study the time window in which real abnormality occurs after yellow alarms, we

Table 4.4: predictive probability versus prior probability without windowing

		# of predicted ground truth			% of predicted ground truth		
		V	S	F	V	S	F
yellow alarm	V	467	122	14	77.45	20.23	2.32
	S	36	15	0	70.59	28.41	0
	F	40	60	5	38.10	57.14	4.76
total		543	197	19	71.54	25.96	2.50

Table 4.5: predictive probability versus prior probability within 10 beats' window

		# of predicted ground truth			% of predicted ground truth		
		V	S	F	V	S	F
yellow alarm	V	290	85	12	74.94	21.96	3.10
	S	22	13	0	62.86	37.14	0
	F	29	37	6	40.28	51.39	8.33
total		341	135	18	69.03	27.32	3.64

also studied a window of 10 consecutive samples following a yellow alarm. Similarly, prior and posterior probabilities are compared to evaluate the performance as shown in Table.4.5.

Compared with the result without windowing, the predicting performance within 10 beats window shows that the proposed algorithm can better predict the occurrence of abnormalities in a certain time window. Especially for type S, the probability of observing a type S sample within 10 beats after a yellow alarm is 27.32% while given that the yellow alarm is type S, the posterior probability is raise to 37.14%. With almost 10% increase, it's proved that the yellow alarm types are informative. The results shows that same improvements are made within the 10-sample window as well. In general, the predicting performance are promising, indicating the efficiency of personalized classifier and deviation analysis.

Chapter 5

Conclusions And Future works

5.1 Conclusions

In this thesis, we a patient-adaptable ECG classification framework. The system has a two-staged hierarchical classifier structure including Global Classifier and Personal Classifier. While Global Classifier is designed to filter the signal with severe distortion and abnormal waveforms by triggering red alarms and pass other samples to the deviation detection stage. In this stage, the personal dynamic normal cluster is constructed and used to specify the normal range for each patient. By comparing the current sample and personalized normal range, this module decides if a yellow alarm will be triggered to provide predictive information about upcoming abnormalities. If a sample is detected with deviation towards abnormal clusters, it will be passed to the Personal Classifier and labeled as one of the three abnormal types. Whereas samples without deviation are further feed back to personal dynamic normal cluster to update the classification system about the newest personal normal range.

In Chapter 3, a kernel based nonlinear transformation is proposed to address the problem

of cluster topology in original feature space. Inspired by Support Vector Machine, kernel functions are deployed in this method as a spatial transformation function. The target topology is formulated as two objective functions so that by tuning the parameters in kernel function, the system is able to select the best transformation for the following predicting stage. This non-convex multi-objective optimization is solved with Multi-Objective Particle Swarm Optimization. In order to validate improvement by using high order kernel function, we compared the Pareto front generated with linear combination of original features and mapped high order features with polynomial kernel. The result verifies that applying high order kernel function allows more degree of freedom so that the topology can be further optimized according to objective functions. Having this concept proved, we applied this method on MITDB test data and obtained similar sensitivity and specificity as proposed in the literatures. More importantly, the predicting capacity of yellow alarms are analyzed. The performance is quantified by comparing prior probability and posterior probability giving the types of yellows alarm. The comparison result shows that a promising improvement has been made by applying the nonlinear transformation.

While the method in Chapter 3 demonstrated capacity of predicting upcoming abnormalities, it's challenging to interpret the mechanisms of the systems and thus hindering the generalization of predictive warning to other applications of biomedical signals. Therefore, the main object of Chapter 4 is developing a classification system with abnormality predicting capacity based on spatial topology studied in Chapter 3. In Chapter 4, we proposed a novel spatial transformation specifically designed to reshape the feature space according to angles between cluster center. In this method, between cluster cosine distance are optimized through orthogonalization in spherical coordinate space and within cluster variance is reduced by a mapping function which is fitted piecewise with a basis function. The basis function proposed in the chapter has the feature of saturating at the boundaries, similar

to sigmoid function but more flexible. An advantage of deploying such basis function is that the cluster geometry may be preserved after spatial transformation. With this novel module integrated in the patient-adaptable classification framework, the performance of this system is evaluated through classification and prediction results on the test set data. The classification results show that by triggering yellow alarm through this method, specificity of abnormal types is improved. Especially for Supraventricular types, the proposed system performs better than all 5 methods in the literature. The same conclusion holds for prediction performance. Compared to the method proposed in Chapter 3, this method improves predicting capacity for all abnormal classes and the most significant improvement is for type S. Moreover, we also studied the time delay of real abnormalities following a yellow alarm. It's proved that most of the real abnormalities occurs within 10 beat after a yellow alarm. Generally speaking, the system is proved to be efficient both in classification and prediction.

5.2 Future works

In this research, we focused on two challenges of ECG classification, namely, inter-patient variation and anomaly prediction. The framework of patient-adaptable classifier includes both features. The methods of improving prediction accuracy are proposed and studied. While the result shows the efficiency of designed system, further improvements can be made through research. The following tasks can be resolved as a continuation of this research:

- Research on other kernel functions which is potentially a better transformation for spatial topology optimization.
- Investigate on the deterministic solution for the objective functions proposed in Chapter 3.

- Assess the performance of proposed spatial transformation on other biomedical signals with similar characters as ECG signal
- Improve the deterministic mapping function in Chapter 4 by including the variance of individual clusters into function parameters

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