
DL: Assignment 1

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Abstract

In this report, the main focus is to go through the assignment, starting with a rough Numpy implementation, and then using State-of-the-art PyTorch.

1 Derivatives

Test123asdadasdasdasd asdasdasd

2 PyTorch Implementation

Test123asdadasdasdasd asdasdasd

3 Layer normalization

3.2a: Manual implementation of backward pass

I will start by writing down, in essence, all known shapes.

1. $X \in \mathbb{R}^{S \times M}$
2. $Y \in \mathbb{R}^{S \times M}$ (same shape as X)
3. $L \in \mathbb{R}^1$
4. $\gamma \in \mathbb{R}^M$
5. $\beta \in \mathbb{R}^M$
6. $\frac{\delta L}{\delta \gamma} \in \mathbb{R}^M$
7. $\frac{\delta L}{\delta \beta} \in \mathbb{R}^M$
8. $\frac{\delta L}{\delta Y} \in \mathbb{R}^{S \times M}$
9. $\frac{\delta L}{\delta X} \in \mathbb{R}^{S \times M}$

To start, the first derivative we calculate is that of $\frac{\delta L}{\delta \gamma}$.

$$\begin{aligned}
\frac{\delta L}{\delta \gamma} &=> \left[\frac{\delta L}{\delta \gamma} \right]_i = \frac{\delta L}{\delta \gamma_i} = \sum_{sj} \frac{\delta L}{\delta Y_{sj}} * \frac{\delta Y_{sj}}{\delta \gamma_i} \\
&= \sum_{sj} \frac{\delta L}{\delta Y_{sj}} * \frac{\delta \gamma_j \hat{X}_{sj}}{\delta \gamma_i} \\
&= \sum_{sj} \frac{\delta L}{\delta Y_{sj}} * \delta_{ji} \hat{X}_{sj} \\
&= \sum_s \frac{\delta L}{\delta Y_{si}} * \hat{X}_{si} \\
&= \sum_s \mathbf{1}_s * \frac{\delta L}{\delta Y_{si}} * \hat{X}_{si} \\
&=> \mathbf{1}^T * \left[\frac{\delta L}{\delta Y} \circ \hat{X} \right]
\end{aligned}$$

where $\mathbf{1}$ is a $1 \times S$ vector

In a similar way we can calculate the derivative with respect to β .

$$\begin{aligned}
\frac{\delta L}{\delta \beta} &=> \left[\frac{\delta L}{\delta \beta} \right]_i = \frac{\delta L}{\delta \beta_i} = \sum_{sj} \frac{\delta L}{\delta Y_{sj}} * \frac{\delta Y_{sj}}{\delta \beta_i} \\
&= \sum_{sj} \frac{\delta L}{\delta Y_{sj}} * \frac{\delta \gamma_j \hat{X}_{sj} + \beta_j}{\delta \beta_i} \\
&= \sum_{sj} \frac{\delta L}{\delta Y_{sj}} * \delta_{ji} \\
&= \sum_s \frac{\delta L}{\delta Y_{si}} \\
&= \mathbf{1}^T * \frac{\delta L}{\delta Y}
\end{aligned}$$

where $\mathbf{1}$ is a $1 \times S$ vector

Now on to calculating the derivative with respect to X . It would be good to first define the starting chain:

$$\frac{\delta L}{\delta X} => \frac{\delta L}{\delta X_{ri}} = \sum_{sj} \frac{\delta L}{\delta Y_{sj}} * \frac{\delta Y_{sj}}{\delta X_{ri}} \quad (1)$$

When focusing on $\frac{\delta Y_{sj}}{\delta X_{ri}}$, there are a number of aspects that come to play. To start, we can break it down into a chain, where we explicitly focus on the "contribution" that μ and σ have on X .

$$\frac{\delta Y_{sj}}{\delta X_{ri}} = \frac{\delta Y_{sj}}{\delta \hat{X}_{sj}} * \frac{\delta \hat{X}_{sj}}{\delta X_{ri}} + \frac{\delta Y_{sj}}{\delta \mu_j} * \frac{\delta \mu_j}{\delta X_{ri}} + \frac{\delta Y_{sj}}{\delta \sigma_j^2} * \frac{\delta \sigma_j^2}{\delta X_{ri}} \quad (2)$$

This contains quite a number of steps