

Code Folien

# Code „Simulation“

- Brief:
  - Joachim

# Code „ANOVA“

- Normal:
  - **Function:**  
`ow_a(rma_data, id = 1)`
  - **Define needed constants :**  
# Number of entities in one group  
`n_group = nrow(ow_rma_data)`  
  
# Number of factor levels  
`k = ncol(ow_rma_data) - 1`  
  
# Number of entities  
`n = (k * n_group)`

# Code „ANOVA“

- **Define basic ANOVA components:**

# Computation of the baseline component

```
grand_mean = mean(as.matrix(ow_rma_data[,2:(k + 1)]))
```

```
baseline_components = matrix(rep(grand_mean, times = n), nrow = n_group)
```

# Computation of the factor level components

```
conditional_means = apply(dependent_variable, 2, mean)
```

```
factor_level_components =
```

```
matrix(rep(conditional_means - grand_mean, each = n_group), nrow = n_group)
```

# Computation of the error components

```
error_components_ANOVA =
```

```
dependent_variable - baseline_components - factor_level_components
```

# Code „ANOVA“

- **Decomposition matrix:**

```
decomposition_matrix_ANOVA = data.frame("dependent_variable" = numeric(n),  
                                         "baseline" = numeric(n),  
                                         "factor_level" = numeric(n),  
                                         "error" = numeric(n)  
                                         )
```

```
decomposition_matrix_ANOVA$dependent_variable =      as.vector(dependent_variable)  
decomposition_matrix_ANOVA$baseline = as.vector(baseline_components)  
decomposition_matrix_ANOVA$factor_level =      as.vector(factor_level_components)  
decomposition_matrix_ANOVA$error = as.vector(error_components_ANOVA)
```

- **Compute sums of squares:**

```
ss_ANOVA = as.data.frame(t(colSums(decomposition_matrix_ANOVA^2)))  
rownames(ss_ANOVA) = "sums_of_squares,,
```

# Code „rmANOVA“

- Detailed:
  - **Function:**  
`ow_rma(rma_data, id = 1)`
  - **Define needed constants:**  
# Number of entities  
`n = nrow(ow_rma_data)`  
  
# Number of factor levels  
`k = ncol(ow_rma_data) - 1`
  - **Define basic rmANOVA components:**  
`grand_mean = mean(as.matrix(ow_rma_data[,2:(k + 1)]))`  
`baseline_components = matrix(rep(grand_mean, times = k*n), nrow = n)`  
  
`conditional_means = apply(dependent_variable, 2, mean)`  
`factor_level_components = matrix(rep(conditional_means - grand_mean, each = n), nrow = n)`  
  
`subject_means = apply(dependent_variable, 1, mean)`  
`subject_components = matrix(rep(subject_means - grand_mean, times = k), nrow = n)`  
  
`error_components = dependent_variable - baseline_components - factor_level_components - subject_components`

# Code „rmANOVA“

- Detailed:
  - **Decomposition matrix:**

```
decomposition_matrix = data.frame("dependent_variable" = numeric(n*k),  
                                "baseline" = numeric(n*k),  
                                "factor_level" = numeric(n*k),  
                                "subject_level" = numeric(n*k),  
                                "error" = numeric(n*k)  
                                )  
  
decomposition_matrix$dependent_variable = as.vector(dependent_variable)  
decomposition_matrix$baseline = as.vector(baseline_components)  
decomposition_matrix$factor_level = as.vector(factor_level_components)  
decomposition_matrix$subject_level = as.vector(subject_components)  
decomposition_matrix$error = as.vector(error_components)
```

# Code „rmANOVA“

- **Compute sums of squares:**

```
ss = as.data.frame(t(colSums(decomposition_matrix^2)))  
rownames(ss) = "sums_of_squares"
```

- **Set degrees of freedom:**

```
dof = data.frame("dependent_variable" = n*k,  
                 "baseline" = 1,  
                 "factor_level" = k-1,  
                 "subject_level" = n-1,  
                 "error" = (n*k)-1-(k-1)-(n-1)  
                 )
```

- **Compute mean squares:**

```
ms = ss / dof  
rownames(ms) = "mean_squares"
```

- **Compute corrected total sum of squares (variance):**

```
corrected_sst = ss$dependent_variable - ss$baseline  
variance = corrected_sst / (dof$dependent_variable - dof$baseline)
```



# Code „rmANOVA“

- **Compute F-values:**

`F_value_factor = ms$factor_level / ms$error`

`F_value_baseline = ms$baseline / ms$subject_level`

- **Set p-values of F distribution:**

`p_factor = 1 - pf(F_value_factor, dof$factor_level, dof$error)`

`p_baseline = 1 - pf(F_value_baseline, dof$baseline, dof$subject_level)`

# Code „Between Subject SS“

- Brief:
  - Function:  
`ow_rma_sse_reduct(rma_data, id = 1, plot_type = "pie", return_anova_table = FALSE)`
  - SSE in RM ANOVA is equal to SSE ANOVA minus SS Subjects:  
# ANOVA-tables of rmANOVA and ANOVA without repeated measures  
`ow_a_results = ow_a(ow_rma_data)[[1]]`  
`ow_rma_results = ow_rma(ow_rma_data)[[1]]`  
  
`sse_anova = ow_a_results[3, 2]`  
`ss_subject_anova = 0`  
# Always zero because the subject effect is not considered in an ANOVA without repeated measures  
  
`sse_rma = ow_rma_results[4, 2]`  
`ss_subject_rma = ow_rma_results[3, 2]`

# Code „CI“

- Brief:
  - **Function:**  
`rma_ci(rma_data, C_level = 0.95, id = 1, print_plot = TRUE)`
  - **Compute CI for Anova without repeated measures:**  
# Standard errors of the conditional means  
`SE = tapply(rma_data_long$value, rma_data_long$condition, sd)/sqrt(n)`  
  
# CI for ANOVA without repeated measures  
`Cldist_unadj = abs(qt((1 - C_level)/2, (n - 1))) * SE`
  - **Compute CI for Anova with repeated measures:**  
# Correction factor established by Morey (2008)  
`cf = sqrt(k/(k - 1))`  
  
`AdjVal = data.frame(Adj = (cf * ((rma_data_long$value - EEmlong$Em + Gm) - MeFlmlong$Flm)) + MeFlmlong$Flm)`  
`rma_data_long_adj = cbind.data.frame(rma_data_long, AdjVal)`  
  
# Standard errors of the conditional means adjusted with the method of O'Brien and Cousineau (2014, see also Loftus & Masson; 1994)  
`SE_adj = (tapply(rma_data_long_adj$Adj, rma_data_long_adj$condition, sd)/sqrt(n))`  
`Cldist_adj = abs(qt((1 - C_level)/2, (n - 1))) * SE_adj`

# Code „Effekt Size“

- Brief:
  - **Function:**  
`rma_eta(rma_data, id = 1, append = FALSE)`
  - **Compute effect size measures:**  
# Compute standard  $\eta^2$   
$$\eta_{sq} = SS_{Factor} / SS_{K\_Total}$$
  
  
# Compute partial  $\eta^2$   
$$\eta_{partial} = SS_{Factor} / (SS_{Factor} + SS_{Error})$$

# Code „Mauchly's Test“

- Medium:
  - **Defining some variables:**  
# Factor degrees of freedom  
df = k - 1  
  
# Empirical covariance matrix  
covariance\_matix = cov(dependent\_variable)
  - **Helmert matrix required for the computation of mauchly's W:**  
helmert = function(k) {  
 H = matrix(0, k, k)  
 diag(H) = (0:df) \* (-((0:df) \* ((0:df) + 1))^-0.5))  
 for (i in 2:k) {  
 H[i, 1:(i - 1)] = ((i - 1) \* (i))^-0.5  
 }  
 # H[1,] = 1/sqrt(k)  
 return(H)  
}  
  
# The first row of the helmert matrix is not required for further use in this procedure  
C = helmert(k)[-1, ]

# Code „Mauchly's Test“

- Medium:
  - **Computation of mauchly's W:**  
$$w = \det(C \% \% \text{covariance\_matix} \% \% t(C)) / ((\text{sum}(\text{diag}(C \% \% \text{covariance\_matix} \% \% t(C))) / df)^{df})$$
  - **Chi-Square Test:**  
# Computing the degrees of freedom for the chi-square value  
$$df\_w = ((k * df) / 2) - 1$$
  
  
# Computing the chi-square value  
$$f = 1 - ((2 * (df^2) + df + 2) / (6 * df * (n - 1)))$$
  
$$chi\_sq\_w = -(n - 1) * f * \log(w)$$
  
  
# Computing the corresponding p-value  
$$p\_w = 1 - \text{pchisq}(chi\_sq\_w, df\_w)$$

# Code „Correction of p-Values“

- Brief:
  - **The three different correction factors (epsilon):**
    - # Lower-Bound correction (Greenhouse & Geisser, 1959)  
 $\epsilon_{lb} = 1/df$
    - # Box correction (Geisser & Greenhouse, 1958)  
$$\epsilon_{gg} = (\text{sum}(\text{diag}(C \%*\% \text{covariance\_matix} \%*\% t(C)))^2) / (df * \text{sum}(\text{diag}(t((C \%*\% \text{covariance\_matix} \%*\% t(C))) \%*\% (C \%*\% \text{covariance\_matix} \%*\% t(C)))))$$
    - # Huynh-Feldt correction (Huynh & Feldt, 1976)  
$$\epsilon_{hf} = \min((n * df * \epsilon_{gg} - 2) / (df * (n - 1) - (df^2 * \epsilon_{gg})), 1)$$

# Code „Correction of p-Values“

- Brief:
  - **Coose recomendet adjustment and add to ANOVA-table:**  
`anova_table = rma(rma_data)[[1]]`  
  
`if (p_w < 0.05) {  
 if (p_factor_lb < 0.05) {  
 anova_table[, "Recommended Lower-Bound corrected p-Value (Greenhouse & Geisser,  
1959)"] = c(NA, p_factor_lb, NA, NA, NA, NA)  
 } else {  
 if (epsilon_gg < 0.75) {  
 anova_table[, "Recommended Box corrected p-Value (Geisser & Greenhouse, 1958)"] =  
c(NA, p_factor_gg, NA, NA, NA, NA)  
 } else {  
 anova_table[, "Recommended Huynh-Feldt corrected p-Value (Huynh & Feldt, 1976)"] =  
c(NA, p_factor_hf, NA, NA, NA, NA)  
 }  
 }  
}`



# Code „Orthogonal Polynomial Contrasts“

- Medium:
    - **Contrast analyses:**
- ```
# Applying formula for linear contrasts
weighted_dependend_variables = dependent_variable[rep(1:n, each = maxpoly), ] *
(constraint_weights)[rep(1:maxpoly, n), ]
linear_subject_contrasts = matrix(rowSums(weighted_dependend_variables), byrow = TRUE, ncol = maxpoly)

# Computing contrast estimators for each orthogonal polynomial contrast as well as standard errors for these
estimators
contrast_estimator = colMeans(linear_subject_contrasts)
contrast_se = sqrt(apply(linear_subject_contrasts, 2, var))/sqrt(n)

# Computing t-values for each contrast
contrast_t_values = contrast_estimator/contrast_se
# contrast_F_values = contrast_t_values^2

# Computing the corresponding p-values
contrast_p_values = 1 - pt(abs(contrast_t_values), n - 1)

# Computing sums of squares for each contrast
contrast_ss = n * contrast_estimator^2/rowSums(constraint_weights^2)
```

# Code „Displaying Trends“

- Detailed:
  - Niko
  - ggplot

# Code „Package“

- Medium:
  - Joachim und Niko

# Hinweise:

- Der Code ist natürlich hier noch nicht die Endfassung... wir sollten den entsprechenden finalen Code verwenden
- In der Subfunktion für die normale anova im Quantlet „SSE Reduct“ sollte auch noch das „id“ Argument eingebaut werden...
- Ich weiß, dass ist ganz schön viel Code, aber ich denke das ist gar nicht so schlecht, Sachen weglassen und überspringen kann man immer noch