

Homework #6

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For all questions, choose the **best** answer.

For questions 1 to 3, assume the following chart containing rod lengths to price:

length i	1	2	3	4	5
price p_i	2	3	5	7	8

1. What is $r[5]$?
 - a. 8
 - b. 9
 - c. 10
 - d. 11
 - e. 6

$R=[0, 2, 4, 6, 8, 10]$

Rod length 5 has a max revenue equal to max revenue of length 4 (which is 8) and max revenue of length 1 (which is 2). $8 + 2 = 10$

Cut is 4 pieces of rod length 1, which is max revenue 8. Plus 1 which is max revenue 2. In other words, 5 pieces of rod length 1.

2. Which of the following gives the max revenue to cut rod length 5?
 - a. No cuts
 - b. Five rods of length 1.
 - c. Two rods of length 2 and one rod of length 1.
 - d. One rod of length 4 and one rod of length 1.
 - e. Two rod of length 4 and one rod of length 1.
3. What is the total max revenue if you had rod length 3 and rod length 4?
 - a. 15
 - b. 10
 - c. 14
 - d. 18
 - e. 16

$r=[0, 2, 4, 6, 8, 10]$

Array r tells us the max revenue per each rod length. Answer is $6+8 = 14$

For questions 4 and 5, assume the following matrices and their corresponding dimensions:

$$\begin{aligned}A &= 3 \times 8 \\B &= 8 \times 10 \\C &= 10 \times 2 \\D &= 2 \times 4\end{aligned}$$

4. If you wanted to conduct the multiplication ABCD, what is the minimum number of multiplications?
- a. 1920
 - b. 2400
 - c. 800
 - d. 232
 - e. 340

Options are:

$(A(BC))D$
 $A((BC)D)$
 $A(B(CD))$
 $(AB)(CD)$
 $((AB)C)D$

$(A(BC))D$:

$$BC = 8 \times 10 \times 2 = 160$$

$$A(BC) = 160 + 3 \times 8 \times 2 = 208$$

$$(A(BC))D = 208 + 3 \times 2 \times 4 = 232$$

$A((BC)D)$:

$$BC = 8 \times 10 \times 2 = 160$$

$$(BC)D = 8 \times 2 \times 4 + 160 = 224$$

$$A((BC)D) = 3 \times 8 \times 4 + 224 = 320$$

Options $A(B(CD))$, $(AB)(CD)$, and $((AB)C)D$ produce total multiplications greater than 232 as well. So the minimum is 232.

5. What is the ordering of matrix multiplication that would produce the minimum number of multiplications?
- a. $((AB)C)D$
 - b. $((A(BC))D)$
 - c. $(A(B(CD)))$
 - d. $((AB)(CD))$
 - e. $(A((BC)D))$