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Part 2

2a) 1. $(a \vee b) \oplus (c \wedge d)$

2. $\neg a$

3. $\neg c$

4. $\neg \neg \neg c$ (3, double negation)

5. $\neg \neg \neg c \vee \neg d$ (4, addition)

6. $\neg (\neg \neg c \wedge d)$ (5, De Morgan)

7. $\neg (c \wedge d)$ (6, double negation)

8. $a \vee b$ (7, 1)

9. b (8, 2)

2b) 1. Assum: $f(0)=0$, $f(1)=2$, $f(n) = f(n-1) + 3f(n-2) + 4$, and $f(n)$ equals an odd number, for some $n < 0$

2. However: the least value n for which $f(n)$ is defined is $n=0$ as $f(0)=0$. It contradicts with the assumption of $f(n)$ for some $n < 0$. Therefore, for every $n \geq 0$, $f(n) = f(n-1) + 3f(n-2) + 4$ equals an even number