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1  // A validator to check and verify something has a factored form...
2  function factorCheck(f,g) {
3      // This validator is designed to check that a student is submitting a factored polynomial
4      // Checking that there are the correct number of non-numeric and non-inverse factors as
5      // Checking that the submitted answer and the expected answer are the same via real Xr
6      // Checking that the outer most (last to be computed when following order of operations
7
8      var operCheck = f.tree[0]; // Check to see if the root operation is multiplication at end
9      var studentFactors = f.tree.length; // Temporary number of student-provided factors (+1 b
10
11     // Now we adjust the length to remove any numeric factors, or division factors, etc to a
12     for (var i = 0; i < f.tree.length; i++) {
13         if ((typeof f.tree[i] === 'number') || (f.tree[i][0] == '-') || (f.tree[i][0] == '/')) {
14             studentFactors = studentFactors - 1;
15         }
16     }
17
18     // Now we do the same with the provided answer, in case sage or something provides a we
19     var answerFactors = g.tree.length;
20
21     // Adjust length in the same way, so that it will match the students if it should.
22     for (var i = 0; i < g.tree.length; i++) {
23         if (typeof g.tree[i] === 'number') {
24             answerFactors = answerFactors - 1;
25         }
26     }
27
28     // Note: An especially dedicated student could pad with weird factors that are happen to
29     // For example, a student could enter sin^2(x)+cos^2(x) as a multiplicative factor to pa
30     // This would be somewhat difficult to think of, even on purpose.
31     // Until I can reliably evaluate the factors themselves as functions though, there isn't
32
33     return ((f.equals(g)) && (studentFactors == answerFactors) && (operCheck == '*'))
34 }

```

Note: Make sure to **fully** factor each of the below. Remember that, factor by grouping is just **one** step in the factoring process, you should check any resulting factors you get after factor by grouping (or any other factoring method) to see if they are still factorable.

Problem 1 Factor the following polynomial:

$$3x^3 + x^2 - 3x - 1 = \boxed{(3x + 1)(x + 1)(x - 1)}$$

Feedback(attempt): You want to factor by grouping, so you want to group up terms into pairs and then factor out any common terms from each pair. For example, if you had $9x^3 + 8x^2 - 144x - 128$ then you could group it as $(9x^3 + 8x^2) + (-144x - 128)$, then factor out any common factors in each group; $x^2(9x + 8) - 16(9x + 8)$, then pull out the common term in the parentheses (only works if they are the same!) to get $(9x + 8)(x^2 - 16)$. This isn't the end though; you need to fully factor, so you need to check both terms to see if either is factorable, in this case $(x^2 - 16)$ is factorable to $(x - 4)(x + 4)$ which gets you $(9x + 8)(x - 4)(x + 4)$ as your final factoring.

Problem 2 Factor the following polynomial:

$$3x^3 - 5x^2 - 12x + 20 = \boxed{(3x - 5)(x + 2)(x - 2)}$$

Feedback(attempt): You want to factor by grouping, so you want to group up terms into pairs and then factor out any common terms from each pair. For example, if you had $9x^3 + 8x^2 - 144x - 128$ then you could group it as $(9x^3 + 8x^2) + (-144x - 128)$, then factor out any common factors in each group; $x^2(9x + 8) - 16(9x + 8)$, then pull out the common term in the parentheses (only works if they are the same!) to get $(9x + 8)(x^2 - 16)$. This isn't the end though; you need to fully factor, so you need to check both terms to see if either is factorable, in this case $(x^2 - 16)$ is factorable to $(x - 4)(x + 4)$ which gets you $(9x + 8)(x - 4)(x + 4)$ as your final factoring.

Problem 3 Factor the following polynomial:

$$2x^3 + 5x^2 - 128x - 320 = \boxed{(2x + 5)(x + 8)(x - 8)}$$

Feedback(attempt): You want to factor by grouping, so you want to group up terms into pairs and then factor out any common terms from each pair. For example, if you had $9x^3 + 8x^2 - 144x - 128$ then you could group it as $(9x^3 + 8x^2) + (-144x - 128)$, then factor out any common factors in each group; $x^2(9x + 8) - 16(9x + 8)$, then pull out the common term in the parentheses (only works if they are the same!) to get $(9x + 8)(x^2 - 16)$. This isn't the end though; you need to fully factor, so you need to check both terms to see if either is factorable, in this case $(x^2 - 16)$ is factorable to $(x - 4)(x + 4)$ which gets you $(9x + 8)(x - 4)(x + 4)$ as your final factoring.

Problem 4 Factor the following polynomial:

$$4x^3 + 2x^2 - 196x - 98 = \boxed{(4x + 2)(x + 7)(x - 7)}$$

Feedback(attempt): You want to factor by grouping, so you want to group up terms into pairs and then factor out any common terms from each pair. For example, if you had $9x^3 + 8x^2 - 144x - 128$ then you could group it as $(9x^3 + 8x^2) + (-144x - 128)$, then factor out any common factors in each group; $x^2(9x + 8) + -16(9x + 8)$, then pull out the common term in the parentheses (only works if they are the same!) to get $(9x + 8)(x^2 - 16)$. This isn't the end though; you need to fully factor, so you need to check both terms to see if either is factorable, in this case $(x^2 - 16)$ is factorable to $(x - 4)(x + 4)$ which gets you $(9x + 8)(x - 4)(x + 4)$ as your final factoring.

Problem 5 Factor the following polynomial:

$$x^5 + 4x^4 - 29x^3 - 116x^2 + 100x + 400 = \boxed{(x + 5)(x + 4)(x + 2)(x - 2)(x - 5)}$$

Feedback(attempt): You want to factor by grouping, so you want to group up terms into pairs and then factor out any common terms from each pair. For example, if you had $9x^3 + 8x^2 - 144x - 128$ then you could group it as $(9x^3 + 8x^2) + (-144x - 128)$, then factor out any common factors in each group; $x^2(9x + 8) + -16(9x + 8)$, then pull out the common term in the parentheses (only works if they are the same!) to get $(9x + 8)(x^2 - 16)$. This isn't the end though; you need to fully factor, so you need to check both terms to see if either is factorable, in this case $(x^2 - 16)$ is factorable to $(x - 4)(x + 4)$ which gets you $(9x + 8)(x - 4)(x + 4)$ as your final factoring.
