

JavaScript

```

1  var x;
2
3  // sameDerivative checks to see if the derivative with respect to x and C are equal.
4  sameDerivative = function(a,b) {
5      return (a.derivative('x').equals( b.derivative('x') ) && a.derivative('C').equals( b
6  });
7
8
9  function factorCheck(f,g) {
10     // This validator is designed to check that a student is submitting a factored polynomial
11     // Checking that there are the correct number of non-numeric and non-inverse factors
12     // Checking that the submitted answer and the expected answer are the same via regular expressions
13     // Checking that the outer most (last to be computed when following order of operations)
14
15     var operCheck = f.tree[0]; // Check to see if the root operation is multiplication or division
16     var studentFactors = f.tree.length; // Temporary number of student-provided factors
17
18     // Now we adjust the length to remove any numeric factors, or division factors, etc
19     for (var i = 0; i < f.tree.length; i++) {
20         if ((typeof f.tree[i] === 'number') || (f.tree[i][0] == '-') || (f.tree[i][0] == '/') || (f.tree[i][0] == '^')) {
21             studentFactors = studentFactors - 1;
22         }
23     }
24
25     // Now we do the same with the provided answer, in case sage or something provides a simplified answer
26     var answerFactors = g.tree.length;
27
28     // Adjust length in the same way, so that it will match the students if it should.
29     for (var i = 0; i < g.tree.length; i++) {
30         if (typeof g.tree[i] === 'number') {
31             answerFactors = answerFactors - 1;
32         }
33     }
34
35     // Note: An especially dedicated student could pad with weird factors that all happen to be 1
36     // For example, a student could enter sin^2(x)+cos^2(x) as a multiplicative factor that is always 1
37     // This would be somewhat difficult to think of, even on purpose.
38     // Until I can reliably evaluate the factors themselves as functions though, there is no way to check this
39
40     return ((f.equals(g)) && (studentFactors === answerFactors) && (operCheck === '*'))
41 }
42

```

Problem 1 Factor the following radicand to force the type two radical into

being a type one radical:

$$\sqrt{25x^3 + 135x^2 + 216x + 108} = \sqrt{(5x + 6)(5x + 6)(x + 3)}$$

Feedback(attempt): You should have all linear factors above. In particular you should not have any factors higher than degree 1 polynomials. Essentially you can treat the radicand as if it were a polynomial factoring problem and factor the polynomial just like you would have normally.

Note: Repeated factors should be entered in distinctly for the validator. For example, instead of writing something like $x^2(x - 1)^2$ you should enter it in as $(x - 0)(x - 0)(x - 1)(x - 1)$.

Problem 2 Factor the following radicand to force the type two radical into being a type one radical:

$$\sqrt{4x^2 - 8x - 12} = \sqrt{(2x + 2)(2x - 6)}$$

Feedback(attempt): You should have all linear factors above. In particular you should not have any factors higher than degree 1 polynomials. Essentially you can treat the radicand as if it were a polynomial factoring problem and factor the polynomial just like you would have normally.

Note: Repeated factors should be entered in distinctly for the validator. For example, instead of writing something like $x^2(x - 1)^2$ you should enter it in as $(x - 0)(x - 0)(x - 1)(x - 1)$.

Problem 3 Factor the following radicand to force the type two radical into being a type one radical:

$$\sqrt{36x^4 + 108x^3 - 576x^2 + 432x} = \sqrt{(3x)(4x - 4)(3x - 6)(x + 6)}$$

Feedback(attempt): You should have all linear factors above. In particular you should not have any factors higher than degree 1 polynomials. Essentially you can treat the radicand as if it were a polynomial factoring problem and factor the polynomial just like you would have normally.

Note: Repeated factors should be entered in distinctly for the validator. For example, instead of writing something like $x^2(x - 1)^2$ you should enter it in as $(x - 0)(x - 0)(x - 1)(x - 1)$.