

Laurent series

$$\begin{aligned}e^z &= \sum_{n=0}^{\infty} \frac{1}{n!} z^n & |z| < \infty \\ \sin z &= \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n+1)!} z^{2n+1} & |z| < \infty \\ \cos z &= \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n)!} z^{2n} & |z| < \infty \\ \sinh z &= \sum_{n=0}^{\infty} \frac{1}{(2n+1)!} z^{2n+1} & |z| < \infty \\ \cosh z &= \sum_{n=0}^{\infty} \frac{1}{(2n)!} z^{2n} & |z| < \infty \\ \frac{1}{1-z} &= \sum_{n=0}^{\infty} z^n & |z| < 1 \\ \frac{1}{1-z} &= \sum_{n=0}^{\infty} -z^{-n-1} & |z| > 1 \\ \frac{1}{1+z} &= \sum_{n=0}^{\infty} (-1)^n z^n & |z| < 1 \\ \ln(1+z) &= \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} z^n & |z| < 1 \\ (1+z)^\alpha &= \sum_{n=0}^{\infty} \binom{\alpha}{n} z^n & |z| < 1 \\ e^{-1/z^2} &= \sum_{n=0}^{\infty} \frac{(-1)^n}{n!} z^{-2n} & 0 < |z| < \infty \\ \arcsin z &= \sum_{n=0}^{\infty} \frac{(2n)!}{4^n (n!)^2 (2n+1)} z^{2n+1} & |z| < 1 \\ \arctan z &= \sum_{n=0}^{\infty} \frac{(-1)^n}{2n+1} z^{2n+1} & |z| < 1\end{aligned}$$