Discrete time systems and z-transform

Exercises module 4

1. Calculate the inverse z-transform of the following sequences:

a)
$$X(z) = (1+3z)(1+2z^{-1})(1-z^{-1})$$

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b) $X(z) = \frac{1-\frac{1}{2}z^{-1}}{1+\frac{3}{4}z^{-1}+\frac{1}{8}z^{-2}} |z| > \frac{1}{2}$

c)
$$X(z) = \frac{1 - \frac{1}{2}z^{-1}}{1 - \frac{1}{4}z^{-2}}$$
 $|z| > \frac{1}{2}$

d)
$$X(z) = \frac{1-az^{-1}}{z^{-1}-a} |z| > \left|\frac{1}{a}\right|$$

e)
$$X(z) = \ln(1 - 4z)$$
 $|z| < \frac{1}{4}$

c)
$$X(z) = \frac{1 - \frac{1}{2}z^{-1}}{1 - \frac{1}{4}z^{-2}}$$
 $|z| > \frac{1}{2}$
d) $X(z) = \frac{1 - az^{-1}}{z^{-1} - a}$ $|z| > \left| \frac{1}{a} \right|$
e) $X(z) = \ln(1 - 4z)$ $|z| < \frac{1}{4}$
f) $X(z) = \frac{3 - 7z^{-1} + 5z^{-2}}{1 - \frac{5}{2}z^{-1} + z^{-2}}$ $\frac{1}{2} < |z| < 2$