432 Class 19 Slides

github.com/THOMASELOVE/432-2018

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Setup

```
library(skimr)
library(arm)
library(rms)
library(boot)
library(MASS)
library(HSAUR)
library(pscl)
library(lmtest)
library(sandwich)
library(broom)
library(tidyverse)
```

Project 2 Instructions

Project 2

Instructions are here. There are three deliverables.

- 2018-04-17 Registration/Scheduling Form
 - If you can't do May 3, 7, and 8, here's the place to tell me.
- Portfolio (R Markdown + HTML + data or pseudo-data)
 - 3 hours before your presentation
 - 2 template options, or go off on your own (carefully)
- Presentation May 3, 7 or 8
 - in a few cases by special arrangement, before May 3

Overview

Today's Materials

Regression Models for Count Outcomes

- Poisson Regression model
- Negative Binomial Regression model
- Zero-inflated models

The medicare data

The medicare example

The data we will use come from the NMES1988 data set in R's AER package, although I have built a cleaner version for you in the medicare.csv file on our web site. These are essentially the same data as are used in my main resource from the University of Virginia for hurdle models.

These data are a cross-section originating from the US National Medical Expenditure Survey (NMES) conducted in 1987 and 1988. The NMES is based upon a representative, national probability sample of the civilian non-institutionalized population and individuals admitted to long-term care facilities during 1987. The data are a subsample of individuals ages 66 and over all of whom are covered by Medicare (a public insurance program providing substantial protection against health-care costs), and some of whom also have private supplemental insurance.

```
medicare <- read.csv("medicare.csv") %>% tbl_df
```

The medicare code book

Variable	Description
subject	subject number
visits	outcome of interest: number of physician office visits
hospital	number of hospital stays
health	self-perceived health status (poor, average, excellent)
chronic	number of chronic conditions
sex	male or female
school	number of years of education
insurance	is the subject (also) covered by private insurance? (yes or no)

Today's Goal

Predict visits using some combination of these 6 predictors...

Predictor	Description
hospital	number of hospital stays
health	self-perceived health status (poor, average, excellent)
chronic	number of chronic conditions
sex	male or female
school	number of years of education
insurance	is the subject (also) covered by private insurance? (yes or no)

The medicare tibble

```
# A tibble: 4,406 x 8
  subject visits hospital health chronic sex school
    <int> <int> <int> <fct>
                                   <int> <fct>
                                                 <int>
               5
                                       2 male
                        1 average
                                       2 female
                                                    10
                        0 average
              13
                        3 poor
                                       4 female
                                                    10
              16
                        1 poor
                                       2 male
 5
        5
               3
                                      2 female
                        0 average
 6
        6
              17
                                     5 female
                        0 poor
                                       0 female
                         average
        8
8
                         average
                                       0 female
                         average
                                       0 female
       10
10
                         average
                                       0 female
```

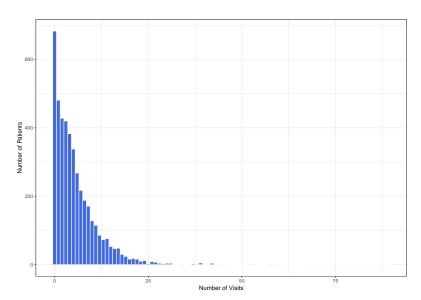
... with 4,396 more rows, and 1 more variable:

[#] insurance <fct>

A skim of medicare

```
> skim(medicare)
Skim summary statistics
n obs: 4406
n variables: 8
Variable type: factor
  variable missing complete
                              n n_unique
                                                                   top_counts ordered
   health
                      4406 4406
                                        3 ave: 3509, poo: 554, exc: 343, NA: 0
                                                                                FALSE
 insurance
                      4406 4406
                                                     ves: 3421. no: 985. NA: 0
                                                                                FALSE
                                                   fem: 2628. mal: 1778. NA: 0
                      4406 4406
                                                                                 FALSE
       sex
                 0
Variable type: integer
 variable missing complete
                                                      p25 median
                                                                     p75 p100
                                                                                  hist
                                  mean
                                            sd p0
  chronic
                0
                     4406 4406
                                  1.54
                                          1.35 0
hospital
                     4406 4406
                                  0.3
                                           0.75 0
  school
                0
                     4406 4406
                                 10.29
                                           3.74
                                                                            18
  subject
                      4406 4406 2203.5 1272.05 1 1102.25 2203.5 3304.75 4406
   visits
                      4406 4406
                                  5.77
                                           6.76 0
                                                                            89
```

Our outcome, visits



Counting the visits

medicare %>% count(visits)

```
A tibble: 60 \times 2
   visits
                n
    <int> <int>
 1
         0
              683
              481
3
              428
         3
              420
 5
         4
              383
6
         5
              338
         6
              268
8
              217
9
         8
              188
         9
10
              171
  ... with 50 more rows
```

visits summary

describe(medicare\$visits)

medicare\$visits

missing	distinct	${\tt Info}$	Mean	Gmd
0	60	0.992	5.774	6.227
.10	.25	.50	.75	.90
0	1	4	8	13
	0.10	0 60 .10 .25	0 60 0.992 .10 .25 .50	0 60 0.992 5.774 .10 .25 .50 .75

lowest: 0 1 2 3 4, highest: 63 65 66 68 89

Reiterating the Goal

Predict visits using some combination of these 6 predictors...

Predictor	Description
hospital	number of hospital stays
health	self-perceived health status (poor, average, excellent)
chronic	number of chronic conditions
sex	male or female
school	number of years of education
insurance	is the subject (also) covered by private insurance? (yes or no)

Model 1: A Poisson Regression

Poisson Regression

Assume our count data (visits) follows a Poisson distribution with a mean conditional on our predictors.

Remember the sample size here. Is statistical significance going to be our problem?

Model 1 (Poisson Regression)

 mod_1

```
Call: glm(formula = visits ~ hospital + health + chronic + se
  insurance, family = "poisson", data = medicare)
```

Coefficients:

```
      (Intercept)
      hospital
      healthexcellent

      1.02887
      0.16480
      -0.36199

      healthpoor
      chronic
      sexmale

      0.24831
      0.14664
      -0.11232

      school
      insuranceyes

      0.02614
      0.20169
```

Degrees of Freedom: 4405 Total (i.e. Null); 4398 Residual

Null Deviance: 26940

Residual Deviance: 23170 AIC: 35960

tidy(mod_1) with rounding and p values

```
tidy(mod_1, conf.int = F) %>%
  kable(format = "pandoc", digits = 2)
```

term	estimate	std.error	statistic	p.value
(Intercept)	1.03	0.02	43.26	0
hospital	0.16	0.01	27.48	0
healthexcellent	-0.36	0.03	-11.95	0
healthpoor	0.25	0.02	13.92	0
chronic	0.15	0.00	32.02	0
sexmale	-0.11	0.01	-8.68	0
school	0.03	0.00	14.18	0
insuranceyes	0.20	0.02	11.96	0

tidy(mod_1) with rounding and CI

```
tidy(mod_1, conf.int = T) %>%
    select(-statistic, -p.value) %>%
    kable(format = "pandoc", digits = 2)
```

term	estimate	std.error	conf.low	conf.high
(Intercept)	1.03	0.02	0.98	1.08
hospital	0.16	0.01	0.15	0.18
healthexcellent	-0.36	0.03	-0.42	-0.30
healthpoor	0.25	0.02	0.21	0.28
chronic	0.15	0.00	0.14	0.16
sexmale	-0.11	0.01	-0.14	-0.09
school	0.03	0.00	0.02	0.03
insuranceyes	0.20	0.02	0.17	0.23

Interpret the male and chronic variables

We have an additive model in the log(visits) scale.

- Coefficient of male is -0.11, with 95% CI (-0.14, -0.09)
 - If Harry and Sally share the same values for all other variables in the model, but Harry is male and Sally is female, then log(visits) for Harry is estimated to be -0.11 smaller than log(visits) for Sally.
- Coefficient of chronic is 0.15, with 95% CI (0.14, 0.16)
 - If Harry and Steve share the same values for all other variables in the model, but Harry has one more chronic illness than Steve, then log(visits) for Harry is estimated to be 0.15 larger than log(visits) for Steve.

The Fitted Equation

$$\begin{array}{l} \textit{log(} \ \text{visits }) = 1.03 + 0.16 \ \text{hospital} \ -0.36 (\ \text{health} = \text{excellent }) + \\ 0.25 (\ \text{health} = \text{poor }) + 0.15 \ \text{chronic} \ -0.11 (\ \text{sex} = \text{male }) \\ + 0.03 \ \text{school} \ + 0.20 (\ \text{insurance} = \text{yes}) \end{array}$$

So, the count of visits follows a Poisson distribution, with mean λ , where:

$$\begin{split} \lambda = \exp[1.03 + 0.16 \text{ hospital } -0.36(\text{ health} = \text{excellent }) + \\ 0.25(\text{ health} = \text{poor }) + 0.15 \text{ chronic } -0.11(\text{ sex} = \text{male }) \\ +0.03 \text{ school } +0.20(\text{ insurance} = \text{yes})] \end{split}$$

Expressing the model differently

```
tidy(mod_1, exponentiate = T, conf.int = T) %>%
    select(-statistic, -p.value) %>%
    kable(format = "pandoc", digits = 2)
```

term	estimate	std.error	conf.low	conf.high
(Intercept)	2.80	0.02	2.67	2.93
hospital	1.18	0.01	1.17	1.19
healthexcellent	0.70	0.03	0.66	0.74
healthpoor	1.28	0.02	1.24	1.33
chronic	1.16	0.00	1.15	1.17
sexmale	0.89	0.01	0.87	0.92
school	1.03	0.00	1.02	1.03
insuranceyes	1.22	0.02	1.18	1.26

Interpret the male and chronic after exponentiation

Now, we have a multiplicative model in the visits scale.

- exp(male) is 0.89, with 95% CI (0.87, 0.92)
 - If Harry and Sally share the same values for all other variables in the model, but Harry is male and Sally is female, then visits for Harry is estimated to be 0.89 times the visits for Sally. Harry is expected to have 89% of the visits Sally has.
- exp(chronic) is 1.16, with 95% CI (1.15, 1.17)
 - If Harry and Steve share the same values for all other variables in the model, but Harry has one more chronic illness than Steve, then visits for Harry is estimated to be 1.16 times visits for Steve. Harry is expected to have 116% of the visits Steve has.

display(mod_1) from arm package

display(mod_1)

```
glm(formula = visits ~ hospital + health + chronic + sex + scl
   insurance, family = "poisson", data = medicare)
             coef.est coef.se
(Intercept) 1.03 0.02
hospital
       0.16 0.01
healthexcellent -0.36 0.03
healthpoor 0.25 0.02
chronic 0.15 0.00
sexmale -0.11 0.01
school 0.03 0.00
insuranceyes 0.20 0.02
 n = 4406, k = 8
 residual deviance = 23167.8, null deviance = 26942.9 (differ
```

summary(mod_1)

```
summary(mod_1)
Call:
qlm(formula = visits \sim hospital + health + chronic + sex + school +
   insurance, family = "poisson", data = medicare)
Deviance Residuals:
   Min
             10 Median
                                     Max
                             30
-8.4055 -1.9962 -0.6737
                         0.7049 16.3620
Coefficients:
               Estimate Std. Error z value Pr(>|z|)
(Intercept)
                         0.023785 43.258
                                           <2e-16 ***
               1.028874
                         0.005997 27.478
hospital
               0.164797
                                           <2e-16 ***
healthexcellent -0.361993
                         0.030304 -11.945 <2e-16 ***
healthpoor
               0.248307
                         0.017845 13.915
                                           <2e-16 ***
chronic
               0.146639
                         0.004580 32.020
                                           <2e-16 ***
sexmale
       -0.112320
                         0.012945 -8.677 <2e-16 ***
school
       0.026143
                         0.001843 14.182
                                           <2e-16 ***
               0.201687
                         0.016860 11.963
                                            <2e-16 ***
insuranceves
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for poisson family taken to be 1)
   Null deviance: 26943 on 4405 degrees of freedom
Residual deviance: 23168 on 4398 degrees of freedom
AIC: 35959
Number of Fisher Scoring iterations: 5
```

confint(mod_1)

confint(mod_1)

Waiting for profiling to be done...

	2.5 %	97.5 %
(Intercept)	0.98214199	1.07537749
hospital	0.15296768	0.17647770
${\tt healthexcellent}$	-0.42189692	-0.30309508
healthpoor	0.21324851	0.28319940
chronic	0.13764952	0.15560166
sexmale	-0.13771836	-0.08697322
school	0.02253268	0.02975845
insuranceyes	0.16873364	0.23482518

Testing the Predictors

> anova(mod_1, test = "Chisq")

- Wald tests are provided with the Poisson regression summary.
- ANOVA approach lets us do sequential likelihood ratio tests.

```
Analysis of Deviance Table
Model: poisson, link: log
Response: visits
Terms added sequentially (first to last)
         Df Deviance Resid. Df Resid. Dev Pr(>Chi)
NULL
                        4405
                                  26943
hospital 1 1494.22
                        4404
                                  25449 < 2.2e-16
health 2 756.68
                                                 ***
                        4402
                                  24692 < 2.2e-16
chronic 1 961.76
                                  23730 < 2.2e-16
                                                 ***
                        4401
              61.27
                        4400
                                  23669 4.981e-15
                                                 ***
sex
school.
             353.21
                                                 ***
                        4399
                                  23316 < 2.2e-16
```

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Making Predictions

```
medicare %>% head(2)
```

Store Predictions

```
1 5 5.658592 -0.6585917
2 1 5.961186 -4.9611865
```

Calculating a Pseudo-R² for mod_1

```
(mod_1_r <- with(mod_1_aug, cor(visits, .fitted)))
[1] 0.3144637
(mod_1_r^2)</pre>
```

[1] 0.09888744

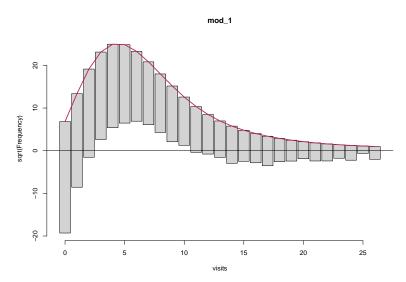
glance(mod 1)

Summarizing the Model's Fit

```
null.deviance df.null logLik AIC BIC
1 26942.92 4405 -17971.61 35959.23 36010.35
deviance df.residual
1 23167.81 4398
```

Rootogram: See the Fit (using default choices)

countreg::rootogram(mod_1)

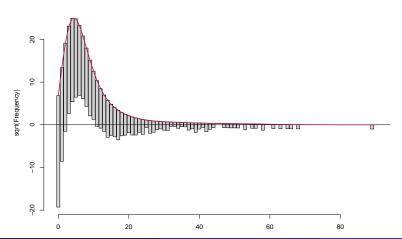


Interpreting the Hanging Rootogram

- The red curved line is the theoretical Poisson fit.
- "Hanging" from each point on the red line is a bar, the height of which represents the difference between expected and observed counts.
 - A bar hanging below 0 indicates underfitting. (In this case, this refers to when our predict fewer values than the data show.)
 - A bar hanging above 0 indicates overfitting. (In this case, this refers to when our model predicts more values than the data show.)
- The counts have been transformed with a square root transformation to prevent smaller counts from getting obscured and overwhelmed by larger counts.

The Complete Hanging Rootogram for Model 1

Rootogram for Poisson mod_1



Interpreting the Rootogram for Model 1

In mod_1, we see a great deal of underfitting for counts of 0 and 1, then overfitting for visit counts in the 3-10 range, with some underfitting again at more than a dozen or so visits.

• Our Poisson model (mod_1) doesn't fit enough zeros or ones, and fits too many 3-12 values, then not enough of the higher values.

How many zero counts does Model 1 predict?

```
lam <- predict(mod_1, type = "response") # exp. mean count
exp <- sum(dpois(x = 0, lambda = lam)) # sum the prob(0)
round(exp)</pre>
```

[1] 47

How many subjects with zero visits did we see?

Do we have an overdispersion problem?

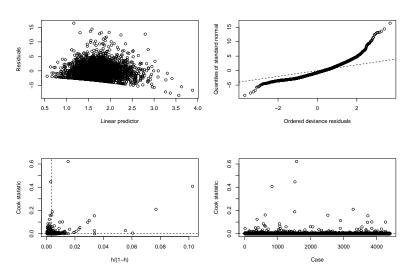
overdispersion ratio is 6.706136

p value of overdispersion test: (

Code used on previous slide

```
yhat <- predict(mod_1, type = "response")
n <- 4406; k <- 8 # use display(mod_1) to see these
z <- (mod_1_aug$visits - mod_1_aug$.fitted) /
    sqrt(mod_1_aug$.fitted)
cat("overdispersion ratio is ", sum(z^2)/ (n - k), "\n")
cat("p value of overdispersion test: ",
    pchisq(sum(z^2), df = n-k, lower.tail = FALSE), "\n")</pre>
```

glm.diag.plots from boot for Model 1



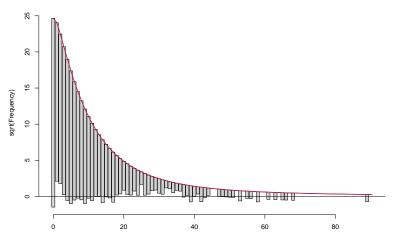
The Negative Binomial Model (mod_2)

Fitting the Negative Binomial Model

Looks like our data are overdispersed compared to what a Poisson model expects.

Rootogram for Negative Binomial Model





Save predicted values and residuals

```
# A tibble: 2 x 3
  visits fitted resid
  <int> <dbl> <dbl>
1     5     5.79 -0.787
2     1     5.88 -4.88
```

Pseudo-R² for Neg. Bin. model (mod_2)

We can calculate a proxy for R^2 as the squared correlation of the fitted values and the observed values.

```
mod2_r <- with(mod_2_aug, cor(visits, fitted))
mod2_r^2</pre>
```

```
[1] 0.08271151
```

What is a Zero-Inflated Model?

Zero-Inflated Poisson (ZIP) model

The zero-inflated Poisson or (ZIP) model is used to describe count data with an excess of zero counts.

The model posits that there are two processes involved:

- a logit model is used to predict excess zeros
- while a Poisson model is used to predict the counts

The pscl package is used here, which can conflict with the countreg package we used to fit rootograms.

Fitting the ZIP model (Model mod_3)

summary(mod_3) (and see next 2 slides)

```
> summary(mod 3)
Call:
zeroinfl(formula = visits ~ hospital + health + chronic + sex + school + insurance, data = medicare)
Pearson residuals:
   Min
           10 Median
                                Max
                          30
-5.4092 -1.1579 -0.4769 0.5435 25.0380
Count model coefficients (poisson with log link):
               Estimate Std. Error z value Pr(>|z|)
(Intercept)
               1.405812
                         0.024175 58.152 < 2e-16 ***
hospital
               0.159011 0.006060 26.239 < 2e-16 ***
healthexcellent -0.304134    0.031151    -9.763    < 2e-16 ***
healthpoor
              0.253454 0.017705 14.315 < 2e-16 ***
chronic
              0.101836    0.004721    21.571    < 2e-16 ***
sexmale
              school
              insuranceyes
               0.080557
                         0.017145 4.699 2.62e-06 ***
Zero-inflation model coefficients (binomial with logit link):
              Estimate Std. Error z value Pr(>|z|)
(Intercept)
              -0.08102 0.14233 -0.569 0.569219
hospital
              -0.30330 0.09158 -3.312 0.000927 ***
healthexcellent 0.23786
                         0.14990 1.587 0.112550
healthpoor
               0.02166
                         0.16170 0.134 0.893431
                      0.04601 -11.545 < 2e-16
chronic
              -0.53117
sexmale
                      0.08919 4.656 3.22e-06
            0.41527
              -0.05677
                      0.01223 -4.640 3.49e-06 ***
school
              -0.75294
                         0.10257 -7.341 2.12e-13 ***
insuranceyes
Signif, codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Number of iterations in BFGS optimization: 24
Log-likelihood: -1.613e+04 on 16 Df
```

Zero-inflation model coefficients in mod_3

```
Zero-inflation model coefficients (binomial with logit link):
              Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.08102
                        0.14233 -0.569 0.569219
                        0.09158 -3.312 0.000927 ***
hospital
        -0.30330
healthexcellent 0.23786
                        0.14990 1.587 0.112550
healthpoor 0.02166
                        0.16170 0.134 0.893431
chronic
       -0.53117
                        0.04601 - 11.545 < 2e - 16
sexmale 0.41527
                        0.08919 4.656 3.22e-06
school
      -0.05677
                        0.01223 -4.640 3.49e-06
insuranceyes -0.75294
                        0.10257 -7.341 2.12e-13
                                              ***
Signif. codes: 0 '***'
                    0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Count model coefficients in mod_3

```
Count model coefficients (poisson with log link):
               Estimate Std. Error z value Pr(>|z|)
(Intercept)
               1.405812 0.024175 58.152 < 2e-16
hospital
        0.159011 0.006060 26.239 < 2e-16
healthexcellent -0.304134 0.031151 -9.763 < 2e-16
                                                ***
healthpoor 0.253454
                         0.017705 14.315 < 2e-16
                                                ***
chronic
             0.101836 0.004721 21.571 < 2e-16
sexmale -0.062332 0.013054 -4.775 1.80e-06
                                                ***
school
             0.019144
                         0.001873 10.221 < 2e-16
                                                ***
                                                ***
               0.080557
                         0.017145
                                   4.699 2.62e-06
insuranceyes
```

The Fitted Equation (part 1 of 2)

The form of the model equation for a zero-inflated Poisson regression requires us to take two separate models into account.

First, we have a logistic regression model to predict the log odds of zero visits. . .

That takes care of the extra zeros.

The Fitted Equation (part 2 of 2)

The form of the model equation for a zero-inflated Poisson regression requires us to take two separate models into account.

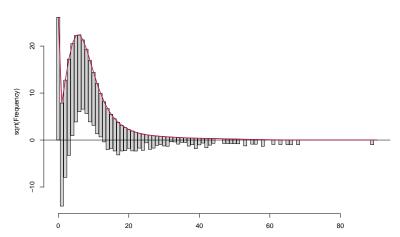
Second, we have a Poisson regression model to predict log(visits)...

```
log(visits) = 1.41 + 0.16 hospital -
     0.30 health = excellent + 0.25 health = poor +
     0.10 chronic - 0.06 sex = male + 0.02 school +
     0.08 insurance = yes
```

This may produce some additional zero count estimates.

Rootogram for ZIP model

ZIP model Rootogram: mod_3



Save predicted values and residuals

```
# A tibble: 2 x 3
  visits fitted resid
  <int> <dbl> <dbl> 1
    5   5.98 -0.982
    1   6.05 -5.05
```

Is ZIP significantly better than Poisson (Vuong test)

```
vuong(mod_3, mod_1)
```

17.05999 model1 > model2 < 2.22e-16

AIC-corrected

Pseudo-R² for ZIP model (mod_3)

We can calculate a proxy for R2 as the squared correlation of the fitted values and the observed values.

```
mod3_r <- with(mod_3_aug, cor(visits, fitted))
mod3_r^2</pre>
```

[1] 0.1073657

The Zero-Inflated Negative Binomial Model

Fitting the Zero-Inflated Negative Binomial (mod_4)

summary(mod_4) (and see next 2 slides)

```
> summary(mod_4)
Call:
zeroinfl(formula = visits ~ hospital + health + chronic + sex + school + insurance, data = medicare, dist = "negbin")
Pearson residuals:
   Min
            10 Median
                                  Max
-1.1966 -0.7097 -0.2784 0.3256 17.7661
Count model coefficients (negbin with log link):
                Estimate Std. Error z value Pr(>|z|)
(Intercept)
                1.193466
                          0.056737 21.035 < 2e-16 ***
hospital
                0 201214
                          0 020392 9 867 < 2e-16 ***
healthexcellent -0.313540
                         0.062977 -4.979 6.40e-07 ***
healthpoor
            0.287190
                         0.045940 6.251 4.07e-10 ***
                0.128955
                          0.011938 10.802 < 2e-16 ***
chronic
sexmale
               -0.080093
                         0.031035 -2.581 0.00986 **
school
              0.021338
                         0.004368 4.886 1.03e-06 ***
insuranceyes
              0.126815
                          0.041687 3.042 0.00235 **
Log(theta)
                          0 035145 11 231 < 2e-16 ***
                0.394731
Zero-inflation model coefficients (binomial with logit link):
               Estimate Std. Error z value Pr(>|z|)
(Intercept)
                          0.27668 -0.230 0.81837
               -0.06354
hospital
               -0.81760
                          0.43875 -1.863 0.06240 .
healthexcellent 0.10488
                          0.30965 0.339 0.73484
healthpoor
                0.10178
                          0.44071 0.231 0.81735
chronic
               -1.24630
                          0.17918 -6.956 3.51e-12 ***
                          0.20046
                                   3.239 0.00120 **
sexmale
              0.64937
school
               -0.08481
                          0.02676 -3.169 0.00153 **
insuranceves -1.15808
                          0 22436 -5 162 2 45e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Theta = 1.484
Number of iterations in BFGS optimization: 31
Log-likelihood: -1.209e+04 on 17 Df
```

Zero-inflation model coefficients in mod_4

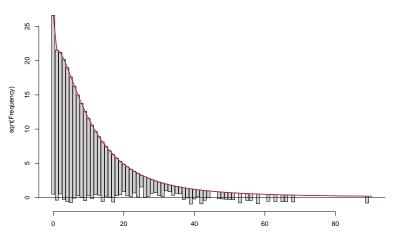
```
Zero-inflation model coefficients (binomial with logit link):
              Estimate Std. Error z value Pr(>|z|)
(Intercept)
              -0.06354
                        0.27668
                                -0.230 0.81837
hospital
        -0.81760
                        0.43875 -1.863 0.06240 .
healthexcellent 0.10488
                        0.30965 0.339 0.73484
healthpoor
          0.10178
                        0.44071 0.231 0.81735
chronic
                        0.17918 -6.956 3.51e-12
           -1.24630
sexmale
           0.64937
                        0.20046 3.239 0.00120
school
           -0.08481
                        0.02676 -3.169 0.00153
                                               ***
insuranceyes
              -1.15808
                        0.22436
                                -5.162 2.45e-07
```

Count model coefficients in mod_4

```
Count model coefficients (negbin with log link):
                Estimate Std. Error z value Pr(>|z|)
(Intercept)
                           0.056737 21.035
                                            < 2e-16
                1.193466
hospital
                0.201214
                           0.020392 9.867
                                            < 2e-16
healthexcellent -0.313540
                                                    ***
                           0.062977 -4.979 6.40e-07
                                     6.251 4.07e-10
                                                    ***
healthpoor
                0.287190
                           0.045940
chronic
                                                    ***
                0.128955
                           0.011938 10.802
                                            < 2e-16
sexmale
               -0.080093
                           0.031035
                                    -2.581
                                            0.00986
                                                    **
school
                0.021338
                           0.004368 4.886 1.03e-06
                                                    ***
                                                    **
insuranceyes
                0.126815
                           0.041687 3.042
                                            0.00235
Log(theta)
                0.394731
                           0.035145
                                    11.231
                                            < 2e-16
```

Rootogram for ZINB model

ZINB model Rootogram: mod_4



Save predicted values and residuals

```
# A tibble: 2 x 3
  visits fitted resid
  <int> <dbl> <dbl>
1     5     6.14 -1.14
2     1     5.94 -4.94
```

Is ZINB significantly better than Negative Binomial?

```
vuong(mod_4, mod_2)
```

 $3.431859 \mod 11 > \mod 20.00029973$

BIC-corrected

Pseudo-R² for ZINB model (mod_4)

We can calculate a proxy for R2 as the squared correlation of the fitted values and the observed values.

```
mod4_r <- with(mod_4_aug, cor(visits, fitted))
mod4_r^2</pre>
```

[1] 0.09620424

So Far ...

Model	Pseudo-R ²	Rootogram?	Comments
Poisson	0.099	Many problems.	Data appear overdispersed.
Neg. Bin.	0.083	Better.	Still not enough zeros.
ZIP	0.107	All but 0 a problem.	Not enough 1-3.
ZINB	0.096	Better.	Zeros not a perfect fit.

Next Time - The Hurdle Model

The hurdle model is a two-part model that specifies one process for zero counts and another process for positive counts. The idea is that positive counts occur once a threshold is crossed, or put another way, a hurdle is cleared. If the hurdle is not cleared, then we have a count of 0.

- The first part of the model is typically a binary logit model. This models whether an observation takes a positive count or not.
- The second part of the model is usually a truncated Poisson or Negative Binomial model. Truncated means we're only fitting positive counts. If we were to fit a hurdle model to our [medicare] data, the interpretation would be that one process governs whether a patient visits a doctor or not, and another process governs how many visits are made.

Next Time - The Tobit (Censored Regression) Model

The idea of the tobit model (sometimes called a censored regression model) is to estimate associations for outcomes where we can see either left-censoring (censoring from below) or right-censoring (censoring from above.)

We'll look at a different example for the tobit, since we don't have an upper bound (technically) for the visit counts in the medicare data.