### 432 Class 26 Slides

github.com/THOMASELOVE/432-2018

2018-04-19

**Getting Started** 

### **Preliminaries**

```
library(skimr)
library(rms)
library(aplore3) # for a data set
library(ResourceSelection) # for Hosmer-Lemeshow test
library(bestglm) # for a demonstration of all subsets
library(broom)
library(tidyverse)
```

# Today's Agenda

- Loose Ends
  - Spending Degrees of Freedom in Project 2, and in Life
  - Logistic Regression
    - The Hosmer-Lemeshow test
    - Variable Selection with "All Subsets" / bestglm
- Replicable Research and the Crisis in Science
  - ASA Statement on P values
  - Is changing the p value cutoff the right strategy?
  - Second-generation p values: A next step?
- Retrospective Power and why most smart folks avoid it
  - Type S and Type M error: Saying something more useful

**Spending Degrees of Freedom** 

# For Project 2

Remember that for Project 2, I've simplified your decision-making. See section 6.19 of the instructions or the Class 26 README.

- Basically, I want you to restrain yourself on the size of the model you wind up with.
- Even if you have a big sample, don't fit project 2 models with more than 20 degrees of freedom or more than 8 predictors, if you can possibly help it.
  - My brain can't hold even that many degrees of freedom together at one time. Anything more will leave me a quivering mess.

# On Fitting Regression Models

Some things are always true. . .

- Being honest about your findings is important.
- Identifying a stable phenomenon to study is crucial.
- Measuring that phenomenon well is crucial.
- Being transparent about your work is important. Describing your work so it can be replicated, and then actually replicating it, are good things. Sharing your data and your materials is a good idea.
- Having a large sample size (n) is helpful in fitting models.

but the impact of lots of other things changes depending on why you're fitting a regression model.

# The Key Point

Decide what your research question is, and use it to help you think about what's important in your modeling.

- Models that account for only a few of the possibly important dimensions of a problem don't lead to causal conclusions, but can help screen out important from less important areas for future work.
- Model development strategies that work well with large sample sizes

   (n) and small numbers of predictors to consider don't necessarily work well when the situation is reversed.
- Most problems involve missing data, and problems in measurement.
   Getting those issues settled effectively is often overlooked.
- The sample size you need to fit a regression model changes depending on your aims.

What are some of the reasons you might fit a linear (or generalized linear) model?

- All prediction, no explanations
- All description, external validity is irrelevant
- Olinical/Scientific Prediction with strong priors
- Above all else, simplicity
- Causal inference
- Risk Adjustment

What are some of the reasons you might fit a linear (or generalized linear) model?

- (All prediction, no explanations) Because you want to make predictions about an outcome in new data based on some training data you have, but you're happy to take those predictions as emerging from a mysterious magic "black box" that cannot be peered into without spoiling the surprise. You don't care if your results are a little biased, so long as the predictions are strong. Parsimony doesn't matter to you.
- Some especially useful tools here include: variable (feature) selection through cross-validation, stepwise approaches, AIC and BIC, machine learning tools like regression trees, and other means of quickly searching through many possible models.
- Sample size is rarely a big issue here. The big problem is having more variables than you can possibly plot at once. You usually have enough data to partition into separate development and test samples.

- (All description, external validity is irrelevant) Because you want to describe, as accurately as possible, the nature of the associations you observe in the available data, but you don't care much at all whether the conclusions you draw will hold up in new data.
- Confidence intervals for coefficients (slopes, mostly), and sometimes you'll run the model on clinically relevant cutpoints rather than continuous predictors to see what's happening more simply. Simple polynomial models can be appealing, and you'll sometimes want to build this in the ANCOVA context, where you're looking for the impact of specific pre-specified interactions.
- Residual plots play a big role here in deciding whether the model "fits" well enough, or identifying cases when it doesn't.
- Cross-validation is useful, but not a big part of model selection or convincing people that the model is "right" or not.

- (Clinical prediction) You want to do an excellent job predicting an outcome in new data, but you have a lot of prior knowledge about the predictors under consideration, and want to use that information to help produce prediction rules as effectively as possible. You welcome the fact that most relationships are non-linear, but would like to be parsimonious if possible, as data are often expensive.
- Some especially useful tools here include: scatterplot matrices (when the number of predictors is modest), cross-validation, assessments of discrimination and calibration, Spearman's  $\rho^2$  plot to point the way to non-linear terms that might be impactful if present, restricted cubic splines, polynomial functions, and graphical tools like nomograms
- Most stepwise tools aren't helpful here. We try to not "peek" at the outcome-predictor relationships to maintain unbiased estimates of the relationship without extensive validation.

- (Above all else, simplicity) You want the problem to look like one in a statistics textbook, where everything is fit with the simplest possible model, where every term adds statistically significant predictive value, and where obtaining an unbiased estimate of the outcome is especially important. You still care a bit about what happens in new data, but you're mostly concerned about parsimonious model development.
  - Some especially useful tools include best subsets, stepwise approaches, and methods for pruning a set of predictors with clustering or principal components analysis. These models usually make the (often incorrect) assumption that relationships are linear.
- Often this approach is used by people who are trying to pre-specify their entire model in advance, and want to be sure they can "explain" the result when they are done. That may not be a reasonable thing to hope for. This is a place where the "rule of 20" can be very helpful in setting expectations in advance.

- (Causal inference) You want to identify whether a particular causal pathway you have pre-specified matches up well with what you see in new data.
- (Risk Adjustment) You want to identify the impact of a particular exposure/predictor on an outcome, while controlling for the effects of a series of additional predictors. Perhaps you've done a randomized experiment / clinical trial, and want to identify whether particular results meet a standard for statistical (as well as clinical) significance. Power is very important.
- In either case, bias is very important, and you want to avoid it. Careful design of a comparison group (like I teach in 500) is a very good way to go about this work, but it's also true that there's a lot of epidemiology that goes into drawing causal conclusions, or even thinking hard about an association.
- Often the details of modeling take a back seat here to the details of designing the study (and the comparison groups) in the first place.

# Asssessing the Quality of a Logistic Regression Model

# A Quick Example

SOURCE: Hosmer and Lemeshow (2000) Applied Logistic Regression: Second Edition. These data are copyrighted by John Wiley & Sons Inc. and must be acknowledged and used accordingly. Data were collected at Baystate Medical Center, Springfield, Massachusetts during 1986.

```
# uses aplore3 package for data set
lbw <- aplore3::lowbwt
head(lbw,3)</pre>
```

```
id low age lwt race smoke ptl ht ui ftv
1 4 < 2500 g 28 120 Other Yes One No Yes None
2 10 < 2500 g 29 130 White No None No Yes Two, etc.
3 11 < 2500 g 34 187 Black Yes None Yes No None
   bwt
1 709
2 1021
3 1135</pre>
```

# Fit a logistic regression model

```
model_10 <- glm(low ~ lwt + ptl + ht,
              data = lbw, family = binomial)
model 10
Call: glm(formula = low ~ lwt + ptl + ht, family = binomial,
Coefficients:
 (Intercept)
                    lwt
                           ptlOne ptlTwo, etc.
    1.17016 -0.01851
                           1.74219 0.15105
      htYes
    1.91234
Degrees of Freedom: 188 Total (i.e. Null); 184 Residual
Null Deviance: 234.7
Residual Deviance: 207.4 AIC: 217.4
```

### The Hosmer-Lemeshow Test of Goodness of Fit

#### See this link from Jonathan Bartlett.

- The Hosmer-Lemeshow goodness of fit test is based on dividing the sample into g groups (g is often chosen to be 10) according to their predicted probabilities.
- We then calculate the expected number of Y=1 outcomes (based on the model probabilities of Y=1 in the group) in each of the 10 groups, and compare those results to what is observed in the data using a Pearson goodness of fit statistic.
- A significant result indicates statistically significant "lack of fit" but it's easy to criticize the test (among other things, if you change the choice of g, you can materially change the p value.)

## **Running the Hosmer-Lemeshow Test**

```
# requires ResourceSelection package
hos <- hoslem.test(model_10$y, fitted(model_10), g = 10)
hos</pre>
```

Hosmer and Lemeshow goodness of fit (GOF) test

```
data: model_10$y, fitted(model_10)
X-squared = 5.6459, df = 8, p-value = 0.6868
```

So there's no evidence of poor fit. We can also get a table of observed vs. expected.

# Observed vs. Expected Table from H-L test

```
cbind(hos$observed, hos$expected)
```

```
y0 y1
                      yhat0
                                yhat1
[0.0305,0.14] 16 3 17.226390
                            1.773610
(0.14, 0.2] 16 4 16.600448 3.399552
(0.2, 0.225] 20 4 18.773041 5.226959
(0.225,0.252] 12 2 10.599250 3.400750
(0.252,0.263] 16 4 14.817304 5.182696
(0.263,0.288] 14 3 12.265960 4.734040
(0.288, 0.322]
             12 6 12.521738 5.478262
(0.322.0.384] 11 8 12.395653 6.604347
(0.384.0.637) 7 12 9.658303 9.341697
(0.637.0.947) 6 13 5.141914 13.858086
```

# Change the number of groups, g?

[1] 0.1888862 [1] 0.6682719 [1] 0.7830653 [1] 0.6564895 [1] 0.6868256 [1] 0.4444073 [1] 0.4520327 [1] 0.6381505 [1] 0.6437715 [1] 0.07773936 Can we use "best subsets" or "all subsets" in logistic regression?

# Using the bestglm package to do "best subsets" with logistic models

There are several available tools. If you're interested, I'd start with this link.

- The bestglm package does an exhaustive (all subsets) search through a glm (slowly) using AIC, BIC or cross-validation, for example.
- This expects the data to be in a certain form, for instance, the outcome must be named y and you can have no extraneous variables present.
- The tutorial you'll find at the link above is pre-tidyverse. I don't know how well bestglm works with the tidyverse, but it's not likely to be much worse than leaps does.
- This approach can also be used with linear models which include multi-categorical predictors.
- bestglm is going to do an exhaustive search, which will be slow with large data sets, or large pools of predictors.
- In addition to bestglm there are several other appealing tools for looking at large numbers of potential models quickly.

## **Preparing the Data Set**

```
lbw_for_bestglm <- lbw %>%
  mutate(y = low) %>%
  select(age, lwt, race, smoke, ptl, ht, ui, ftv, y)
```

Must include only the variables we want to include in the search, and then the outcome, which must be labeled y, in that order.

## lbw\_for\_bestglm data: First few observations

### head(lbw\_for\_bestglm)

```
age lwt race smoke ptl ht ui ftv y
1 28 120 Other Yes One No Yes None < 2500 g
2 29 130 White No None No Yes Two, etc. < 2500 g
3 34 187 Black Yes None Yes No None < 2500 g
4 25 105 Other No One Yes No None < 2500 g
5 25 85 Other No None No Yes None < 2500 g
6 27 150 Other No None No No None < 2500 g
```

# Search through all subsets, with AIC as criterion

Morgan-Tatar search since family is non-gaussian. Note: factors present with more than 2 levels.

This approach (with a gaussian family) can also be used for OLS.

# Show top 5 models chosen by AIC

#### res.best.logistic\$BestModels

```
age lwt race smoke ptl ht ui ftv Criterion
1 FALSE TRUE TRUE TRUE TRUE TRUE TRUE FALSE 211.1647
2 TRUE TRUE TRUE TRUE TRUE TRUE TRUE FALSE 211.9063
3 FALSE TRUE TRUE TRUE TRUE TRUE FALSE FALSE 212.2697
4 TRUE TRUE TRUE TRUE TRUE TRUE FALSE FALSE 212.6828
5 TRUE TRUE FALSE FALSE TRUE TRUE TRUE FALSE 213.4539
```

# Show result for best model, according to AIC

```
> summarv(res.best.logistic$BestModel)
Call:
glm(formula = y \sim ... family = family, data = Xi, weights = weights)
Deviance Residuals:
   Min
            10 Median 30
                                    Max
-1.8643 -0.7803 -0.5172 0.9308
                                 2.2013
Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.015463 0.982536 -0.016 0.98744
lwt
           -0.016773 0.007081 -2.369 0.01786 *
raceBlack
                      0.534975 2.338 0.01937 *
           1.250947
race0ther 0.827222
                      0.446817 1.851 0.06412 .
smokeYes 0.875302
                      0.410139 2.134 0.03283 *
ptlone 1.463051 0.506699 2.887 0.00388 **
ptlTwo, etc. -0.163819 0.945560 -0.173 0.86245
htYes
       1.875815
                      0.716529 2.618 0.00885 **
uiYes
            0.828436
                      0.466987
                                1.774 0.07606 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 234.67 on 188 degrees of freedom
Residual deviance: 195.16 on 180 degrees of freedom
AIC: 213.16
Number of Fisher Scoring iterations: 4
```

# Search all subsets, using BIC instead of AIC

Morgan-Tatar search since family is non-gaussian. Note: factors present with more than 2 levels.

## Show top 5 models by BIC

#### res.best.logistic2\$BestModels

```
age lwt race smoke ptl ht ui ftv Criterion
1 FALSE TRUE FALSE FALSE TRUE TRUE FALSE FALSE 228.3477
2 FALSE FALSE FALSE FALSE TRUE FALSE FALSE FALSE 230.1914
3 TRUE FALSE FALSE FALSE TRUE FALSE FALSE FALSE 230.2738
4 FALSE TRUE FALSE FALSE TRUE FALSE FALSE FALSE 230.3406
5 FALSE TRUE FALSE FALSE TRUE TRUE TRUE FALSE 230.3604
```

# Show result for best model, according to BIC

```
summary(res.best.logistic2$BestModel)
Call:
glm(formula = y \sim ., family = family, data = Xi, weights = weights)
Deviance Residuals:
   Min
            10 Median 30
                                   Max
-1.7662 -0.7929 -0.6853 0.9083 2.2843
Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) 1.170161 0.870866 1.344 0.179054
lwt
      ptlone 1.742193 0.486423 3.582 0.000341 ***
ptlTwo, etc. 0.151047 0.905990 0.<u>167 0.867590</u>
htYes 1.912342 0.734647 2.603 0.009239 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 234.67 on 188 degrees of freedom
Residual deviance: 207.38 on 184 degrees of freedom
AIC: 217.38
Number of Fisher Scoring iterations: 4
```

# Best Models, by Criterion

There are 8 predictors under consideration.

• age, lwt, race, smoke, ptl, ht, ui and ftv

Model (by AIC)	Rank	Model (by BIC)
lwt, smoke, ptl, ht, ui	1	lwt, ptl, ht
all except ftv	2	ptl
<pre>lwt, race, smoke, ptl, ht</pre>	3	age, ptl
all except ui, ftv	4	lwt, ptl
age, lwt, ptl, ht, ui	5	lwt, ptl, ht, ui

# Search all subsets, using Cross-Validation

Can be done when all predictors are continuous or binary, but **not** if you have categorical predictors with more than two levels.

# Reacting to Published Research

# Roger Peng's description of a successful data analysis

A data analysis is successful if the audience to which it is presented accepts the results.

• "What is a Successful Data Analysis?" *simplystatistics.org* (2018-04-17).

So what makes a data analysis more believable / more acceptable?

### Problems with P Values

- P values are inherently unstable
- The p value, or statistical significance, does not measure the size of an effect or the importance of a result
- $\odot$  Scientific conclusions should not be based only on whether a p value passes a specific threshold
- Proper inference requires full reporting and transparency
- By itself, a p value does not provide a good measure of evidence regarding a model or hypothesis

Link

#### Solutions to the P Value Problems

- Estimation of the Size of the Effect
- Precision of the Estimate (Confidence Intervals)
- Inference About the Target Population
- Determination of Whether the Results Are Compatible With a Clinically Meaningful Effect
- Replication and Steady Accumulation of Knowledge

Link

## Importance of Meta-Analytic Thinking

In JAMA Otolaryngology: Head & Neck Surgery, we look to publish original investigations where the investigators planned the study with sufficient sample size to have adequate power to detect a clinically meaningful effect and report the results with effect sizes and Cls. Authors should interpret the effect sizes in relation to previous research and use CIs to help determine whether the results are compatible with clinically meaningful effects. And finally, we acknowledge that no single study can define truth and that the advancement of medical knowledge and patient care depends on the steady accumulation of reliable clinical information.

Link

#### The Value of a p-Valueless Paper

Jason T. Connor (2004) American J of Gastroenterology 99(9): 1638-40.

Abstract: As is common in current bio-medical research, about 85% of original contributions in The American Journal of Gastroenterology in 2004 have reported p-values. However, none are reported in this issue's article by Abraham et al. who, instead, rely exclusively on effect size estimates and associated confidence intervals to summarize their findings. Authors using confidence intervals communicate much more information in a clear and efficient manner than those using p-values. This strategy also prevents readers from drawing erroneous conclusions caused by **common misunderstandings about** *p***-values**. I outline how standard, two-sided confidence intervals can be used to measure whether two treatments differ or test whether they are clinically equivalent.

Link

#### Editorial from JAMA Cardiology 2016-10-12

Editor's Note

#### Do Not Over (P) Value Your Research Article

Laine E. Thomas. PhD: Michael J. Pencina. PhD

P value is by far the most prevalent statistic in the medical literature but also one attracting considerable controversy. Recently, the American Statistical Association' released a policy statement on P values, noting that misunderstanding and misuse of P values is an im-



misuse of P values is an important contributing factor to the common problem of scientific conclusions that fail to

be reproducible. Furthermore, reliance on P values may distract from the good scientific principles that are needed for high-quality research. Mark et al² delve deeper into the history and interpretation of the P value in this issue of JAMA Cardiology. Herein, we take the opportunity to state a few principles to help guide authors in the use and reporting of P values in the journal.

When the limitations surrounding P values are emphasized, a common question is, "What should we do instead?" Ron Wasserstein of the American Statistical Association explained: "In the post p<0.05 era, scientific argumentation is not based on whether a p-value is small enough or not. Attention is paid to effect sizes and confidence intervals. Evidence is thought of as being continuous rather than some sort of dichotomy... Instead, journals should evaluate papers based on clear and detailed description of the study design, execution, and analysis, having conclusions that are based on valid statistical interpretations and scientific arguments, and reported transparently and thoroughly enough to be rigorously scrutinized by others."<sup>3</sup>

We suggest that researchers submitting manuscripts to JAMA Cardiology should also consider the following:

- Data that are descriptive of the sample (ie, indicating imbalances between observed groups but not making inference to a population) should not be associated with Pualues. Appropriate language, in this case, would describe numerical differences and sample summary statistics and focus on differences of clinical importance.
- In addition to summary statistics and confidence intervals, standardized differences (rather than P values) are a preferred way to exhibit imbalances between groups.
- P values are most meaningful in the context of clear, a priori hypotheses that support the main conclusions of a manuscript.
- 4. Reporting stand-alone P values is discouraged, and preference should be given to presentation and interpretation of effect sizes and their uncertainty (confidence intervals) in the scientific context and in light of other evidence. Crossing a threshold (eg, P < .05) by itself constitutes only weak evidence.</p>
- Researchers should define and interpret effect measures that are clinically relevant. For example, clinical importance is often difficult to establish on the odds ratio scale but is clearer on the risk ratio or absolute risk difference scale.

In summary, following Mark et al, <sup>2</sup> we encourage researchers to focus on interpreting clinical research data in terms of treatment "effect" magnitude and precision, using P value only as one of many complementary tools in the statistical toolbox.

#### Mark, Lee, Harrell JAMA Cardiol 2016-10-12

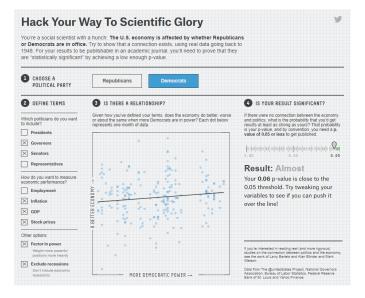
#### **Abstract**

P values and hypothesis testing methods are frequently misused in clinical research. Much of this misuse appears to be owing to the widespread, mistaken belief that they provide simple, reliable, and objective triage tools for separating the true and important from the untrue or unimportant. The primary focus in interpreting therapeutic clinical research data should be on the treatment ("oomph") effect, a metaphorical force that moves patients given an effective treatment to a different clinical state relative to their control counterparts. This effect is assessed using 2 complementary types of statistical measures calculated from the data, namely, effect magnitude or size and precision of the effect size. In a randomized trial, effect size is often summarized using constructs, such as odds ratios, hazard ratios, relative risks, or adverse event rate differences. How large a treatment effect has to be to be consequential is a matter for clinical judgment. The precision of the effect size (conceptually related to the amount of spread in the data) is usually addressed with confidence intervals. P values (significance tests) were first proposed as an informal heuristic to help assess how "unexpected" the observed effect size was if the true state of nature was no effect or no difference. Hypothesis testing was a modification of the significance test approach that envisioned controlling the false-positive rate of study results over many (hypothetical) repetitions of the experiment of interest. Both can be helpful but, by themselves. provide only a tunnel vision perspective on study results that ignores the clinical effects the study was conducted to measure.

doi:10.1001/jamacardio.2016.3312

p-Hacking

## Hack Your Way To Scientific Glory (fivethirtyeight)



## "Researcher Degrees of Freedom", 1

[I]t is unacceptably easy to publish statistically significant evidence consistent with any hypothesis.

The culprit is a construct we refer to as **researcher degrees of freedom**. In the course of collecting and analyzing data, researchers have many decisions to make: Should more data be collected? Should some observations be excluded? Which conditions should be combined and which ones compared? Which control variables should be considered? Should specific measures be combined or transformed or both?

Simmons et al. link

## "Researcher Degrees of Freedom", 2

... It is rare, and sometimes impractical, for researchers to make all these decisions beforehand. Rather, it is common (and accepted practice) for researchers to explore various analytic alternatives, to search for a combination that yields statistical significance, and to then report only what worked. The problem, of course, is that the likelihood of at least one (of many) analyses producing a falsely positive finding at the 5% level is necessarily greater than 5%.

#### For more, see

- Gelman's blog 2012 11 01 "Researcher Degrees of Freedom",
- Paper by *Simmons* and others, defining the term.

## And this is really hard to deal with...

The garden of forking paths: Why multiple comparisons can be a problem, even when there is no "fishing expedition" or p-hacking and the research hypothesis was posited ahead of time

Researcher degrees of freedom can lead to a multiple comparisons problem, even in settings where researchers perform only a single analysis on their data. The problem is there can be a large number of potential comparisons when the details of data analysis are highly contingent on data, without the researcher having to perform any conscious procedure of fishing or examining multiple p-values. We discuss in the context of several examples of published papers where data-analysis decisions were theoretically-motivated based on previous literature, but where the details of data selection and analysis were not pre-specified and, as a result, were contingent on data.

• Link to the paper from Gelman and Loken







Hey Stats folk, what's your 280 character definition of a confidence interval?

4:30 PM - 13 Mar 2018



Follow

Replying to @ChelseaParlett

An interval drawn such that, were repeated, equal-sized samples of units drawn from the population of units using an identical sampling procedure and the same estimator was applied to each sample,  $100*(1-\alpha)\%$  of those intervals would contain the population parameter of interest.

4:58 PM - 13 Mar 2018





A confidence interval is a meaure of uncertainty such that all definitions of it elicit corrections from Bayesians.

(Didn't need all 280.)



Jenny Bryan @JennyBryan

Following

Pedantry about the definition of a confidence interval ... why is this the hill statisticians choose to die on? Every time you feel the urge, go convert a table to a figure. It is likely to do more good.



Replying to @f2harrell

I just feel like the people we're often trying to reach aren't making informed comparisons of frequentist vs Bayesian methods, they're still struggling with decision making under uncertainty

1:02 PM - 28 Dec 2017

## **Using Bayesian Ideas: Confidence Intervals**

My current favorite (hypothetical) example is an epidemiology study of some small effect where the point estimate of the odds ratio is 3.0 with a 95% conf interval of [1.1, 8.2].

As a 95% conf interval, this is fine (assuming the underlying assumptions regarding sampling, causal identification, etc. are valid).

```
(but on some level you need to deal with the fact that...)
```

... real-world odds ratios are much more likely to be near 1.1 than to be near 8.2.

See Gelman 2014-12-11.

## **Uncertainty intervals?**

I've (Gelman) become increasingly uncomfortable with the term "confidence interval" for several reasons:

- The well-known difficulties in interpretation (officially the confidence statement can be interpreted only on average, but people typically implicitly give the Bayesian interpretation to each case.)
- The ambiguity between confidence intervals and predictive intervals.
- The awkwardness of explaining that confidence intervals are big in noisy situations where you have less confidence, and confidence intervals are small when you have more confidence.

So here's my proposal. Let's use the term "uncertainty interval" instead. The uncertainty interval tells you how much uncertainty you have.

See Gelman 2010-12-21.

## Dividing Data Comparisons into Categories based on p values

## Regina Nuzzo in Nature on Statistical Errors

#### **PROBABLE CAUSE**

A P value measures whether an observed result can be attributed to chance. But it cannot answer a researcher's real question: what are the odds that a hypothesis is correct? Those odds depend on how strong the result was and, most importantly, on how plausible the hypothesis is in the first place.

Chance of real effect
 Chance of no real effect

#### Before the experiment

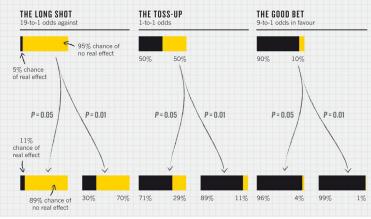
The plausibility of the hypothesis — the odds of it being true — can be estimated from previous experiments, conjectured mechanisms and other expert knowledge. Three examples are shown here.

#### The measured P value

A value of 0.05 is conventionally deemed 'statistically significant'; a value of 0.01 is considered 'very significant'.

#### After the experiment

A small P value can make a hypothesis more plausible, but the difference may not be



## Gelman on p values, 1

The common practice of dividing data comparisons into categories based on significance levels is terrible, but it happens all the time. . . . so it's worth examining the prevalence of this error.

Consider, for example, this division:

- "really significant" for p < .01,
- "significant" for p < .05,
- "marginally significant" for p < .1, and
- "not at all significant" otherwise.

Now consider some typical p-values in these ranges: say, p=.005, p=.03, p=.08, and p=.2.

Translate these two-sided *p*-values back into z-scores. . .

Gelman 2016-10-15

#### Gelman on p values, 2

Description	really sig.	sig.	marginally sig.	not at all sig.
p value	0.005	0.03	0.08	0.20
Z score	2.8	2.2	1.8	1.3

The seemingly yawning gap in p-values comparing the not at all significant p-value of .2 to the really significant p-value of .005, is only a z score of 1.5.

If you had two independent experiments with z-scores of 2.8 and 1.3 and with equal standard errors and you wanted to compare them, you'd get a difference of 1.5 with a standard error of 1.4, which is completely consistent with noise.

#### Gelman on p values, 3

From a **statistical** point of view, the trouble with using the p-value as a data summary is that the p-value is only interpretable in the context of the null hypothesis of zero effect, and (much of the time), nobody's interested in the null hypothesis.

Indeed, once you see comparisons between large, marginal, and small effects, the null hypothesis is irrelevant, as you want to be comparing effect sizes.

From a **psychological** point of view, the trouble with using the p-value as a data summary is that this is a kind of deterministic thinking, an attempt to convert real uncertainty into firm statements that are just not possible (or, as we would say now, just not replicable).

**The key point**: The difference between statistically significant and NOT statistically significant is not, generally, statistically significant.

## **Some Noisy Recent Suggestions**

## Benjamin et al 2017 Redefine Statistical Significance

We propose to change the default P-value threshold for statistical significance for claims of new discoveries from 0.05 to 0.005.

#### Motivations:

- links to Bayes Factor interretation
- 0.005 is stringent enough to "break" the current system makes it very difficult for researchers to reach threshold with noisy, useless studies.

Visit the main article. Visit an explanatory piece in Science.

#### Lakens et al. Justify Your Alpha

"In response to recommendations to redefine statistical significance to  $p \le .005$ , we propose that researchers should transparently report and justify all choices they make when designing a study, including the alpha level." Visit *link*.

## **Abandon Statistical Significance**

Gelman blog 2017 - 09 - 26 on "Abandon Statistical Significance"

"Measurement error and variation are concerns even if your estimate is more than 2 standard errors from zero. Indeed, if variation or measurement error are high, then you learn almost nothing from an estimate even if it happens to be 'statistically significant.'"

Read the whole paper *here* 

## JAMA 2018-04-10 (just 8 days ago!)

Opinion

#### VIEWPOINT

#### John P. A. loannidis, MD, DSc Stanford Prevention Research Center, Meta-Research Innovation Center at Stanford, Departments of Medicine, Health Research and Policy, Biomedical Data Science, and Statistics, Stanford University,

Stanford, California.

#### The Proposal to Lower P Value Thresholds to .005

P values and accompanying methods of statistical significance testing are creating challenges in biomedical science and other disciplines. The vast majority (96%) of articles that report P values in the abstract, full text, or both include some values of .05 or less.1 However. many of the claims that these reports highlight are likely false.2 Recognizing the major importance of the statistical significance conundrum, the American Statistical Association (ASA) published3 a statement on P values in 2016. The status quo is widely believed to be problematic, but how exactly to fix the problem is far more contentious. The contributors to the ASA statement also wrote 20 independent, accompanying commentaries focusing on different aspects and prioritizing different solutions. Another large coalition of 72 methodologists recently proposed4 a specific, simple move: lowering the routine P value threshold for claiming statistical significance from .05 to .005 for new discoveries. The proposal met with strong endorsement in some circles and concerns in others.

P values are misinterpreted, overtrusted, and misused. The language of the ASA statement enables the disfully considered how low a P value should be for a research finding to have a sufficiently high chance of being true. For example, adoption of genome-wide significance thresholds ( $P < 5 \times 10^{-8}$ ) in population genomics has made discovered associations highly replicable and these associations also appear consistently when tested in new populations. The human genome is very complex, but the extent of multiplicity of significance testing involved is known, the analyses are systematic and transparent, and a requirement for  $P < 5 \times 10^{-8}$  can be cogently arrived at.

However, for most other types of biomedical research, the multiplicity involved is unclear and the analyses are nonsystematic and nontransparent. For most observational exploratory research that lacks preregistered protocols and analysis plans, it is unclear how many analyses were performed and what various analytic paths were explored. Hidden multiplicity, nonsystematic exploration, and selective reporting may affect even experimental research and randomized trials. Even though it is now more common to have a preexisting protocol and statistical analysis plan and preregistration of

## Blume et al. PLoS ONE (2018) 13(3): e0188299

**BESEARCH ARTICLE** 

Second-generation *p*-values: Improved rigor, reproducibility, & transparency in statistical analyses

Jeffrey D. Blume<sup>1</sup>\*, Lucy D'Agostino McGowan<sup>2</sup>, William D. Dupont<sup>3</sup>, Robert A. Greevy, Jr.<sup>1</sup>

#### Second-generation p values

Verifying that a statistically significant result is scientifically meaningful is not only good scientific practice, it is a natural way to control the Type I error rate. Here we introduce a novel extension of the p-value—a second-generation p-value  $(p_{\bar{p}})$ —that formally accounts for scientific relevance and leverages this natural Type I Error control. The approach relies on a pre-specified interval null hypothesis that represents the collection of effect sizes that are scientifically uninteresting or are practically null. The second-generation p-value is the proportion of data-supported hypotheses that are also null hypotheses. As such, second-generation p-values indicate when the data are compatible with null hypotheses ( $p_{\bar{\sigma}} = 1$ ), or with alternative hypotheses ( $p_{\bar{o}} = 0$ ), or when the data are inconclusive ( $0 < p_{\bar{o}} < 1$ ). Moreover, second-generation p-values provide a proper scientific adjustment for multiple comparisons and reduce false discovery rates. This is an advance for environments rich in data, where traditional p-value adjustments are needlessly punitive. Second-generation p-values promote transparency, rigor and reproducibility of scientific results by a priori specifying which candidate hypotheses are practically meaningful and by providing a more reliable statistical summary of when the data are compatible with alternative or null hypotheses.

## Nature P values are just the tip of the iceberg!

COMMENT

# P values are just the tip of the iceberg

Ridding science of shoddy statistics will require scrutiny of every step, not merely the last one, say **Jeffrey T. Leek** and **Roger D. Peng**.

**Evaluation through Retrospective Design** 

#### Gelman, 2016-03-11

Reviewing "The Association Between Men's Sexist Attitudes and Facial Hair" PubMed 26510427 (*Arch Sex Behavior* May 2016)

Headline Finding: A sample of  $\sim\!500$  men from America and India shows a significant relationship between sexist views and the presence of facial hair.

#### Excerpt 1:

Since a linear relationship has been found between facial hair thickness and perceived masculinity . . . we explored the relationship between facial hair thickness and sexism. . . . Pearson's correlation found no significant relationships between facial hair thickness and hostile or benevolent sexism, education, age, sexual orientation, or relationship status.

#### Facial Hair and Sexist Attitudes

#### Excerpt 2:

We conducted pairwise comparisons between clean-shaven men and each facial hair style on hostile and benevolent sexism scores. . . . For the purpose of further analyses, participants were classified as either clean-shaven or having facial hair based on their self- reported facial hair style . . . There was a significant Facial Hair Status by Sexism Type interaction . . .

 So their headline finding appeared only because, after their first analysis failed, they shook and shook the data until they found something statistically significant.

#### Facial Hair and Sexist Attitudes

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- So their headline finding appeared only because, after their first analysis failed, they shook and shook the data until they found something statistically significant.
- All credit to the researchers for admitting that they did this, but poor
  practice of them to present their result in the abstract to their paper
  without making this clear, and too bad that the journal got suckered
  into publishing this.

#### How should we react to this?

#### Gelman:

- Statisticians such as myself should recognize that the point of criticizing a study is, in general, to shed light on statistical errors, maybe with the hope of reforming future statistical education.
- Researchers and policymakers should not just trust what they read in published journals.

#### Assessing Type S (Sign) and Type M (Magnitude) Errors

• Gelman and Carlin Psychological Science 2014 9(6): 641-651.

## Some Ways of Thinking About Power

### **Specifying effect sizes for power calculations**

- Empirical: assuming an effect size equal to the estimate from a previous study or from the data at hand (if performed retrospectively).
  - · generally based on small samples
  - when preliminary results look interesting, they are more likely biased towards unrealistically large effects
- On the basis of goals: assuming an effect size deemed to be substantively important or more specifically the minimum effect that would be substantively important.
  - Can also lead to specifying effect sizes that are larger than what is likely to be the true effect.
  - Both lead to performing studies that are too small or misinterpretation of findings after completion.

#### Gelman and Carlin

- The idea of a design analysis is to improve the design and evaluation of research, when you want to summarize your inference through concepts related to statistical significance.
- Type 1 and Type 2 errors are tricky concepts and aren't easy to describe before data are collected, and are very difficult to use well after data are collected.
- These problems are made worse when you have
  - Noisy studies, where the signal may be overwhelmed,
  - Small Sample Sizes
  - No pre-registered (prior to data gathering) specifications for analysis
- Top statisticians avoid "post hoc power analysis"...
  - Why? It's usually crummy.

### Why not post hoc power analysis?

So you collected data and analyzed the results. Now you want to do an after data gathering (post hoc) power analysis.

- What will you use as your "true" effect size?
  - Often, point estimate from data yuck results very misleading power is generally seriously overestimated when computed on the basis of statistically significant results.
  - Much better (but rarer) to identify plausible effect sizes based on external information rather than on your sparkling new result.
- ② What are you trying to do? (too often)
  - get researcher off the hook (I didn't get p < 0.05 because I had low power an alibi to explain away non-significant findings) or
  - encourage overconfidence in the finding.

### Gelman and Carlin: Broader Design Ideas

 A broader notion of design, though, can be useful before and after data are gathered.

Gelman and Carlin recommend design calculations to estimate

- Type S (sign) error the probability of an estimate being in the wrong direction, and
- Type M (magnitude) error, or exaggeration ratio the factor by which the magnitude of an effect might be overestimated.
- These can (and should) have value **both** before data collection/analysis and afterwards (especially when an apparently strong and significant effect is found.)
- The big challenge remains identifying plausible effect sizes based on external information. Crucial to base our design analysis on an external estimate.

You perform a study that yields estimate d with standard error s. Think of d as an estimated mean difference, for example.

• Looks significant if |d/s| > 2, which roughly corresponds to p < 0.05. Inconclusive otherwise

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- Now, consider a true effect size D (the value that d would take if you had an enormous sample)

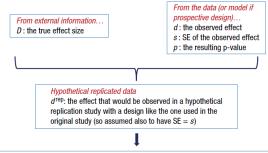
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  had an enormous sample)
- D is hypothesized based on external information (Other available data, Literature review, Modeling as appropriate, etc.)
- Define  $d^{rep}$  as the estimate that would be observed in a hypothetical replication study with a design identical to our original study.

### Design Analysis (Gelman and Carlin)



#### Design calculations:

- Power: the probability that the replication d<sup>rep</sup> is larger (in absolute value) than the
  critical value that is considered to define "statistical significance" in this analysis.
- Type S error rate: the probability that the replicated estimate has the incorrect sign, if it is statistically significantly different from zero.
- Exaggeration ratio (expected Type M error): expectation of the absolute value of the
  estimate divided by the effect size, if statistically significantly different from zero.

**Figure 1.** Diagram of our recommended approach to design analysis. It will typically make sense to consider different plausible values of *D*, the assumed true effect size.

## Retrodesign function (shown on next slide)

#### Inputs to the function:

- D, the hypothesized true effect size (actually called A in the function)
- s. the standard error of the estimate
- alpha, the statistical significance threshold (default 0.05)
- df, the degrees of freedom (default assumption: infinite)

#### Output:

- the power
- the Type S error rate
- the exaggeration ratio

## Retrodesign function (Gelman and Carlin)

```
retrodesign <- function(A, s, alpha=.05, df=Inf,
                          n.sims=10000){
    z \leftarrow qt(1-alpha/2, df)
    p.hi \leftarrow 1 - pt(z-A/s, df)
    p.lo \leftarrow pt(-z-A/s, df)
    power <- p.hi + p.lo
    typeS <- p.lo/power
    estimate <- A + s*rt(n.sims.df)
    significant <- abs(estimate) > s*z
    exaggeration <- mean(abs(estimate)[significant])/A
    return(list(power=power, typeS=typeS,
                 exaggeration=exaggeration))
```

### What if we have a beautiful, unbiased study?

Suppose the true effect that is 2.8 standard errors away from zero, in a study built to have 80% power for that effect with 95% confidence.

```
set.seed(201803161)
retrodesign(A = 28, s = 10, alpha = 0.05)
```

```
$power
[1] 0.7995569
```

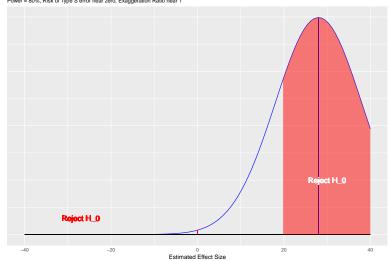
```
$typeS
[1] 1.210843e-06
```

```
$exaggeration [1] 1.12875
```

- With the power this high (80%), we have a type S error rate of  $1.2 \times 10^{-6}$  and an expected exaggeration factor of 1.13.
- Nothing to worry about with either direction of a statistically

# 80% power; large effect (2.8 SE above $H_0$ )

True Effect 2.8 SE above Null Hypothesis (Strong Effect)
Power = 80%, Risk of Type S error near zero, Exaggeration Ratio near 1



#### retrodesign for Zero Effect

```
set.seed(201803162)
retrodesign(A = 0, s = 10)

$power
[1] 0.05
```

```
$exaggeration
```

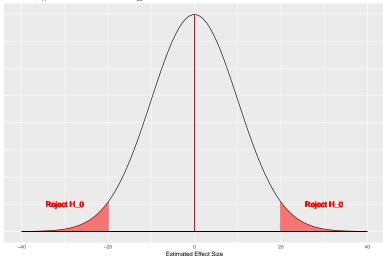
\$typeS [1] 0.5

• Power = 0.5,  $Pr(Type\ S\ error) = 0.5$ , Exaggeration Ratio is infinite.

#### Power, Type S and Type M Errors: Zero Effect



Power = 0.05, Type S error rate = 50% and infinite Exaggeration Ratio



## Retrodesign for a true effect 1.2 SE above $H_0$

```
set.seed(201803163)
retrodesign(A = 12, s = 10)
```

```
$power
[1] 0.224427

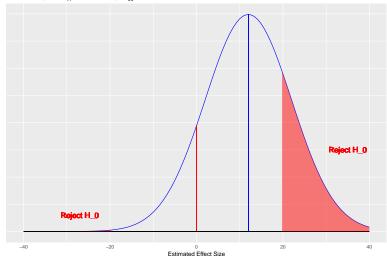
$typeS
[1] 0.003515367

$exaggeration
[1] 2.117846
```

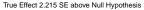
### What 22.4% power looks like...

True Effect 1.2 SE above Null Hypothesis

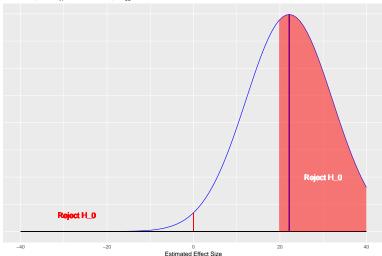
Power = 22.4%, Risk of Type S error is 0.004, Exaggeration Ratio is 2.12



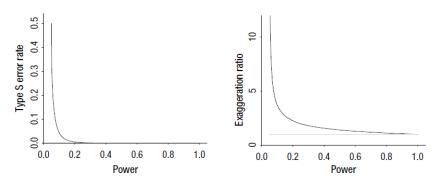
#### What 60% Power Looks Like



Power = 0.60, Risk of Type S error is <0.01%, Exaggeration Ratio is about 1.3



## Gelman & Carlin, Figure 2



**Figure 2.** Type S error rate and exaggeration ratio as a function of statistical power for unbiased estimates that are normally distributed. If the estimate is unbiased, the power must be between 0.05 and 1.0, the Type S error rate must be less than 0.5, and the exaggeration ratio must be greater than 1. For studies with high power, the Type S error rate and the exaggeration ratio are low. But when power gets much below 0.5, the exaggeration ratio becomes high (that is, statistically significant estimates tend to be much larger in magnitude than true effect sizes). And when power goes below 0.1, the Type S error rate becomes high (that is, statistically significant estimates are likely to be the wrong sign).

#### **Example: Beauty and Sex Ratios**

Kanazawa study of 2972 respondents from the National Longitudinal Study of Adolescent Health

- Each subject was assigned an attractiveness rating on a 1-5 scale and then, years later, had at least one child.
- Of the first-born children with parents in the most attractive category, 56% were girls, compared with 48% girls in the other groups.
- So the estimated difference was 8 percentage points with a reported p = 0.015
- Kanazawa stopped there, but Gelman and Carlin don't.

#### **Beauty and Sex Ratios**

We need to postulate an effect size, which will not be 8 percentage points. Instead, Gelman and colleagues hypothesized a range of true effect sizes using the scientific literature.

There is a large literature on variation in the sex ratio of human births, and the effects that have been found have been on the order of 1 percentage point (for example, the probability of a girl birth shifting from 48.5 percent to 49.5 percent). Variation attributable to factors such as race, parental age, birth order, maternal weight, partnership status and season of birth is estimated at from less than 0.3 percentage points to about 2 percentage points, with larger changes (as high as 3 percentage points) arising under economic conditions of poverty and famine. (There are) reliable findings that male fetuses (and also male babies and adults) are more likely than females to die under adverse conditions.

#### So, what is a reasonable effect size?

- Small observed differences in sex ratios in a multitude of studies of other issues (much more like 1 percentage point, tops)
- Noisiness of the subjective attractiveness rating (1-5) used in this particular study

So, Gelman and colleagues hypothesized three potential effect sizes (0.1, 0.3 and 1.0 percentage points) and under each effect size, considered what might happen in a study with sample size equal to Kanazawa's study.

#### How big is the standard error?

- From the reported estimate of 8 percentage points and p value of 0.015, the standard error of the difference is 3.29 percentage points.
  - If p value = 0.015 (two-sided), then Z score = qnorm(p = 0.015/2, lower.tail=FALSE) = 2.432
  - $\bullet$  Z = estimate/SE, and if estimate = 8 and Z = 2.432, then SE = 8/2.432=3.29

### Retrodesign Results: Option 1

- Assume true difference D=0.1 percentage point (probability of girl births differing by 0.1 percentage points, comparing attractive with unattractive parents).
- Standard error assumed to be 3.29, and  $\alpha = 0.05$

```
set.seed(201803164)
retrodesign(A = 0.1, s = 3.29, alpha = 0.05)
```

```
$power
[1] 0.05010584
```

```
$typeS
[1] 0.4645306
```

```
$exaggeration [1] 76.93614
```

### **Option 1 Conclusions**

Assuming the true difference is 0.1 means that probability of girl births differs by 0.1 percentage points, comparing attractive with unattractive parents.

If the estimate is statistically significant, then:

- There is a 46% chance it will have the wrong sign (from the Type S error rate).
- 2 The power is 5% and the Type S error rate of 46%. Multiplying those gives a 2.3% probability that we will find a statistically significant result in the wrong direction.
- **3** We thus have a power 2.3% = 2.7% probability of showing statistical significance in the correct direction.
- In expectation, a statistically significant result will be 78 times too high (the exaggeration ratio).

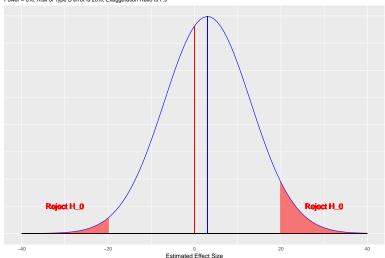
### Retrodesign Results: Options 2 and 3

Assumption	Power	Type S	Exaggeration Ratio
D = 0.1	0.05	0.46	78
D = 0.3	0.05	0.39	25
D = 1.0	0.06	0.19	7.8

- Under a true difference of 1.0 percentage point, there would be
  - a 4.9% chance of the result being statistically significantly positive and a 1.1% chance of a statistically significantly negative result.
  - A statistically significant finding in this case has a 19% chance of appearing with the wrong sign, and
  - the magnitude of the true effect would be overestimated by an expected factor of 8.

### What 6% power looks like...

True Effect 0.3 SE above Null Hypothesis
Power = 6%, Risk of Type S error is 20%, Exaggeration Ratio is 7.9



#### Gelman's Chief Criticism: 6% Power = D.O.A.

Their effect size is tiny and their measurement error is huge. My best analogy is that they are trying to use a bathroom scale to weigh a feather . . . and the feather is resting loosely in the pouch of a kangaroo that is vigorously jumping up and down.



#### What to do?

In advance, **and** after the fact, think hard about what a plausible effect size might be.

#### Then...

- Analyze all your data.
- Present all your comparisons, not just a select few.
  - A big table, or even a graph, is what you want.
- Make your data public.
  - If the topic is worth studying, you should want others to be able to make rapid progress.

## But I do studies with 80% power?

Based on some reasonable assumptions regarding main effects and interactions (specifically that the interactions are half the size of the main effects), you need **16 times** the sample size to estimate an interaction that you need to estimate a main effect.

And this implies a major, major problem with the usual plan of designing a study with a focus on the main effect, maybe even preregistering, and then looking to see what shows up in the interactions.

Or, even worse, designing a study, not finding the anticipated main effect, and then using the interactions to bail you out. The problem is not just that this sort of analysis is "exploratory"; it's that these data are a lot noisier than you realize, so what you think of as interesting exploratory findings could be just a bunch of noise.

#### What I Think I Think Now

- Null hypothesis significance testing is much harder than I thought.
  - The null hypothesis is almost never a real thing.
  - Rather than rejiggering the cutoff, I would mostly abandon the p value as a summary
  - Replication is far more useful than I thought it was.
- Some hills aren't worth dying on.
  - Think about uncertainty intervals more than confidence or credible intervals
  - Retrospective calculations about Type S (sign) and Type M (magnitude) errors can help me illustrate ideas.
- Which method to use is far less important than finding better data
  - The biggest mistake I make regularly is throwing away useful data
  - I'm not the only one with this problem.
- The best thing I do most days is communicate more clearly.
  - When stuck in a design, I think about how to get better data.
  - When stuck in an analysis, I try to turn a table into a graph.
- I have A LOT to learn.