432 Homework 1 Answer Sketch

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4 Question 4. (5 points)							
0.	.1 Setup and Data Ingest						
	Jote: It's good practice not to load any more than you must, although you should install the complete f packages on our web site.	list					
1i 1i	ibrary(skimr) ibrary(broom) ibrary(tableone) ibrary(tidyverse)						
	- Attaching packages						
v v	ggplot2 2.2.1 v purrr 0.2.4 tibble 1.4.2 v dplyr 0.7.4 tidyr 0.7.2 v stringr 1.2.0 readr 1.1.1 v forcats 0.2.0						
x	- Conflictsdplyr::contains() masks skimr::contains()						

x dplyr::everything() masks skimr::everything()

x dplyr::filter() masks stats::filter()
x dplyr::lag() masks stats::lag()

Note: I loaded the data for this assignment into a subfolder of my R Project directory for Homework 1 called data. Hence, I use the following command to load in the hbp330.csv data.

```
hbp330 <- read.csv("data/hbp330.csv") %>% tbl_df
```

1 Question 1 (40 points)

Note: I don't expect or need you to include the question in your response to homework assignments. I include them here to provide some context for the sketch.

Build a Table 1 to compare the subjects in practice A to the subjects in practice B on the following nine variables: age, race, Hispanic ethnicity, sex, primary insurance, body mass index, BMI category, and systolic and diastolic blood pressure. Make the Table as well as you can within R, and display the result as part of your HTML file. Include a description of the results of your Table 1 that does not exceed 100 words, using complete English sentences.

1.1 Creating the BMI and BMI Category variables

With the metric system, the formula for BMI is weight (in kilograms) divided by the square of height (in meters.)

```
hbp330 <- hbp330 %>%

# first we'll create the bmi values

mutate( bmi = weight / (height*height) ) %>%

# next we'll create the bmi categories with case_when
# note that values of NA in bmi return NA in bmi_cat, too

mutate( bmi_cat = case_when(
    bmi < 18.5 ~ "Underweight",
    bmi < 25 ~ "Normal",
    bmi < 30 ~ "Overweight",
    bmi >= 30 ~ "Obese")) %>%

# finally we arrange the bmi_cat by the median(bmi) levels
# we could instead have arranged by hand using fct_relevel

mutate( bmi_cat = fct_reorder( bmi_cat, bmi, median ))
```

As a sanity check, let's ensure that the subjects in each bmi_cat have bmi values as we expect...

```
hbp330 %>% group_by(bmi_cat) %>% skim(bmi)
```

```
Skim summary statistics n obs: 330
```

```
n variables: 21
group variables: bmi_cat
Variable type: numeric
                                                      p0 p25 median
    bmi_cat variable missing complete
                                     n mean
                                                sd
Underweight
                          0
                                 2
                                     2 17.41 0.97 16.73 17.07
                                                              17.41
                bmi
     Normal
                 bmi
                          0
                                  25 25 22.96 1.67 19.68 21.41 23.68
                                 63 63 27.66 1.43 25.05 26.6
 Overweight
                          0
                                                               27.32
                bmi
      Obese
                 bmi
                                 240 240 38.1 6.81 30.01 33.06 36.67
  p75 p100
17.76 18.1
24.32 24.99
28.88 30
40.97 64.04
```

OK. The minima and maxima match what we're looking for.

Note: In practical work, we would likely collapse together the Underweight and Normal categories, since there are so few patients in the Underweight category.

And again, a little sanity check to ensure we've not made a mistake.

0

A provider

```
hbp330 %>% count(bmi_cat, bmi_cat3)
```

```
# A tibble: 4 x 3
 bmi cat
             bmi_cat3
                                 n
              <fct>
  <fct>
                             <int>
1 Underweight Not_Overweight
                                 2
2 Normal
             Not_Overweight
                                25
3 Overweight Overweight
                                63
4 Obese
              Obese
                               240
```

1.2 Checking for Missing Values

```
hbp330 %>%
  group_by(practice) %>%
 skim()
Skim summary statistics
n obs: 330
n variables: 22
group variables: practice
Variable type: factor
practice variable missing complete
                                       n n unique
        Α
           bmi_cat
                          0
                                 180 180
                                                3
        A bmi_cat3
                          0
                                 180 180
        Α
           depdiag
                          0
                                 180 180
                                                2
                                                2
                          4
                                 176 180
        A eth hisp
                                                4
        A insurance
                          0
                                 180 180
```

180 180

7

```
race
                                   179 180
                                                    3
        Α
                            1
                                   180 180
                                                    2
        Α
                            0
                 sex
        Α
             subject
                            0
                                   180 180
                                                  180
                                                   3
             tobacco
                            0
                                   180 180
        Α
        В
             bmi_cat
                            0
                                   150 150
                                                    4
        В
                            0
                                   150 150
                                                    3
           bmi cat3
        В
                            0
                                   150 150
                                                    2
             depdiag
                                                    2
        В
           eth_hisp
                            1
                                   149 150
        B insurance
                            0
                                   150 150
                                                    4
                            0
                                                    7
        В
           provider
                                   150 150
        В
                race
                            1
                                   149 150
                                                    4
                                                    2
        В
                            0
                                   150 150
                 sex
        В
                            0
                                   150 150
                                                 150
             subject
        В
                            0
             tobacco
                                   150 150
                                                    3
                           top_counts ordered
 Obe: 136, Ove: 32, Nor: 11, Und: 1
                                         FALSE
  Obe: 136, Ove: 32, Not: 12, NA: 0
                                         FALSE
            No: 102, Yes: 78, NA: 0
                                         FALSE
             No: 174, NA: 4, Yes: 2
                                         FALSE
  Med: 76, Med: 66, Com: 35, Uni: 3
                                         FALSE
 A10: 44, A10: 37, A10: 32, A10: 31
                                         FALSE
    Bla: 166, Whi: 9, Mul: 4, NA: 1
                                         FALSE
                F: 119, M: 61, NA: 0
                                         FALSE
     A00: 1, A00: 1, A00: 1, A00: 1
                                         FALSE
   for: 75, nev: 70, cur: 35, NA: 0
                                         FALSE
 Obe: 104, Ove: 31, Nor: 14, Und: 1
                                         FALSE
  Obe: 104, Ove: 31, Not: 15, NA: 0
                                         FALSE
             No: 112, Yes: 38, NA: 0
                                         FALSE
             No: 87, Yes: 62, NA: 1
                                         FALSE
Med: 68, Med: 54, Com: 18, Uni: 10
                                         FALSE
 B10: 29, B10: 25, B10: 25, B10: 19
                                         FALSE
 Whi: 122, Bla: 14, Asi: 10, Mul: 3
                                         FALSE
                 F: 84, M: 66, NA: 0
                                         FALSE
     B00: 1, B00: 1, B00: 1, B00: 1
                                         FALSE
   nev: 70, for: 42, cur: 38, NA: 0
                                         FALSE
Variable type: integer
practice variable missing complete
                                                                       p25
                                               mean
                                                           sd
                                                                  p0
                                         n
                           0
                                  180 180
                                              56.34
                                                        11.17
                                                                  24
                                                                        49
        Α
                age
                           0
                                  180 180
                                                         0.48
                                                                   0
                                                                         0
             bpmed
                                               0.64
        Α
                           0
                                  180 180
                                                                  41
                                                                        67
        Α
                dbp
                                              74.49
                                                        11.4
        Α
                           0
                                  180 180
                                              82.73
                                                        12.48
                                                                  -2
                                                                        78
             hsgrad
                           0
        Α
             income
                                  180 180 34780
                                                     19412.55
                                                                 100 24675
        Α
                ldl
                          27
                                  153 180
                                             108.18
                                                        37.16
                                                                  39
                                                                        82
                sbp
        Α
                           0
                                  180 180
                                             130.82
                                                        15.38
                                                                  84
                                                                       120
                           0
                                  180 180
                                               0.7
                                                         0.46
                                                                   0
                                                                         0
        Α
             statin
        В
                           0
                                  150 150
                                              54.17
                                                        11.89
                                                                  23
                                                                        46
                age
        В
                           0
                                                                   0
                                                                         0
             bpmed
                                  150 150
                                               0.67
                                                         0.47
        В
                dbp
                           0
                                  150 150
                                              75.05
                                                         8.58
                                                                  54
                                                                        69
        В
             hsgrad
                           0
                                  150 150
                                              80.03
                                                         7.72
                                                                  68
                                                                        74
        В
                           0
                                  150 150 35799.33 10768.65 15600 25925
             income
        В
                ldl
                          51
                                   99 150
                                              96.06
                                                        33.85
                                                                  35
                                                                        70
        В
                           0
                                  150 150
                                             125.44
                                                        19
                                                                  85
                                                                       113
                sbp
        В
             statin
                           0
                                  150 150
                                               0.71
                                                         0.45
                                                                   0
                                                                         0
```

```
p75
 median
                      p100
   58
             65
                        77
    1
              1
                         1
   74
             83
                       101
   84
             91
                       100
29150
         42825
                    147400
  102
                       245
           132
                       194
  131
            139
    1
              1
                         1
   55.5
                        75
             64
    1
              1
                         1
   74.5
             80
                       106
            86.75
   78
                        97
34550
         42275
                     71400
           123.5
                       174
   93
  123.5
            134.75
                       191
    1
              1
                          1
```

Variable type: numeric

```
р0
practice variable missing complete
                                     n mean
                                                 sd
                                                            p25 median
       Α
              bmi
                        0
                               180 180 35.2
                                               8.2 16.73 30.05
                                                                 34.06
       Α
           height
                        0
                               180 180
                                        1.68 0.12
                                                    1.38
                                                          1.6
                        0
                               180 180 98.51 22.76 53
                                                                 94.5
       Α
           weight
                                                          82.52
       В
                        0
                               150 150 34.39 7.83 18.1
                                                          28.74
                                                                 33.48
              bmi
       В
                        0
                                                           1.55
                                                                  1.63
           height
                               150 150 1.64 0.12 1.4
       В
           weight
                        0
                               150 150 92.39 23.42 50.4 75.6
                                                                 90.45
   p75
        p100
 39.3
        64.04
         1.95
  1.76
112.53 162.4
 38.98
       63.55
  1.71
         1.93
106.97 181.5
```

We're missing the following values:

- 1dl on 78 subjects, but that's not in our Table 1, so we won't worry about that now, and
- race on 2 subjects (1 in practice A and 1 in practice B), and
- eth_hisp on 5 subjects (4 in practice A and 1 in practice B).

1.3 First Attempt at Table 1

1.4 Making Decisions about Summary Approaches

Note that if we look at a summary of this Table 1, we see that:

- the difference in p values between the "normal" and "non-normal" versions of each of the continuous variables is small enough that if we're going to compare the p values to, say, 0.05, it won't matter which we choose, and
- the practical impact of the choice of p values between the "approximate" and "exact" versions of each of the categorical variables is also small.

summary(hw1_table1)

Summary of continuous variables

practice: A

n miss p.miss mean sd median p25 p75 min max skew kurt 0 56 11 58 49 65 24 77 -0.57 -0.03 age 180 bmi 180 0 0 35 8 34 30 39 17 64 0.93 1.35 0 0 131 15 131 120 139 84 194 0.57 1.89 sbp 180 dbp 180 0 74 11 74 67 83 41 101 -0.07 -0.20

practice: B

n miss p.miss mean sd median p25 p75 min max skew kurt 56 46 64 23 75 -0.4 -0.4 age 150 0 54 12 bmi 150 0 34 8 33 29 39 18 64 0.8 1.3 0 sbp 150 0 0 125 19 124 113 135 85 191 0.7 0.6 dbp 150 0 75 9 74 69 80 54 106 0.2 0.7

p-values

pNormal pNonNormal

age 0.088489264 0.1122326040

bmi 0.365264000 0.4971154515

sbp 0.004781282 0.0003634655

dbp 0.617464601 0.7253555322

Standardize mean differences

1 vs 2

age 0.18834212

bmi 0.10044371

sbp 0.31105472

dbp 0.05596318

Summary of categorical variables

practice: A

var	n	miss	p.miss	level	freq	percent	cum.percent
race	180	1	0.6	Asian/PI	0	0.0	0.0
				Black/AA	166	92.7	92.7
				${\tt Multi-Racial}$	4	2.2	95.0
				White	9	5.0	100.0
eth_hisp	180	4	2.2	No	174	98.9	98.9
				Yes	2	1.1	100.0
sex	180	0	0.0	F	119	66.1	66.1
				M	61	33.9	100.0

insurance		0	0.0	Commercial Medicaid Medicare Uninsured Underweight Normal Overweight Obese	11 32		19.4 56.1 98.3 100.0 0.6 6.7 24.4 100.0
practice: H	3						
var	n	miss	p.miss	level	${\tt freq}$	percent	<pre>cum.percent</pre>
race	150	1	0.7	Asian/PI	10	6.7	6.7
				Black/AA			
				Multi-Racial	3		
				White	122	81.9	100.0
eth_hisp	150	1	0.7	No	87	58.4	58.4
				Yes	62	41.6	100.0
sex	150	0	0.0	F	84	56.0	56.0
				M	66	44.0	100.0
insurance	150	0	0.0	Commercial	18	12.0	12.0
				Medicaid	68	45.3	57.3
				Medicare	54	36.0	93.3
				Uninsured	10	6.7	100.0
bmi_cat	150	0	0.0	Underweight	1	0.7	0.7
_				•	14		10.0
				Overweight	31	20.7	30.7
				Obese	104	69.3	100.0

p-values

pApprox pExact race 1.041050e-50 7.529447e-61 eth_hisp 2.207408e-19 1.531820e-22 sex 7.738092e-02 6.927716e-02 insurance 1.593679e-02 1.580010e-02 bmi_cat 5.868027e-01 5.894708e-01

Standardize mean differences

1 vs 2

race 3.1557762 eth_hisp 1.1352992 sex 0.2084780 insurance 0.3569322 bmi_cat 0.1531995

1.4.1 A closer look at Age

As an example, let's plot the age data within each practice to evaluate Normality. Just for fun, I'll run

- a boxplot
- a histogram, and
- a normal Q-Q plot

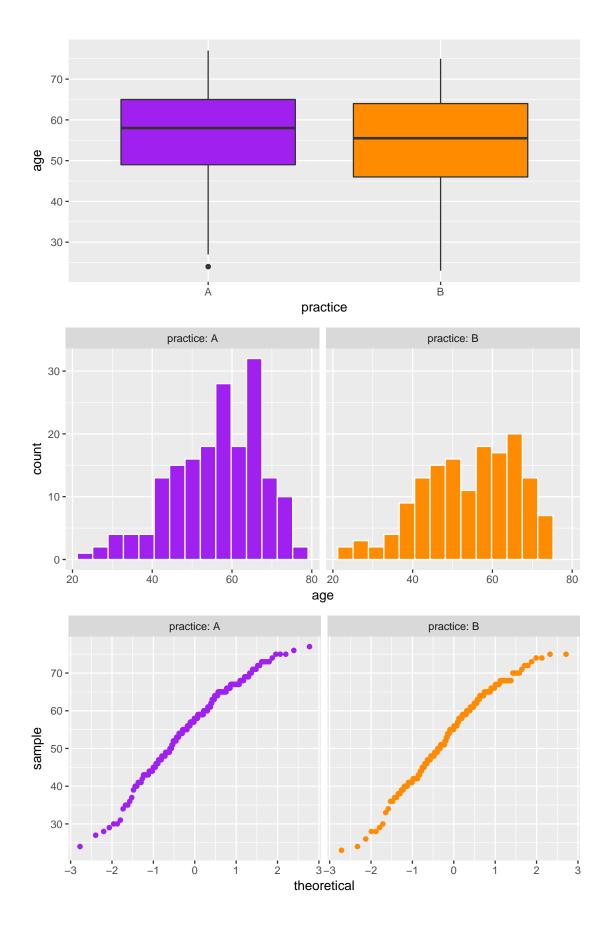
of the ages within each practice.

```
p1 <- ggplot(hbp330, aes(x = practice, y = age)) +
    geom_boxplot(fill = c("purple", "darkorange"))

p2 <- ggplot(hbp330, aes(x = age, fill = practice)) +
    geom_histogram(bins = 15, col = "white") +
    scale_fill_manual(values = c("purple", "darkorange")) +
    guides(fill = FALSE) +
    facet_wrap( ~ practice, labeller = label_both)

p3 <- ggplot(hbp330, aes(sample = age, color = practice)) +
    geom_qq() +
    scale_color_manual(values = c("purple", "darkorange")) +
    guides(color = FALSE) +
    facet_wrap( ~ practice, labeller = label_both)

gridExtra::grid.arrange(p1, p2, p3, ncol=1)</pre>
```



The data aren't *perfectly* Normally distributed, of course, but I don't see a big problem with summarizing via means and standard deviations. We could do something similar with each of the other quantitative variables.

1.5 Final Table 1 and Notes

print(hw1_table1)

Stratified by practice								
	Α		В		p	test		
n	180		150					
age (mean (sd))	56.34	(11.17)	54.17	(11.89)	0.088			
race (%)					<0.001			
Asian/PI	0	(0.0)	10	(6.7)				
Black/AA	166	(92.7)	14	(9.4)				
Multi-Racial	4	(2.2)	3	(2.0)				
White	9	(5.0)	122	(81.9)				
eth_hisp = Yes (%)	2	(1.1)	62	(41.6)	<0.001			
sex = M (%)	61	(33.9)	66	(44.0)	0.077			
insurance (%)					0.016			
Commercial	35	(19.4)	18	(12.0)				
Medicaid	66	(36.7)	68	(45.3)				
Medicare	76	(42.2)	54	(36.0)				
Uninsured	3	(1.7)	10	(6.7)				
bmi (mean (sd))	35.20	(8.20)	34.39	(7.83)	0.365			
<pre>bmi_cat (%)</pre>					0.587			
Underweight	1	(0.6)	1	(0.7)				
Normal	11	(6.1)	14	(9.3)				
Overweight	32	(17.8)	31	(20.7)				
Obese	136	(75.6)	104	(69.3)				
sbp (mean (sd))	130.82	(15.38)	125.44	(19.00)	0.005			
dbp (mean (sd))	74.49	(11.40)	75.05	(8.58)	0.617			

Notes for Table 1:

- 1. There are 4 subjects missing Hispanic ethnicity status in practice A, and 1 in practice B.
- 2. There is 1 subject in each practice missing Race.
- 3. Results are shown in terms of means and standard deviations for quantitative variables, and t tests are used for comparisons, because a Normal approximation was a reasonable choice for each such variable.
- 4. For categorical variables, we display counts and percentages, and use Pearson chi-square tests of significance.

1.5.1 Describing the Table in a few sentences

The key conclusions of this Table 1 are that the two practices are not especially comparable on demographic features, or systolic blood pressure, but show generally similar diastolic blood pressure and body mass index distributions. Subjects seen in Practice A are more frequently of Black race, less often of Hispanic ethnicity, more likely to have Cpmmercial or Medicare insurance (but less likely to have Medicaid or be uninsured) and display larger systolic blood pressure values that Practice B subjects. Practice A patients are also a bit older on average, and more likely to be female.

2 Question 2. (30 points)

0

1

0

1

64

116

101

49

128

133

117

127

127

133

119

128

13.3

16.0

17.4

19.1

1 A

2 A

3 B

4 B

Does which practice a person attends seem to have a meaningful impact on their systolic blood pressure, adjusting for whether or not they are on a blood pressure medication? Decide whether your model should include an interaction term sensibly, and then fit your choice of model and interpret and display the findings carefully. Be sure to provide a written explanation of your findings, in complete sentences. Responses without graphs are not complete.

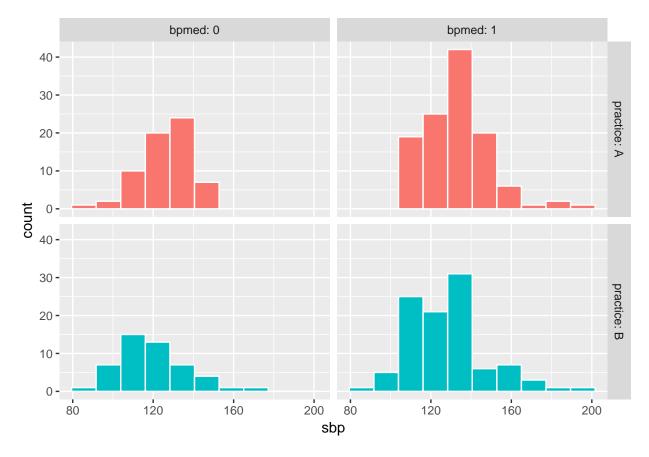
2.1 We'll start with a summary table and graph

We want to understand something about the impact of practice on SBP, adjusting for BP medication status.

Let's start with some numbers. We'll run a count of the number of patients within the practice and medication groups, along with some basic summaries of the sbp data within each group.

It looks like we have a plausible sample size to look at a picture in each case (there are no very small cells here) and that the medians and means are quite close in each group. Let's try some graphs, first of the raw data distributions...

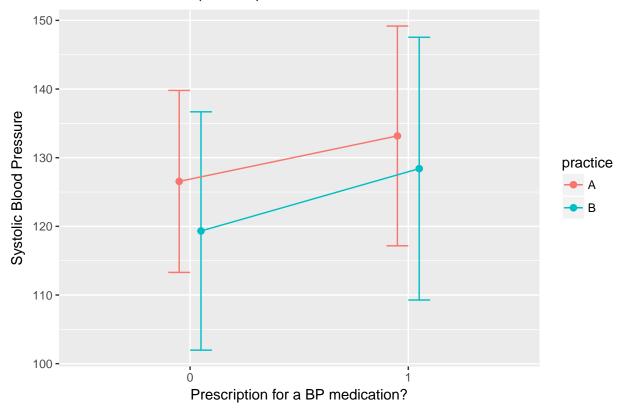
```
ggplot(hbp330, aes(x = sbp, fill = factor(practice))) +
  geom_histogram(bins = 10, col = "white") +
  guides(fill = FALSE) +
  facet_grid(practice ~ bpmed, labeller = label_both)
```



and I don't see any major problems with assuming that a mean and standard deviation might be reasonable choices to summarize the data from these four groups.

So, let's try graphing the means and standard deviations. . .

Observed Means (+/- SD) for SBP



I don't see much to suggest a meaningful interaction here. The lines joining the points are essentially parallel. It looks like the group with the lowest (healthiest) mean SBP are the subjects in practice B without a medication.

2.2 A Two-Way ANOVA model with Interaction

We'll run the two models (with and without interaction) but I expect the interaction to play only a small role.

```
hw1_q2_with_int <- lm(sbp ~ practice*bpmed, data = hbp330)
anova(hw1_q2_with_int)</pre>
```

Analysis of Variance Table

```
Response: sbp
                Df Sum Sq Mean Sq F value
                                             Pr(>F)
practice
                     2365 2365.2 8.4176
                                          0.003969 **
bpmed
                     4420
                           4420.0 15.7303 8.984e-05 ***
                            110.4 0.3928 0.531264
practice:bpmed
                 1
                      110
Residuals
               326
                   91602
                            281.0
               0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
```

It doesn't look like the interaction is either significant, or accounts for a large fraction of the variation in the SBP values. So we'll run and interpret the ANOVA model without interaction.

2.3 A Two-Way ANOVA model without interaction (Main Effects only)

```
hw1_q2_no_int <- lm(sbp ~ practice + bpmed, data = hbp330)
summary(hw1_q2_no_int)
Call:
lm(formula = sbp ~ practice + bpmed, data = hbp330)
Residuals:
   Min
            10 Median
                            3Q
                                   Max
-41.844 -11.961 -0.702
                         9.369 63.039
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 125.844
                         1.768 71.164 < 2e-16 ***
practiceB
             -5.600
                         1.852 -3.023
                                         0.0027 **
              7.716
                         1.944
                                 3.970 8.85e-05 ***
bpmed
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 16.75 on 327 degrees of freedom
Multiple R-squared: 0.06889,
                               Adjusted R-squared: 0.06319
F-statistic: 12.1 on 2 and 327 DF, p-value: 8.548e-06
```

Since each of the two factors is binary, we can simply read off that both practice and bpmed appear to have a significant impact on SBP, with practice B having lower SBP levels, on average, and subjects without BP medications having lower SBP levels, on average.

3 Question 3 (25 points)

Does the addition of the subject's age add meaningful predictive value to the model you developed in question 2? Does it change the nature of the conclusions you can draw from the model? How do you know? Be sure to provide a written explanation of your findings, in complete sentences, to accompany any output you choose to include. Responses without graphs are not complete.

3.1 ANCOVA: Adding age to the "no interaction" model

We'll build the new (ANCOVA) model including age and compare it to the no-interaction two-way ANOVA model.

```
hw1_q3 \leftarrow lm(sbp \sim practice + bpmed + age, data = hbp330)
```

3.2 Comparison to the "no interaction" model via ANOVA

```
anova(hw1_q3, hw1_q2_no_int)
Analysis of Variance Table
Model 1: sbp ~ practice + bpmed + age
```

```
Model 2: sbp ~ practice + bpmed
Res.Df RSS Df Sum of Sq F Pr(>F)

1 326 90178

2 327 91712 -1 -1534.3 5.5467 0.01911 *
---

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

It does appear that age adds significant predictive value to the no-interaction model.

3.3 Comparison to the "no interaction" model via fit quality summaries

In terms of summarizing the two models,

```
glance(hw1_q3)
   r.squared adj.r.squared
                              sigma statistic
                                                    p.value df
                                                                  logLik
1 0.08446494
                0.07603977 16.63185
                                    10.02531 2.452493e-06 4 -1393.973
       AIC
                BIC deviance df.residual
1 2797.946 2816.941 90177.6
                                     326
glance(hw1_q2_no_int)
   r.squared adj.r.squared
                              sigma statistic
                                                   p.value df
                                                                  logLik
1 0.06888764
                0.06319276 16.74708 12.09642 8.547555e-06 3 -1396.757
               BIC deviance df.residual
       AIC
1 2801.513 2816.71 91711.92
                                    327
```

The model with age included performs a bit better in terms of adjusted (and raw) R² and AIC and performs comparably in terms of BIC.

3.4 Comparison to the "no interaction" model in terms of conclusions

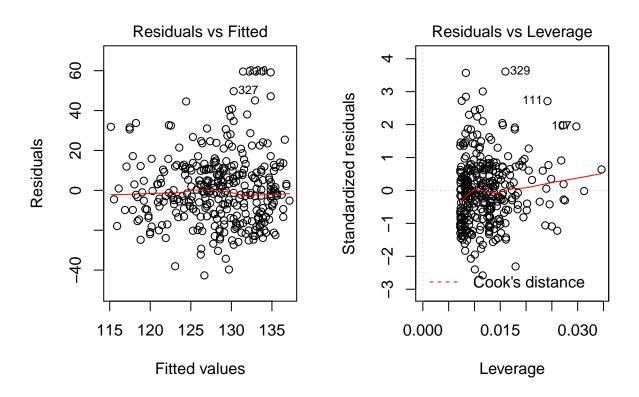
```
summary(hw1_q3)
Call:
lm(formula = sbp ~ practice + bpmed + age, data = hbp330)
Residuals:
   Min
            1Q Median
                            3Q
                                   Max
-42.670 -11.420 -1.185
                         9.917
                               59.559
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 115.65014
                        4.67108 24.759 < 2e-16 ***
            -5.14834
                        1.84952 -2.784 0.005689 **
practiceB
bpmed
             6.63315
                        1.98433
                                  3.343 0.000926 ***
             0.19333
                        0.08209
                                  2.355 0.019108 *
age
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 16.63 on 326 degrees of freedom
Multiple R-squared: 0.08446,
                               Adjusted R-squared: 0.07604
F-statistic: 10.03 on 3 and 326 DF, p-value: 2.452e-06
```

In terms of conclusions from the model, the adjustment for age does not change the fundamental conclusions from the no-interaction model. Specifically, we continue to see a significant effect of both practice (with B showing lower SBPs) and bpmed (with those not prescribed such a medication having smaller SBPs.)

3.5 Regression diagnostics for the ANCOVA model

I don't see any substantial problems with regression residuals in either a plot of residuals vs. fitted values, and there are no particularly influential points.

```
par(mfrow = c(1,2))
plot(hw1_q3, which = c(1, 5))
```



```
par(mfrow = c(1,1))
```

4 Question 4. (5 points)

Provide your GitHub name.

No sketch here. We want to know your GitHub name because we're hoping that before the semester is over, we can figure out a way to facilitate your posting the best and most sharable parts of your project portfolios to GitHub rather than just to Canvas. But for now, we just need the list of GitHub names.