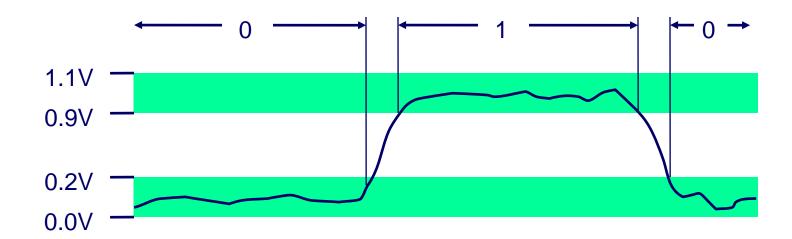
Bits, Bytes, and Integers – Ch2

- **■** Representing information as bits
- **■** Bit-level manipulations
- Integers
 - Representation: unsigned and signed
 - Conversion, casting
 - Expanding, truncating
 - Addition, negation, multiplication, shifting
 - Summary
- Representations in memory, pointers, strings



Everything is bits

- Each bit is 0 or 1
- **■** Why bits? Electronic Implementation
 - Easy to store with bistable elements
 - Reliably transmitted on noisy and inaccurate wires



Representing numbers in binary

■ Base 2 Number Representation

- Represent 15213₁₀ as 11101101101101₂
- Represent 1.20₁₀ as 1.0011001100110011[0011]...₂
- Represent 1.5213 X 10⁴ as 1.1101101101101₂ X 2¹³



Decimal to Binary conversion

Successive Division by 2

Read the remainders from the bottom up

29 decimal = 11101 binary



Decimal to Binary for fractions

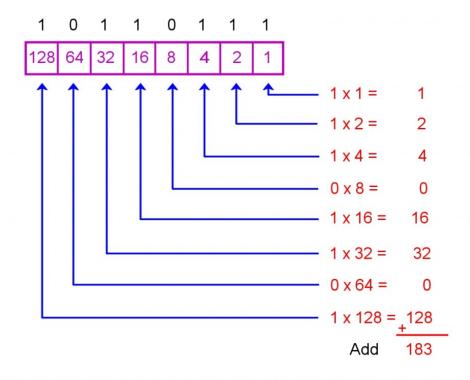
■ For 0.35

Binary Point	+			
	0	with a carry of	= 0.70	0.35 X 2
	1	with a carry of	= 0.40	0.70 X 2
Read Down	0	with a carry of	= 0.80	0.40 X 2
	1	with a carry of	= 0.60	0.80 X 2
	1 ,	with a carry of	= 0.20	0.60 X 2
Circuit Globe				



Binary to Decimal conversion





10110111 = 183 decimal



Encoding Byte Values

- Byte = 8 bits
 - **Binary** 000000002 to 111111112
 - **Decimal**: 0₁₀ to 255₁₀
 - ► Hexadecimal 00₁₆ to FF₁₆
 - ✓ Base 16 number representation
 - ✓ Use characters '0' to '9' and 'A' to 'F'
 - ✓ Write FA1D37B₁₆ in C as
 - ► 0xFA1D37B
 - Oxfa1d37b

Hex Decimanary

•	•	-
0	0	0000
1	1	0001
1 2 3	2 3	0010
	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
В	11	1011
С	12	1100
D	13	1101
E	14	1110
F	15	1111



■ Perform number conversions:

- Binary 10011011100111101101 to hexadecimal
- 0xD5E4C to binary

Hex Decimanary

0	0	0000
1	1	0001
1 2 3	2 3	0010
		0011
4 5	4 5	0100
5	5	0101
6 7 8	6 7	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
В	11	1011
B	12	1100
D	13	1101
E	14	1110
F	15	1111



■ Perform number conversions:

- Binary 10011011100111101101 to hexadecimal
- 0xD5E4C to binary

Binary 1001101110011110110101 to hexadecimal:

Binary	10	0110	1110	0111	1011	0101
Hexadecimal	2	6	E	7	В	5
Hexadecimal		D	5	E	4	C
Binary	110	1 01	.01 1	110	0100	1100

He	t De	Binary
0	0	0000
1	1	0001
1 2 3 4 5 6 7 8	1 2 3 4 5 6 7	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
Α	10	1010
В	11	1011
B C D	12	1011 1100
D	11 12 13	1101
E	14	1110
F	15	1111



- **■** Perform the following addition and subtractions in Hex
 - 0x503c + 0x8 =
 - B. 0x503c 0x40 =

	Decim	131 A
, et	Sec.	ina
K,	V	? `

0	0	0000
1	1	0001
1 2 3	2	0010
	ფ	0011
4	4	0100
4 5 6	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
В	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

■ Perform the following addition and subtractions in Hex

- -0x503c + 0x8 =
- 0x503c 0x40 =

- 0x503c + 0x8 = 0x5044. Adding 8 to hex c gives 4 with a carry of 1.
- 0x503c 0x40 = 0x4ffc. Subtracting 4 from 3 in the second digit position requires a borrow from the third. Since this digit is 0, we must also borrow from the fourth position.

Today: Bits, Bytes, and Integers

- **■** Representing information as bits
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Boolean Algebra

Developed by George Boole in 19th Century

- Algebraic representation of logic
 - Encode "True" as 1 and "False" as 0

And

■ A&B = 1 when both A=1 and B=1

&	0	1
0	0	0
1	0	1

Not

■ ~A = 1 when A=0

~	
0	1
1	0

Or

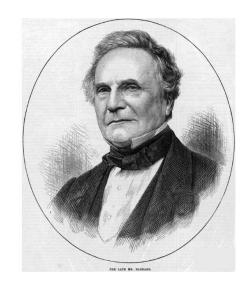
■ A | B = 1 when either A=1 or B=1

	0	1
0	0	1
1	1	1

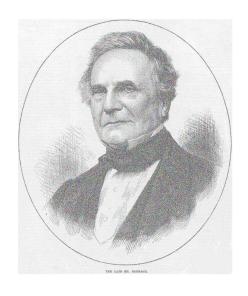
Exclusive-Or (Xor)

■ A^B = 1 when either A=1 or B=1, but not both

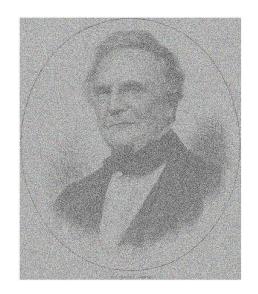
Guess the operation



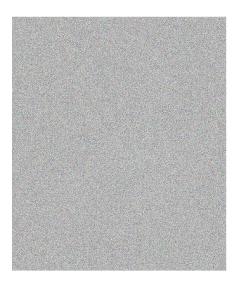
Original



Original OR random stream



Original AND Random stream



Original XOR random stream

Resource: khanacademy.org



General Boolean Algebras

- Operate on Bit Vectors
 - Operations applied bitwise

```
01101001 01101001 01101001

& 01010101 | 01010101 ^ 01010101 ~ 01010101

01000001 01111101 00111100 1010101
```

■ All of the Properties of Boolean Algebra Apply

Boolean Laws

T1: Commutative Law

- (a) A + B = B + A
- (b) A & B = B & A

T2: Associate Law

- (a) (A + B) + C = A + (B + C)
- (b) (A & B) & C = A & (B & C)

T3: Distributive Law

- (a) A & (B + C) = A & B + A & C
- (b) A + (B & C) = (A + B) & (A + C)

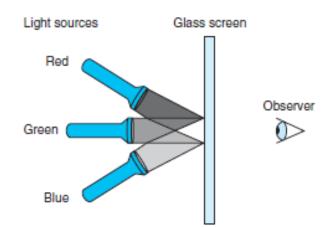
T4: Identity Law

- (a) A + A = A
- (b) A & A = A



■ We can create eight different colors based on the absence (0) or presence (1) of light sources R, G, and *B*:

- Describe the effect of applying **Boolean operations on the following** colors:
 - Blue | Green =
 - Cyan (011)
 - Yellow & Cyan =
 - Green (010)
 - Red ^ Magenta =
 - Blue (001)



R	\boldsymbol{G}	В	Color
0	0	0	Black
0	0	1	Blue
0	1	0	Green
0	1	1	Cyan
1	0	0	Red
1	0	1	Magenta
1	1	0	Yellow
1	1	1	White



Bit-Level Operations in C

- **■** Operations &, |, ~, ^ Available in C
 - Apply to any "integral" data type
 - long, int, short, char, unsigned
 - View arguments as bit vectors
 - Arguments applied bit-wise

Examples (Char data type)

- ~0x41 -> 0xBE
 - ~01000001₂ -> 10111110₂
- ~0x00 -> 0xFF
 - ~000000002 -> 1111111112
- 0x69 & 0x55 -> 0x41
 - 011010012 & 010101012 -> 010000012
- 0x69 | 0x55 -> 0x7D
 - 01101001₂ | 01010101₂ -> 01111101₂

```
#include <stdio.h>
                      x represents unsigned
void main()
    unsigned char A = 'A';
    unsigned char Anot = \sim A;
    printf("0x%x\n",A);
    printf("0x%x\n",Anot);
```

0x41 0xbe hex integer

Contrast: Logic Operations in C

Contrast to Logical Operators

- **&** &&, ||,!
 - View 0 as "False"
 - Anything nonzero as "True"
 - Always return 0 or 1
 - Early termination

Examples (char data type)

- !0x41 -> 0x00
- !0x00 -> 0x01
- !!0x41 -> 0x01
- 0x69 && 0x55 -> 0x01
- 0x69 || 0x55 -> 0x01

Contrast: Logic Operations in C

Contrast to Logical Operators

- **&**&, ||,!
 - View 0 as "False"
 - Anything nonzero as
 - Always return 0 or 1
 - Early termination

Examples (char data)

- !0x41 -> 0x00
- !0x00 -> 0x01
- !!0x41 -> 0x01
- 0x69 && 0x55 -> 0x01
- 0x69 || 0x55 -> 0x01

Watch out for && vs. & (and | vs. |)... one of the common oopsies in **C** programming

Practice 2.14

■ Suppose that x and y have byte values 0x66 and 0x39, respectively. Fill in the following table indicating the byte values of the different C expressions:

Expression	Value	Expression	Value
х&у		х && у	
хІу		хII у	
~x ~y		!x !y	
x & ! y		х && ~у	

Practice 2.14

■ Suppose that x and y have byte values 0x66 and 0x39, respectively. Fill in the following table indicating the byte values of the different C expressions:

Expression	Value	Expression	Value	X = 0110 0110 Y = 0011 1001	~X = 1001 1001 ~Y = 1100 0110
х & у	0x20	х && у	0x01	. 3311 1331	
хІу	0x7F	хІІу	0x01	0110 0110	1001 1001
~x ~y	0xDF	!x !y	0x00	& 0011 1001	1100 0110
y & Iv	0.00	v ## ~v	0×01	<u> </u>	+======

0110 0110 | 0011 1001

Shift Operations

- Left Shift: x << y
 - Shift bit-vector x left y positions
 - Throw away extra bits on left
 - Fill with 0's on right
- Right Shift: x >> y
 - Shift bit-vector x right y positions
 - Throw away extra bits on right
 - Logical shift
 - Fill with 0's on left
 - Arithmetic shift
 - Replicate most significant bit on left

■ Undefined Behavior

Shift amount < 0 or ≥ word size</p>

Argument x	01100010	
<< 3	00010 <i>000</i>	
Log. >> 2	00011000	
Arith. >> 2	00011000	

Argument x	10100010	
<< 3	00010 <i>000</i>	
Log. >> 2	<i>00</i> 101000	
Arith. >> 2	<i>11</i> 101000	

In C:

>> unsigned is logical
>> signed is Arithmetic



Shift Operations

```
unsigned int num1 = 64;
int num2 = -64;
printf("0x\%08x %d\n", num1, num1);
printf("0x\%08x %d\n", num1>>4, num1>>4);
printf("0x\%08x %d\n", num1<<4, num1<<4);
printf("\n");
printf("0x%x %d\n", num2, num2);
printf("0x%x %d\n", num2>>4, num2>>4);
printf("0x\%x %d\n", num2<<4, num2<<4);
```

```
0x00000040
            64
0x00000004
            4
0x00000400 1024
            -64
0xfffffc00
            -1024
```

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