

```

ln[1]:= q = q0 * Exp[I * (k * x + w * t)];
qjn = q0 * Exp[I * (k * xj + w * tn)];
qjbar = Integrate[q, {x, xj - dx/2, xj + dx/2}] / (dx);
qjnbar = qjbar /. t -> tn;
MA = qjn / qjnbar;

qntbar = Integrate[q, {t, tn, tn + dt}] / (dt);
qjntbar = qntbar /. x -> xj;
MtA = qjntbar / qjn;

qjphn = q0 * Exp[I * (k * (xj + dx/2) + w * tn)];
RA = Simplify[MA * qjphn / (qjn)];

vmultG = H + H^3 / 3 * k^2;
GnA = -U * RA / vmultG;
GGA = RA / vmultG;
GcA = -U * H / vmultG;

fn1A = H * vh + U * eh;
fn1A = fn1A /. vh -> (GGA * Gca + GnA * eca) /. eh -> RA * eca;
fn1Gca0A = fn1A /. Gca -> 0;
fn1eca0A = fn1A /. eca -> 0;
fnnA = Simplify[fn1Gca0A / eca];
fnGA = fn1eca0A / Gca;
fncA = H * GcA;

fG1A = U * Gh + U * H * vh + g * H * eh;
fG1A = fG1A /. vh -> (GGA * Gca + GnA * eca) /. eh -> RA * eca /. Gh -> RA * Gca;
fG1Gca0A = fG1A /. Gca -> 0;
fG1eca0A = fG1A /. eca -> 0;
fGnA = Simplify[fG1Gca0A / eca];
fGGA = Simplify[fG1eca0A / Gca];
fGcA = U * H * GcA;

FnnA = -MtA * dt / dx * (1 - Exp[-I * k * dx]) * fnnA;
FnGA = -MtA * dt / dx * (1 - Exp[-I * k * dx]) * fnGA;
FGnA = -MtA * dt / dx * (1 - Exp[-I * k * dx]) * fGnA;
FGGA = -MtA * dt / dx * (1 - Exp[-I * k * dx]) * fGGA;

MatA = {{FnnA, FnGA}, {FGnA, FGGA}};
EA = {{1, 0}, {0, 1}} + MatA;

```

$$wAp = U * k + \frac{\sqrt{3} k \sqrt{g H (3 + H^2 k^2)}}{3 + H^2 k^2};$$

$$wAm = U * k - \frac{\sqrt{3} k \sqrt{g H (3 + H^2 k^2)}}{3 + H^2 k^2};$$

```
In[37]:= M = 1;
Merr = Series[M - MA, {dx, 0, 4}];
Rm = 1;
Rmerr = Series[Rm - RA, {dx, 0, 4}];
Rp = Exp[I * k * dx];
Rperr = Series[Rp - RA, {dx, 0, 4}];
Ru = (1 + Exp[I * k * dx]) / 2;
Ruerr = Series[Ru - Exp[I * k * dx / 2], {dx, 0, 4}];
Gold = H - H^3 / 3 * (2 * Cos[k * dx] - 2) / dx^2;
GG2 = Simplify[Ru / Gold];
GG2err = Series[GG2 - GGA, {dx, 0, 5}];
Gn2 = Simplify[-U * Ru / Gold];
Gn2err = Series[Gn2 - GnA, {dx, 0, 5}];
```

```
In[50]:= Text[Row[{"M  ||  ", M}]]
Text[Row[{"M  ||  ", TeXForm[M]}]]
Text[Row[{"M error  ||  ", TeXForm[Merr]}]]
Text[Row[{"M error  ||  ", Merr}]]
Text[" "]
Text[Row[{"Rm  ||  ", Rm}]]
Text[Row[{"Rm  ||  ", TeXForm[Rm]}]]
Text[Row[{"Rm error  ||  ", Rmerr}]]
Text[Row[{"Rm error  ||  ", TeXForm[Rmerr]}]]
Text[" "]
Text[Row[{"Rp  ||  ", Rp}]]
Text[Row[{"Rp  ||  ", TeXForm[Rp]}]]
Text[Row[{"Rp error  ||  ", Rperr}]]
Text[Row[{"Rp error  ||  ", TeXForm[Rperr]}]]
Text[" "]
Text[Row[{"GG2  ||  ", GG2}]]
Text[Row[{"GG2  ||  ", TeXForm[GG2]}]]
Text[Row[{"GG2 error  ||  ", GG2err}]]
Text[Row[{"GG2 error  ||  ", TeXForm[GG2err]}]]
Text[" "]
Text[Row[{"Gn2  ||  ", Gn2}]]
Text[Row[{"Gn2  ||  ", TeXForm[Gn2]}]]
Text[Row[{"Gn2 error  ||  ", Gn2err}]]
Text[Row[{"Gn2 error  ||  ", TeXForm[Gn2err]}]]
```

Out[50]= M || 1

Out[51]= M || 1

Out[52]= M error || $-\frac{\text{dx}^2 k^2}{24} - \frac{7 \text{dx}^4 k^4}{5760} + O(\text{dx}^5)$

Out[53]= M error || $-\frac{k^2 \text{dx}^2}{24} - \frac{7 k^4 \text{dx}^4}{5760} + O[\text{dx}]^5$

Out[54]=

Out[55]= Rm || 1

Out[56]= Rm || 1

Out[57]= Rm error || $-\frac{1}{2} i k \text{dx} + \frac{k^2 \text{dx}^2}{12} + \frac{k^4 \text{dx}^4}{720} + O[\text{dx}]^5$

Out[58]= Rm error || $-\frac{1}{2} i \text{dx} k + \frac{\text{dx}^2 k^2}{12} + \frac{\text{dx}^4 k^4}{720} + O(\text{dx}^5)$

Out[59]=

Out[60]= Rp || $e^{i \text{dx} k}$

Out[61]= Rp || $e^{i \text{dx} k}$

Out[62]= Rp error || $\frac{i k \text{dx}}{2} - \frac{5 k^2 \text{dx}^2}{12} - \frac{1}{6} i k^3 \text{dx}^3 + \frac{31 k^4 \text{dx}^4}{720} + O[\text{dx}]^5$

Out[63]= Rp error || $\frac{i \text{dx} k}{2} - \frac{5 \text{dx}^2 k^2}{12} - \frac{1}{6} i \text{dx}^3 k^3 + \frac{31 \text{dx}^4 k^4}{720} + O(\text{dx}^5)$

Out[64]=

Out[65]= GG2 || $\frac{1 + e^{i \text{dx} k}}{2 \left(H - \frac{2 H^3 (-1 + \cos[\text{dx} k])}{3 \text{dx}^2} \right)}$

Out[66]= GG2 || $\frac{1 + e^{i \text{dx} k}}{2 \left(H - \frac{2 H^3 (\cos(\text{dx} k) - 1)}{3 \text{dx}^2} \right)}$

Out[67]= GG2 error || $\frac{(-6 k^2 - H^2 k^4) \text{dx}^2}{4 H (3 + H^2 k^2)^2} - \frac{i (6 k^3 + H^2 k^5) \text{dx}^3}{8 H (3 + H^2 k^2)^2} + \frac{(144 k^4 + 45 H^2 k^6 + 4 H^4 k^8) \text{dx}^4}{240 H (3 + H^2 k^2)^3} - \frac{i (-54 k^5 + H^4 k^9) \text{dx}^5}{480 H (3 + H^2 k^2)^3} + O[\text{dx}]^6$

Out[68]= GG2 error ||

$\frac{\text{dx}^2 \left(-H^2 k^4 - 6 k^2 \right)}{4 H \left(H^2 k^2 + 3 \right)^2} - \frac{i \text{dx}^3 \left(H^2 k^5 + 6 k^3 \right)}{8 H \left(H^2 k^2 + 3 \right)^2} + \frac{\text{dx}^4 \left(4 H^4 k^8 + 45 H^2 k^6 + 144 k^4 \right)}{240 H \left(H^2 k^2 + 3 \right)^3} - \frac{i \text{dx}^5 \left(H^4 k^9 - 54 k^5 \right)}{480 H \left(H^2 k^2 + 3 \right)^3} + O(\text{dx}^6)$

Out[69]=

Out[70]= Gn2 || $-\frac{(1 + e^{i \text{dx} k}) U}{2 \left(H - \frac{2 H^3 (-1 + \cos[\text{dx} k])}{3 \text{dx}^2} \right)}$

Out[71]= Gn2 || $-\frac{U \left(1 + e^{i \text{dx} k} \right)}{2 \left(H - \frac{2 H^3 (\cos(\text{dx} k) - 1)}{3 \text{dx}^2} \right)}$

$$\text{Out}[72]= \text{Gn2 error} \parallel \frac{(6k^2+H^2k^4)Udx^2}{4H(3+H^2k^2)^2} + \frac{i(6k^3+H^2k^5)Udx^3}{8H(3+H^2k^2)^2} - \frac{((144k^4+45H^2k^6+4H^4k^8)U)dx^4}{240(H(3+H^2k^2)^3)} + \frac{i(-54k^5+H^4k^9)Udx^5}{480H(3+H^2k^2)^3} + O[dx]^6$$

$$\text{Out}[73]= \text{Gn2 error} \parallel \frac{\text{dx}^2 U \left(H^2 k^4 + 6 k^2 \right)}{4 H \left(H^2 k^2 + 3 \right)^2} + \frac{i \text{dx}^3 U \left(H^2 k^5 + 6 k^3 \right)}{8 H \left(H^2 k^2 + 3 \right)^2} - \frac{\text{dx}^4 \left(U \left(4 H^4 k^8 + 45 H^2 k^6 + 144 k^4 \right) \right)}{240 \left(H \left(H^2 k^2 + 3 \right)^3 \right)} + \frac{i \text{dx}^5 U \left(H^4 k^9 - 54 k^5 \right)}{480 H \left(H^2 k^2 + 3 \right)^3} + O \left(\text{dx}^6 \right)$$

```

In[74]:= KurF = (fm*ap - fp*am + am*ap*(qp - qm)) / (ap - am);
KurFWS = KurF /. ap -> (U + Sqrt[g*H]) /. am -> (U - Sqrt[g*H]);
KurFWSeta =
  KurFWS /. fp -> (H*v + U*Rpp*n) /. fm -> (H*v + U*Rmp*n) /. qp -> Rpp*n /.
  qm -> Rmp*n;
KurFWSeta = KurFWSeta /. v -> (GGp*G + Gnp*n);
Kfnnp = FullSimplify[KurFWSeta /. G -> 0 /. n -> 1];
KfnGp = FullSimplify[KurFWSeta /. n -> 0 /. G -> 1];
Kfnn = Kfnnp /. Rpp -> Rp /. Rmp -> Rm /. GGp -> GG2 /. Gnp -> Gn2;
KfnG = KfnGp /. Rpp -> Rp /. Rmp -> Rm /. GGp -> GG2 /. Gnp -> Gn2;
Fnn2 = -dt*(1 - Exp[-I*k*dx])/dx*Kfnn;
Fnn2TA = Series[Fnn2 - FnnA, {dx, 0, 3}, {dt, 0, 3}];
Fnn2TA = Refine[Fnn2TA, {k > 0, U > 0, H > 0, g > 0}];
FnG2 = -dt*(1 - Exp[-I*k*dx])/dx*KfnG;
FnG2TA = Series[FnG2 - FnGA, {dx, 0, 3}, {dt, 0, 3}];
FnG2TA = Refine[FnG2TA, {k > 0, U > 0, H > 0, g > 0}];

KurFWSG = KurFWS /. fp -> (U*Rpp*G + U*H*v + g*H*Rpp*n) /.
  fm -> (U*Rmp*G + U*H*v + g*H*Rmp*n) /. qp -> Rpp*G /. qm -> Rmp*G;
KurFWSG = KurFWSG /. v -> (GGp*G + Gnp*n);
KfGnp = FullSimplify[KurFWSG /. G -> 0 /. n -> 1];
KfGGp = FullSimplify[KurFWSG /. n -> 0 /. G -> 1];
KfGn = KfGnp /. Rpp -> Rp /. Rmp -> Rm /. GGp -> GG2 /. Gnp -> Gn2;
KfGG = KfGGp /. Rpp -> Rp /. Rmp -> Rm /. GGp -> GG2 /. Gnp -> Gn2;

FGn2 = -dt*(1 - Exp[-I*k*dx])/dx*KfGn;
FGn2TA = Series[FGn2 - FGnA, {dx, 0, 3}, {dt, 0, 3}];
FGn2TA = Refine[FGn2TA, {k > 0, U > 0, H > 0, g > 0}];
fGG2 = U*H*GG2 + U/2*(Rm + Rp) - (Sqrt[g*H])/2*(Rp - Rm);
FGG2 = -dt*(1 - Exp[-I*k*dx])/dx*KfGG;
FGG2TA = Series[FGG2 - FGGA, {dx, 0, 4}, {dt, 0, 3}];
FGG2TA = Refine[FGG2TA, {k > 0, U > 0, H > 0, g > 0}];
Fmat2 = {{Fnn2, FnG2}, {FGn2, FGG2}};
Emat2 = IdentityMatrix[2] + Fmat2;
Eerr = Series[Emat2 - EA, {dx, 0, 4}, {dt, 0, 4}];

```

```

EigvFmat2 = Eigenvalues[Fmat2];

RKStep = Log[1 + EigvFmat2] / (I * dt);
RKstepTay = Series[RKStep, {dx, 0, 4}, {dt, 0, 4}];
RKstepTayr = Simplify[-RKstepTay - {wAp, wAm}, {k > 0, H > 0, g > 0, U > 0}];

Text[Row[{" -Sqrt(gH) < U < Sqrt(gH)"}]]
Text[" "]
Text[Row[{"Fnn || ", Kfnnp}]]
Text[Row[{"Fnn || ", TeXForm[Kfnnp]}]]
Text[Row[{"Fnn error || ", Fnn2TAr}]]
Text[Row[{"Fnn error || ", TeXForm[Fnn2TAr]}]]
Text[" "]
Text[Row[{"FnG || ", KfnGp}]]
Text[Row[{"FnG || ", TeXForm[KfnGp]}]]
Text[Row[{"FnG error || ", FnG2TAr}]]
Text[Row[{"FnG error || ", TeXForm[FnG2TAr]}]]
Text[" "]
Text[Row[{"FGn || ", KfGnp}]]
Text[Row[{"FGn || ", TeXForm[KfGnp]}]]
Text[Row[{"FGn error || ", FGn2TAr}]]
Text[Row[{"FGn error || ", TeXForm[FGn2TAr]}]]
Text[" "]
Text[Row[{"FGG || ", KfGGp}]]
Text[Row[{"FGG || ", TeXForm[KfGGp]}]]
Text[Row[{"FGG error || ", FGG2TAr}]]
Text[Row[{"FGG error || ", TeXForm[FGG2TAr]}]]
Text[" "]
Text[" "]
Text[Row[{"Omega error || ", RKstepTayr}]]
Text[Row[{"Omega error || ", TeXForm[RKstepTayr]}]]
Text[" "]
Text[Row[{"EA || ", EA}]]
Text[Row[{"EA || ", TeXForm[EA]}]]
Text[Row[{"Eerr || ", Eerr}]]
Text[Row[{"Eerr || ", TeXForm[Eerr]}]]

```

Out[108]= $-\text{Sqrt}(gH) < U < \text{Sqrt}(gH)$

Out[109]=

$$\text{Out}[110]= \text{Fnn} \parallel \frac{1}{2} \left(2 \text{Gnp} H + \text{Rpp} \left(-\sqrt{g H} + U \right) + \text{Rmp} \left(\sqrt{g H} + U \right) \right)$$

$$\text{Out}[111]= \text{Fnn} \parallel \frac{1}{2} \left(\text{Rmp} \left(\sqrt{g H} + U \right) + \text{Rpp} \left(U - \sqrt{g H} \right) + 2 \text{Gnp} H \right)$$

$$\text{Out}[112]= \text{Fnn error} \parallel \left(-\frac{H^2 k^3 U w}{2(3+H^2 k^2)} - \frac{i H^2 k^3 U w^2 dt^3}{6(3+H^2 k^2)} + O[dt]^4 \right) + \left(-\frac{1}{2} \left(\sqrt{g H} k^2 \right) dt + O[dt]^4 \right) dx +$$

$$\left(\frac{i(9 H^2 k^5 + 2 H^4 k^7) U dt}{12(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + \left(\frac{1}{24} \sqrt{g H} k^4 dt + O[dt]^4 \right) dx^3 + O[dx]^4$$

$$\text{Out}[113]= \text{Fnn error} \parallel$$

$$\left(-\frac{dt^2}{2} \left(H^2 k^3 U w \right) \right) \frac{1}{2} \left(H^2 k^2 + 3 \right) - \frac{i}{6} \frac{dt^3}{2} H^2 k^3 U w^2 \left(H^2 k^2 + 3 \right) + O(dt^4) + dx \left(-\frac{1}{2} \sqrt{g H} k^2 \right) dt + O(dx^2)$$

$$+ O(dt^4) + dx^2 \left(\frac{i}{12} \left(2 H^4 k^7 + 9 H^2 k^5 \right) U dt \right) \frac{1}{2} \left(H^2 k^2 + 3 \right)^2 + O(dt^4) + dx^3 \left(\frac{1}{24} \sqrt{g H} k^4 dt \right) + O(dx^4)$$

$$\text{Out}[114]=$$

$$\text{Out}[115]= \text{FnG} \parallel \text{GGp} H$$

$$\text{Out}[116]= \text{FnG} \parallel \text{GGp} H$$

$$\text{Out}[117]= \text{FnG error} \parallel \left(-\frac{3(k w) dt^2}{2(3+H^2 k^2)} - \frac{i k w^2 dt^3}{2(3+H^2 k^2)} + O[dt]^4 \right) + \left(\frac{i(6 k^3 + H^2 k^5) dt}{4(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + O[dx]^4$$

$$\text{Out}[118]= \text{FnG error} \parallel \left(-\frac{3}{2} \frac{dt^2}{2} (k w) \right) \frac{1}{2} \left(H^2 k^2 + 3 \right) - \frac{i}{6} \frac{dt^3}{2} k w^2 \left(H^2 k^2 + 3 \right) + O(dt^4) + dx^2 \left(\frac{i}{4} \left(H^2 k^5 + 6 k^3 \right) U dt \right) \frac{1}{2} \left(H^2 k^2 + 3 \right)^2 + O(dt^4) + dx^3 \left(\frac{1}{24} \sqrt{g H} k^4 U dt \right) + O(dx^4)$$

$$\text{Out}[119]=$$

$$\text{Out}[120]= \text{FGn} \parallel \frac{1}{2} \left(g H (\text{Rmp} + \text{Rpp}) + \left(2 \text{Gnp} H + \sqrt{g H} (\text{Rmp} - \text{Rpp}) \right) U \right)$$

$$\text{Out}[121]= \text{FGn} \parallel$$

$$\frac{1}{2} \left(U \left(\sqrt{g H} (\text{Rmp} - \text{Rpp}) + 2 \text{Gnp} H \right) + g H (\text{Rmp} + \text{Rpp}) \right)$$

$$\text{Out}[122]= \text{FGn error} \parallel \left(-\frac{(k(3 g H + g H^3 k^2 - 3 U^2) w) dt^2}{2(3+H^2 k^2)} - \frac{i k(3 g H + g H^3 k^2 - 3 U^2) w^2 dt^3}{6(3+H^2 k^2)} + O[dt]^4 \right) + \left(-\frac{1}{2} \left(\sqrt{g H} k^2 U \right) dt + O[dt]^4 \right) dx +$$

$$\left(\frac{i(18 g H k^3 + 12 g H^3 k^5 + 2 g H^5 k^7 - 18 k^3 U^2 - 3 H^2 k^5 U^2) dt}{12(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + \left(\frac{1}{24} \sqrt{g H} k^4 U dt + O[dt]^4 \right) dx^3 + O[dx]^4$$

$$\text{Out}[123]= \text{FGn error} \parallel$$

$$\left(-\frac{dt^2}{2} (k w \left(g H^3 k^2 + 3 g H - 3 U^2 \right)) \right) \frac{1}{2} \left(H^2 k^2 + 3 \right) - \frac{i}{6} \frac{dt^3}{2} k w^2 \left(g H^3 k^2 + 3 g H - 3 U^2 \right) + O(dt^4) + dx \left(-\frac{1}{2} \sqrt{g H} k^2 U \right) dt + O(dx^2)$$

$$+ O(dt^4) + dx^2 \left(\frac{i}{12} \left(2 g H^5 k^7 + 12 g H^3 k^5 - 3 H^2 U^2 k^5 - 18 U^2 k^3 + 18 g H k^3 \right) U dt \right) \frac{1}{2} \left(H^2 k^2 + 3 \right)^2 + O(dt^4) + dx^3 \left(\frac{1}{24} \sqrt{g H} k^4 U dt \right) + O(dx^4)$$

Out[124]=

$$\text{Out[125]= FGG} \parallel \frac{1}{2} \left(\sqrt{g H} \text{ Rmp} - \sqrt{g H} \text{ Rpp} + (2 \text{ GGp} H + \text{ Rmp} + \text{ Rpp}) U \right)$$

$$\text{Out[126]= FGG} \parallel \frac{1}{2} \left(\text{Rmp} \sqrt{g H} - \text{Rpp} \sqrt{g H} + U (2 \text{ GGp} H + \text{Rmp} + \text{Rpp}) \right)$$

$$\begin{aligned} \text{Out[127]= FGG error} \parallel & \left(-\frac{k(6+H^2 k^2) U w}{2(3+H^2 k^2)} \frac{dt^2}{6(3+H^2 k^2)} + O[dt]^4 \right) + \\ & \left(-\frac{1}{2} \left(\sqrt{g H} k^2 \right) dt + O[dt]^4 \right) dx + \left(\frac{i(36 k^3 U + 15 H^2 k^5 U + 2 H^4 k^7 U) dt}{12(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + \\ & \left(\frac{1}{24} \sqrt{g H} k^4 dt + O[dt]^4 \right) dx^3 + \left(-\frac{i(108 k^5 U + 54 H^2 k^7 U + 17 H^4 k^9 U + 2 H^6 k^{11} U) dt}{240(3+H^2 k^2)^3} + O[dt]^4 \right) dx^4 + O[dx]^5 \end{aligned}$$

Out[128]= FGG error ||

$$\begin{aligned} & \left(-\frac{1}{2} \left(\text{Rmp} \sqrt{g H} - \text{Rpp} \sqrt{g H} + U (2 \text{ GGp} H + \text{Rmp} + \text{Rpp}) \right) \right) \\ & \left(-\frac{1}{2} \left(\sqrt{g H} k^2 \right) dt + O[dt]^4 \right) dx + \left(\frac{i(36 k^3 U + 15 H^2 k^5 U + 2 H^4 k^7 U) dt}{12(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + \\ & \left(\frac{1}{24} \sqrt{g H} k^4 dt + O[dt]^4 \right) dx^3 + \left(-\frac{i(108 k^5 U + 54 H^2 k^7 U + 17 H^4 k^9 U + 2 H^6 k^{11} U) dt}{240(3+H^2 k^2)^3} + O[dt]^4 \right) dx^4 + O[dx]^5 \end{aligned}$$

Out[129]=

Out[130]=

$$\begin{aligned} \text{Out[131]= Omega error} \parallel & \left\{ \frac{i \left(\sqrt{3} k \sqrt{g H (3+H^2 k^2)} + 3 k U + H^2 k^3 U \right)^2 dt}{2(3+H^2 k^2)^2} - \frac{1}{3(3+H^2 k^2)^2} \right. \\ & \left(k^3 \left(\sqrt{3} \sqrt{g H (3+H^2 k^2)} + (3+H^2 k^2) U \right) \left(3 g H + U \left(2 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + (3+H^2 k^2) U \right) \right) \right) dt^2 - \\ & \frac{1}{4(3+H^2 k^2)^3} i k^4 \left(\sqrt{3} \sqrt{g H (3+H^2 k^2)} + (3+H^2 k^2) U \right) \left(3 g \left(\sqrt{3} H \sqrt{g H (3+H^2 k^2)} + 9 H U + 3 H^3 k^2 U \right) \right. \\ & \left. U^2 \left(H^4 k^4 U + 9 \left(\sqrt{3} \sqrt{g H (3+H^2 k^2)} + U \right) + 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3+H^2 k^2)} + 2 H^2 U \right) \right) \right) dt^3 + \\ & \frac{1}{5(3+H^2 k^2)^3} k^5 \left(\sqrt{3} \sqrt{g H (3+H^2 k^2)} + (3+H^2 k^2) U \right) \\ & \left(9 g^2 H^2 + 6 g H U \left(2 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + 3(3+H^2 k^2) U \right) + \right. \\ & \left. U^3 \left(12 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + 9 U + H^4 k^4 U + 2 k^2 \left(2 \sqrt{3} \sqrt{g H^5 (3+H^2 k^2)} + 3 H^2 U \right) \right) \right) dt^4 + \\ & \left. O[dt]^5 \right\} + \left(-\frac{1}{4} i k^2 \left(2 \sqrt{g H} + \frac{\sqrt{3} U}{\sqrt{3+H^2 k^2}} \right) + \frac{k^3 \left(2 \sqrt{g H (3+H^2 k^2)} + \sqrt{3} U \right) \left(\sqrt{3} \sqrt{g H (3+H^2 k^2)} + (3+H^2 k^2) U \right) dt}{4(3+H^2 k^2)^{3/2}} + \right. \\ & \frac{1}{4(3+H^2 k^2)^{3/2}} i k^4 \left(2 \sqrt{g H (3+H^2 k^2)} + \sqrt{3} U \right) \left(3 g H + U \left(2 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + (3+H^2 k^2) U \right) \right) dt^2 - \\ & \left. \frac{1}{4(3+H^2 k^2)^{5/2}} \left(k^5 \left(2 \sqrt{g H (3+H^2 k^2)} + \sqrt{3} U \right) \left(3 g \left(\sqrt{3} H \sqrt{g H (3+H^2 k^2)} + 9 H U + 3 H^3 k^2 U \right) + \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
& U^2 \left(H^4 k^4 U + 9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + U \right) + 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 2 H^2 U \right) \right) \\
& dt^3 - \frac{1}{4(3+H^2 k^2)^{3/2}} i k^6 \left(2 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} U \right) \\
& \left(9 g^2 H^2 + 6 g H U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + 2 k^2 \left(2 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 3 H^2 U \right) \right) \right) dt^4 + \\
& O[dt]^5 \left) dx + \left(- \left(\left(k^3 \left(12 \sqrt{3} g H (4 + H^2 k^2) + U \left(48 \sqrt{g H (3 + H^2 k^2)} - 9 \sqrt{3} U + \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. k^2 \left(16 \sqrt{g H^5 (3 + H^2 k^2)} - 3 \sqrt{3} H^2 U \right) \right) \right) \right) / \left(96 \left(\sqrt{g H (3 + H^2 k^2)^{3/2}} \right) \right) - \right. \\
& \left(i k^4 \left(9 U^2 \left(16 \sqrt{g H (3 + H^2 k^2)} - 3 \sqrt{3} U \right) + k^4 U^2 \left(16 \sqrt{g H^9 (3 + H^2 k^2)} - 3 \sqrt{3} H^4 U \right) + \right. \right. \\
& 6 k^2 \left(18 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 16 \sqrt{g H^5 (3 + H^2 k^2)} U^2 - 3 \sqrt{3} H^2 U^3 \right) + \\
& 4 g H \left(63 \sqrt{g H (3 + H^2 k^2)} + 99 \sqrt{3} U + 63 \sqrt{3} H^2 k^2 U + \right. \\
& \left. k^4 \left(3 \sqrt{g H^9 (3 + H^2 k^2)} + 10 \sqrt{3} H^4 U \right) \right) \right) dt \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) + \\
& \left(k^5 \left(12 \sqrt{3} g^2 H^2 (30 + 15 H^2 k^2 + 2 H^4 k^4) + 9 U^3 \left(16 \sqrt{g H (3 + H^2 k^2)} - 3 \sqrt{3} U \right) + \right. \right. \\
& k^4 U^3 \left(16 \sqrt{g H^9 (3 + H^2 k^2)} - 3 \sqrt{3} H^4 U \right) + \\
& 6 k^2 \left(56 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 16 \sqrt{g H^5 (3 + H^2 k^2)} U^3 - 3 \sqrt{3} H^2 U^4 \right) + \\
& g H U \left(864 \sqrt{g H (3 + H^2 k^2)} + 675 \sqrt{3} U + 429 \sqrt{3} H^2 k^2 U + \right. \\
& \left. 4 k^4 \left(6 \sqrt{g H^9 (3 + H^2 k^2)} + 17 \sqrt{3} H^4 U \right) \right) \right) dt^2 \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) + \\
& \frac{1}{96 \sqrt{g H (3 + H^2 k^2)^{7/2}}} i k^6 \left(9 k^2 \left(84 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 404 \sqrt{3} g^2 H^4 U + 438 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + \right. \right. \\
& 314 \sqrt{3} g H^3 U^3 + 48 \sqrt{g H^5 (3 + H^2 k^2)} U^4 - 9 \sqrt{3} H^2 U^5 \Big) + \\
& 27 \left(52 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 172 \sqrt{3} g^2 H^2 U + 16 \sqrt{g H (3 + H^2 k^2)} U^4 - \right. \\
& 3 \sqrt{3} U^5 + g H U^2 \left(210 \sqrt{g H (3 + H^2 k^2)} + 109 \sqrt{3} U \right) \Big) + \\
& 3 k^4 \left(36 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 304 \sqrt{3} g^2 H^6 U + 48 \sqrt{g H^9 (3 + H^2 k^2)} U^4 - \right. \\
& 9 \sqrt{3} H^4 U^5 + g H^5 U^2 \left(264 \sqrt{g H (3 + H^2 k^2)} + 301 \sqrt{3} U \right) \Big) + \\
& k^6 U \left(72 \sqrt{3} g^2 H^8 + 12 g H^7 U \left(3 \sqrt{g H (3 + H^2 k^2)} + 8 \sqrt{3} U \right) + \right. \\
& \left. U^3 \left(16 \sqrt{g H^{13} (3 + H^2 k^2)} - 3 \sqrt{3} H^6 U \right) \right) \Big) dt^3 - \frac{1}{96 \left(\sqrt{g H (3 + H^2 k^2)^{7/2}} \right)} \\
& \left(k^7 \left(36 \sqrt{3} g^3 H^3 (48 + 27 H^2 k^2 + 4 H^4 k^4) + 3 \sqrt{3} g^2 H^2 (4113 + 3075 H^2 k^2 + 712 H^4 k^4 + 48 H^6 k^6) U^2 + \right. \right. \\
& 2 g H U^3 \left(5076 \sqrt{g H (3 + H^2 k^2)} + 1971 \sqrt{3} U + 1872 \sqrt{3} H^2 k^2 U + \right.
\end{aligned}$$

$$\begin{aligned}
& \left(3 k^4 \left(216 \sqrt{g H^9 (3 + H^2 k^2)} + 197 \sqrt{3} H^4 U \right) + 2 k^6 \left(12 \sqrt{g H^{13} (3 + H^2 k^2)} + 31 \sqrt{3} H^6 U \right) \right) + U \left(7344 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 432 \sqrt{g H (3 + H^2 k^2)} U^4 - 81 \sqrt{3} U^5 + \right. \\
& k^6 U^4 \left(16 \sqrt{g H^{13} (3 + H^2 k^2)} - 3 \sqrt{3} H^6 U \right) + 9 k^2 \left(400 \sqrt{g^5 H^9 (3 + H^2 k^2)} + \right. \\
& 760 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 48 \sqrt{g H^5 (3 + H^2 k^2)} U^4 - 9 \sqrt{3} H^2 U^5 \left. \right) + \\
& \left. 9 k^4 \left(48 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 16 \sqrt{g H^9 (3 + H^2 k^2)} U^4 - 3 \sqrt{3} H^4 U^5 \right) \right) dt^4 + O[dt]^5 \Big) \\
& dx^2 + \left(\left(i k^4 \left(3 \sqrt{3} (3 + H^2 k^2) U^3 + 4 g H \left(12 \sqrt{g H (3 + H^2 k^2)} + 6 \sqrt{3} U + \right. \right. \right. \right. \\
& \left. \left. \left. k^2 \left(4 \sqrt{g H^5 (3 + H^2 k^2)} + \sqrt{3} H^2 U \right) \right) \right) \right) / (384 g H (3 + H^2 k^2)^{3/2}) - \\
& \left(k^5 \left(8 \sqrt{3} g^2 H^2 (54 + 33 H^2 k^2 + 5 H^4 k^4) + 3 \sqrt{3} (3 + H^2 k^2)^2 U^4 + 2 g H U \right. \right. \\
& \left. \left(81 \left(4 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} U \right) + 24 k^2 \left(7 \sqrt{g H^5 (3 + H^2 k^2)} + 2 \sqrt{3} H^2 U \right) + \right. \right. \\
& \left. \left. k^4 \left(24 \sqrt{g H^9 (3 + H^2 k^2)} + 7 \sqrt{3} H^4 U \right) \right) \right) dt \Big) / (384 (g H (3 + H^2 k^2)^{5/2})) - \\
& \left(i k^6 \left(3 k^2 \left(96 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 380 \sqrt{3} g^2 H^4 U + 224 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + \right. \right. \right. \\
& 51 \sqrt{3} g H^3 U^3 + 6 \sqrt{3} H^2 U^5 \left. \right) + k^4 \left(16 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 168 \sqrt{3} g^2 H^6 U + \right. \\
& 3 \sqrt{3} H^4 U^5 + 8 g H^5 U^2 \left(10 \sqrt{g H (3 + H^2 k^2)} + 3 \sqrt{3} U \right) \left. \right) + 9 \left(96 \sqrt{g^5 H^5 (3 + H^2 k^2)} + \right. \\
& 224 \sqrt{3} g^2 H^2 U + 3 \sqrt{3} U^5 + g H U^2 \left(160 \sqrt{g H (3 + H^2 k^2)} + 27 \sqrt{3} U \right) \left. \right) dt^2 \Big) / \\
& (384 g H (3 + H^2 k^2)^{5/2}) + \frac{1}{384 g H (3 + H^2 k^2)^{7/2}} k^7 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(3 k^2 \left(184 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 608 \sqrt{3} g^2 H^4 U + 334 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 72 \sqrt{3} g H^3 U^3 - \right. \right. \\
& 3 \sqrt{g H^5 (3 + H^2 k^2)} U^4 + 6 \sqrt{3} H^2 U^5 \left. \right) + k^4 \left(48 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + \right. \\
& 272 \sqrt{3} g^2 H^6 U + 3 \sqrt{3} H^4 U^5 + 2 g H^5 U^2 \left(56 \sqrt{g H (3 + H^2 k^2)} + 17 \sqrt{3} U \right) \left. \right) + \\
& 9 \left(160 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 352 \sqrt{3} g^2 H^2 U - 3 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\
& 3 \sqrt{3} U^5 + 2 g H U^2 \left(121 \sqrt{g H (3 + H^2 k^2)} + 19 \sqrt{3} U \right) \left. \right) dt^3 + \\
& \frac{1}{384 g H (3 + H^2 k^2)^{9/2}} i k^8 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right)^2 \\
& \left(3 k^2 \left(304 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 884 \sqrt{3} g^2 H^4 U + 456 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 95 \sqrt{3} g H^3 U^3 - \right. \right. \\
& 6 \sqrt{g H^5 (3 + H^2 k^2)} U^4 + 6 \sqrt{3} H^2 U^5 \left. \right) + k^4 \left(96 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + \right. \\
& 400 \sqrt{3} g^2 H^6 U + 3 \sqrt{3} H^4 U^5 + 4 g H^5 U^2 \left(36 \sqrt{g H (3 + H^2 k^2)} + 11 \sqrt{3} U \right) \left. \right) + \\
& 27 \left(80 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 168 \sqrt{3} g^2 H^2 U - 2 \sqrt{g H (3 + H^2 k^2)} U^4 + \sqrt{3} U^5 + \right. \\
& \left. \left. \left. \left(160 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 380 \sqrt{3} g^2 H^4 U + 224 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 9888 \sqrt{3} \, g^2 H^{10} U^3 - 75 \sqrt{3} \, H^8 U^7 + 16 g H^9 U^4 \left(96 \sqrt{g H (3 + H^2 k^2)} - 5 \sqrt{3} \, U \right) \Big) dt^3 + \\
& \frac{1}{92160 (g H)^{3/2} (3 + H^2 k^2)^{9/2}} k^9 \Big(144 \sqrt{3} \, g^4 H^4 (23832 + 22104 H^2 k^2 + 7395 H^4 k^4 + 1000 H^6 k^6 + 40 H^8 k^8) + \\
& 24 \sqrt{3} \, g^3 H^3 (893700 + 953451 H^2 k^2 + 376029 H^4 k^4 + 64744 H^6 k^6 + 4080 H^8 k^8) U^2 + \\
& 3 \sqrt{3} \, g^2 H^2 (3 + H^2 k^2)^2 (197625 + 114352 H^2 k^2 + 16944 H^4 k^4) U^4 + \\
& 2 g H U^5 \left(238464 \sqrt{g H (3 + H^2 k^2)} - 8505 \sqrt{3} \, U - 13365 \sqrt{3} \, H^2 k^2 U + \right. \\
& 27 k^4 \left(5888 \sqrt{g H^9 (3 + H^2 k^2)} - 285 \sqrt{3} \, H^4 U \right) + 3 k^6 \left(11776 \sqrt{g H^{13} (3 + H^2 k^2)} - 645 \right. \\
& \left. \sqrt{3} \, H^6 U \right) + 4 k^8 \left(736 \sqrt{g H^{17} (3 + H^2 k^2)} - 45 \sqrt{3} \, H^8 U \right) \Big) + \\
& 3 U \Big(135 \left(33920 \sqrt{g^7 H^7 (3 + H^2 k^2)} + 39424 \sqrt{g^5 H^5 (3 + H^2 k^2)} U^2 - 45 \sqrt{3} \, U^7 \right) + \\
& 36 k^2 \left(105472 \sqrt{g^7 H^{11} (3 + H^2 k^2)} + 144512 \sqrt{g^5 H^9 (3 + H^2 k^2)} \right. \\
& \left. U^2 + 5888 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^4 - 225 \sqrt{3} \, H^2 U^7 \right) + \\
& 18 k^4 \left(60608 \sqrt{g^7 H^{15} (3 + H^2 k^2)} + 100096 \sqrt{g^5 H^{13} (3 + H^2 k^2)} U^2 - 225 \sqrt{3} \, H^4 U^7 \right) + \\
& 12 k^6 \left(9600 \sqrt{g^7 H^{19} (3 + H^2 k^2)} + 20864 \sqrt{g^5 H^{17} (3 + H^2 k^2)} U^2 - 75 \sqrt{3} \, H^6 U^7 \right) + \\
& \left. 5 k^8 \left(384 \sqrt{g^7 H^{23} (3 + H^2 k^2)} + 2048 \sqrt{g^5 H^{21} (3 + H^2 k^2)} U^2 - 15 \sqrt{3} \, H^8 U^7 \right) \right) dt^4 + \\
& O[dt]^5 \Big) dx^4 + O[dx]^5, \left(\frac{i \left(-\sqrt{3} \, k \sqrt{g H (3 + H^2 k^2)} + 3 k U + H^2 k^3 U \right)^2 dt}{2 (3 + H^2 k^2)^2} - \frac{1}{3 (3 + H^2 k^2)^2} \right. \\
& \left(k^3 \left(-\sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right. \\
& \left. \left(3 g H + U \left(-2 \sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) \right) dt^2 - \\
& \frac{1}{4 (3 + H^2 k^2)^3} i k^4 \left(-\sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(3 g H \left(-\sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^2 \left(-9 \sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U - 3 k^2 \left(\sqrt{3} \, \sqrt{g H^5 (3 + H^2 k^2)} - 2 H^2 U \right) \right) \right) dt^3 + \\
& \frac{1}{5 (3 + H^2 k^2)^3} k^5 \left(-\sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(9 g^2 H^2 + 6 g H U \left(-2 \sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(-12 \sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + k^2 \left(-4 \sqrt{3} \, \sqrt{g H^5 (3 + H^2 k^2)} + 6 H^2 U \right) \right) \right) dt^4 + O[\\
& dt]^5 \Big) + \\
& \left(\frac{1}{2 (3 + H^2 k^2)^3} k^3 \left(2 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} \, U \right) \left(-\sqrt{3} \, \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) dt \right.
\end{aligned}$$

$$\begin{aligned}
& \left(-\frac{1}{4} i k^2 \left(2 \sqrt{g H} - \frac{\sqrt{3} U}{\sqrt{3+H^2 k^2}} \right) + \frac{\left(\sqrt{g H} - \frac{\sqrt{3} U}{\sqrt{3+H^2 k^2}} \right) \left(\sqrt{g H} - \frac{\sqrt{3} U}{\sqrt{3+H^2 k^2}} \right)}{4 (3+H^2 k^2)^{3/2}} + \right. \\
& \quad \frac{1}{4 (3+H^2 k^2)^{3/2}} \\
& \quad i k^4 \left(2 \sqrt{g H (3+H^2 k^2)} - \sqrt{3} U \right) \\
& \quad \left(3 g H + U \left(-2 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + (3+H^2 k^2) U \right) \right) \\
& \quad dt^2 - \frac{1}{4 (3+H^2 k^2)^{3/2}} \\
& \quad \left(k^2 \left(2 \sqrt{g H (3+H^2 k^2)} - \sqrt{3} U \right) \left(3 g H \left(-\sqrt{3} \sqrt{g H (3+H^2 k^2)} + 3 (3+H^2 k^2) U \right) + \right. \right. \\
& \quad \left. \left. U^2 \left(-9 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + 9 U + H^4 k^4 U - 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3+H^2 k^2)} - 2 H^2 U \right) \right) \right) \right) \\
& \quad dt^3 - \frac{1}{4 (3+H^2 k^2)^{3/2}} i k^6 \left(2 \sqrt{g H (3+H^2 k^2)} - \sqrt{3} U \right) \\
& \quad \left(9 g^2 H^2 + 6 g H U \left(-2 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + 3 (3+H^2 k^2) U \right) + \right. \\
& \quad \left. U^3 \left(-12 \sqrt{3} \sqrt{g H (3+H^2 k^2)} + 9 U + H^4 k^4 U + k^2 \left(-4 \sqrt{3} \sqrt{g H^5 (3+H^2 k^2)} + 6 H^2 U \right) \right) \right) dt^4 + \\
& \quad O[dt]^5 \Bigg) dx + \left(\left(k^3 \left(12 \sqrt{3} g H (4+H^2 k^2) - U \left(48 \sqrt{g H (3+H^2 k^2)} + 9 \sqrt{3} U + \right. \right. \right. \right. \\
& \quad \left. \left. \left. k^2 \left(16 \sqrt{g H^5 (3+H^2 k^2)} + 3 \sqrt{3} H^2 U \right) \right) \right) \right) / \left(96 \sqrt{g H} (3+H^2 k^2)^{3/2} \right) - \\
& \quad \left(i k^4 \left(9 U^2 \left(16 \sqrt{g H (3+H^2 k^2)} + 3 \sqrt{3} U \right) + k^4 U^2 \left(16 \sqrt{g H^9 (3+H^2 k^2)} + 3 \sqrt{3} H^4 U \right) + \right. \right. \\
& \quad 6 k^2 \left(18 \sqrt{g^3 H^7 (3+H^2 k^2)} + 16 \sqrt{g H^5 (3+H^2 k^2)} U^2 + 3 \sqrt{3} H^2 U^3 \right) + \\
& \quad 4 g H \left(63 \sqrt{g H (3+H^2 k^2)} - 99 \sqrt{3} U - 63 \sqrt{3} H^2 k^2 U + \right. \\
& \quad \left. k^4 \left(3 \sqrt{g H^9 (3+H^2 k^2)} - 10 \sqrt{3} H^4 U \right) \right) \Bigg) dt \Bigg) / \left(96 \sqrt{g H} (3+H^2 k^2)^{5/2} \right) + \\
& \quad \left(k^5 \left(-12 \sqrt{3} g^2 H^2 (30 + 15 H^2 k^2 + 2 H^4 k^4) + 9 U^3 \left(16 \sqrt{g H (3+H^2 k^2)} + 3 \sqrt{3} U \right) + \right. \right. \\
& \quad k^4 U^3 \left(16 \sqrt{g H^9 (3+H^2 k^2)} + 3 \sqrt{3} H^4 U \right) + \\
& \quad 6 k^2 \left(56 \sqrt{g^3 H^7 (3+H^2 k^2)} U + 16 \sqrt{g H^5 (3+H^2 k^2)} U^3 + 3 \sqrt{3} H^2 U^4 \right) + \\
& \quad g H U \left(864 \sqrt{g H (3+H^2 k^2)} - 675 \sqrt{3} U - 429 \sqrt{3} H^2 k^2 U + \right. \\
& \quad \left. 4 k^4 \left(6 \sqrt{g H^9 (3+H^2 k^2)} - 17 \sqrt{3} H^4 U \right) \right) \Bigg) dt^2 \Bigg) / \left(96 \sqrt{g H} (3+H^2 k^2)^{5/2} \right) + \\
& \quad \frac{1}{96 \sqrt{g H} (3+H^2 k^2)^{7/2}} i k^6 \left(9 k^2 \left(84 \sqrt{g^5 H^9 (3+H^2 k^2)} - 404 \sqrt{3} g^2 H^4 U + 438 \sqrt{g^3 H^7 (3+H^2 k^2)} U^2 - \right. \right. \\
& \quad 314 \sqrt{3} g H^3 U^3 + 48 \sqrt{g H^5 (3+H^2 k^2)} U^4 + 9 \sqrt{3} H^2 U^5 \Bigg) + \\
& \quad 3 k^4 \left(36 \sqrt{g^5 H^{13} (3+H^2 k^2)} - 304 \sqrt{3} g^2 H^6 U + 48 \sqrt{g H^9 (3+H^2 k^2)} U^4 + \right. \\
& \quad \left. 9 \sqrt{3} H^4 U^5 + 9 H^5 U^2 \left(264 \sqrt{g H (3+H^2 k^2)} - 301 \sqrt{3} U \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& \left(-\sqrt{g^5 H^5 (3 + H^2 k^2)} - 172 \sqrt{3} g^2 H^2 U + 16 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\
& \quad \left. 3 \sqrt{3} U^5 + g H U^2 \left(210 \sqrt{g H (3 + H^2 k^2)} - 109 \sqrt{3} U \right) \right) - \\
& \quad k^6 U \left(72 \sqrt{3} g^2 H^8 + 12 g H^7 U \left(-3 \sqrt{g H (3 + H^2 k^2)} + 8 \sqrt{3} U \right) - \right. \\
& \quad \left. U^3 \left(16 \sqrt{g H^{13} (3 + H^2 k^2)} + 3 \sqrt{3} H^6 U \right) \right) \Bigg) dt^3 + \frac{1}{96 \sqrt{g H (3 + H^2 k^2)^{7/2}}} \\
& \quad k^7 \left(36 \sqrt{3} g^3 H^3 (48 + 27 H^2 k^2 + 4 H^4 k^4) + 3 \sqrt{3} g^2 H^2 (4113 + 3075 H^2 k^2 + 712 H^4 k^4 + 48 H^6 k^6) U^2 + \right. \\
& \quad \left. 2 g H U^3 \left(-5076 \sqrt{g H (3 + H^2 k^2)} + 1971 \sqrt{3} U + 1872 \sqrt{3} H^2 k^2 U + \right. \right. \\
& \quad \left. \left. 3 k^4 \left(-216 \sqrt{g H^9 (3 + H^2 k^2)} + 197 \sqrt{3} H^4 U \right) + \right. \right. \\
& \quad \left. \left. 2 k^6 \left(-12 \sqrt{g H^{13} (3 + H^2 k^2)} + 31 \sqrt{3} H^6 U \right) \right) \right) - \\
& \quad U \left(7344 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 432 \sqrt{g H (3 + H^2 k^2)} U^4 + 81 \sqrt{3} U^5 + \right. \\
& \quad \left. k^6 U^4 \left(16 \sqrt{g H^{13} (3 + H^2 k^2)} + 3 \sqrt{3} H^6 U \right) + 9 k^2 \left(400 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 760 \right. \right. \\
& \quad \left. \left. \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 48 \sqrt{g H^5 (3 + H^2 k^2)} U^4 + 9 \sqrt{3} H^2 U^5 \right) + \right. \\
& \quad \left. \left. 9 k^4 \left(48 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 16 \sqrt{g H^9 (3 + H^2 k^2)} U^4 + 3 \sqrt{3} H^4 U^5 \right) \right) \right) dt^4 + O[dt]^5 \Bigg) dx^2 + \\
& \quad \left(- \left(i k^4 \left(3 \sqrt{3} (3 + H^2 k^2) U^3 + 4 g H \left(-12 \sqrt{g H (3 + H^2 k^2)} + 6 \sqrt{3} U + \right. \right. \right. \right. \\
& \quad \left. \left. \left. k^2 \left(-4 \sqrt{g H^5 (3 + H^2 k^2)} + \sqrt{3} H^2 U \right) \right) \right) \right) / (384 g H (3 + H^2 k^2)^{3/2}) \right) + \\
& \quad \left(k^5 \left(8 \sqrt{3} g^2 H^2 (54 + 33 H^2 k^2 + 5 H^4 k^4) + 3 \sqrt{3} (3 + H^2 k^2)^2 U^4 - 2 g H U \right. \right. \\
& \quad \left. \left(324 \sqrt{g H (3 + H^2 k^2)} - 81 \sqrt{3} U + 24 k^2 \left(7 \sqrt{g H^5 (3 + H^2 k^2)} - 2 \sqrt{3} H^2 U \right) + \right. \right. \\
& \quad \left. \left. k^4 \left(24 \sqrt{g H^9 (3 + H^2 k^2)} - 7 \sqrt{3} H^4 U \right) \right) \right) dt \Bigg) / (384 g H (3 + H^2 k^2)^{5/2}) - \\
& \quad \left(i k^6 \left(3 k^2 \left(96 \sqrt{g^5 H^9 (3 + H^2 k^2)} - 380 \sqrt{3} g^2 H^4 U + 224 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 - \right. \right. \right. \\
& \quad \left. \left. 51 \sqrt{3} g H^3 U^3 - 6 \sqrt{3} H^2 U^5 \right) + 9 \left(96 \sqrt{g^5 H^5 (3 + H^2 k^2)} - 224 \sqrt{3} g^2 H^2 U - \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} U^5 + g H U^2 \left(160 \sqrt{g H (3 + H^2 k^2)} - 27 \sqrt{3} U \right) \right) + k^4 \left(16 \sqrt{g^5 H^{13} (3 + H^2 k^2)} - \right. \right. \\
& \quad \left. \left. 168 \sqrt{3} g^2 H^6 U - 3 \sqrt{3} H^4 U^5 + 8 g H^5 U^2 \left(10 \sqrt{g H (3 + H^2 k^2)} - 3 \sqrt{3} U \right) \right) \right) dt^2 \Bigg) / \\
& \quad \left(384 g H (3 + H^2 k^2)^{5/2} \right) - \frac{1}{384 (g H (3 + H^2 k^2)^{7/2})} \left(k^7 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right. \\
& \quad \left. \left(-3 k^2 \left(184 \sqrt{g^5 H^9 (3 + H^2 k^2)} - 608 \sqrt{3} g^2 H^4 U + 334 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 - \right. \right. \right. \\
& \quad \left. \left. 72 \sqrt{3} g H^3 U^3 - 3 \sqrt{g H^5 (3 + H^2 k^2)} U^4 - 6 \sqrt{3} H^2 U^5 \right) - \right. \\
& \quad \left. 9 \left(160 \sqrt{g^5 H^5 (3 + H^2 k^2)} - 352 \sqrt{3} g^2 H^2 U - 3 \sqrt{g H (3 + H^2 k^2)} U^4 - 3 \sqrt{3} U^5 + \right. \right. \\
& \quad \left. \left. 2 g H U^2 \left(121 \sqrt{g H (3 + H^2 k^2)} - 19 \sqrt{3} U \right) \right) - k^4 \left(48 \sqrt{g^5 H^{13} (3 + H^2 k^2)} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 272 \sqrt{3} g^2 H^6 U - 3 \sqrt{3} H^4 U^5 + 2 g H^5 U^2 \left(56 \sqrt{g H (3 + H^2 k^2)} - 17 \sqrt{3} U \right) \Big) \Big) \\
& dt^3 - \frac{1}{384 g H (3 + H^2 k^2)^{9/2}} i k^8 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right)^2 \\
& \left(-3 k^2 \left(304 \sqrt{g^5 H^9 (3 + H^2 k^2)} - 884 \sqrt{3} g^2 H^4 U + 456 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 - \right. \right. \\
& \quad \left. 95 \sqrt{3} g H^3 U^3 - 6 \sqrt{g H^5 (3 + H^2 k^2)} U^4 - 6 \sqrt{3} H^2 U^5 \right) - \\
& \quad 27 \left(80 \sqrt{g^5 H^5 (3 + H^2 k^2)} - 168 \sqrt{3} g^2 H^2 U - 2 \sqrt{g H (3 + H^2 k^2)} U^4 - \right. \\
& \quad \left. \sqrt{3} U^5 + g H U^2 \left(112 \sqrt{g H (3 + H^2 k^2)} - 17 \sqrt{3} U \right) \right) - \\
& \quad k^4 \left(96 \sqrt{g^5 H^{13} (3 + H^2 k^2)} - 400 \sqrt{3} g^2 H^6 U - 3 \sqrt{3} H^4 U^5 + \right. \\
& \quad \left. 4 g H^5 U^2 \left(36 \sqrt{g H (3 + H^2 k^2)} - 11 \sqrt{3} U \right) \right) \Big) dt^4 + O[dt]^5 \Big) dx^3 + \\
& \left(\left(k^5 \left(-16 \sqrt{3} g^2 H^2 (144 + 48 H^2 k^2 + 5 H^4 k^4) + 75 \sqrt{3} (3 + H^2 k^2)^2 U^4 + 8 g H (3 + H^2 k^2) U \right. \right. \right. \\
& \quad \left. \left. \left(96 \sqrt{g H (3 + H^2 k^2)} + k^2 \left(32 \sqrt{g H^5 (3 + H^2 k^2)} - 5 \sqrt{3} H^2 U \right) \right) \right) \right) / \\
& \quad \left(30720 (g H)^{3/2} (3 + H^2 k^2)^{5/2} \right) + \frac{1}{92160 (g H)^{3/2} (3 + H^2 k^2)^{7/2}} \\
& \quad i k^6 \left(9 k^2 \left(8448 \sqrt{g^5 H^9 (3 + H^2 k^2)} - 16160 \sqrt{3} g^2 H^4 U + 6144 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + \right. \right. \\
& \quad \left. 240 \sqrt{3} g H^3 U^3 + 675 \sqrt{3} H^2 U^5 \right) + k^6 \left(1920 \sqrt{g^5 H^{17} (3 + H^2 k^2)} - \right. \\
& \quad \left. 4368 \sqrt{3} g^2 H^8 U + 2048 g H^7 \sqrt{g H (3 + H^2 k^2)} U^2 + 225 \sqrt{3} H^6 U^5 \right) + \\
& \quad 3 k^4 \left(6720 \sqrt{g^5 H^{13} (3 + H^2 k^2)} - 14512 \sqrt{3} g^2 H^6 U + 675 \sqrt{3} H^4 U^5 + \right. \\
& \quad \left. 24 g H^5 U^2 \left(256 \sqrt{g H (3 + H^2 k^2)} + 5 \sqrt{3} U \right) \right) + 27 \left(3968 \sqrt{g^5 H^5 (3 + H^2 k^2)} - \right. \\
& \quad \left. 6016 \sqrt{3} g^2 H^2 U + 225 \sqrt{3} U^5 + 8 g H U^2 \left(256 \sqrt{g H (3 + H^2 k^2)} + 15 \sqrt{3} U \right) \right) \Big) dt - \\
& \frac{1}{92160 (g H)^{3/2} (3 + H^2 k^2)^{7/2}} \left(k^7 \left(-48 \sqrt{3} g^3 H^3 (6192 + 5004 H^2 k^2 + 1425 H^4 k^4 + 140 H^6 k^6) - \right. \right. \\
& \quad 8 \sqrt{3} g^2 H^2 (60426 + 55557 H^2 k^2 + 17121 H^4 k^4 + 1772 H^6 k^6) U^2 + \\
& \quad g H U^3 \left(89856 \sqrt{g H (3 + H^2 k^2)} + 5265 \sqrt{3} U + 4590 \sqrt{3} H^2 k^2 U + \right. \\
& \quad \left. 9 k^4 \left(3328 \sqrt{g H^9 (3 + H^2 k^2)} + 145 \sqrt{3} H^4 U \right) + 8 k^6 \left(416 \sqrt{g H^{13} (3 + H^2 k^2)} + \right. \\
& \quad \left. 15 \sqrt{3} H^6 U \right) \Big) + 3 U \left(81 \left(2816 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 25 \sqrt{3} U^5 \right) + \right. \\
& \quad \left. 3 k^2 \left(52352 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 9984 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 675 \sqrt{3} H^2 U^5 \right) + \right. \\
& \quad \left. 3 k^4 \left(11776 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 225 \sqrt{3} H^4 U^5 \right) + \right. \\
& \quad \left. 5 k^6 \left(512 \sqrt{g^5 H^{17} (3 + H^2 k^2)} + 15 \sqrt{3} H^6 U^5 \right) \right) \Big) \Big) dt^2 - \frac{1}{30720 (g H)^{3/2} (3 + H^2 k^2)^{9/2}} \\
& i k^8 \left(27 k^2 \left(20416 \sqrt{g^7 H^{11} (3 + H^2 k^2)} - 80544 \sqrt{3} g^3 H^5 U + 82240 \sqrt{g^5 H^9 (3 + H^2 k^2)} U^2 - \right. \right.
\end{aligned}$$

$$\begin{aligned} & 46\,960\sqrt{3}\,g^2H^4U^3 + 6144\sqrt{g^3H^7(3+H^2k^2)}\,U^4 + 305\sqrt{3}\,gH^3U^5 + 300\sqrt{3}\,H^2U^7 \Big) + \\ & k^8 \Big(480\sqrt{g^7H^{23}(3+H^2k^2)} - 11\,520\sqrt{3}\,g^3H^{11}U + 5760\sqrt{g^5H^{21}(3+H^2k^2)}\,U^2 - \\ & 9888\sqrt{3}\,g^2H^{10}U^3 + 75\sqrt{3}\,H^8U^7 + 16gH^9U^4 \Big(96\sqrt{gH(3+H^2k^2)} + 5\sqrt{3}\,U \Big) \Big) + \\ & 243 \Big(2592\sqrt{g^7H^7(3+H^2k^2)} - 8128\sqrt{3}\,g^3H^3U + 9152\sqrt{g^5H^5(3+H^2k^2)}\,U^2 - \\ & 4168\sqrt{3}\,g^2H^2U^3 + 25\sqrt{3}\,U^7 + gH^4U^4 \Big(512\sqrt{gH(3+H^2k^2)} + 25\sqrt{3}\,U \Big) \Big) + \\ & 3k^6 \Big(6720\sqrt{g^7H^{19}(3+H^2k^2)} - 55\,216\sqrt{3}\,g^3H^9U + 39\,488\sqrt{g^5H^{17}(3+H^2k^2)}\,U^2 - \\ & 41\,728\sqrt{3}\,g^2H^8U^3 + 300\sqrt{3}\,H^6U^7 + 3gH^7U^4 \Big(2048\sqrt{gH(3+H^2k^2)} + 105\sqrt{3}\,U \Big) \Big) + \\ & 9k^4 \Big(19\,040\sqrt{g^7H^{15}(3+H^2k^2)} - 99\,856\sqrt{3}\,g^3H^7U + 88\,512\sqrt{g^5H^{13}(3+H^2k^2)}\,U^2 - 66\,296 \\ & \sqrt{3}\,g^2H^6U^3 + 450\sqrt{3}\,H^4U^7 + 3gH^5U^4 \Big(3072\sqrt{gH(3+H^2k^2)} + 155\sqrt{3}\,U \Big) \Big) \Big) dt^3 + \\ & \frac{1}{92\,160(gH)^{3/2}(3+H^2k^2)^{9/2}} k^9 \Big(-144\sqrt{3}\,g^4H^4(23\,832 + 22\,104H^2k^2 + 7395H^4k^4 + 1000H^6k^6 + 40H^8k^8) - \\ & 24\sqrt{3}\,g^3H^3(893\,700 + 953\,451H^2k^2 + 376\,029H^4k^4 + 64\,744H^6k^6 + 4080H^8k^8)U^2 - \\ & 3\sqrt{3}\,g^2H^2(3+H^2k^2)^2(197\,625 + 114\,352H^2k^2 + 16\,944H^4k^4)U^4 + \\ & 2gH^5U^5 \Big(238\,464\sqrt{gH(3+H^2k^2)} + 8505\sqrt{3}\,U + 13\,365\sqrt{3}\,H^2k^2U + \\ & 27k^4 \Big(5888\sqrt{gH^9(3+H^2k^2)} + 285\sqrt{3}\,H^4U \Big) + 3k^6 \Big(11\,776\sqrt{gH^{13}(3+H^2k^2)} + 645 \\ & \sqrt{3}\,H^6U \Big) + 4k^8 \Big(736\sqrt{gH^{17}(3+H^2k^2)} + 45\sqrt{3}\,H^8U \Big) \Big) \Big) + \\ & 3U \Big(135 \Big(33\,920\sqrt{g^7H^7(3+H^2k^2)} + 39\,424\sqrt{g^5H^5(3+H^2k^2)}\,U^2 + 45\sqrt{3}\,U^7 \Big) + \\ & 36k^2 \Big(105\,472\sqrt{g^7H^{11}(3+H^2k^2)} + 144\,512\sqrt{g^5H^9(3+H^2k^2)} \\ & U^2 + 5888\sqrt{g^3H^7(3+H^2k^2)}\,U^4 + 225\sqrt{3}\,H^2U^7 \Big) + \\ & 18k^4 \Big(60\,608\sqrt{g^7H^{15}(3+H^2k^2)} + 100\,096\sqrt{g^5H^{13}(3+H^2k^2)}\,U^2 + 225\sqrt{3}\,H^4U^7 \Big) + \\ & 12k^6 \Big(9600\sqrt{g^7H^{19}(3+H^2k^2)} + 20\,864\sqrt{g^5H^{17}(3+H^2k^2)}\,U^2 + 75\sqrt{3}\,H^6U^7 \Big) + \\ & 5k^8 \Big(384\sqrt{g^7H^{23}(3+H^2k^2)} + 2048\sqrt{g^5H^{21}(3+H^2k^2)} \\ & U^2 + 15\sqrt{3}\,H^8U^7 \Big) \Big) \Big) dt^4 + O[dt]^5 \Big) dx^4 + O[dx]^5 \Big\} \end{aligned}$$

```
Out[132]= Omega error ||
```

$$\frac{\left(\frac{i}{\sqrt{H^2 U^3 + 3 U + \sqrt{3}}} \sqrt{g H \left(H^2 k^2 + 3\right)} k\right)^2 \text{ (dt)}^2 \left(H^2 k^2 + 3\right)^2 - \frac{\left(k^3 \left(\left(H^2 k^2 + 3\right) U + \sqrt{3}\right) \sqrt{g H \left(H^2 k^2 + 3\right)}\right) \left(\left(3 g H + U \left(\left(H^2 k^2 + 3\right) U + 2 \sqrt{3}\right) \sqrt{g H \left(H^2 k^2 + 3\right)}\right)\right) \text{ (dt)}^2 \right)^3 \left(H^2 k^2 + 3\right)^2 - \frac{i k^4 \left(\left(H^2 k^2 + 3\right) U + \sqrt{3}\right) \sqrt{g H \left(H^2 k^2 + 3\right)}}{\left(H^4 U k^4 + 3 \left(2 U H^2 + \sqrt{3}\right) \sqrt{g H^5 \left(H^2 k^2 + 3\right)}\right) k^2 + 9 \left(U + \sqrt{3}\right) \sqrt{g H \left(H^2 k^2 + 3\right)}} U^2 + 3 g \left(3 k^2 U H^3 + 9 U H + \sqrt{3}\right) \sqrt{g H \left(H^2 k^2 + 3\right)} H\right) \text{ (dt)}^3 \left(4 \left(H^2 k^2 + 3\right)^3 + \frac{k^5 \left(\left(H^2 k^2 + 3\right) U + \sqrt{3}\right) \sqrt{g H \left(H^2 k^2 + 3\right)}}{\left(H^4 U k^4 + 3 \left(2 U H^2 + \sqrt{3}\right) \sqrt{g H^5 \left(H^2 k^2 + 3\right)}\right) k^2 + 9 \left(U + \sqrt{3}\right) \sqrt{g H \left(H^2 k^2 + 3\right)}}\right)$$

[illegible]

$$\begin{aligned} & H^4 U^5 + 16 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} U^4 + 48 \sqrt{g^5 H^{13} \left(H^2 k^2 + 3 \right)} \right) \\ & k^4 + 9 \left(-9 \sqrt{3} H^2 U^5 + 48 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} U^4 + 760 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} U^2 + 400 \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) \\ & k^2 - 81 \sqrt{3} U^5 + 432 \sqrt{g H \left(H^2 k^2 + 3 \right)} U^4 + 7344 \sqrt{g^5 H^5 \left(H^2 k^2 + 3 \right)} \right) \right) \text{ \texttt{dt}}^4 \{ 96 \\ & \left(\sqrt{g H} \left(H^2 k^2 + 3 \right)^{7/2} \right) + O \left(\text{ \texttt{dt}}^5 \right) \right) \text{ \texttt{dx}}^2 + \left(\frac{i}{k^4 \left(3 \sqrt{3} \left(H^2 k^2 + 3 \right) U^3 + 4 g H \left(\left(\sqrt{3} U H^2 + 4 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) \right) \right) \right.} \right. \\ & k^2 + 6 \sqrt{3} U + 12 \sqrt{g H \left(H^2 k^2 + 3 \right)} \left. \right) \} 384 g H \left(H^2 k^2 + 3 \right)^{3/2} - \frac{\left(k^5 \left(3 \sqrt{3} \left(H^2 k^2 + 3 \right) U^4 + 2 g H \left(\left(7 \sqrt{3} U H^4 + 24 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) \right) \right. \right.} \\ & k^4 + 24 \left(2 \sqrt{3} U H^2 + 7 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) \left. \right) \right) k^2 + 81 \left(\sqrt{3} U + 4 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \\ & U + 8 \sqrt{3} g^2 H^2 \left(5 H^4 k^4 + 33 H^2 k^2 + 54 \right) \right) \text{ \texttt{dt}} \} \{ 384 \left(g H \left(H^2 k^2 + 3 \right)^{5/2} \right) - \frac{i}{k^6 \left(\left(168 \sqrt{3} g^2 U H^6 + 8 g U^2 \left(3 \sqrt{3} U + 10 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right.} \right. \\ & H^5 + 3 \sqrt{3} U^5 H^4 + 16 \sqrt{g^5 H^{13} \left(H^2 k^2 + 3 \right)} \left. \right) \right) k^4 + 3 \left(6 \sqrt{3} H^2 U^5 + 51 \sqrt{3} g H^3 U^3 + 224 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} U^2 + 380 \sqrt{3} g^2 H^4 U + 96 \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) \\ & k^2 + 9 \left(3 \sqrt{3} U^5 + g H \left(27 \sqrt{3} U + 160 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \\ & U^2 + 224 \sqrt{3} g^2 H^2 U + 96 \sqrt{g^5 H^5 \left(H^2 k^2 + 3 \right)} \left. \right) \text{ \texttt{dt}}^2 \} 384 g \\ & H \left(H^2 k^2 + 3 \right)^{5/2} + \frac{k^7 \left(\left(H^2 k^2 + 3 \right) U + \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \left(\left(272 \sqrt{3} g^2 U H^6 + 2 g U^2 \left(17 \sqrt{3} U + 56 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right. \right.} \\ & H^5 + 3 \sqrt{3} U^5 H^4 + 48 \sqrt{g^5 H^{13} \left(H^2 k^2 + 3 \right)} \left. \right) \right) k^4 + 3 \left(6 \sqrt{3} H^2 U^5 - 3 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} U^4 + 72 \sqrt{3} g H^3 U^3 + 334 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} U^2 + 608 \sqrt{3} g^2 H^4 U + 184 \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) \\ & k^2 + 9 \left(3 \sqrt{3} U^5 - 3 \sqrt{g H \left(H^2 k^2 + 3 \right)} U^4 + 2 g H \left(19 \sqrt{3} U + 121 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \\ & U^2 + 352 \sqrt{3} g^2 H^2 U + 160 \sqrt{g^5 H^5 \left(H^2 k^2 + 3 \right)} \left. \right) \text{ \texttt{dt}}^3 \} \{ 384 g H \left(H^2 k^2 + 3 \right)^{7/2} + \frac{i}{k^8 \left(\left(H^2 k^2 + 3 \right) U + \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \left(\left(400 \sqrt{3} g^2 U H^6 + 4 g U^2 \left(11 \sqrt{3} U + 36 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right.} \right.} \\ & H^5 + 3 \sqrt{3} U^5 H^4 + 96 \sqrt{g^5 H^{13} \left(H^2 k^2 + 3 \right)} \left. \right) \right) k^4 + 3 \left(6 \sqrt{3} H^2 U^5 - 6 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} U^4 + 95 \sqrt{3} g H^3 U^3 + 456 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} U^2 + 884 \sqrt{3} g^2 H^4 U + 304 \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) \\ & k^2 + 27 \left(\sqrt{3} U^5 - 2 \sqrt{g H \left(H^2 k^2 + 3 \right)} U^4 + g H \left(17 \sqrt{3} U + 112 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \\ & U^2 + 168 \sqrt{3} g^2 H^2 U + 80 \sqrt{g^5 H^5 \left(H^2 k^2 + 3 \right)} \left. \right) \text{ \texttt{dt}}^4 \} 384 g H \\ & \left(H^2 k^2 + 3 \right)^{9/2} + O \left(\text{ \texttt{dt}}^5 \right) \right) \text{ \texttt{dx}}^3 + \left(\frac{k^5 \left(\left(-75 \sqrt{3} \left(\left(H^2 k^2 + 3 \right)^2 U^4 + 8 g H \left(H^2 k^2 + 3 \right) \left(\left(5 \sqrt{3} U H^2 + 32 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) \right) \right. \right. \right. \right.} \right. \\ & k^2 + 96 \sqrt{g H \left(H^2 k^2 + 3 \right)} \left. \right) U + 16 \sqrt{3} g^2 H^2 \left(5 H^4 k^4 + 48 H^2 k^2 + 144 \right) \left. \right) \} \{ 30720 \left(g H \right)^{3/2} \left(H^2 k^2 + 3 \right)^{5/2} + \frac{i}{k^6 \left(\left(4368 \sqrt{3} g^2 U H^8 + 2048 g \sqrt{g H \left(H^2 k^2 + 3 \right)} U^2 H^7 - 225 \sqrt{3} U^5 H^6 + 1920 \sqrt{g^5 H^{17} \left(H^2 k^2 + 3 \right)} \right) \right) \right.} \\ & k^6 + 3 \left(14512 \sqrt{3} g^2 U H^6 + 24 g U^2 \left(256 \sqrt{g H \left(H^2 k^2 + 3 \right)} - 5 \sqrt{3} U \right) H^5 - 675 \sqrt{3} U^5 H^4 + 6720 \sqrt{g^5 H^{13} \left(H^2 k^2 + 3 \right)} \right) \\ & k^4 + 9 \left(-675 \sqrt{3} H^2 U^5 - 240 \sqrt{3} g H^3 U^3 + 6144 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} U^2 + 16160 \sqrt{3} g^2 H^4 U + 8448 \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) \\ & k^2 + 27 \left(-225 \sqrt{3} U^5 + 8 g H \left(256 \sqrt{g H \left(H^2 k^2 + 3 \right)} - 15 \sqrt{3} U \right) U^2 + 6016 \sqrt{3} g^2 H^2 U + 3968 \sqrt{g^5 H^5 \left(H^2 k^2 + 3 \right)} \right) \end{aligned}$$

$$\begin{aligned}
& k^2+3\right)\right)\right) \text{ \texttt{dt}}\}\{92160 (g H)^{3/2} \left(H^2 k^2+3\right)^{7/2}\}-\frac{\left(k^7\right. \\
& \left.\left(48 \sqrt{3} g^3 \left(140 H^6 k^6+1425 H^4 k^4+5004 H^2 k^2+6192\right) H^3+8 \sqrt{3} g^2\right. \right. \\
& \left.\left(1772 H^6 k^6+17121 H^4 k^4+55557 H^2 k^2+60426\right) U^2 H^2+g U^3 \left(8 \left(416\right. \right. \right. \\
& \left.\left.\sqrt{3} g H^{13} \left(H^2 k^2+3\right)\right)\right)-15 \sqrt{3} H^6 U\right) k^6+9 \left(3328 \sqrt{3} g H^9 \left(H^2\right. \right. \\
& \left.\left.k^2+3\right)\right)\right)-145 \sqrt{3} H^4 U\right) k^4-4590 \sqrt{3} H^2 U k^2-5265 \sqrt{3} U+89856 \sqrt{3} g \\
& H \left(H^2 k^2+3\right)\right)\right) H+3 U \left(5 \left(512 \sqrt{3} g^5 H^{17} \left(H^2 k^2+3\right)\right)\right)-15 \\
& \sqrt{3} H^6 U^5\right) k^6+3 \left(11776 \sqrt{3} g^5 H^{13} \left(H^2 k^2+3\right)\right)\right)-225 \sqrt{3} \\
& H^4 U^5\right) k^4+3 \left(-675 \sqrt{3} H^2 U^5+9984 \sqrt{3} g^3 H^7 \left(H^2 k^2+3\right)\right)\right) \\
& U^2+52352 \sqrt{3} g^5 H^9 \left(H^2 k^2+3\right)\right)\right) k^2+81 \left(2816 \sqrt{3} g^5 H^5 \left(H^2\right. \right. \\
& \left.\left.k^2+3\right)\right)\right)-25 \sqrt{3} U^5\right)\right)\right) \text{ \texttt{dt}}^2\}\{92160 \left((g H)^{3/2} \left(H^2\right. \right. \\
& \left.\left.k^2+3\right)\right)^{7/2}\right)\right)-\frac{i k^8 \left(\left(11520 \sqrt{3} g^3 U H^{11}+9888 \sqrt{3} g^2 U^3\right. \right. \\
& \left.\left.H^{10}+16 g U^4 \left(96 \sqrt{3} g H \left(H^2 k^2+3\right)\right)\right)-5 \sqrt{3} U\right) H^9-75 \sqrt{3} \\
& U^7 H^8+5760 \sqrt{3} g^5 H^{21} \left(H^2 k^2+3\right)\right) U^2+480 \sqrt{3} g^7 H^{23} \left(H^2\right. \\
& \left.\left.k^2+3\right)\right)\right)\right) k^8+3 \left(55216 \sqrt{3} g^3 U H^9+41728 \sqrt{3} g^2 U^3 H^8+3 g U^4\right. \\
& \left.\left(2048 \sqrt{3} g H \left(H^2 k^2+3\right)\right)\right)-105 \sqrt{3} U\right) H^7-300 \sqrt{3} U^7 H^6+39488 \\
& \sqrt{3} g^5 H^{17} \left(H^2 k^2+3\right)\right) U^2+6720 \sqrt{3} g^7 H^{19} \left(H^2 k^2+3\right)\right)\right) k^6+9 \\
& \left(99856 \sqrt{3} g^3 U H^7+66296 \sqrt{3} g^2 U^3 H^6+3 g U^4 \left(3072 \sqrt{3} g H \left(H^2\right. \right. \right. \\
& \left.\left.\left.k^2+3\right)\right)\right)\right)-155 \sqrt{3} U\right) H^5-450 \sqrt{3} U^7 H^4+88512 \sqrt{3} g^5 H^{13} \left(H^2\right. \\
& \left.\left.k^2+3\right)\right)\right) U^2+19040 \sqrt{3} g^7 H^{15} \left(H^2 k^2+3\right)\right)\right) k^4+27 \left(-300 \sqrt{3} \\
& H^2 U^7-305 \sqrt{3} g H^3 U^5+6144 \sqrt{3} g^3 H^7 \left(H^2 k^2+3\right)\right) U^4+46960 \sqrt{3} g^2 \\
& H^4 U^3+82240 \sqrt{3} g^5 H^9 \left(H^2 k^2+3\right)\right) U^2+80544 \sqrt{3} g^3 H^5 U+20416 \sqrt{3} g^7 \\
& H^{11} \left(H^2 k^2+3\right)\right)\right) k^2+243 \left(-25 \sqrt{3} U^7+g H \left(512 \sqrt{3} g H \left(H^2\right. \right. \right. \\
& \left.\left.\left.k^2+3\right)\right)\right)\right)-25 \sqrt{3} U\right) U^4+4168 \sqrt{3} g^2 H^2 U^3+9152 \sqrt{3} g^5 H^5 \left(H^2\right. \\
& \left.\left.k^2+3\right)\right)\right) U^2+8128 \sqrt{3} g^3 H^3 U+2592 \sqrt{3} g^7 H^7 \left(H^2 k^2+3\right)\right)\right)\right) \\
& \text{ \texttt{dt}}^3\}\{30720 (g H)^{3/2} \left(H^2 k^2+3\right)^{9/2}\}+\frac{k^9 \left(2 g H \left(4 \left(736 \sqrt{3} g\right. \right. \right. \\
& \left.\left.\left.H^{17} \left(H^2 k^2+3\right)\right)\right)\right)-45 \sqrt{3} H^8 U\right) k^8+3 \left(11776 \sqrt{3} g H^{13} \left(H^2\right. \right. \\
& \left.\left.k^2+3\right)\right)\right)-645 \sqrt{3} H^6 U\right) k^6+27 \left(5888 \sqrt{3} g H^9 \left(H^2 k^2+3\right)\right)\right)-285 \\
& \sqrt{3} H^4 U\right) k^4-13365 \sqrt{3} H^2 U k^2-8505 \sqrt{3} U+238464 \sqrt{3} g H \left(H^2\right. \\
& \left.\left.k^2+3\right)\right)\right) U^5+3 \sqrt{3} g^2 H^2 \left(H^2 k^2+3\right)^2 \left(16944 H^4 k^4+114352\right. \\
& \left.\left.H^2 k^2+197625\right) U^4+24 \sqrt{3} g^3 H^3 \left(4080 H^8 k^8+64744 H^6 k^6+376029 H^4\right. \right. \\
& \left.\left.k^4+953451 H^2 k^2+893700\right) U^2+3 \left(5 \left(-15 \sqrt{3} U^7 H^8+2048 \sqrt{3} g^5 H^{21}\right. \right. \right. \\
& \left.\left.\left(H^2 k^2+3\right)\right)\right) U^2+384 \sqrt{3} g^7 H^{23} \left(H^2 k^2+3\right)\right)\right) k^8+12 \left(-75\right. \\
& \left.\sqrt{3} H^6 U^7+20864 \sqrt{3} g^5 H^{17} \left(H^2 k^2+3\right)\right) U^2+9600 \sqrt{3} g^7 H^{19} \left(H^2\right. \\
& \left.\left.k^2+3\right)\right)\right) k^6+18 \left(-225 \sqrt{3} H^4 U^7+100096 \sqrt{3} g^5 H^{13} \left(H^2 k^2+3\right)\right)\right) \\
& U^2+60608 \sqrt{3} g^7 H^{15} \left(H^2 k^2+3\right)\right)\right) k^4+36 \left(-225 \sqrt{3} H^2 U^7+5888\right. \\
& \left.\sqrt{3} g^3 H^7 \left(H^2 k^2+3\right)\right) U^4+144512 \sqrt{3} g^5 H^9 \left(H^2 k^2+3\right)\right) U^2+105472 \\
& \sqrt{3} g^7 H^{11} \left(H^2 k^2+3\right)\right)\right) k^2+135 \left(-45 \sqrt{3} U^7+39424 \sqrt{3} g^5\right. \\
& \left.\left.H^5 \left(H^2 k^2+3\right)\right) U^2+33920 \sqrt{3} g^7 H^7 \left(H^2 k^2+3\right)\right)\right)\right) U+144 \\
& \sqrt{3} g^4 H^4 \left(40 H^8 k^8+1000 H^6 k^6+7395 H^4 k^4+22104 H^2 k^2+23832\right) \right)\right) \\
& \text{ \texttt{dt}}^4\}\{92160 (g H)^{3/2} \left(H^2 k^2+3\right)^{9/2}\}+O\left(\text{ \texttt{dt}}^5\right)\right) \\
& \text{ \texttt{dx}}^4+O\left(\text{ \texttt{dx}}^5\right), \left(\frac{i \left(H^2 U k^3+3 U k-\sqrt{3}\right) \sqrt{3} g H \left(H^2\right. \right. \\
& \left.\left.k^2+3\right)\right) k\right)^2 \text{ \texttt{dt}}\}\{2 \left(H^2 k^2+3\right)^2-\frac{\left(k^3 \left(H^2 k^2+3\right)\right. \right. \\
& \left.\left.U-\sqrt{3}\right) \sqrt{3} g H \left(H^2 k^2+3\right)\right) \left(3 g H+U \left(H^2 k^2+3\right) U-2 \sqrt{3}\right)\}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right) \text{dt}^2 \{ 3 \left(H^2 k^2 + 3 \right)^2 - \frac{i}{k^4} \left(\left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \left(\left(H^4 U \right. \right. \\
& k^4 - 3 \left. \left(\sqrt{3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} - 2 H^2 U \right) k^2 + 9 U - 9 \sqrt{3} \sqrt{g H} \\
& \left. \left(H^2 k^2 + 3 \right) \right) \right) U^2 + 3 g H \left(3 \left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H \left(H^2 \right.} \\
& k^2 + 3 \left. \right) \right) \text{dt}^3 \{ 4 \left(H^2 k^2 + 3 \right)^3 + \frac{k^5}{\left(H^2 k^2 + 3 \right)} U - \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \left(\left(H^4 U \right. \right. \\
& k^4 + \left. \left(6 H^2 U - 4 \sqrt{3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 U - 12 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \\
& U^3 + 6 g H \left(3 \left(H^2 k^2 + 3 \right) U - 2 \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U + 9 g^2 \\
& H^2 \text{dt}^4 \{ 5 \left(H^2 k^2 + 3 \right)^3 + O \left(\text{dt}^5 \right) \right) + \left(- \frac{1}{4} \right) i k^2 \left(2 \sqrt{g H} - \frac{\sqrt{3}}{\sqrt{3}} U \right) \sqrt{H^2 k^2 + 3} \right) + \frac{k^3}{\left(2 \sqrt{g H} \right.} \\
& \left. \left(H^2 k^2 + 3 \right) - \sqrt{3} U \right) \left(\left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H \left(H^2 \right.} \\
& k^2 + 3 \left. \right) \right) \text{dt} \{ 4 \left(H^2 k^2 + 3 \right)^{3/2} + \frac{i}{\sqrt{3}} k^4 \left(2 \sqrt{g H \left(H^2 \right.} \right. \\
& k^2 + 3 \left. \right) - \sqrt{3} U \right) \left(3 g H + U \left(\left(H^2 k^2 + 3 \right) U - 2 \sqrt{3} \right) \sqrt{g H} \right. \\
& \left. \left(H^2 k^2 + 3 \right) \right) \right) \text{dt}^2 \{ 4 \left(H^2 k^2 + 3 \right)^{3/2} - \frac{\left(k^5 \right.} \\
& \left. \left(2 \sqrt{g H \left(H^2 k^2 + 3 \right)} - \sqrt{3} U \right) \left(\left(H^4 U \right. \right. \right. \\
& k^4 - 3 \left. \left(\sqrt{3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} - 2 H^2 U \right) k^2 + 9 U - 9 \sqrt{3} \sqrt{g H \left(H^2 \right.} \\
& k^2 + 3 \left. \right) \right) U^2 + 3 g H \left(3 \left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H \left(H^2 \right.} \\
& k^2 + 3 \left. \right) \right) \text{dt}^3 \{ 4 \left(H^2 k^2 + 3 \right)^{5/2} - \frac{i}{\sqrt{3}} k^6 \left(2 \sqrt{g H \left(H^2 k^2 + 3 \right)} - \sqrt{3} U \right) \left(\left(H^4 U \right. \right. \\
& k^4 + \left. \left(6 H^2 U - 4 \sqrt{3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 U - 12 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^3 + 6 g H \\
& \left(3 \left(H^2 k^2 + 3 \right) U - 2 \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U + 9 g^2 H^2 \text{dt}^4 \{ 4 \left(H^2 k^2 + 3 \right)^{5/2} + O \left(\text{dt}^5 \right) \} \\
& \text{dx} + \left(\frac{k^3}{\left(12 \sqrt{3} \right) g H \left(H^2 k^2 + 4 \right) - U \left(\left(3 \sqrt{3} \right) U H^2 + 16 \sqrt{g H^5 \left(H^2 \right.} \right.} \right. \\
& k^2 + 3 \left. \right) \right) k^2 + 9 \sqrt{3} U + 48 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \{ 96 \sqrt{g H} \\
& \left(H^2 k^2 + 3 \right)^{3/2} - \frac{i}{\sqrt{3}} k^4 \left(U^2 \left(3 \sqrt{3} \right) U H^4 + 16 \sqrt{g H^9 \left(H^2 \right.} \right. \\
& k^2 + 3 \left. \right) \right) k^4 + 6 \left(3 \sqrt{3} \right) H^2 U^3 + 16 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^2 + 18 \\
& \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 U^2 \left(3 \sqrt{3} \right) U + 16 \sqrt{g H \left(H^2 \right.} \\
& k^2 + 3 \left. \right) \right) + 4 g H \left(\left(3 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} - 10 \sqrt{3} \right) H^4 U \right) \\
& k^4 - 63 \sqrt{3} H^2 U k^2 - 99 \sqrt{3} U + 63 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \text{dt} \{ 96 \\
& \sqrt{g H} \left(H^2 k^2 + 3 \right)^{5/2} + \frac{k^5}{\left(U^3 \left(3 \sqrt{3} \right) U H^4 + 16 \sqrt{g H^9 \right.} \right.} \\
& \left. \left(H^2 k^2 + 3 \right) \right) \right) k^4 + 6 \left(3 \sqrt{3} \right) H^2 U^4 + 16 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) \\
& U^3 + 56 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) U \right) k^2 - 12 \sqrt{3} g^2 H^2 \left(2 H^4 k^4 + 15 \right. \\
& H^2 k^2 + 30 \left. \right) + 9 U^3 \left(3 \sqrt{3} \right) U + 16 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) + g H U \\
& \left(4 \left(6 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} - 17 \sqrt{3} \right) H^4 U \right) k^4 - 429 \sqrt{3} H^2 \\
& U k^2 - 675 \sqrt{3} U + 864 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \text{dt}^2 \{ 96 \sqrt{g H} \\
& \left(H^2 k^2 + 3 \right)^{5/2} + \frac{i}{\sqrt{3}} k^6 \left(- U \left(72 \sqrt{3} \right) g^2 H^8 + 12 g U \left(8 \sqrt{3} \right) U - 3 \right. \\
& \left. \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) H^7 - U^3 \left(3 \sqrt{3} \right) U H^6 + 16 \sqrt{g H^{13} \left(H^2 \right.} \right. \\
& k^2 + 3 \left. \right) \right) k^6 + 3 \left(- 304 \sqrt{3} \right) g^2 U H^6 + g U^2 \left(264 \sqrt{g H \left(H^2 \right.} \right. \\
& k^2 + 3 \left. \right) \right) - 301 \sqrt{3} U \right) H^5 + 9 \sqrt{3} U^5 H^4 + 48 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \\
& U^4 + 36 \sqrt{g^5 H^{13} \left(H^2 k^2 + 3 \right)} \right) k^4 + 9 \left(9 \sqrt{3} \right) H^2 U^5 + 48 \sqrt{g} \\
& H^5 \left(H^2 k^2 + 3 \right) U^4 - 314 \sqrt{3} g H^3 U^3 + 438 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \\
& U^2 - 404 \sqrt{3} g^2 H^4 U + 84 \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) k^2 + 27 \left(3 \sqrt{3} \right) \\
& U^5 + 16 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^4 + g H \left(210 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) - 109
\end{aligned}$$

$$\begin{aligned}
& \sqrt{3} \, U \right) U^{2-1/2} \sqrt{3} \, g^2 H^2 U + 52 \sqrt{3} g^5 H^5 \left(H^2 k^2 + 3 \right) \right) \right) \right) \\
& \text{dt}^3 \{ 96 \sqrt{3} g H \left(H^2 k^2 + 3 \right)^{7/2} \} + \frac{k^7 \left(36 \sqrt{3} g^3 \left(4 H^4 k^4 + 27 \right. \right. \\
& H^2 k^2 + 48 \right) H^3 + 3 \sqrt{3} g^2 \left(48 H^6 k^6 + 712 H^4 k^4 + 3075 H^2 k^2 + 4113 \right) \\
& U^2 H^2 + 2 g U^3 \left(2 \left(31 \sqrt{3} H^6 U - 12 \sqrt{3} g H^3 \left(H^2 k^2 + 3 \right) \right) \right) \\
& k^6 + 3 \left(197 \sqrt{3} H^4 U - 216 \sqrt{3} g H^9 \left(H^2 k^2 + 3 \right) \right) \right) k^4 + 1872 \sqrt{3} \\
& H^2 U k^2 + 1971 \sqrt{3} U - 5076 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) \right) H - U \left(U^4 \left(3 \right. \right. \\
& \sqrt{3} U H^6 + 16 \sqrt{3} g H^3 \left(H^2 k^2 + 3 \right) \right) \right) k^6 + 9 \left(3 \sqrt{3} H^4 U^5 + 16 \right. \\
& \sqrt{3} g H^9 \left(H^2 k^2 + 3 \right) \right) U^4 + 48 \sqrt{3} g^5 H^3 \left(H^2 k^2 + 3 \right) \right) \right) k^4 + 9 \\
& \left(9 \sqrt{3} H^2 U^5 + 48 \sqrt{3} g H^5 \left(H^2 k^2 + 3 \right) \right) U^4 + 760 \sqrt{3} g^3 H^7 \left(H^2 \right. \\
& k^2 + 3 \right) \right) U^2 + 400 \sqrt{3} g^5 H^9 \left(H^2 k^2 + 3 \right) \right) \right) k^2 + 81 \sqrt{3} U^5 + 432 \sqrt{3} g \\
& H \left(H^2 k^2 + 3 \right) \right) U^4 + 7344 \sqrt{3} g^5 H^5 \left(H^2 k^2 + 3 \right) \right) \right) \text{dt}^4 \{ 96 \\
& \sqrt{3} g H \left(H^2 k^2 + 3 \right)^{7/2} \} + O \left(\text{dt}^5 \right) \right) \text{dx}^2 + \left(-\frac{i k^4}{\left(3 \sqrt{3} \right. \right. \\
& \left. \left. \left(H^2 k^2 + 3 \right) U^3 + 4 g H \left(\left(\sqrt{3} H^2 U - 4 \sqrt{3} g H^5 \left(H^2 \right. \right. \right. \right. \right. \right. \right. \\
& k^2 + 3 \right) \right) \right) k^2 + 6 \sqrt{3} U - 12 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) \right) \right) \{ 384 g H \left(H^2 \right. \\
& k^2 + 3 \right)^{3/2} \} + \frac{k^5 \left(3 \sqrt{3} \left(H^2 k^2 + 3 \right)^2 U^4 - 2 g H \left(24 \sqrt{3} g \right. \right. \\
& H^9 \left(H^2 k^2 + 3 \right) \right) - 7 \sqrt{3} H^4 U \right) k^4 + 24 \left(7 \sqrt{3} g H^5 \left(H^2 k^2 + 3 \right) \right) - 2 \\
& \sqrt{3} H^2 U \right) k^2 - 81 \sqrt{3} U + 324 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) \right) U + 8 \sqrt{3} g^2 \\
& H^2 \left(5 H^4 k^4 + 33 H^2 k^2 + 54 \right) \right) \text{dt} \{ 384 g H \left(H^2 k^2 + 3 \right)^{5/2} \} - \frac{i}{\left(k^6 \left(\left(-168 \sqrt{3} \right. \right. \right. \\
& g^2 U H^6 + 8 g U^2 \left(10 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) - 3 \sqrt{3} U \right) H^5 - 3 \sqrt{3} U^5 H^4 + 16 \sqrt{3} g^5 H^3 \left(H^2 k^2 + 3 \right) \right) \right) \right) k^4 + 3 \left(-6 \right. \\
& \sqrt{3} H^2 U^5 - 51 \sqrt{3} g H^3 U^3 + 224 \sqrt{3} g^3 H^7 \left(H^2 k^2 + 3 \right) \right) U^2 - 380 \sqrt{3} \\
& g^2 H^4 U + 96 \sqrt{3} g^5 H^9 \left(H^2 k^2 + 3 \right) \right) \right) k^2 + 9 \left(-3 \sqrt{3} U^5 + g H \left(160 \right. \right. \\
& \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) - 27 \sqrt{3} U \right) U^2 - 224 \sqrt{3} g^2 H^2 U + 96 \sqrt{3} g^5 H^5 \\
& \left(H^2 k^2 + 3 \right) \right) \right) \text{dt}^2 \{ 384 g H \left(H^2 k^2 + 3 \right)^{5/2} \} - \frac{\left(k^7 \left(\left(H^2 k^2 + 3 \right) U - \sqrt{3} \right. \right. \\
& \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) \right) \left(-\left(-272 \sqrt{3} \right. \right. \\
& g^2 U H^6 + 2 g U^2 \left(56 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) - 17 \sqrt{3} U \right) H^5 - 3 \sqrt{3} U^5 \\
& H^4 + 48 \sqrt{3} g^5 H^3 \left(H^2 k^2 + 3 \right) \right) \right) k^4 - 3 \left(-6 \sqrt{3} H^2 U^5 - 3 \sqrt{3} g H^5 \\
& \left(H^2 k^2 + 3 \right) \right) U^4 - 72 \sqrt{3} g H^3 U^3 + 334 \sqrt{3} g^3 H^7 \left(H^2 k^2 + 3 \right) \right) U^2 - 608 \\
& \sqrt{3} g^2 H^4 U + 184 \sqrt{3} g^5 H^9 \left(H^2 k^2 + 3 \right) \right) \right) k^2 - 9 \left(-3 \sqrt{3} U^5 - 3 \right. \\
& \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) U^4 + 2 g H \left(121 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) - 19 \sqrt{3} \\
& U \right) U^2 - 352 \sqrt{3} g^2 H^2 U + 160 \sqrt{3} g^5 H^5 \left(H^2 k^2 + 3 \right) \right) \right) \right) \text{dt}^3 \{ 384 \left(g H \left(H^2 k^2 + 3 \right)^{7/2} \right) - \frac{i k^8 \left(\sqrt{3} \sqrt{3} g H \left(H^2 \right. \right. \\
& k^2 + 3 \right) \right) - \left(H^2 k^2 + 3 \right) U \right) \right)^2 \left(-\left(-400 \sqrt{3} \right. \right. \\
& g^2 U H^6 + 4 g U^2 \left(36 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) - 11 \sqrt{3} U \right) H^5 - 3 \sqrt{3} U^5 H^4 + 96 \sqrt{3} g^5 H^3 \left(H^2 k^2 + 3 \right) \right) \right) \\
& k^4 - 3 \left(-6 \sqrt{3} H^2 U^5 - 6 \sqrt{3} g H^5 \left(H^2 k^2 + 3 \right) \right) \\
& U^4 - 95 \sqrt{3} g H^3 U^3 + 456 \sqrt{3} g^3 H^7 \left(H^2 k^2 + 3 \right) \right) U^2 - 884 \sqrt{3} g^2 H^4 \\
& U + 304 \sqrt{3} g^5 H^9 \left(H^2 k^2 + 3 \right) \right) \right) k^2 - 27 \left(-\sqrt{3} U^5 - 2 \sqrt{3} g H \left(H^2 \right. \right. \\
& k^2 + 3 \right) \right) U^4 + g H \left(112 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) - 17 \sqrt{3} U \right) U^2 - 168 \\
& \sqrt{3} g^2 H^2 U + 80 \sqrt{3} g^5 H^5 \left(H^2 k^2 + 3 \right) \right) \right) \text{dt}^4 \{ 384 g H \left(H^2 \right. \\
& k^2 + 3 \right)^{9/2} \} + O \left(\text{dt}^5 \right) \right) \text{dx}^3 + \left(\frac{k^5 \left(75 \sqrt{3} \left(H^2 \right. \right. \right. \\
& k^2 + 3 \right)^2 U^4 + 8 g H \left(H^2 k^2 + 3 \right) \left(\left(32 \sqrt{3} g H^5 \left(H^2 k^2 + 3 \right) \right) - 5 \right. \\
& \sqrt{3} H^2 U \right) k^2 + 96 \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) \right) U - 16 \sqrt{3} g^2 H^2 \left(5 \right. \\
& H^4 k^4 + 48 H^2 k^2 + 144 \right) \right) \right) \{ 30720 (g H)^{3/2} \left(H^2 k^2 + 3 \right)^{5/2} \} + \frac{i k^6}{\left(\left(-4368 \sqrt{3} \right. \right. \\
& g^2 U H^8 + 2048 g \sqrt{3} g H \left(H^2 k^2 + 3 \right) \right) U^2 H^7 + 225 \sqrt{3} \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\left(\left(-4508 \sqrt{3} \right) g^2 U H^6 + 2048 g^2 \sqrt{3} H^6 \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 H^7 + 225 \sqrt{3} U^5 H^6 + 1920 \sqrt{3} g^5 H^{17} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^6 + 3 \left(-14512 \sqrt{3} g^2 U H^6 + 24 g U^2 \left(5 \sqrt{3} U + 256 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) H^5 + 675 \sqrt{3} U^5 H^4 + 6720 \sqrt{3} g^5 H^{13} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^4 + 9 \left(675 \sqrt{3} H^2 U^5 + 240 \sqrt{3} g H^3 U^3 + 6144 \sqrt{3} g^3 H^7 \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 - 16160 \sqrt{3} g^2 H^4 U + 8448 \sqrt{3} g^5 H^9 \left(\left(H^2 k^2 + 3 \right) \right) k^2 + 27 \left(225 \sqrt{3} U^5 + 8 g H \left(15 \sqrt{3} U + 256 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 - 6016 \sqrt{3} g^2 H^2 U + 3968 \sqrt{3} g^5 H^5 \left(\left(H^2 k^2 + 3 \right) \right) \right) \right) \text{dt} \} \{ 92160 (g H)^{3/2} \left(\left(H^2 k^2 + 3 \right) \right)^{7/2} \} - \frac{\left(k^7 \left(-48 \sqrt{3} g^3 \left(140 H^6 k^6 + 1425 H^4 k^4 + 5004 H^2 k^2 + 6192 \right) H^3 - 8 \sqrt{3} g^2 \left(1772 H^6 k^6 + 17121 H^4 k^4 + 55557 H^2 k^2 + 60426 \right) U^2 H^2 + g U^3 \left(8 \left(15 \sqrt{3} U + H^6 + 416 \sqrt{3} g H^{13} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^6 + 9 \left(145 \sqrt{3} U H^4 + 3328 \sqrt{3} g H^9 \left(\left(H^2 k^2 + 3 \right) \right) \right) k^4 + 4590 \sqrt{3} H^2 U k^2 + 5265 \sqrt{3} U + 89856 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) H + 3 U \left(5 \left(15 \sqrt{3} U^5 H^6 + 512 \sqrt{3} g^5 H^{17} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^6 + 3 \left(225 \sqrt{3} H^4 U^5 + 11776 \sqrt{3} g^5 H^{13} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^4 + 3 \left(675 \sqrt{3} H^2 U^5 + 9984 \sqrt{3} g^3 H^7 \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 + 52352 \sqrt{3} g^5 H^9 \left(\left(H^2 k^2 + 3 \right) \right) \right) k^2 + 81 \left(25 \sqrt{3} U^5 + 2816 \sqrt{3} g^5 H^5 \left(\left(H^2 k^2 + 3 \right) \right) \right) \right) \right) \text{dt}^2 \} \{ 92160 \left((g H)^{3/2} \left(\left(H^2 k^2 + 3 \right) \right)^{7/2} \right) \} - \frac{i k^8 \left(\left(-11520 \sqrt{3} g^3 U H^{11} - 9888 \sqrt{3} g^2 U^3 H^{10} + 16 g U^4 \left(5 \sqrt{3} U + 96 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) H^9 + 75 \sqrt{3} U^7 H^8 + 5760 \sqrt{3} g^5 H^{21} \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 + 480 \sqrt{3} g^7 H^{23} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^8 + 3 \left(-55216 \sqrt{3} g^3 U H^9 - 41728 \sqrt{3} g^2 U^3 H^8 + 3 g U^4 \left(105 \sqrt{3} U + 2048 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) H^7 + 300 \sqrt{3} U^7 H^6 + 39488 \sqrt{3} g^5 H^{17} \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 + 6720 \sqrt{3} g^7 H^{19} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^6 + 9 \left(-99856 \sqrt{3} g^3 U H^7 - 66296 \sqrt{3} g^2 U^3 H^6 + 3 g U^4 \left(155 \sqrt{3} U + 3072 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) H^5 + 450 \sqrt{3} U^7 H^4 + 88512 \sqrt{3} g^5 H^{13} \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 + 19040 \sqrt{3} g^7 H^{15} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^4 + 27 \left(300 \sqrt{3} H^2 U^7 + 305 \sqrt{3} g H^3 U^5 + 6144 \sqrt{3} g^3 H^7 \left(\left(H^2 k^2 + 3 \right) \right) \right) U^4 - 46960 \sqrt{3} g^2 H^4 U^3 + 82240 \sqrt{3} g^5 H^9 \left(\left(H^2 k^2 + 3 \right) \right) U^2 - 80544 \sqrt{3} g^3 H^5 U + 20416 \sqrt{3} g^7 H^{11} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^2 + 243 \left(25 \sqrt{3} U^7 + g H \left(25 \sqrt{3} U + 512 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) U^4 - 4168 \sqrt{3} g^2 H^2 U^3 + 9152 \sqrt{3} g^5 H^5 \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 - 8128 \sqrt{3} g^3 H^3 U + 2592 \sqrt{3} g^7 H^7 \left(\left(H^2 k^2 + 3 \right) \right) \right) \text{dt}^3 \} \{ 30720 (g H)^{3/2} \left(\left(H^2 k^2 + 3 \right) \right)^{9/2} \} + \frac{k^9 \left(2 g H \left(4 \left(45 \sqrt{3} U H^8 + 736 \sqrt{3} g H^{17} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^8 + 3 \left(645 \sqrt{3} U H^6 + 11776 \sqrt{3} g H^{13} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^6 + 27 \left(285 \sqrt{3} U H^4 + 5888 \sqrt{3} g H^9 \left(\left(H^2 k^2 + 3 \right) \right) \right) k^4 + 13365 \sqrt{3} H^2 U k^2 + 8505 \sqrt{3} U + 238464 \sqrt{3} g H \left(\left(H^2 k^2 + 3 \right) \right) \right) U^5 - 3 \sqrt{3} g^2 H^2 \left(\left(H^2 k^2 + 3 \right) \right)^2 \left(16944 H^4 k^4 + 114352 H^2 k^2 + 197625 \right) U^4 - 24 \sqrt{3} g^3 H^3 \left(4080 H^8 k^8 + 64744 H^6 k^6 + 376029 H^4 k^4 + 953451 H^2 k^2 + 893700 \right) U^2 + 3 \left(5 \left(15 \sqrt{3} U^7 H^8 + 2048 \sqrt{3} g^5 H^{21} \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 + 384 \sqrt{3} g^7 H^{23} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^8 + 12 \left(75 \sqrt{3} H^6 U^7 + 20864 \sqrt{3} g^5 H^{17} \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 + 9600 \sqrt{3} g^7 H^{19} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^6 + 18 \left(225 \sqrt{3} H^4 U^7 + 100096 \sqrt{3} g^5 H^{13} \left(\left(H^2 k^2 + 3 \right) \right) \right) U^2 + 60608 \sqrt{3} g^7 H^{15} \left(\left(H^2 k^2 + 3 \right) \right) \right) k^4 + 36 \left(225 \sqrt{3} H^2 U^7 + 5888 \sqrt{3} g^3 H^7 \left(\left(H^2 k^2 + 3 \right) \right) \right) U^4 + 144512 \sqrt{3} g^5 H^9 \left(\left(H^2 k^2 + 3 \right) \right) U^2 + 105472 \sqrt{3} g^7 H^{11} \left(\left(H^2 k^2 + 3 \right) \right) \right) \right)
\end{aligned}$$


```

Out[137]= Eerr || \left(
\begin{array}{cc}
\left(-\frac{\left(H^2 k^3 U w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i H^2 k^3}{U w^2 \text{dt}^3}\right)\left\{6 \left(H^2 k^2+3\right)\right\}+\frac{H^2 k^3 U w^3 \text{dt}^4}{24 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right)+\left(-\frac{1}{2}\right) \left(\sqrt{g H} k^2\right) U \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}+\left(\frac{i \left(2 H^4 k^7+9 H^2 k^5\right) U \text{dt}\right)\left\{12 \left(H^2 k^2+3\right)^2\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(\frac{1}{24}\right) \sqrt{g H} k^4 \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}^3+\left(-\frac{i k^7 \left(2 H^4 U H^6+19 k^2 U H^4+54 U H^2\right) \text{dt}\right)\left\{240 \left(H^2 k^2+3\right)^3\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \& \left(-\frac{3}{2}\left(k w\right) \text{dt}^2\right)\left\{2 \left(H^2 k^2+3\right)\right\}-\frac{i k w^2 \text{dt}^3}{2 \left(H^2 k^2+3\right)}+\frac{k w^3 \text{dt}^4}{8 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right)+\left(\frac{i \left(H^2 k^5+6 k^3\right) \text{dt}\right)\left\{4 \left(H^2 k^2+3\right)^2\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(\frac{i \left(H^4 k^9-54 k^5\right) \text{dt}\right)\left\{240 \left(H^2 k^2+3\right)^3\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \\
\left(-\frac{\left(\left(k \left(g k^2 H^3+3 g H-3 U^2\right) w\right) \text{dt}^2\right)\left\{2 \left(H^2 k^2+3\right)\right\}-\frac{i k \left(g k^2 H^3+3 g H-3 U^2\right) w^2 \text{dt}^3}{6 \left(H^2 k^2+3\right)}+\frac{k \left(g k^2 H^3+3 g H-3 U^2\right) w^3 \text{dt}^4}{24 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right)+\left(-\frac{1}{2}\right) \left(\sqrt{g H} k^2 U\right) \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}+\left(\frac{i \left(2 g H^5 k^7+12 g H^3 k^5-3 H^2 U^2 k^5-18 U^2 k^3+18 g H k^3\right) \text{dt}\right)\left\{12 \left(H^2 k^2+3\right)^2\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(\frac{1}{24}\right) \sqrt{g H} k^4 U \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}^3+\left(-\frac{i \left(2 g H^7 k^{11}+18 g H^5 k^9+H^4 U^2 k^9+54 g H^3 k^7-54 U^2 k^5+54 g H k^5\right) \text{dt}\right)\left\{240 \left(H^2 k^2+3\right)^3\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \& \left(-\frac{\left(k \left(H^2 k^2+6\right) U w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i k \left(H^2 k^2+6\right) U w^2 \text{dt}^3}{6 \left(H^2 k^2+3\right)}+\frac{k \left(H^2 k^2+6\right) U w^3 \text{dt}^4}{24 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right)+\left(-\frac{1}{2}\right) \left(\sqrt{g H} k^2\right) U \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}+\left(\frac{i \left(2 H^4 U k^7+15 H^2 U k^5+36 U k^3\right) \text{dt}\right)\left\{12 \left(H^2 k^2+3\right)^2\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(\frac{1}{24}\right) \sqrt{g H} k^4 \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}^3+\left(-\frac{i \left(2 H^6 U k^{11}+17 H^4 U k^9+54 H^2 U k^7+108 U k^5\right) \text{dt}\right)\left\{240 \left(H^2 k^2+3\right)^3\right\}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \\
\end{array}
\right)

```

```

In[138]:= KurF = (fm * ap - fp * am + am * ap * (qp - qm)) / (ap - am);
KurFWS = KurF /. ap -> (U + Sqrt[g * H]) /. am -> 0;
KurFWSeta =
  KurFWS /. fp -> (H * v + U * Rpp * n) /. fm -> (H * v + U * Rmp * n) /. qp -> Rpp * n /.
  qm -> Rmp * n;
KurFWSeta = KurFWSeta /. v -> (GGp * G + Gnp * n);
Kfnnp = FullSimplify[KurFWSeta /. G -> 0 /. n -> 1];
KfnGp = FullSimplify[KurFWSeta /. n -> 0 /. G -> 1];
Kfnn = Kfnnp /. Rpp -> Rp /. Rmp -> Rm /. GGp -> GG2 /. Gnp -> Gn2;

```

```

KfnG = KfnGp /. Rpp → Rp /. Rmp → Rm /. GGp → GG2 /. Gnp → Gn2;
Fnn2 = -dt * (1 - Exp[-I * k * dx]) / dx * Kfnn;
Fnn2TA = Series[Fnn2 - FnnA, {dx, 0, 3}, {dt, 0, 3}];
Fnn2TAr = Refine[Fnn2TA, {k > 0, U > 0, H > 0, g > 0}];
FnG2 = -dt * (1 - Exp[-I * k * dx]) / dx * KfnG;
FnG2TA = Series[FnG2 - FnGA, {dx, 0, 3}, {dt, 0, 3}];
FnG2TAr = Refine[FnG2TA, {k > 0, U > 0, H > 0, g > 0}];

KurFWSG = KurFWS /. fp → (U * Rpp * G + U * H * v + g * H * Rpp * n) /.
    fm → (U * Rmp * G + U * H * v + g * H * Rmp * n) /. qp → Rpp * G /. qm → Rmp * G;
KurFWSG = KurFWSG /. v → (GGp * G + Gnp * n);
KfGnp = FullSimplify[KurFWSG /. G → 0 /. n → 1];
KfGGp = FullSimplify[KurFWSG /. n → 0 /. G → 1];
KfGn = KfGnp /. Rpp → Rp /. Rmp → Rm /. GGp → GG2 /. Gnp → Gn2;
KfGG = KfGGp /. Rpp → Rp /. Rmp → Rm /. GGp → GG2 /. Gnp → Gn2;

FGn2 = -dt * (1 - Exp[-I * k * dx]) / dx * KfGn;
FGn2TA = Series[FGn2 - FGnA, {dx, 0, 3}, {dt, 0, 3}];
FGn2TAr = Refine[FGn2TA, {k > 0, U > 0, H > 0, g > 0}];
fGG2 = U * H * GG2 + U / 2 * (Rm + Rp) - (Sqrt[g * H]) / (2) * (Rp - Rm);
FGG2 = -dt * (1 - Exp[-I * k * dx]) / dx * KfGG;
FGG2TA = Series[FGG2 - FGGA, {dx, 0, 4}, {dt, 0, 3}];
FGG2TAr = Refine[FGG2TA, {k > 0, U > 0, H > 0, g > 0}];
Fmat2 = {{Fnn2, FnG2}, {FGn2, FGG2}};
Emat2 = IdentityMatrix[2] + Fmat2;
Eerr = Series[Emat2 - EA, {dx, 0, 4}, {dt, 0, 4}];
EigvFmat2 = Eigenvalues[Fmat2];

RKStep = Log[1 + EigvFmat2] / (I * dt);
RKstepTay = Series[RKStep, {dx, 0, 4}, {dt, 0, 4}];
RKstepTayr = Simplify[-RKstepTay - {wAp, wAm}, {k > 0, H > 0, g > 0, U > 0}];

Text[Row[{" U > Sqrt(gH)"}]]
Text[" "]
Text[Row[{"Fnn || ", Kfnnp}]]
Text[Row[{"Fnn || ", TeXForm[Kfnnp]}]]
Text[Row[{"Fnn error || ", Fnn2TAr}]]
Text[Row[{"Fnn error || ", TeXForm[Fnn2TAr]}]]
Text[" "]
Text[Row[{"FnG || ", KfnGp}]]
Text[Row[{"FnG || ", TeXForm[KfnGp]}]]
Text[Row[{"FnG error || ", FnG2TAr}]]

```



```

Text[Row[{"FnG error  ||  ", TeXForm[FnG2TAr]}]]
Text[" "]
Text[Row[{"FGn  ||  ", KfGnp}]]
Text[Row[{"FGn  ||  ", TeXForm[KfGnp]}]]
Text[Row[{"FGn error  ||  ", FGn2TAr}]]
Text[Row[{"FGn error  ||  ", TeXForm[FGn2TAr]}]]
Text[" "]
Text[Row[{"FGG  ||  ", KfGGp}]]
Text[Row[{"FGG  ||  ", TeXForm[KfGGp]}]]
Text[Row[{"FGG error  ||  ", FGG2TAr}]]
Text[Row[{"FGG error  ||  ", TeXForm[FGG2TAr]}]]
Text[" "]
Text[" "]
Text[Row[{"Omega error  ||  ", RKstepTayr}]]
Text[Row[{"Omega error  ||  ", TeXForm[RKstepTayr]}]]
Text[" "]
Text[Row[{"EA  ||  ", EA}]]
Text[Row[{"EA  ||  ", TeXForm[EA]}]]
Text[Row[{"Eerr  ||  ", Eerr}]]
Text[Row[{"Eerr  ||  ", TeXForm[Eerr]}]]

```

Out[172]= $U > \text{Sqrt}(gH)$

Out[173]=

Out[174]= $F_{nn} \parallel G_{np} H + R_{mp} U$

Out[175]= $F_{nn} \parallel \text{\texttt{Gnp}} H + \text{\texttt{Rmp}} U$

Out[176]=
$$F_{nn} \text{ error } \parallel \left(-\frac{(H^2 k^3 U w) dt^2}{2(3+H^2 k^2)} - \frac{i H^2 k^3 U w^2 dt^3}{6(3+H^2 k^2)} + O[dt]^4 \right) +$$

$$\left(-\frac{1}{2} (k^2 U) dt + O[dt]^4 \right) dx + \left(\frac{i(9 H^2 k^5 + 2 H^4 k^7) U dt}{12(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + \left(\frac{1}{24} k^4 U dt + O[dt]^4 \right) dx^3 + O[dx]^4$$

Out[177]=
$$F_{nn} \text{ error } \parallel$$

$$\left(-\frac{\text{\texttt{dt}}^2 \left(H^2 k^3 U w \right)}{2 \left(H^2 k^2 + 3 \right)} - \frac{i \text{\texttt{dt}}^3 H^2 k^3 U w^2}{6 \left(H^2 k^2 + 3 \right)} + O \left(\text{\texttt{dt}}^4 \right) \right) + \text{\texttt{dx}} \left(-\frac{1}{2} \left(k^2 U \right) \text{\texttt{dt}} + O \left(\text{\texttt{dt}}^4 \right) \right) +$$

$$\text{\texttt{dx}}^2 \left(\frac{i \left(9 H^2 k^5 + 2 H^4 k^7 \right) U \text{\texttt{dt}}}{12 \left(H^2 k^2 + 3 \right)^2} + O \left(\text{\texttt{dt}}^4 \right) \right) + \text{\texttt{dx}}^3 \left(\frac{1}{24} k^4 U \text{\texttt{dt}} + O \left(\text{\texttt{dt}}^4 \right) \right) + O \left(\text{\texttt{dx}}^4 \right)$$

Out[178]=

Out[179]= $F_{nG} \parallel G_{Gp} H$

Out[180]= $F_{nG} \parallel \text{\texttt{GGp}} H$

Out[181]=
$$F_{nG} \text{ error } \parallel \left(-\frac{3(k w) dt^2}{2(3+H^2 k^2)} - \frac{i k w^2 dt^3}{2(3+H^2 k^2)} + O[dt]^4 \right) + \left(\frac{i(6 k^3 + H^2 k^5) dt}{4(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + O[dx]^4$$

$$\text{Out[182]= FnG error} \parallel \left(-\frac{3}{2} \frac{\text{dt}^2 (k w)}{\left(H^2 k^2 + 3 \right)} - \frac{i}{6} \frac{\text{dt}^3 k w^2}{\left(H^2 k^2 + 3 \right)} + O\left(\text{dt}^4 \right) \right) + \text{dx}^2 \left(\frac{i}{2} \frac{\left(H^2 k^5 + 6 k^3 \right)}{\left(H^2 k^2 + 3 \right)} \text{dt} + O\left(\text{dt}^4 \right) \right) + O\left(\text{dt}^4 \right) \text{dx} + O\left(\text{dx}^4 \right)$$

Out[183]=

$$\text{Out[184]= FGn} \parallel H (g \text{Rmp} + \text{Gnp} U)$$

$$\text{Out[185]= FGn} \parallel H (g \text{Rmp} + \text{Gnp} U)$$

$$\text{Out[186]= FGn error} \parallel \left(-\frac{(k(3gH + gH^3k^2 - 3U^2)w)dt^2}{2(3 + H^2k^2)} - \frac{ik(3gH + gH^3k^2 - 3U^2)w^2dt^3}{6(3 + H^2k^2)} + O[dt]^4 \right) + \left(-\frac{1}{2} (gHk^2) dt + O[dt]^4 \right) dx + \left(\frac{i(18gHk^3 + 12gH^3k^5 + 2gH^5k^7 - 18k^3U^2 - 3H^2k^5U^2)dt}{12(3 + H^2k^2)^2} + O[dt]^4 \right) dx^2 + \left(\frac{1}{24} gHk^4 dt + O[dt]^4 \right) dx^3 + O[dx]^4$$

$$\text{Out[187]= FGn error} \parallel$$

$$\left(-\frac{\text{dt}^2 (k w \left(g H^3 k^2 + 3 g H - 3 U^2 \right))}{6 \left(H^2 k^2 + 3 \right)} - \frac{i}{6} \frac{\text{dt}^3 k w^2 \left(g H^3 k^2 + 3 g H - 3 U^2 \right)}{\left(H^2 k^2 + 3 \right)} + O\left(\text{dt}^4 \right) \right) + \text{dx}^2 \left(\frac{i}{2} \frac{\left(2 g H^5 k^7 + 12 g H^3 k^5 - 3 H^2 U^2 k^5 - 18 U^2 k^3 + 18 g H k^3 \right)}{\left(H^2 k^2 + 3 \right)^2} \text{dt} + O\left(\text{dt}^4 \right) \right) + \text{dx}^3 \left(\frac{i}{24} g H k^4 \text{dt} + O\left(\text{dt}^4 \right) \right) + O\left(\text{dx}^4 \right)$$

Out[188]=

$$\text{Out[189]= FGG} \parallel (G \text{Gp} H + \text{Rmp}) U$$

$$\text{Out[190]= FGG} \parallel U (\text{GGp} H + \text{Rmp})$$

$$\text{Out[191]= FGG error} \parallel$$

$$\left(-\frac{(k(6 + H^2k^2)Uw)dt^2}{2(3 + H^2k^2)} - \frac{ik(6 + H^2k^2)Uw^2dt^3}{6(3 + H^2k^2)} + O[dt]^4 \right) + \left(-\frac{1}{2} (k^2 U) dt + O[dt]^4 \right) dx + \left(\frac{i(36k^3 + 15H^2k^5 + 2H^4k^7)Udt}{12(3 + H^2k^2)^2} + O[dt]^4 \right) dx^2 + \left(\frac{1}{24} k^4 U dt + O[dt]^4 \right) dx^3 + \left(-\frac{i(108k^5 + 54H^2k^7 + 17H^4k^9 + 2H^6k^{11})Udt}{240(3 + H^2k^2)^3} + O[dt]^4 \right) dx^4 + O[dx]^5$$

$$\text{Out[192]= FGG error} \parallel$$

$$\left(-\frac{\text{dt}^2 (k U w \left(H^2 k^2 + 6 \right))}{6 \left(H^2 k^2 + 3 \right)} - \frac{i}{6} \frac{\text{dt}^3 k U w^2 \left(H^2 k^2 + 6 \right)}{\left(H^2 k^2 + 3 \right)} + O\left(\text{dt}^4 \right) \right) + \text{dx}^2 \left(\frac{i}{2} \frac{\left(2 H^4 k^7 + 15 H^2 k^5 + 36 k^3 \right) U}{\left(H^2 k^2 + 3 \right)^2} \text{dt} + O\left(\text{dt}^4 \right) \right) + \text{dx}^3 \left(\frac{i}{24} k^4 U \text{dt} + O\left(\text{dt}^4 \right) \right) + \text{dx}^4 \left(-\frac{i}{240} \frac{\left(2 H^6 k^{11} + 17 H^4 k^9 + 54 H^2 k^7 + 108 k^5 \right) U}{\left(H^2 k^2 + 3 \right)^3} \text{dt} + O\left(\text{dt}^4 \right) \right) + O\left(\text{dx}^5 \right)$$

Out[193]=

Out[194]=

$$\text{Out[195]= Omega error} \parallel \left\{ \frac{i \left(\sqrt{3} k \sqrt{g H (3 + H^2 k^2)} + 3 k U + H^2 k^3 U \right)^2 dt}{2 (3 + H^2 k^2)^2} - \frac{1}{3 (3 + H^2 k^2)^2} \right\}$$

$$\begin{aligned}
& \left[\left(k^3 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(3 g H + U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) \right) dt^2 - \right. \\
& \frac{1}{4(3 + H^2 k^2)^3} i k^4 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(3 g \left(\sqrt{3} H \sqrt{g H (3 + H^2 k^2)} + 9 H U + 3 H^3 k^2 U \right) + \right. \\
& \left. U^2 \left(H^4 k^4 U + 9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + U \right) + 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 2 H^2 U \right) \right) \right) dt^3 + \\
& \frac{1}{5(3 + H^2 k^2)^3} k^5 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(9 g^2 H^2 + 6 g H U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + 2 k^2 \left(2 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 3 H^2 U \right) \right) \right) dt^4 + \\
& \left. O[dt]^5 \right] + \left(-\frac{1}{4} i k^2 \left(\sqrt{3} \sqrt{\frac{g H}{3 + H^2 k^2}} + 2 U \right) + \frac{k^3 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) dt}{4 \sqrt{g H} (3 + H^2 k^2)^{3/2}} + \right. \\
& \left(i k^4 \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g H + U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) dt^2 \right) / \\
& \left(4 \sqrt{g H} (3 + H^2 k^2)^{3/2} \right) - \\
& \left(k^5 \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g \left(\sqrt{3} H \sqrt{g H (3 + H^2 k^2)} + 9 H U + 3 H^3 k^2 U \right) + \right. \right. \\
& \left. U^2 \left(H^4 k^4 U + 9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + U \right) + 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 2 H^2 U \right) \right) \right) \\
& dt^3 \Big) / \left(4 \left(\sqrt{g H} (3 + H^2 k^2)^{5/2} \right) \right) - \left(i k^6 \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) \right. \\
& \left(9 g^2 H^2 + 6 g H U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + 2 k^2 \left(2 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 3 H^2 U \right) \right) \right) \\
& dt^4 \Big) / \left(4 \sqrt{g H} (3 + H^2 k^2)^{5/2} \right) + O[dt]^5 \Big) dx + \\
& \left(- \left(k^3 \left(3 \sqrt{3} g H (13 + 3 H^2 k^2) + 16 \left(3 \sqrt{g H (3 + H^2 k^2)} + k^2 \sqrt{g H^5 (3 + H^2 k^2)} \right) U \right) \right) / \right. \\
& \left(96 \left(\sqrt{g H} (3 + H^2 k^2)^{3/2} \right) \right) - \\
& \left(i k^4 \left(g H \left(144 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (369 + 234 H^2 k^2 + 37 H^4 k^4) U \right) + 4 \left(63 \sqrt{g H (3 + H^2 k^2)} U^2 + \right. \right. \\
& \left. 7 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 14 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) \\
& dt \Big) / \left(96 \sqrt{g H} (3 + H^2 k^2)^{5/2} \right) + \left(k^5 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right. \\
& \left(g H \left(171 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (477 + 306 H^2 k^2 + 49 H^4 k^4) U \right) + 5 \left(72 \sqrt{g H (3 + H^2 k^2)} U^2 + \right. \right. \\
& \left. 8 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 16 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \\
& dt^2 \Big) / \left(96 \sqrt{g H} (3 + H^2 k^2)^{7/2} \right) + \left(i k^6 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right)^2
\end{aligned}$$

$$\begin{aligned}
& \left(468 \sqrt{g H (3 + H^2 k^2)} U^2 + 52 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \\
& \quad \left. g H \left(198 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (585 + 378 H^2 k^2 + 61 H^4 k^4) U \right) + \right. \\
& \quad \left. 6 k^2 \left(9 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 52 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) dt^3 \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)}^{9/2} \right) - \\
& \left(\left(k^7 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right)^3 \left(576 \sqrt{g H (3 + H^2 k^2)} U^2 + 64 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \right. \\
& \quad \left. \left. g H \left(225 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (693 + 450 H^2 k^2 + 73 H^4 k^4) U \right) + \right. \right. \\
& \quad \left. \left. 3 k^2 \left(21 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 128 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) dt^4 \right) \Big/ \\
& \left(96 \left(\sqrt{g H (3 + H^2 k^2)}^{11/2} \right) + O[dt]^5 \right) dx^2 + \left(\frac{i k^4 \left(\sqrt{3} g H (33 + 7 H^2 k^2) + 16 \left(3 \sqrt{g H (3 + H^2 k^2)} + k^2 \sqrt{g H^5 (3 + H^2 k^2)} \right) U \right)}{384 \sqrt{g H (3 + H^2 k^2)}^{3/2}} - \right. \\
& \left(\left(k^5 \left(g H \left(72 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (207 + 126 H^2 k^2 + 19 H^4 k^4) U \right) + 16 \left(9 \sqrt{g H (3 + H^2 k^2)} U^2 + \right. \right. \right. \\
& \quad \left. \left. k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + k^2 \left(\sqrt{g^3 H^7 (3 + H^2 k^2)} + 6 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt \Big/ \\
& \left(128 \left(\sqrt{g H (3 + H^2 k^2)}^{5/2} \right) \right) - \left(i k^6 \left(9 \sqrt{3} g^2 H^2 (13 + 3 H^2 k^2) + 5 g H U \left(96 \sqrt{g H (3 + H^2 k^2)} + \right. \right. \right. \\
& \quad \left. \left. \sqrt{3} (129 + 82 H^2 k^2 + 13 H^4 k^4) U \right) + 32 \left(9 \sqrt{g H (3 + H^2 k^2)} U^3 + k^4 \sqrt{g H^9 (3 + H^2 k^2)} \right. \right. \\
& \quad \left. \left. U^3 + 2 k^2 \left(2 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 3 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) dt^2 \Big/ \\
& \left(128 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) + \left(k^7 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(24 \sqrt{3} g^2 H^2 (21 + 5 H^2 k^2) + \right. \right. \\
& \quad \left. \left. 3 g H U \left(717 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1011 + 646 H^2 k^2 + 103 H^4 k^4) U \right) + \right. \right. \\
& \quad \left. \left. 5 \left(288 \sqrt{g H (3 + H^2 k^2)} U^3 + 32 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + \right. \right. \right. \\
& \quad \left. \left. \left. 3 k^2 \left(39 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 64 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) dt^3 \right) \Big/ \\
& \left(384 \sqrt{g H (3 + H^2 k^2)}^{7/2} \right) + \left(i k^8 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right)^2 \right. \\
& \quad \left(5 \sqrt{3} g^2 H^2 (45 + 11 H^2 k^2) + 720 \sqrt{g H (3 + H^2 k^2)} U^3 + 80 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + \right. \\
& \quad \left. g H U \left(990 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1449 + 930 H^2 k^2 + 149 H^4 k^4) U \right) + \right. \\
& \quad \left. \left. 2 k^2 \left(137 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 240 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right. \\
& \quad \left. dt^4 \right) \Big/ \left(128 \sqrt{g H (3 + H^2 k^2)}^{9/2} \right) + O[dt]^5 \Big) dx^3 + \\
& \left(\left(k^5 \left(3 \sqrt{3} g H (543 + 146 H^2 k^2 + 15 H^4 k^4) + 256 \left(9 \sqrt{g H (3 + H^2 k^2)} + 6 k^2 \sqrt{g H^5 (3 + H^2 k^2)} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. k^4 \sqrt{g H^9 (3 + H^2 k^2)} \right) \right) \right) \Big/ \left(30720 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left(i k^6 \left(3 g H \left(18432 \sqrt{g H (3 + H^2 k^2)} + 51039 \sqrt{3} U + 45735 \sqrt{3} H^2 k^2 U + \right. \right. \right. \\
& \quad \left. \left. 1381 \sqrt{3} H^6 k^6 U + k^4 \left(960 \sqrt{g H^9 (3 + H^2 k^2)} + 13717 \sqrt{3} H^4 U \right) \right) \right) + \\
& \quad 128 \left(837 \sqrt{g H (3 + H^2 k^2)} U^2 + 279 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 31 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} U^2 + \right. \\
& \quad \left. 27 k^2 \left(7 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 31 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \Big) dt \Big) / \\
& \left(92160 \sqrt{g H (3 + H^2 k^2)^{7/2}} \right) - \left(\left(k^7 \left(9 \sqrt{3} g^2 H^2 (12999 + 6258 H^2 k^2 + 775 H^4 k^4) + \right. \right. \right. \\
& \quad g H U \left(617661 \sqrt{3} H^2 k^2 U + 20551 \sqrt{3} H^6 k^6 U + 81 \left(5888 \sqrt{g H (3 + H^2 k^2)} + \right. \right. \\
& \quad \left. \left. 8053 \sqrt{3} U \right) + 3 k^4 \left(12288 \sqrt{g H^9 (3 + H^2 k^2)} + 65021 \sqrt{3} H^4 U \right) \right) + \\
& \quad \left. 128 \left(2322 \sqrt{g H (3 + H^2 k^2)} U^3 + 774 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 86 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} \right. \right. \\
& \quad \left. \left. U^3 + 9 k^2 \left(229 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 258 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) \\
& dt^2 \Big) / \left(92160 \left(\sqrt{g H (3 + H^2 k^2)^{7/2}} \right) \right) - \frac{1}{30720 \sqrt{g H (3 + H^2 k^2)^{9/2}}} \\
& i k^8 \left(k^8 U^3 \left(21253 \sqrt{3} g H^9 + 7776 \sqrt{g H^{17} (3 + H^2 k^2)} U \right) + \right. \\
& \quad 243 \left(832 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 4423 \sqrt{3} g^2 H^2 U + 2592 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\
& \quad g H U^2 \left(8832 \sqrt{g H (3 + H^2 k^2)} + 7823 \sqrt{3} U \right) \Big) + 3 k^6 U \left(9181 \sqrt{3} g^2 H^8 + \right. \\
& \quad \left. 31104 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + 4 g H^7 U \left(5312 \sqrt{g H (3 + H^2 k^2)} + 21787 \sqrt{3} U \right) \right) + \\
& \quad 27 k^2 \left(35319 \sqrt{3} g^2 H^4 U + 91580 \sqrt{3} g H^3 U^3 + \right. \\
& \quad \left. 64 \left(59 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 1155 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 486 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \right) \right) + \\
& \quad 9 k^4 \left(31231 \sqrt{3} g^2 H^6 U + 2 g H^5 U^2 \left(34336 \sqrt{g H (3 + H^2 k^2)} + 67003 \sqrt{3} U \right) + \right. \\
& \quad \left. 288 \left(5 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 162 \sqrt{g H^9 (3 + H^2 k^2)} U^4 \right) \right) \Big) dt^3 + \\
& \frac{1}{92160 \sqrt{g H (3 + H^2 k^2)^{11/2}}} k^9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(k^8 U^3 \left(111559 \sqrt{3} g H^9 + 42368 \sqrt{g H^{17} (3 + H^2 k^2)} U \right) + \right. \\
& \quad 27 k^2 \left(18078 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 172047 \sqrt{3} g^2 H^4 U + 372075 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + \right. \\
& \quad \left. 477940 \sqrt{3} g H^3 U^3 + 169472 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \right) + \\
& \quad 81 \left(11603 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 63917 \sqrt{3} g^2 H^2 U + 42368 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\
& \quad g H U^2 \left(132513 \sqrt{g H (3 + H^2 k^2)} + 122207 \sqrt{3} U \right) \Big) + 3 k^6 U \left(45573 \sqrt{3} g^2 H^8 + \right. \\
& \quad \left. 169472 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + g H^7 U \left(108089 \sqrt{g H (3 + H^2 k^2)} + 456644 \sqrt{3} U \right) \right) + \\
& \quad 9 k^4 \left(7035 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 153703 \sqrt{3} g^2 H^6 U + 254208 \sqrt{g H^9 (3 + H^2 k^2)} U^4 + \right.
\end{aligned}$$

$$\begin{aligned}
& g H^5 U^2 \left(347651 \sqrt{g H (3 + H^2 k^2)} + 700818 \sqrt{3} U \right) dt^4 + O[dt]^5 \Big) dx^4 + O[dx]^5, \\
& \left(\frac{i \left(-\sqrt{3} k \sqrt{g H (3 + H^2 k^2)} + 3 k U + H^2 k^3 U \right)^2 dt}{2 (3 + H^2 k^2)^2} - \frac{1}{3 (3 + H^2 k^2)^2} \left(k^3 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right. \right. \\
& \quad \left. \left(3 g H + U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) dt^2 - \right. \\
& \quad \frac{1}{4 (3 + H^2 k^2)^3} i k^4 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \quad \left(3 g H \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \quad \left. U^2 \left(-9 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U - 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} - 2 H^2 U \right) \right) \right) dt^3 + \\
& \quad \frac{1}{5 (3 + H^2 k^2)^3} k^5 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \quad \left(9 g^2 H^2 + 6 g H U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \quad \left. U^3 \left(-12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + k^2 \left(-4 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 6 H^2 U \right) \right) \right) dt^4 + O[\\
& \quad dt]^5 \Big) + \\
& \left(\frac{1}{4} i k^2 \left(\sqrt{3} \sqrt{\frac{g H}{3 + H^2 k^2}} - 2 U \right) - \frac{\left(k^3 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) \right) dt}{4 \left(\sqrt{g H (3 + H^2 k^2)} \right)^{3/2}} - \right. \\
& \quad \left(i k^4 \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g H + U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) dt^2 \right) / \\
& \quad \left(4 \sqrt{g H (3 + H^2 k^2)}^{3/2} \right) + \\
& \quad \left(k^5 \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g H \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + U^2 \right. \right. \\
& \quad \left. \left. \left(-9 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U - 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} - 2 H^2 U \right) \right) \right) dt^3 \right) / \\
& \quad \left(4 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) + \left(i k^6 \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) \right. \\
& \quad \left(9 g^2 H^2 + 6 g H U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \quad \left. U^3 \left(-12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + k^2 \left(-4 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 6 H^2 U \right) \right) \right) \\
& \quad \left. dt^4 \right) / \left(4 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) + O[dt]^5 \Big) dx + \\
& \left(\frac{k^3 \left(3 \sqrt{3} g H (13 + 3 H^2 k^2) - 16 \left(3 \sqrt{g H (3 + H^2 k^2)} U + k^2 \sqrt{g H^5 (3 + H^2 k^2)} U \right) \right)}{4} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left(96 \sqrt{g H (3 + H^2 k^2)^{3/2}} \right. \\
& \left(i k^4 \left(g H \left(-144 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (369 + 234 H^2 k^2 + 37 H^4 k^4) U \right) - \right. \right. \\
& \quad 4 \left(63 \sqrt{g H (3 + H^2 k^2)} U^2 + 7 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \\
& \quad \quad \left. 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 14 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \left. \right) dt \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) - \\
& \left(\left(k^5 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right) \left(g H \left(171 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} (477 + 306 H^2 k^2 + \right. \right. \right. \\
& \quad \left. \left. 49 H^4 k^4) U \right) + 5 \left(72 \sqrt{g H (3 + H^2 k^2)} U^2 + 8 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \\
& \quad \left. \left. 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 16 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt^2 \Big/ \right. \\
& \left(96 \left(\sqrt{g H (3 + H^2 k^2)^{7/2}} \right) \right) + \left(i k^6 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right)^2 \right. \\
& \quad \left(468 \sqrt{g H (3 + H^2 k^2)} U^2 + 52 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \\
& \quad g H \left(198 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} (585 + 378 H^2 k^2 + 61 H^4 k^4) U \right) + \\
& \quad \left. 6 k^2 \left(9 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 52 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) dt^3 \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{9/2}} \right) + \\
& \left(k^7 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right)^3 \left(576 \sqrt{g H (3 + H^2 k^2)} U^2 + 64 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \\
& \quad g H \left(225 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} (693 + 450 H^2 k^2 + 73 H^4 k^4) U \right) + \\
& \quad \left. 3 k^2 \left(21 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 128 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) dt^4 \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{11/2}} \right) + \\
& O[dt]^5 \Big) dx^2 + \left(\frac{i k^4 \left(-\sqrt{3} g H (33 + 7 H^2 k^2) + 16 \left(3 \sqrt{g H (3 + H^2 k^2)} + k^2 \sqrt{g H^5 (3 + H^2 k^2)} \right) U \right)}{384 \sqrt{g H (3 + H^2 k^2)^{3/2}}} + \right. \\
& \left(k^5 \left(g H \left(-72 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (207 + 126 H^2 k^2 + 19 H^4 k^4) U \right) - \right. \right. \\
& \quad 16 \left(9 \sqrt{g H (3 + H^2 k^2)} U^2 + k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \\
& \quad \quad \left. k^2 \left(\sqrt{g^3 H^7 (3 + H^2 k^2)} + 6 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \left. \right) dt \Big/ \left(128 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) + \\
& \left(i k^6 \left(9 \sqrt{3} g^2 H^2 (13 + 3 H^2 k^2) + 5 g H U \left(-96 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (129 + 82 H^2 k^2 + 13 H^4 k^4) U \right) - \right. \right. \\
& \quad 32 \left(9 \sqrt{g H (3 + H^2 k^2)} U^3 + k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 2 k^2 \left(2 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + \right. \right. \\
& \quad \quad \left. \left. 3 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \left. \right) dt^2 \Big/ \left(128 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) - \\
& \left(\left(k^7 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(24 \sqrt{3} g^2 H^2 (21 + 5 H^2 k^2) + \right. \right. \right. \\
& \quad 3 g H U \left(-717 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1011 + 646 H^2 k^2 + 103 H^4 k^4) U \right) - \\
& \quad \left. 5 \left(288 \sqrt{g H (3 + H^2 k^2)} U^3 + 32 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + \right. \right. \\
& \quad \quad \left. \left. 3 k^2 \left(39 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 64 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) dt^3 \Big/ \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\left(\left(\left(\left(\left(\sqrt{g H (3 + H^2 k^2)^{7/2}} \right) \right) - \left(i k^8 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right)^2 \left(5 \sqrt{3} g^2 H^2 \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. (45 + 11 H^2 k^2) + g H U \left(-990 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1449 + 930 H^2 k^2 + 149 H^4 k^4) U \right) - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 2 \left(360 \sqrt{g H (3 + H^2 k^2)} U^3 + 40 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + k^2 \left(137 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 240 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) \right) \left(128 \sqrt{g H (3 + H^2 k^2)^{9/2}} \right) + O[dt]^5 \Big) dx^3 + \\
& \left(\left(k^5 \left(-3 \sqrt{3} g H (543 + 146 H^2 k^2 + 15 H^4 k^4) + 256 \left(9 \sqrt{g H (3 + H^2 k^2)} + 6 k^2 \sqrt{g H^5 (3 + H^2 k^2)} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. k^4 \sqrt{g H^9 (3 + H^2 k^2)} U \right) \right) \right) \left(30720 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) + \\
& \left(i k^6 \left(-3 g H \left(-18432 \sqrt{g H (3 + H^2 k^2)} + 51039 \sqrt{3} U + 45735 \sqrt{3} H^2 k^2 U + \right. \right. \right. \\
& \quad \left. \left. \left. 1381 \sqrt{3} H^6 k^6 U + k^4 \left(-960 \sqrt{g H^9 (3 + H^2 k^2)} + 13717 \sqrt{3} H^4 U \right) \right) \right) + \\
& \quad 128 \left(837 \sqrt{g H (3 + H^2 k^2)} U^2 + 279 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 31 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} U^2 + \right. \\
& \quad \left. 27 k^2 \left(7 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 31 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) dt \Big) / \\
& \left(92160 \sqrt{g H (3 + H^2 k^2)^{7/2}} \right) + \left(k^7 \left(9 \sqrt{3} g^2 H^2 (12999 + 6258 H^2 k^2 + 775 H^4 k^4) + \right. \right. \\
& \quad g H U \left(617661 \sqrt{3} H^2 k^2 U + 20551 \sqrt{3} H^6 k^6 U + 81 \left(-5888 \sqrt{g H (3 + H^2 k^2)} + \right. \right. \\
& \quad \left. \left. 8053 \sqrt{3} U \right) - 3 k^4 \left(12288 \sqrt{g H^9 (3 + H^2 k^2)} - 65021 \sqrt{3} H^4 U \right) \right) - \\
& \quad 128 \left(2322 \sqrt{g H (3 + H^2 k^2)} U^3 + 774 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 86 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + \right. \\
& \quad \left. 9 k^2 \left(229 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 258 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) dt \Big) / \\
& \left(92160 \sqrt{g H (3 + H^2 k^2)^{7/2}} \right) - \frac{1}{30720 \sqrt{g H (3 + H^2 k^2)^{9/2}}} i k^8 \\
& \left(k^8 U^3 \left(-21253 \sqrt{3} g H^9 + 7776 \sqrt{g H^{17} (3 + H^2 k^2)} U \right) + \right. \\
& \quad 243 \left(832 \sqrt{g^5 H^5 (3 + H^2 k^2)} - 4423 \sqrt{3} g^2 H^2 U + 2592 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\
& \quad g H U^2 \left(8832 \sqrt{g H (3 + H^2 k^2)} - 7823 \sqrt{3} U \right) \Big) - 3 k^6 U \left(9181 \sqrt{3} g^2 H^8 - \right. \\
& \quad \left. 31104 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + 4 g H^7 U \left(-5312 \sqrt{g H (3 + H^2 k^2)} + 21787 \sqrt{3} U \right) \right) + \\
& \quad 27 k^2 \left(-35319 \sqrt{3} g^2 H^4 U - 91580 \sqrt{3} g H^3 U^3 + \right. \\
& \quad \left. 64 \left(59 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 1155 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 486 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \right) \right) + \\
& \quad 9 k^4 \left(-31231 \sqrt{3} g^2 H^6 U + 2 g H^5 U^2 \left(34336 \sqrt{g H (3 + H^2 k^2)} - 67003 \sqrt{3} U \right) + \right. \\
& \quad \left. 288 \left(5 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 162 \sqrt{g H^9 (3 + H^2 k^2)} U^4 \right) \right) dt^3 - \frac{1}{30720 \sqrt{g H (3 + H^2 k^2)^{9/2}}}
\end{aligned}$$

$$\begin{aligned} & \left(k^9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right) \left(k^8 U^3 \left(-111 559 \sqrt{3} g H^9 + 42 368 \sqrt{g H^{17} (3 + H^2 k^2)} U \right) + \right. \right. \\ & 27 k^2 \left(18 078 \sqrt{g^5 H^9 (3 + H^2 k^2)} - 172 047 \sqrt{3} g^2 H^4 U + 372 075 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 - \right. \\ & \left. 477 940 \sqrt{3} g H^3 U^3 + 169 472 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \right) + \\ & 9 k^4 \left(7035 \sqrt{g^5 H^{13} (3 + H^2 k^2)} - 153 703 \sqrt{3} g^2 H^6 U + 254 208 \sqrt{g H^9 (3 + H^2 k^2)} U^4 + \right. \\ & \left. g H^5 U^2 \left(347 651 \sqrt{g H (3 + H^2 k^2)} - 700 818 \sqrt{3} U \right) \right) + \\ & 81 \left(11 603 \sqrt{g^5 H^5 (3 + H^2 k^2)} - 63 917 \sqrt{3} g^2 H^2 U + 42 368 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\ & \left. g H U^2 \left(132 513 \sqrt{g H (3 + H^2 k^2)} - 122 207 \sqrt{3} U \right) \right) - \\ & 3 k^6 U \left(45 573 \sqrt{3} g^2 H^8 - 169 472 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + \right. \\ & \left. g H^7 U \left(-108 089 \sqrt{g H (3 + H^2 k^2)} + 456 644 \sqrt{3} U \right) \right) \Big) dt^4 + O[dt]^5 \Big) dx^4 + O[dx]^5 \Big\} \end{aligned}$$

Out[196]= Omega error ||

[illegible]

$$\begin{aligned}
& U \right) \{ 96 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) - \frac{i k^4 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}}{\sqrt[3]{g H \left(H^2 k^2 + 3 \right)}} \left(37 \right. \\
& H^4 k^4 + 234 H^2 k^2 + 369 \right) U + 144 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \right) + 4 \sqrt[3]{7 \sqrt[3]{g H^9} \\
& \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) U^2 k^4 + 3 \sqrt[3]{14 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^2 + 3 \sqrt[3]{g^3 H^7} \\
& \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) \right) k^2 + 63 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^2 \right) \right) \text{Text{dt}} \{ 96 \\
& \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{5}{2}} \} + \frac{k^5 \sqrt[3]{\left(H^2 k^2 + 3 \right) U + \sqrt[3]{3}} \sqrt[3]{g H} \\
& \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \sqrt[3]{\left(g H \sqrt[3]{3} \left(49 H^4 k^4 + 306 H^2 k^2 + 477 \right) U + 171 \right.} \\
& \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^2 k^4 + 3 \sqrt[3]{16 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^2 + 3 \sqrt[3]{g^3 H^7} \\
& \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) \right) k^2 + 72 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^2 \right) \right) \text{Text{dt}}^2 \{ 96 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{7}{2}} \} + \frac{i}{k^6} \\
& \sqrt[3]{\left(H^2 k^2 + 3 \right) U + \sqrt[3]{3}} \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \right)^2 \sqrt[3]{52 \sqrt[3]{g H^9} \left(H^2 k^2 + 3 \right)} U^2 k^4 + 6 \sqrt[3]{52 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^2 + 9 \sqrt[3]{g^3 H^7} \\
& \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) \right) k^2 + 468 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^2 + g H \sqrt[3]{3} \sqrt[3]{61 H^4 k^4 + 378 H^2 k^2 + 585} \right) U + 198 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \right) \text{Text{dt}}^3 \{ 96 \\
& \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{9}{2}} \} - \frac{\sqrt[3]{k^7 \sqrt[3]{\left(H^2 k^2 + 3 \right) U + \sqrt[3]{3}} \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}}^3 \sqrt[3]{64 \sqrt[3]{g H^9 \left(H^2 k^2 + 3 \right)}} U^2 k^4 + 3 \sqrt[3]{128 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^2 + 21 \sqrt[3]{g^3 H^7} \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) \right) k^2 + 576 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^2 + g H \sqrt[3]{3} \sqrt[3]{73 H^4 k^4 + 450 H^2 k^2 + 693} \right) U + 225 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right) \text{Text{dt}}^4 \{ 96 \sqrt[3]{\sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{11}{2}} \right)} + O \left(\text{Text{dt}}^5 \right) \right) \text{Text{dx}}^2 + \sqrt[3]{\frac{i k^4 \sqrt[3]{3}}{g H \left(7 H^2 k^2 + 33 \right)} + 16 \sqrt[3]{\sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} k^2 + 3 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}} U \right) \} \{ 384 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \} - \frac{\sqrt[3]{k^5 \sqrt[3]{g H \left(\sqrt[3]{3} \left(19 H^4 k^4 + 126 H^2 k^2 + 207 \right) U + 72 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right)}} \sqrt[3]{\sqrt[3]{g H^9 \left(H^2 k^2 + 3 \right)}} U^2 k^4 + \sqrt[3]{6 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^2 + \sqrt[3]{g^3 H^7} \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) \right) k^2 + 9 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^2 \right) \right) \right) \text{Text{dt}} \{ 128 \sqrt[3]{\sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{5}{2}} \right)} - \frac{i k^6 \sqrt[3]{9 \sqrt[3]{3}} g^2 \sqrt[3]{3 H^2 k^2 + 13} \right) H^2 + 5 g U \sqrt[3]{3} \sqrt[3]{13 H^4 k^4 + 82 H^2 k^2 + 129} \right) U + 96 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) H + 32 \sqrt[3]{\sqrt[3]{g H^9 \left(H^2 k^2 + 3 \right)}} U^3 k^4 + 2 \sqrt[3]{3 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^3 + 2 \sqrt[3]{g^3 H^7} \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) U \right) k^2 + 9 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^3 \right) \right) \text{Text{dt}}^2 \{ 128 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{5}{2}} \} + \frac{k^7 \sqrt[3]{\left(H^2 k^2 + 3 \right) U + \sqrt[3]{3}} \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \sqrt[3]{24 \sqrt[3]{3}} g^2 \sqrt[3]{5 H^2 k^2 + 21} \right) H^2 + 3 g U \sqrt[3]{3} \sqrt[3]{103 H^4 k^4 + 646 H^2 k^2 + 1011} \right) U + 717 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) H + 5 \sqrt[3]{32 \sqrt[3]{g H^9 \left(H^2 k^2 + 3 \right)}} U^3 k^4 + 3 \sqrt[3]{64 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^3 + 39 \sqrt[3]{g^3 H^7} \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) U \right) k^2 + 288 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^3 \right) \right) \text{Text{dt}}^3 \{ 384 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{7}{2}} \} + \frac{i k^8 \sqrt[3]{\left(H^2 k^2 + 3 \right) U + \sqrt[3]{3}} \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right)^2 \sqrt[3]{80 \sqrt[3]{g H^9 \left(H^2 k^2 + 3 \right)}} U^3 k^4 + 2 \sqrt[3]{240 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} U^3 + 137 \sqrt[3]{g^3 H^7} \left(H^2 k^2 + 3 \right)}^{\frac{3}{2}} \right) U \right) k^2 + 720 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} U^3 + 5 \sqrt[3]{3} g^2 H^2 \sqrt[3]{11 H^2 k^2 + 45} \right) + g H U \sqrt[3]{3} \sqrt[3]{149 H^4 k^4 + 930 H^2 k^2 + 1449} \right) U + 990 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) \right) \text{Text{dt}}^4 \{ 128 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{9}{2}} \} + O \left(\text{Text{dt}}^5 \right) \right) \text{Text{dx}}^3 + \sqrt[3]{\frac{k^5 \sqrt[3]{3}}{g H \left(15 H^4 k^4 + 146 H^2 k^2 + 543 \right)} + 256 \sqrt[3]{\sqrt[3]{g H^9 \left(H^2 k^2 + 3 \right)}} k^4 + 6 \sqrt[3]{g H^5 \left(H^2 k^2 + 3 \right)}} k^2 + 9 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)} \right) U \right) \} \{ 30720 \sqrt[3]{g H \left(H^2 k^2 + 3 \right)}^{\frac{5}{2}} \} + \frac{i k^6 \sqrt[3]{3 g H \left(1381 \sqrt[3]{3} H^6 U k^6 + \left(13717 \sqrt[3]{3} H^4 k^4 + 960 \sqrt[3]{3} H^2 k^2 + 1160 \right) \sqrt[3]{3} \right)}} \sqrt[3]{44 + 45725 \sqrt[3]{3} H^2 U k^2 + 51020} \right)
\end{aligned}$$

[illegible]

$$\begin{aligned}
& k^2+3\right)\} U\right) k^2+9 \sqrt{g H \left(H^2 k^2+3\right)\} U^3\right)\right) \text{ \text{dt}}^2\}\{128 \sqrt{g} \\
& H) \left(H^2 k^2+3\right)\}^{5/2}\}-\frac{\left(k^7 \left(\left(H^2 k^2+3\right)\} U-\sqrt{3}\right) \sqrt{g H} \\
& \left(H^2 k^2+3\right)\}\right) \left(24 \sqrt{3}\right) g^2 \left(5 H^2 k^2+21\right) H^2+3 g U \left(\sqrt{3}\right) \\
& \left(103 H^4 k^4+646 H^2 k^2+1011\right) U-717 \sqrt{g H \left(H^2 k^2+3\right)\}\right) H-5 \\
& \left(32 \sqrt{g H^9 \left(H^2 k^2+3\right)\} U^3 k^4+3 \left(64 \sqrt{g H^5 \left(H^2 k^2+3\right)\}\right) \\
& U^3+39 \sqrt{g^3 H^7 \left(H^2 k^2+3\right)\} U\right) k^2+288 \sqrt{g H \left(H^2 k^2+3\right)\} \\
& U^3\right)\right) \text{ \text{dt}}^3\}\{384 \left(\sqrt{g H} \left(H^2 k^2+3\right)\}^{7/2}\right)\}-\frac{i}{k^8 \left(\sqrt{3}\right) \sqrt{g H \left(H^2 k^2+3\right)\}-\left(H^2 k^2+3\right) U\right)^2 \left(5 \sqrt{3}\right) \\
& g^2 \left(11 H^2 k^2+45\right) H^2+g U \left(\sqrt{3}\right) \left(149 H^4 k^4+930 H^2 k^2+1449\right) \\
& U-990 \sqrt{g H \left(H^2 k^2+3\right)\}\right) H-2 \left(40 \sqrt{g H^9 \left(H^2 k^2+3\right)\} U^3 \\
& k^4+\left(240 \sqrt{g H^5 \left(H^2 k^2+3\right)\} U^3+137 \sqrt{g^3 H^7 \left(H^2 k^2+3\right)\} \right. \\
& \left. U\right) k^2+360 \sqrt{g H \left(H^2 k^2+3\right)\} U^3\right)\right) \text{ \text{dt}}^4\}\{128 \sqrt{g H} \left(H^2 k^2+3\right)\}^{9/2}\}+O\left(\text{ \text{dt}}^5\right)\right) \text{ \text{dx}}^3+\left(\frac{k^5 \left(256 \sqrt{g} H^9 \left(H^2 k^2+3\right)\} k^4+6 \sqrt{g H^5 \left(H^2 k^2+3\right)\} k^2+9 \sqrt{g H \left(H^2 k^2+3\right)\}\right) U-3 \sqrt{3}\right) g H \left(15 H^4 k^4+146 H^2 k^2+543\right)\right)\{30720 \sqrt{g H} \\
& \left(H^2 k^2+3\right)\}^{5/2}\}+\frac{i}{k^6 \left(128 \sqrt{g H^{\{13\}} \left(H^2 k^2+3\right)\} U^2 k^6+279 \sqrt{g H^9 \left(H^2 k^2+3\right)\} U^2 k^4+27 \sqrt{g H^5 \left(H^2 k^2+3\right)\} U^2+7 \sqrt{g^3 H^7 \left(H^2 k^2+3\right)\}\right) k^2+837 \sqrt{g H \left(H^2 k^2+3\right)\} U^2\right)-3 g H \left(1381 \sqrt{3}\right) H^6 U k^6+\left(13717 \sqrt{3}\right) H^4 U-960 \sqrt{g H^9 \left(H^2 k^2+3\right)\}\right) k^4+45735 \sqrt{3}\right) H^2 U k^2+51039 \sqrt{3}\} U-18432 \sqrt{g H \left(H^2 k^2+3\right)\}\right) \text{ \text{dt}}\}\{92160 \sqrt{g H} \left(H^2 k^2+3\right)\}^{7/2}\}+\frac{k^7 \left(9 \sqrt{3}\right) g^2 \left(775 H^4 k^4+6258 H^2 k^2+12999\right) H^2+g U \left(20551 \sqrt{3}\right) H^6 U k^6-3 \left(12288 \sqrt{g H^9 \left(H^2 k^2+3\right)\}-65021 \sqrt{3}\right) H^4 U\right) k^4+617661 \sqrt{3}\right) H^2 U k^2+81 \left(8053 \sqrt{3}\right) U-5888 \sqrt{g H \left(H^2 k^2+3\right)\}\right) \text{ \text{dt}}\} H-128 \left(86 \sqrt{g H^{\{13\}} \left(H^2 k^2+3\right)\} U^3 k^6+774 \sqrt{g H^9 \left(H^2 k^2+3\right)\} U^3 k^4+9 \left(258 \sqrt{g H^5 \left(H^2 k^2+3\right)\} U^3+229 \sqrt{g^3 H^7 \left(H^2 k^2+3\right)\} U\right) k^2+2322 \sqrt{g H \left(H^2 k^2+3\right)\} U^3\right)\right) \text{ \text{dt}}^2\}\{92160 \sqrt{g H} \left(H^2 k^2+3\right)\}^{7/2}\}-\frac{i}{k^8 \left(U^3 \left(7776 \sqrt{g H^{\{17\}} \left(H^2 k^2+3\right)\} U-21253 \sqrt{3}\right) g H^9\right) k^8-3 U \left(9181 \sqrt{3}\right) g^2 H^8+4 g U \left(21787 \sqrt{3}\right) U-5312 \sqrt{g H \left(H^2 k^2+3\right)\}\right) H^7-31104 \sqrt{g H^{\{13\}} \left(H^2 k^2+3\right)\} U^3\right) k^6+9 \left(-31231 \sqrt{3}\right) g^2 U H^6+2 g U^2 \left(34336 \sqrt{g H \left(H^2 k^2+3\right)\}-67003 \sqrt{3}\right) U\right) H^5+288 \left(162 \sqrt{g H^9 \left(H^2 k^2+3\right)\} U^4+5 \sqrt{g^5 H^{\{13\}} \left(H^2 k^2+3\right)\}\right) k^4+27 \left(-35319 \sqrt{3}\right) g^2 U H^4-91580 \sqrt{3}\right) g U^3 H^3+64 \left(486 \sqrt{g H^5 \left(H^2 k^2+3\right)\} U^4+1155 \sqrt{g^3 H^7 \left(H^2 k^2+3\right)\} U^2+59 \sqrt{g^5 H^9 \left(H^2 k^2+3\right)\}\right) k^2+243 \left(2592 \sqrt{g H \left(H^2 k^2+3\right)\} U^4+g H \left(8832 \sqrt{g H \left(H^2 k^2+3\right)\}-7823 \sqrt{3}\right) U\right) U^2-4423 \sqrt{3}\right) g^2 H^2 U+832 \sqrt{g^5 H^5 \left(H^2 k^2+3\right)\}\right) \text{ \text{dt}}^3\}\{30720 \sqrt{g H} \left(H^2 k^2+3\right)\}^{9/2}\}-\frac{\left(k^9 \left(\sqrt{3}\right) \sqrt{g H \left(H^2 k^2+3\right)\}-\left(H^2 k^2+3\right) U\right) \left(U^3 \left(42368 \sqrt{g H^{\{17\}} \left(H^2 k^2+3\right)\} U-111559 \sqrt{3}\right) g H^9\right) k^8-3 U \left(45573 \sqrt{3}\right) g^2 H^8+g U \left(456644 \sqrt{3}\right) U-108089 \sqrt{g H \left(H^2 k^2+3\right)\}\right) H^7-169472 \sqrt{g H^{\{13\}} \left(H^2 k^2+3\right)\} U^3\right) k^6+9 \left(-153703 \sqrt{3}\right) g^2 U H^6+g U^2 \left(347651 \sqrt{g H \left(H^2 k^2+3\right)\}-700818 \sqrt{3}\right) U\right) H^5+254208 \sqrt{g H^9 \left(H^2 k^2+3\right)\} U^4+7035 \sqrt{g^5 H^{\{13\}} \left(H^2 k^2+3\right)\}\right) \right)
\end{aligned}$$

$$\begin{aligned} & k^4 + 27 \sqrt[3]{-172047 \sqrt{3} g^2 U H^4 - 477940 \sqrt{3} g U^3 H^3 + 169472 \sqrt{3} g H^5 \sqrt[3]{H^2 k^2 + 3}} \\ & \sqrt[3]{U^4 + 372075 \sqrt{3} g^3 H^7 \sqrt[3]{H^2 k^2 + 3}} U^2 + 18078 \sqrt[3]{g^5 H^9 \sqrt[3]{H^2 k^2 + 3}} \\ & \sqrt[3]{k^2 + 81 \sqrt[3]{42368 \sqrt{3} g H \sqrt[3]{H^2 k^2 + 3}}} U^4 + g H \sqrt[3]{132513 \sqrt[3]{g H \sqrt[3]{H^2 k^2 + 3}}} \\ & - 122207 \sqrt[3]{3 U} U^2 - 63917 \sqrt[3]{3} g^2 H^2 U + 11603 \sqrt[3]{g^5 H^5 \sqrt[3]{H^2 k^2 + 3}} \\ & \sqrt[3]{\sqrt[3]{92160 \sqrt[3]{g H \sqrt[3]{H^2 k^2 + 3}}}^4} \sqrt[3]{\sqrt[3]{H^2 k^2 + 3}}^{\frac{11}{2}} \sqrt[3]{\sqrt[3]{\sqrt[3]{H^2 k^2 + 3}}^{\frac{11}{2}}}} + O(\sqrt[3]{\sqrt[3]{\sqrt[3]{H^2 k^2 + 3}}^5}) \sqrt[3]{\sqrt[3]{\sqrt[3]{H^2 k^2 + 3}}^4} + O(\sqrt[3]{\sqrt[3]{\sqrt[3]{H^2 k^2 + 3}}^5}) \sqrt[3]{\sqrt[3]{\sqrt[3]{H^2 k^2 + 3}}} \end{aligned}$$

Out[197]=

$$\begin{aligned} \text{Out[198]} = \text{EA} \parallel & \left\{ \left\{ 1 + \frac{i e^{\frac{i dx k}{2}} (1 - e^{-i dx k}) (-1 + e^{i dt w}) H^2 k^3 U \text{Csc}\left[\frac{dx k}{2}\right]}{(6 + 2 H^2 k^2) w}, \frac{i e^{\frac{i dx k}{2}} (1 - e^{-i dx k}) (-1 + e^{i dt w}) H k \text{Csc}\left[\frac{dx k}{2}\right]}{2 \left(H + \frac{H^3 k^2}{3}\right) w} \right\}, \right. \\ & \left. \left\{ \frac{i e^{\frac{i dx k}{2}} (1 - e^{-i dx k}) (-1 + e^{i dt w}) k (g H (3 + H^2 k^2) - 3 U^2) \text{Csc}\left[\frac{dx k}{2}\right]}{(6 + 2 H^2 k^2) w}, 1 + \frac{i e^{\frac{i dx k}{2}} (1 - e^{-i dx k}) (-1 + e^{i dt w}) k (6 + H^2 k^2) U \text{Csc}\left[\frac{dx k}{2}\right]}{(6 + 2 H^2 k^2) w} \right\} \right\} \end{aligned}$$

Out[199]=

$$\begin{aligned} \text{EA} \parallel & \left(\begin{array}{c} \frac{1}{\sqrt[3]{e^{\frac{i}{\sqrt[3]{\text{dx} k}} \sqrt[3]{k^2}}}} \sqrt[3]{\left(1 - e^{-i \sqrt[3]{\text{dx} k}}\right) \sqrt[3]{\left(-1 + e^{i \sqrt[3]{\text{dt} w}}\right) H^2 U \sqrt[3]{\left(\frac{\sqrt[3]{\text{dx} k}}{\sqrt[3]{k^2}}\right) k^3}} \sqrt[3]{\left(2 H^2 k^2 + 6\right) w} + 1}\right)} \\ & \& \frac{1}{\sqrt[3]{e^{\frac{i}{\sqrt[3]{\text{dx} k}} \sqrt[3]{k^2}}}} \sqrt[3]{\left(1 - e^{-i \sqrt[3]{\text{dx} k}}\right) \sqrt[3]{\left(-1 + e^{i \sqrt[3]{\text{dt} w}}\right) H k \sqrt[3]{\left(\frac{\sqrt[3]{\text{dx} k}}{\sqrt[3]{k^2}}\right)^2 \sqrt[3]{\left(k^2 H^3\right) \sqrt[3]{3} + H}} w}\right)} \\ & \frac{1}{\sqrt[3]{e^{\frac{i}{\sqrt[3]{\text{dx} k}} \sqrt[3]{k^2}}}} \sqrt[3]{\left(1 - e^{-i \sqrt[3]{\text{dx} k}}\right) \sqrt[3]{\left(-1 + e^{i \sqrt[3]{\text{dt} w}}\right) k \sqrt[3]{\left(g H \sqrt[3]{\left(H^2 k^2 + 3\right) - 3 U^2}\right) \sqrt[3]{\left(\frac{\sqrt[3]{\text{dx} k}}{\sqrt[3]{k^2}}\right) \sqrt[3]{\left(2 H^2 k^2 + 6\right) w}}\right)} \\ & \& \frac{1}{\sqrt[3]{e^{\frac{i}{\sqrt[3]{\text{dx} k}} \sqrt[3]{k^2}}}} \sqrt[3]{\left(1 - e^{-i \sqrt[3]{\text{dx} k}}\right) \sqrt[3]{\left(-1 + e^{i \sqrt[3]{\text{dt} w}}\right) k \sqrt[3]{\left(H^2 k^2 + 6\right) U \sqrt[3]{\left(\frac{\sqrt[3]{\text{dx} k}}{\sqrt[3]{k^2}}\right) \sqrt[3]{\left(2 H^2 k^2 + 6\right) w} + 1}\right)}} \end{array} \right) \end{aligned}$$

Out[200]=

$$\begin{aligned} \text{Err} \parallel & \left\{ \left(-\frac{H^2 k^3 U w}{2 (3 + H^2 k^2)} \frac{dt^2}{6 (3 + H^2 k^2)} + \frac{H^2 k^3 U w^3 dt^3}{24 (3 + H^2 k^2)} + O[dt]^5 \right) + \left(-\frac{1}{2} (k^2 U) dt + O[dt]^5 \right) dx + \left(\frac{i (9 H^2 k^5 + 2 H^4 k^7) U dt}{12 (3 + H^2 k^2)^2} + O[dt]^5 \right) \right. \\ & dx^2 + \left(\frac{1}{24} k^4 U dt + O[dt]^5 \right) dx^3 + \left(-\frac{i (54 H^2 k^7 + 19 H^4 k^9 + 2 H^6 k^{11}) U dt}{240 (3 + H^2 k^2)^3} + O[dt]^5 \right) dx^4 + O[dx]^5, \\ & \left(-\frac{3 (k w) dt^2}{2 (3 + H^2 k^2)} - \frac{i k w^2 dt^3}{2 (3 + H^2 k^2)} + \frac{k w^3 dt^4}{8 (3 + H^2 k^2)} + O[dt]^5 \right) + \left(\frac{i (6 k^3 + H^2 k^5) dt}{4 (3 + H^2 k^2)^2} + O[dt]^5 \right) dx^2 + \left(\frac{i (-54 k^5 + H^4 k^9) dt}{240 (3 + H^2 k^2)^3} + O[dt]^5 \right) dx^4 + \\ & O[dx]^5 \Bigg\}, \left\{ \left(-\frac{(k (3 g H + g H^3 k^2 - 3 U^2) w) dt^2}{2 (3 + H^2 k^2)} - \frac{i k (3 g H + g H^3 k^2 - 3 U^2) w^2 dt^3}{6 (3 + H^2 k^2)} + \frac{k (3 g H + g H^3 k^2 - 3 U^2) w^3 dt^4}{24 (3 + H^2 k^2)} + O[dt]^5 \right) + \right. \\ & \left(-\frac{1}{2} (g H k^2) dt + O[dt]^5 \right) dx + \left(\frac{i (18 g H k^3 + 12 g H^3 k^5 + 2 g H^5 k^7 - 18 k^3 U^2 - 3 H^2 k^5 U^2) dt}{12 (3 + H^2 k^2)^2} + O[dt]^5 \right) dx^2 + \\ & \left(\frac{1}{24} g H k^4 dt + O[dt]^5 \right) dx^3 + \left(-\frac{i (54 g H k^5 + 54 g H^3 k^7 + 18 g H^5 k^9 + 2 g H^7 k^{11} - 54 k^5 U^2 + H^4 k^9 U^2) dt}{240 (3 + H^2 k^2)^3} + O[dt]^5 \right) dx^4 + O[dx]^5, \\ & \left(-\frac{(k (6 + H^2 k^2) U w) dt^2}{2 (3 + H^2 k^2)} - \frac{i k (6 + H^2 k^2) U w^2 dt^3}{6 (3 + H^2 k^2)} + \frac{k (6 + H^2 k^2) U w^3 dt^4}{24 (3 + H^2 k^2)} + O[dt]^5 \right) + \left(-\frac{1}{2} (k^2 U) dt + O[dt]^5 \right) dx + \\ & \left(\frac{i (36 k^3 + 15 H^2 k^5 + 2 H^4 k^7) U dt}{12 (3 + H^2 k^2)^2} + O[dt]^5 \right) dx^2 + \left(\frac{1}{24} k^4 U dt + O[dt]^5 \right) dx^3 + \\ & \left(-\frac{i (108 k^5 + 54 H^2 k^7 + 17 H^4 k^9 + 2 H^6 k^{11}) U dt}{240 (3 + H^2 k^2)^3} + O[dt]^5 \right) dx^4 + O[dx]^5 \Bigg\} \end{aligned}$$

```

Out[201]= Eerr || \left(
\begin{array}{cc}
\left(-\frac{\left(H^2 k^3 U w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i}{H^2 k^3 U w^2} \text{dt}^3\right)\left\{6 \left(H^2 k^2+3\right)+\frac{H^2 k^3 U w^3}{\text{dt}^4}\right\} 24 \\
\left(H^2 k^2+3\right)+O\left(\text{dt}^5\right)\right) \text{right}+\left(-\frac{1}{2}\right) \left(k^2 U\right) \\
\text{dt}+O\left(\text{dt}^5\right)\right) \text{right} \text{dx}+\left(\frac{i}{\left(2 H^4 k^7+9 H^2 k^5\right) U}\right. \\
\left.\text{dt}\right)\left\{12 \left(H^2 k^2+3\right)^2+O\left(\text{dt}^5\right)\right\} \text{right} \text{dx}^2+\left(\frac{1}{24}\right) \\
k^4 U \text{dt}+O\left(\text{dt}^5\right)\right) \text{right} \text{dx}^3+\left(-\frac{i}{\left(2 H^6 k^{11}+19 H^4\right.}\right. \\
\left.k^9+54 H^2 k^7\right) U \text{dt}\left.\right)\left\{240 \left(H^2 k^2+3\right)^3+O\left(\text{dt}^5\right)\right\} \text{right} \\
\text{dx}^4+O\left(\text{dx}^5\right) \& \left(-\frac{3}{\left(k w\right) \text{dt}^2}\right) 2 \left(H^2\right. \\
\left.k^2+3\right)\left.\right)-\frac{i}{k w^2} \text{dt}^3\left\{2 \left(H^2 k^2+3\right)+\frac{k w^3}{\text{dt}^4}\right\} 8 \left(H^2\right. \\
\left.k^2+3\right)\left.\right)+O\left(\text{dt}^5\right)\right) \text{right}+\left(\frac{i}{\left(H^2 k^5+6 k^3\right) \text{dt}}\right)\left\{4 \left(H^2\right.}\right. \\
\left.k^2+3\right)^2+O\left(\text{dt}^5\right)\right\} \text{right} \text{dx}^2+\left(\frac{i}{\left(H^4 k^9-54 k^5\right)}\right. \\
\left.\text{dt}\right)\left\{240 \left(H^2 k^2+3\right)^3+O\left(\text{dt}^5\right)\right\} \text{right} \text{dx}^4+O\left(\text{dx}^5\right) \backslash \\
\left(-\frac{\left(k \left(g k^2 H^3+3 g H-3 U^2\right) w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i}{k \left(g\right.}\right. \\
\left.k^2 H^3+3 g H-3 U^2\right) w^2} \text{dt}^3\left.\right)\left\{6 \left(H^2 k^2+3\right)+\frac{k \left(g k^2 H^3+3 g H-3\right.}\right. \\
\left.U^2\right) w^3}{\text{dt}^4}\left.\right\} 24 \left(H^2 k^2+3\right)+O\left(\text{dt}^5\right)\right) \text{right}+\left(-\frac{1}{2}\right) \left(g H\right. \\
\left.k^2\right) \text{dt}+O\left(\text{dt}^5\right)\right) \text{right} \text{dx}+\left(\frac{i}{\left(2 g H^5 k^7+12 g H^3 k^5-3 H^2\right.}\right. \\
\left.U^2 k^5-18 U^2 k^3+18 g H k^3\right) \text{dt}\left.\right)\left\{12 \left(H^2 k^2+3\right)^2+O\left(\text{dt}^5\right)\right\} \text{right} \\
\text{dx}^2+\left(\frac{1}{24}\right) g H k^4 \text{dt}+O\left(\text{dt}^5\right)\right) \text{right} \text{dx}^3+\left(-\frac{i}{\left(2 g H^7 k^{11}+18 g H^5 k^9+H^4 U^2 k^9+54 g H^3 k^7-54 U^2 k^5+54 g H k^5\right)}\right. \\
\left.\text{dt}\right)\left\{240 \left(H^2 k^2+3\right)^3+O\left(\text{dt}^5\right)\right\} \text{right} \text{dx}^4+O\left(\text{dx}^5\right) \& \\
\left(-\frac{\left(k \left(H^2 k^2+6\right) U w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i}{k \left(H^2 k^2+6\right) U w^2} \text{dt}^3\right)\left\{6 \left(H^2 k^2+3\right)+\frac{k \left(H^2 k^2+6\right)}{U w^3} \text{dt}^4\right\} 24 \left(H^2 k^2+3\right)+O\left(\text{dt}^5\right)\right) \text{right}+\left(-\frac{1}{2}\right) \\
\left(k^2 U\right) \text{dt}+O\left(\text{dt}^5\right)\right) \text{right} \text{dx}+\left(\frac{i}{\left(2 H^4 k^7+15\right.}\right. \\
\left.H^2 k^5+36 k^3\right) U \text{dt}\left.\right)\left\{12 \left(H^2 k^2+3\right)^2+O\left(\text{dt}^5\right)\right\} \text{right} \\
\text{dx}^2+\left(\frac{1}{24}\right) k^4 U \text{dt}+O\left(\text{dt}^5\right)\right) \text{right} \text{dx}^3+\left(-\frac{i}{\left(2 H^6 k^{11}+17 H^4 k^9+54 H^2 k^7+108 k^5\right) U}\right. \\
\left.\text{dt}\right)\left\{240 \left(H^2\right.}\right. \\
\left.k^2+3\right)^3+O\left(\text{dt}^5\right)\right\} \text{right} \text{dx}^4+O\left(\text{dx}^5\right) \backslash \\
\end{array}
\right)

```

```

In[202]:= KurF = (fm*ap - fp*am + am*ap*(qp - qm)) / (ap - am);
KurFWS = KurF /. ap -> 0 /. am -> (U - Sqrt[g*H]);
KurFWSeta =
  KurFWS /. fp -> (H*v + U*Rpp*n) /. fm -> (H*v + U*Rmp*n) /. qp -> Rpp*n /.
  qm -> Rmp*n;
KurFWSeta = KurFWSeta /. v -> (GGp*G + Gnp*n);
Kfnnp = FullSimplify[KurFWSeta /. G -> 0 /. n -> 1];
KfnGp = FullSimplify[KurFWSeta /. n -> 0 /. G -> 1];
Kfnn = Kfnnp /. Rpp -> Rp /. Rmp -> Rm /. GGp -> GG2 /. Gnp -> Gn2;
KfnG = KfnGp /. Rpp -> Rp /. Rmp -> Rm /. GGp -> GG2 /. Gnp -> Gn2;

```

```

Fnn2 = -dt * (1 - Exp[-I * k * dx]) / dx * Kfnn;
Fnn2TA = Series[Fnn2 - FnnA, {dx, 0, 3}, {dt, 0, 3}];
Fnn2TAr = Refine[Fnn2TA, {k > 0, U > 0, H > 0, g > 0}];
FnG2 = -dt * (1 - Exp[-I * k * dx]) / dx * KfnG;
FnG2TA = Series[FnG2 - FnGA, {dx, 0, 3}, {dt, 0, 3}];
FnG2TAr = Refine[FnG2TA, {k > 0, U > 0, H > 0, g > 0}];

KurFWSG = KurFWS /. fp → (U * Rpp * G + U * H * v + g * H * Rpp * n) /.
  fm → (U * Rmp * G + U * H * v + g * H * Rmp * n) /. qp → Rpp * G /. qm → Rmp * G;
KurFWSG = KurFWSG /. v → (GGp * G + Gnp * n);
KfGnp = FullSimplify[KurFWSG /. G → 0 /. n → 1];
KfGGp = FullSimplify[KurFWSG /. n → 0 /. G → 1];
KfGn = KfGnp /. Rpp → Rp /. Rmp → Rm /. GGp → GG2 /. Gnp → Gn2;
KfGG = KfGGp /. Rpp → Rp /. Rmp → Rm /. GGp → GG2 /. Gnp → Gn2;

FGn2 = -dt * (1 - Exp[-I * k * dx]) / dx * KfGn;
FGn2TA = Series[FGn2 - FGnA, {dx, 0, 3}, {dt, 0, 3}];
FGn2TAr = Refine[FGn2TA, {k > 0, U > 0, H > 0, g > 0}];
fGG2 = U * H * GG2 + U / 2 * (Rm + Rp) - (Sqrt[g * H]) / (2) * (Rp - Rm);
FGG2 = -dt * (1 - Exp[-I * k * dx]) / dx * KfGG;
FGG2TA = Series[FGG2 - FGGA, {dx, 0, 4}, {dt, 0, 3}];
FGG2TAr = Refine[FGG2TA, {k > 0, U > 0, H > 0, g > 0}];
Fmat2 = {{Fnn2, FnG2}, {FGn2, FGG2}};
Emat2 = IdentityMatrix[2] + Fmat2;
Eerr = Series[Emat2 - EA, {dx, 0, 4}, {dt, 0, 4}];
EigvFmat2 = Eigenvalues[Fmat2];

RKStep = Log[1 + EigvFmat2] / (I * dt);
RKstepTay = Series[RKStep, {dx, 0, 4}, {dt, 0, 4}];
RKstepTayr = Simplify[-RKstepTay - {wAp, wAm}, {k > 0, H > 0, g > 0, U > 0}];

Text[Row[{" U < -Sqrt(gH)"}]]
Text[" "]
Text[Row[{"Fnn  ||  ", Kfnnp}]]
Text[Row[{"Fnn  ||  ", TeXForm[Kfnnp]}]]
Text[Row[{"Fnn error  ||  ", Fnn2TAr}]]
Text[Row[{"Fnn error  ||  ", TeXForm[Fnn2TAr]}]]
Text[" "]
Text[Row[{"FnG  ||  ", KfnGp}]]
Text[Row[{"FnG  ||  ", TeXForm[KfnGp]}]]
Text[Row[{"FnG error  ||  ", FnG2TAr}]]
Text[Row[{"FnG error  ||  ", TeXForm[FnG2TAr]}]]

```



```

Text[" "]
Text[Row[{"FGn  ||  ", KfGnp}]]
Text[Row[{"FGn  ||  ", TeXForm[KfGnp]}]]
Text[Row[{"FGn error  ||  ", FGn2TAr}]]
Text[Row[{"FGn error  ||  ", TeXForm[FGn2TAr]}]]
Text[" "]
Text[Row[{"FGG  ||  ", KfGGp}]]
Text[Row[{"FGG  ||  ", TeXForm[KfGGp]}]]
Text[Row[{"FGG error  ||  ", FGG2TAr}]]
Text[Row[{"FGG error  ||  ", TeXForm[FGG2TAr]}]]
Text[" "]
Text[" "]
Text[Row[{"Omega error  ||  ", RKstepTayr}]]
Text[Row[{"Omega error  ||  ", TeXForm[RKstepTayr]}]]
Text[" "]
Text[Row[{"EA  ||  ", EA}]]
Text[Row[{"EA  ||  ", TeXForm[EA]}]]
Text[Row[{"Eerr  ||  ", Eerr}]]
Text[Row[{"Eerr  ||  ", TeXForm[Eerr]}]]

```

Out[236]= $U < -\text{Sqrt}(gH)$

Out[237]=

Out[238]= $F_{nn} \parallel G_{np} H + R_{pp} U$

Out[239]= $F_{nn} \parallel \text{\texttt{\text{Gnp}}} H + \text{\texttt{\text{Rpp}}} U$

Out[240]= $F_{nn} \text{ error } \parallel \left(-\frac{(H^2 k^3 U w) dt^2}{2(3+H^2 k^2)} - \frac{i H^2 k^3 U w^2 dt^3}{6(3+H^2 k^2)} + O[dt]^4 \right) + \left(\frac{1}{2} k^2 U dt + O[dt]^4 \right) dx +$
 $\left(\frac{i(9 H^2 k^5 + 2 H^4 k^7) U dt}{12(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + \left(-\frac{1}{24} (k^4 U) dt + O[dt]^4 \right) dx^3 + O[dx]^4$

Out[241]= $F_{nn} \text{ error } \parallel$
 $\text{\texttt{\text{left}}}(-\frac{\text{\texttt{\text{dt}}}^2 \text{\texttt{\text{left}}}(H^2 k^3 U w \text{\texttt{\text{right}}})}{2 \text{\texttt{\text{left}}}(H^2 k^2 + 3 \text{\texttt{\text{right}}})} - \frac{i \text{\texttt{\text{dt}}}^3 H^2 k^3 U w^2}{6 \text{\texttt{\text{left}}}(H^2 k^2 + 3 \text{\texttt{\text{right}}})} + O(\text{\texttt{\text{dt}}}^4 \text{\texttt{\text{right}}}) + \text{\texttt{\text{dx}}} \text{\texttt{\text{left}}}(\frac{1}{2} k^2 U$
 $\text{\texttt{\text{dt}}} + O(\text{\texttt{\text{dt}}}^4 \text{\texttt{\text{right}}}) + \text{\texttt{\text{dx}}}^2 \text{\texttt{\text{left}}}(\frac{i \text{\texttt{\text{left}}}(2 H^4 k^7 + 9 H^2$
 $k^5 \text{\texttt{\text{right}}}) U \text{\texttt{\text{dt}}}}{12 \text{\texttt{\text{left}}}(H^2 k^2 + 3 \text{\texttt{\text{right}}})^2} + O(\text{\texttt{\text{dt}}}^4 \text{\texttt{\text{right}}}) + \text{\texttt{\text{dx}}}^3$
 $\text{\texttt{\text{left}}}(-\frac{1}{24} \text{\texttt{\text{left}}}(k^4 U \text{\texttt{\text{right}}}) \text{\texttt{\text{dt}}} + O(\text{\texttt{\text{dt}}}^4 \text{\texttt{\text{right}}}) + O(\text{\texttt{\text{dx}}}^4 \text{\texttt{\text{right}}})$

Out[242]=

Out[243]= $F_{nG} \parallel G_{Gp} H$

Out[244]= $F_{nG} \parallel \text{\texttt{\text{GGp}}} H$

Out[245]= $F_{nG} \text{ error } \parallel \left(-\frac{3(k w) dt^2}{2(3+H^2 k^2)} - \frac{i k w^2 dt^3}{2(3+H^2 k^2)} + O[dt]^4 \right) + \left(\frac{i(6 k^3 + H^2 k^5) dt}{4(3+H^2 k^2)^2} + O[dt]^4 \right) dx^2 + O[dx]^4$

$$\text{Out[246]= FNg error} \parallel \left(-\frac{3}{2} \frac{\text{dt}^2 (k w)}{\left(H^2 k^2 + 3 \right)} - \frac{i}{6} \frac{\text{dt}^3 k w^2}{\left(H^2 k^2 + 3 \right)} + O\left(\frac{\text{dt}^4}{\left(H^2 k^2 + 3 \right)} \right) + \text{dx}^2 \frac{i}{12} \frac{\left(H^2 k^5 + 6 k^3 \right)}{\left(H^2 k^2 + 3 \right)} + O\left(\frac{\text{dt}^4}{\left(H^2 k^2 + 3 \right)} \right) + O\left(\frac{\text{dx}^4}{\left(H^2 k^2 + 3 \right)} \right) \right)$$

Out[247]=

$$\text{Out[248]= FGn} \parallel H (g \text{Rpp} + \text{Gnp} U)$$

$$\text{Out[249]= FGn} \parallel H (g \text{Rpp} + \text{Gnp} U)$$

$$\text{Out[250]= FGn error} \parallel \left(-\frac{(k(3gH+gH^3k^2-3U^2)w)dt^2}{2(3+H^2k^2)} - \frac{ik(3gH+gH^3k^2-3U^2)w^2dt^3}{6(3+H^2k^2)} + O[dt]^4 \right) + \left(\frac{1}{2} g H k^2 dt + O[dt]^4 \right) dx + \left(\frac{i(18gHk^3+12gH^3k^5+2gH^5k^7-18k^3U^2-3H^2k^5U^2)dt}{12(3+H^2k^2)^2} + O[dt]^4 \right) dx^2 + \left(-\frac{1}{24} (g H k^4) dt + O[dt]^4 \right) dx^3 + O[dx]^4$$

$$\text{Out[251]= FGn error} \parallel$$

$$\left(-\frac{\text{dt}^2 (k w \left(g H^3 k^2 + 3 g H - 3 U^2 \right))}{6 \left(H^2 k^2 + 3 \right)} - \frac{i}{12} \frac{\text{dt}^3 k w^2 \left(g H^3 k^2 + 3 g H - 3 U^2 \right)}{\left(H^2 k^2 + 3 \right)} + O\left(\frac{\text{dt}^4}{\left(H^2 k^2 + 3 \right)} \right) + \text{dx}^2 \frac{i}{12} \frac{\left(2 g H^5 k^7 + 12 g H^3 k^5 - 3 H^2 U^2 k^5 - 18 U^2 k^3 + 18 g H k^3 \right)}{\left(H^2 k^2 + 3 \right)} + O\left(\frac{\text{dt}^4}{\left(H^2 k^2 + 3 \right)} \right) + \text{dx}^3 \frac{i}{24} \left(-\frac{1}{24} \right) \left(g H k^4 \right) dt + O[dt]^4 \right) dx^3 + O[dx]^4$$

Out[252]=

$$\text{Out[253]= FGG} \parallel (G \text{Gp} H + \text{Rpp}) U$$

$$\text{Out[254]= FGG} \parallel U (\text{GGp} H + \text{Rpp})$$

$$\text{Out[255]= FGG error} \parallel$$

$$\left(-\frac{(k(6+H^2k^2)Uw)dt^2}{2(3+H^2k^2)} - \frac{ik(6+H^2k^2)Uw^2dt^3}{6(3+H^2k^2)} + O[dt]^4 \right) + \left(\frac{1}{2} k^2 U dt + O[dt]^4 \right) dx + \left(\frac{i(36k^3+15H^2k^5+2H^4k^7)Udt}{12(3+H^2k^2)^2} + O[dt]^4 \right) dx^2 + \left(-\frac{1}{24} (k^4 U) dt + O[dt]^4 \right) dx^3 + \left(-\frac{i(108k^5+54H^2k^7+17H^4k^9+2H^6k^{11})Udt}{240(3+H^2k^2)^3} + O[dt]^4 \right) dx^4 + O[dx]^5$$

$$\text{Out[256]= FGG error} \parallel$$

$$\left(-\frac{\text{dt}^2 (k U w \left(H^2 k^2 + 6 \right))}{6 \left(H^2 k^2 + 3 \right)} - \frac{i}{12} \frac{\text{dt}^3 k U w^2 \left(H^2 k^2 + 6 \right)}{\left(H^2 k^2 + 3 \right)} + O\left(\frac{\text{dt}^4}{\left(H^2 k^2 + 3 \right)} \right) + \text{dx}^2 \frac{i}{12} \frac{\left(2 H^4 k^7 + 15 H^2 k^5 + 36 k^3 \right) U}{\left(H^2 k^2 + 3 \right)} + O\left(\frac{\text{dt}^4}{\left(H^2 k^2 + 3 \right)} \right) + \text{dx}^3 \frac{i}{24} \left(-\frac{1}{24} \right) \left(k^4 U \right) dt + O[dt]^4 \right) dx^3 + \left(-\frac{i}{240} \frac{\left(2 H^6 k^{11} + 17 H^4 k^9 + 54 H^2 k^7 + 108 k^5 \right) U}{\left(H^2 k^2 + 3 \right)} + O\left(\frac{\text{dt}^4}{\left(H^2 k^2 + 3 \right)} \right) + O\left(\frac{\text{dx}^5}{\left(H^2 k^2 + 3 \right)} \right) \right) dx^4 + O[dx]^5$$

Out[257]=

Out[258]=

$$\text{Out[259]= Omega error} \parallel \left\{ \frac{i \left(\sqrt{3} k \sqrt{g H (3+H^2 k^2)} + 3 k U + H^2 k^3 U \right)^2 dt}{2 (3+H^2 k^2)^2} - \frac{1}{3 (3+H^2 k^2)^2} \right\}$$

$$\begin{aligned}
& \left[\left(k^3 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(3 g H + U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) \right) dt^2 - \right. \\
& \frac{1}{4(3 + H^2 k^2)^3} i k^4 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(3 g \left(\sqrt{3} H \sqrt{g H (3 + H^2 k^2)} + 9 H U + 3 H^3 k^2 U \right) + \right. \\
& \left. U^2 \left(H^4 k^4 U + 9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + U \right) + 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 2 H^2 U \right) \right) \right) dt^3 + \\
& \frac{1}{5(3 + H^2 k^2)^3} k^5 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(9 g^2 H^2 + 6 g H U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + 2 k^2 \left(2 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 3 H^2 U \right) \right) \right) dt^4 + \\
& \left. O[dt]^5 \right] + \left(\frac{1}{4} i k^2 \left(\sqrt{3} \sqrt{\frac{g H}{3 + H^2 k^2}} + 2 U \right) - \frac{\left(k^3 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) \right) dt}{4 \left(\sqrt{g H (3 + H^2 k^2)} \right)^{3/2}} - \right. \\
& \left(i k^4 \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g H + U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) dt^2 \right) / \\
& \left(4 \sqrt{g H (3 + H^2 k^2)}^{3/2} \right) + \\
& \left(k^5 \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g \left(\sqrt{3} H \sqrt{g H (3 + H^2 k^2)} + 9 H U + 3 H^3 k^2 U \right) + \right. \\
& \left. U^2 \left(H^4 k^4 U + 9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + U \right) + 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 2 H^2 U \right) \right) \right) dt^3 \right) / \\
& \left(4 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) + \left(i k^6 \left(\sqrt{3} g H + 2 \sqrt{g H (3 + H^2 k^2)} U \right) \right. \\
& \left(9 g^2 H^2 + 6 g H U \left(2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + 2 k^2 \left(2 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 3 H^2 U \right) \right) \right) \\
& \left. dt^4 \right) / \left(4 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) + O[dt]^5 \Bigg] dx + \\
& \left(- \left(\left(k^3 \left(3 \sqrt{3} g H (13 + 3 H^2 k^2) + 16 \left(3 \sqrt{g H (3 + H^2 k^2)} + k^2 \sqrt{g H^5 (3 + H^2 k^2)} \right) U \right) \right) / \right. \right. \\
& \left. \left(96 \left(\sqrt{g H (3 + H^2 k^2)}^{3/2} \right) \right) \right) - \\
& \left(i k^4 \left(g H \left(144 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (369 + 234 H^2 k^2 + 37 H^4 k^4) U \right) + 4 \left(63 \sqrt{g H (3 + H^2 k^2)} U^2 + \right. \right. \\
& \left. \left. 7 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 14 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) \\
& dt \right) / \left(96 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) + \left(k^5 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right. \\
& \left(g H \left(171 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (477 + 306 H^2 k^2 + 49 H^4 k^4) U \right) + 5 \left(72 \sqrt{g H (3 + H^2 k^2)} U^2 + \right. \right. \\
& \left. \left. 8 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 16 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) \\
& dt^2 \Bigg) / \left(96 \sqrt{g H (3 + H^2 k^2)}^{7/2} \right) + \left(i k^6 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right)^2
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{d^4}{dt^4} \left(\sqrt{g H (3 + H^2 k^2)} U^2 + 52 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \\
& \quad \left. \left. g H \left(198 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (585 + 378 H^2 k^2 + 61 H^4 k^4) U \right) + \right. \right. \\
& \quad \left. \left. 6 k^2 \left(9 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 52 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) dt^3 \right) / \left(96 \sqrt{g H (3 + H^2 k^2)}^{9/2} \right) - \\
& \left(\left(k^7 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right)^3 \left(576 \sqrt{g H (3 + H^2 k^2)} U^2 + 64 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \right. \\
& \quad \left. \left. g H \left(225 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (693 + 450 H^2 k^2 + 73 H^4 k^4) U \right) + \right. \right. \\
& \quad \left. \left. 3 k^2 \left(21 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 128 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) \\
& \quad \left. dt^4 \right) / \left(96 \left(\sqrt{g H (3 + H^2 k^2)}^{11/2} \right) + O[dt]^5 \right) dx^2 + \\
& \left(- \left(\left(i k^4 \left(\sqrt{3} g H (33 + 7 H^2 k^2) + 16 \left(3 \sqrt{g H (3 + H^2 k^2)} + k^2 \sqrt{g H^5 (3 + H^2 k^2)} \right) U \right) \right) / \right. \right. \\
& \quad \left. \left(384 \sqrt{g H (3 + H^2 k^2)}^{3/2} \right) \right) + \\
& \quad \left(k^5 \left(g H \left(72 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (207 + 126 H^2 k^2 + 19 H^4 k^4) U \right) + \right. \right. \\
& \quad \left. \left. 16 \left(9 \sqrt{g H (3 + H^2 k^2)} U^2 + k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \right. \\
& \quad \left. \left. k^2 \left(\sqrt{g^3 H^7 (3 + H^2 k^2)} + 6 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt \right) / \left(128 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) + \\
& \quad \left(i k^6 \left(9 \sqrt{3} g^2 H^2 (13 + 3 H^2 k^2) + 5 g H U \left(96 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (129 + 82 H^2 k^2 + 13 H^4 k^4) U \right) + \right. \right. \\
& \quad \left. \left. 32 \left(9 \sqrt{g H (3 + H^2 k^2)} U^3 + k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 2 k^2 \left(2 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + \right. \right. \right. \\
& \quad \left. \left. \left. 3 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) dt^2 \right) / \left(128 \sqrt{g H (3 + H^2 k^2)}^{5/2} \right) - \\
& \quad \left(\left(k^7 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(24 \sqrt{3} g^2 H^2 (21 + 5 H^2 k^2) + \right. \right. \right. \\
& \quad \left. \left. 3 g H U \left(717 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1011 + 646 H^2 k^2 + 103 H^4 k^4) U \right) + \right. \right. \\
& \quad \left. \left. 5 \left(288 \sqrt{g H (3 + H^2 k^2)} U^3 + 32 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + \right. \right. \right. \\
& \quad \left. \left. \left. 3 k^2 \left(39 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 64 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) \right) dt^3 \right) / \\
& \quad \left(384 \left(\sqrt{g H (3 + H^2 k^2)}^{7/2} \right) \right) - \left(i k^8 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right)^2 \right. \\
& \quad \left(5 \sqrt{3} g^2 H^2 (45 + 11 H^2 k^2) + 720 \sqrt{g H (3 + H^2 k^2)} U^3 + 80 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + \right. \\
& \quad \left. g H U \left(990 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1449 + 930 H^2 k^2 + 149 H^4 k^4) U \right) + \right. \\
& \quad \left. \left. 2 k^2 \left(137 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 240 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) \\
& \quad \left. dt^4 \right) / \left(128 \sqrt{g H (3 + H^2 k^2)}^{9/2} \right) + O[dt]^5 \Big) dx^3 + \\
& \left(\left(k^5 \left(3 \sqrt{3} g H (543 + 146 H^2 k^2 + 15 H^4 k^4) + 256 \left(9 \sqrt{g H (3 + H^2 k^2)} + 6 k^2 \sqrt{g H^5 (3 + H^2 k^2)} + \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& k^4 \sqrt{g H^9 (3 + H^2 k^2)} U \Big) \Big) \Big/ \Big(30720 \sqrt{g H (3 + H^2 k^2)^{5/2}} + \\
& \Big(i k^6 \Big(3 g H \Big(18432 \sqrt{g H (3 + H^2 k^2)} + 51039 \sqrt{3} U + 45735 \sqrt{3} H^2 k^2 U + \\
& 1381 \sqrt{3} H^6 k^6 U + k^4 \Big(960 \sqrt{g H^9 (3 + H^2 k^2)} + 13717 \sqrt{3} H^4 U \Big) \Big) + \\
& 128 \Big(837 \sqrt{g H (3 + H^2 k^2)} U^2 + 279 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 31 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} U^2 + \\
& 27 k^2 \Big(7 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 31 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \Big) \Big) \Big) \Big) \Big/ \\
& \Big(92160 \sqrt{g H (3 + H^2 k^2)^{7/2}} \Big) - \Big(\Big(k^7 \Big(9 \sqrt{3} g^2 H^2 (12999 + 6258 H^2 k^2 + 775 H^4 k^4) + \\
& g H U \Big(617661 \sqrt{3} H^2 k^2 U + 20551 \sqrt{3} H^6 k^6 U + 81 \Big(5888 \sqrt{g H (3 + H^2 k^2)} + \\
& 8053 \sqrt{3} U \Big) + 3 k^4 \Big(12288 \sqrt{g H^9 (3 + H^2 k^2)} + 65021 \sqrt{3} H^4 U \Big) \Big) + \\
& 128 \Big(2322 \sqrt{g H (3 + H^2 k^2)} U^3 + 774 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 86 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} \\
& U^3 + 9 k^2 \Big(229 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 258 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \Big) \Big) \Big) \Big) \\
& dt^2 \Big) \Big/ \Big(92160 \Big(\sqrt{g H (3 + H^2 k^2)^{7/2}} \Big) \Big) - \frac{1}{30720 \sqrt{g H (3 + H^2 k^2)^{9/2}}} \\
& i k^8 \Big(k^8 U^3 \Big(21253 \sqrt{3} g H^9 + 7776 \sqrt{g H^{17} (3 + H^2 k^2)} U \Big) + \\
& 243 \Big(832 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 4423 \sqrt{3} g^2 H^2 U + 2592 \sqrt{g H (3 + H^2 k^2)} U^4 + \\
& g H U^2 \Big(8832 \sqrt{g H (3 + H^2 k^2)} + 7823 \sqrt{3} U \Big) \Big) + 3 k^6 U \Big(9181 \sqrt{3} g^2 H^8 + \\
& 31104 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + 4 g H^7 U \Big(5312 \sqrt{g H (3 + H^2 k^2)} + 21787 \sqrt{3} U \Big) \Big) + \\
& 27 k^2 \Big(35319 \sqrt{3} g^2 H^4 U + 91580 \sqrt{3} g H^3 U^3 + \\
& 64 \Big(59 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 1155 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 486 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \Big) \Big) + \\
& 9 k^4 \Big(31231 \sqrt{3} g^2 H^6 U + 2 g H^5 U^2 \Big(34336 \sqrt{g H (3 + H^2 k^2)} + 67003 \sqrt{3} U \Big) + \\
& 288 \Big(5 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 162 \sqrt{g H^9 (3 + H^2 k^2)} U^4 \Big) \Big) \Big) dt^3 + \\
& \frac{1}{92160 \sqrt{g H (3 + H^2 k^2)^{11/2}}} k^9 \Big(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \Big) \\
& \Big(k^8 U^3 \Big(111559 \sqrt{3} g H^9 + 42368 \sqrt{g H^{17} (3 + H^2 k^2)} U \Big) + \\
& 27 k^2 \Big(18078 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 172047 \sqrt{3} g^2 H^4 U + 372075 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + \\
& 477940 \sqrt{3} g H^3 U^3 + 169472 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \Big) + \\
& 81 \Big(11603 \sqrt{g^5 H^5 (3 + H^2 k^2)} + 63917 \sqrt{3} g^2 H^2 U + 42368 \sqrt{g H (3 + H^2 k^2)} U^4 + \\
& g H U^2 \Big(132513 \sqrt{g H (3 + H^2 k^2)} + 122207 \sqrt{3} U \Big) \Big) + 3 k^6 U \Big(45573 \sqrt{3} g^2 H^8 + \\
& 169472 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + g H^7 U \Big(108089 \sqrt{g H (3 + H^2 k^2)} + 456644 \sqrt{3} U \Big) \Big) + \\
& 914 \Big(7695 \sqrt{g^5 H^{13} (3 + H^2 k^2)} + 152763 \sqrt{3} g^2 H^6 U + 254288 \sqrt{g H^9 (3 + H^2 k^2)} U^4 +
\end{aligned}$$

$$\begin{aligned}
& 9 K^2 \left(7055 \sqrt{g H^2 (3 + H^2 k^2)} + 155705 \sqrt{3} \sqrt{g H^2 (3 + H^2 k^2)} U + 254208 \sqrt{g H^2 (3 + H^2 k^2)} U^2 + \right. \\
& \left. g H^5 U^2 \left(347651 \sqrt{g H (3 + H^2 k^2)} + 700818 \sqrt{3} U \right) \right) dt^4 + O[dt]^5 \Big) dx^4 + O[dx]^5, \\
& \left(\frac{i \left(-\sqrt{3} k \sqrt{g H (3 + H^2 k^2)} + 3 k U + H^2 k^3 U \right)^2 dt}{2 (3 + H^2 k^2)^2} - \frac{1}{3 (3 + H^2 k^2)^2} \left(k^3 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right. \right. \\
& \left. \left(3 g H + U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) \right) dt^2 - \\
& \frac{1}{4 (3 + H^2 k^2)^3} i k^4 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(3 g H \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^2 \left(-9 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U - 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} - 2 H^2 U \right) \right) \right) dt^3 + \\
& \frac{1}{5 (3 + H^2 k^2)^3} k^5 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \\
& \left(9 g^2 H^2 + 6 g H U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(-12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + k^2 \left(-4 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 6 H^2 U \right) \right) \right) dt^4 + O[\\
& dt]^5 \Big) + \\
& \left(-\frac{1}{4} i k^2 \left(\sqrt{3} \sqrt{\frac{g H}{3 + H^2 k^2}} - 2 U \right) + \frac{k^3 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) dt}{4 \sqrt{g H} (3 + H^2 k^2)^{3/2}} + \right. \\
& \left(i k^4 \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g H + U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \right) dt^2 \right) / \\
& \left(4 \sqrt{g H} (3 + H^2 k^2)^{3/2} \right) - \\
& \left(k^5 \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) \left(3 g H \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \right. \\
& \left. \left. U^2 \left(-9 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U - 3 k^2 \left(\sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} - 2 H^2 U \right) \right) \right) \right) \\
& dt^3 \Big) / \left(4 \left(\sqrt{g H} (3 + H^2 k^2)^{5/2} \right) \right) - \left(i k^6 \left(\sqrt{3} g H - 2 \sqrt{g H (3 + H^2 k^2)} U \right) \right. \\
& \left(9 g^2 H^2 + 6 g H U \left(-2 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 3 (3 + H^2 k^2) U \right) + \right. \\
& \left. U^3 \left(-12 \sqrt{3} \sqrt{g H (3 + H^2 k^2)} + 9 U + H^4 k^4 U + k^2 \left(-4 \sqrt{3} \sqrt{g H^5 (3 + H^2 k^2)} + 6 H^2 U \right) \right) \right) \\
& dt^4 \Big) / \left(4 \sqrt{g H} (3 + H^2 k^2)^{5/2} \right) + O[dt]^5 \Big) dx + \\
& \left(k^3 \left(3 \sqrt{3} g H (13 + 3 H^2 k^2) - 16 \left(3 \sqrt{g H (3 + H^2 k^2)} U + k^2 \sqrt{g H^5 (3 + H^2 k^2)} U \right) \right) \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{\sqrt{96 \sqrt{g H (3 + H^2 k^2)^{3/2}}}}{96 \sqrt{g H (3 + H^2 k^2)^{3/2}}} \right) + \\
& \left(i k^4 \left(g H \left(-144 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (369 + 234 H^2 k^2 + 37 H^4 k^4) U \right) - \right. \right. \\
& \quad 4 \left(63 \sqrt{g H (3 + H^2 k^2)} U^2 + 7 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \\
& \quad \left. \left. 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 14 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) - \\
& \left(\left(k^5 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right) \left(g H \left(171 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} (477 + 306 H^2 k^2 + \right. \right. \right. \\
& \quad \left. \left. 49 H^4 k^4) U \right) + 5 \left(72 \sqrt{g H (3 + H^2 k^2)} U^2 + 8 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \\
& \quad \left. \left. 3 k^2 \left(3 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 16 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt \Big/ \right. \\
& \left(96 \left(\sqrt{g H (3 + H^2 k^2)^{7/2}} \right) \right) + \left(i k^6 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right)^2 \right. \\
& \quad \left(468 \sqrt{g H (3 + H^2 k^2)} U^2 + 52 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \\
& \quad g H \left(198 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} (585 + 378 H^2 k^2 + 61 H^4 k^4) U \right) + \\
& \quad \left. \left. 6 k^2 \left(9 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 52 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt^3 \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{9/2}} \right) + \\
& \left(k^7 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right)^3 \left(576 \sqrt{g H (3 + H^2 k^2)} U^2 + 64 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + \right. \right. \\
& \quad g H \left(225 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} (693 + 450 H^2 k^2 + 73 H^4 k^4) U \right) + \\
& \quad \left. \left. 3 k^2 \left(21 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 128 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt^4 \Big/ \left(96 \sqrt{g H (3 + H^2 k^2)^{11/2}} \right) + \\
& \left. O[dt]^5 \right) dx^2 + \left(\frac{i k^4 \left(\sqrt{3} g H (33 + 7 H^2 k^2) - 16 \left(3 \sqrt{g H (3 + H^2 k^2)} U + k^2 \sqrt{g H^5 (3 + H^2 k^2)} U \right) \right)}{384 \sqrt{g H (3 + H^2 k^2)^{3/2}}} \right) + \\
& \left(k^5 \left(g H \left(72 \sqrt{g H (3 + H^2 k^2)} - \sqrt{3} (207 + 126 H^2 k^2 + 19 H^4 k^4) U \right) + 16 \left(9 \sqrt{g H (3 + H^2 k^2)} U^2 + \right. \right. \right. \\
& \quad \left. \left. k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + k^2 \left(\sqrt{g^3 H^7 (3 + H^2 k^2)} + 6 \sqrt{g H^5 (3 + H^2 k^2)} U^2 \right) \right) \right) dt \Big/ \right. \\
& \left(128 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) + \left(i k^6 \left(-9 \sqrt{3} g^2 H^2 (13 + 3 H^2 k^2) - \right. \right. \\
& \quad 5 g H U \left(-96 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (129 + 82 H^2 k^2 + 13 H^4 k^4) U \right) + \\
& \quad 32 \left(9 \sqrt{g H (3 + H^2 k^2)} U^3 + k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 2 k^2 \left(2 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + \right. \right. \\
& \quad \left. \left. 3 \sqrt{g H^5 (3 + H^2 k^2)} U^3 \right) \right) \right) dt^2 \Big/ \left(128 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) + \\
& \left(k^7 \left(-\sqrt{3} \sqrt{g H (3 + H^2 k^2)} + (3 + H^2 k^2) U \right) \left(24 \sqrt{3} g^2 H^2 (21 + 5 H^2 k^2) + \right. \right. \\
& \quad 3 g H U \left(-717 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1011 + 646 H^2 k^2 + 103 H^4 k^4) U \right) - \\
& \quad \left. \left. 5 \left(288 \sqrt{g H (3 + H^2 k^2)} U^3 + 32 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 3 k^2 \left(39 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left(64 \sqrt{g H^5 (3 + H^2 k^2) U^3} \right) dt^3 \right) / \left(384 \sqrt{g H (3 + H^2 k^2)^{7/2}} \right) + \\
& \left(i k^8 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right)^2 \left(5 \sqrt{3} g^2 H^2 (45 + 11 H^2 k^2) + \right. \right. \\
& \quad g H U \left(-990 \sqrt{g H (3 + H^2 k^2)} + \sqrt{3} (1449 + 930 H^2 k^2 + 149 H^4 k^4) U \right) - \\
& \quad 2 \left(360 \sqrt{g H (3 + H^2 k^2)} U^3 + 40 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + k^2 \left(137 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + \right. \right. \\
& \quad \left. \left. 240 \sqrt{g H^5 (3 + H^2 k^2) U^3} \right) \right) dt^4 \right) / \left(128 \sqrt{g H (3 + H^2 k^2)^{9/2}} \right) + O[dt]^5 \Bigg) dx^3 + \\
& \left(\left(k^5 \left(-3 \sqrt{3} g H (543 + 146 H^2 k^2 + 15 H^4 k^4) + 256 \left(9 \sqrt{g H (3 + H^2 k^2)} + 6 k^2 \sqrt{g H^5 (3 + H^2 k^2)} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. k^4 \sqrt{g H^9 (3 + H^2 k^2)} U \right) \right) \right) / \left(30720 \sqrt{g H (3 + H^2 k^2)^{5/2}} \right) + \\
& \quad \left(i k^6 \left(-3 g H \left(-18432 \sqrt{g H (3 + H^2 k^2)} + 51039 \sqrt{3} U + 45735 \sqrt{3} H^2 k^2 U + \right. \right. \right. \\
& \quad \left. \left. 1381 \sqrt{3} H^6 k^6 U + k^4 \left(-960 \sqrt{g H^9 (3 + H^2 k^2)} + 13717 \sqrt{3} H^4 U \right) \right) \right) + \\
& \quad 128 \left(837 \sqrt{g H (3 + H^2 k^2)} U^2 + 279 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^2 + 31 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} U^2 + \right. \\
& \quad \left. 27 k^2 \left(7 \sqrt{g^3 H^7 (3 + H^2 k^2)} + 31 \sqrt{g H^5 (3 + H^2 k^2) U^2} \right) \right) dt \Bigg) / \\
& \quad \left(92160 \sqrt{g H (3 + H^2 k^2)^{7/2}} \right) + \left(k^7 \left(9 \sqrt{3} g^2 H^2 (12999 + 6258 H^2 k^2 + 775 H^4 k^4) + \right. \right. \\
& \quad g H U \left(617661 \sqrt{3} H^2 k^2 U + 20551 \sqrt{3} H^6 k^6 U + 81 \left(-5888 \sqrt{g H (3 + H^2 k^2)} + \right. \right. \\
& \quad \left. \left. 8053 \sqrt{3} U \right) - 3 k^4 \left(12288 \sqrt{g H^9 (3 + H^2 k^2)} - 65021 \sqrt{3} H^4 U \right) \right) - \\
& \quad 128 \left(2322 \sqrt{g H (3 + H^2 k^2)} U^3 + 774 k^4 \sqrt{g H^9 (3 + H^2 k^2)} U^3 + 86 k^6 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + \right. \\
& \quad \left. 9 k^2 \left(229 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 258 \sqrt{g H^5 (3 + H^2 k^2) U^3} \right) \right) dt^2 \Bigg) / \\
& \quad \left(92160 \sqrt{g H (3 + H^2 k^2)^{7/2}} \right) - \frac{1}{30720 \sqrt{g H (3 + H^2 k^2)^{9/2}}} i k^8 \\
& \quad \left(k^8 U^3 \left(-21253 \sqrt{3} g H^9 + 7776 \sqrt{g H^{17} (3 + H^2 k^2)} U \right) + \right. \\
& \quad 243 \left(832 \sqrt{g^5 H^5 (3 + H^2 k^2)} - 4423 \sqrt{3} g^2 H^2 U + 2592 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\
& \quad g H U^2 \left(8832 \sqrt{g H (3 + H^2 k^2)} - 7823 \sqrt{3} U \right) \Bigg) - 3 k^6 U \left(9181 \sqrt{3} g^2 H^8 - \right. \\
& \quad \left. 31104 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + 4 g H^7 U \left(-5312 \sqrt{g H (3 + H^2 k^2)} + 21787 \sqrt{3} U \right) \right) \Bigg) + \\
& \quad 27 k^2 \left(-35319 \sqrt{3} g^2 H^4 U - 91580 \sqrt{3} g H^3 U^3 + \right. \\
& \quad \left. 64 \left(59 \sqrt{g^5 H^9 (3 + H^2 k^2)} + 1155 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 + 486 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \right) \right) + \\
& \quad 9 k^4 \left(-31231 \sqrt{3} g^2 H^6 U + 2 g H^5 U^2 \left(34336 \sqrt{g H (3 + H^2 k^2)} - 67003 \sqrt{3} U \right) + \right. \\
& \quad \left. 229 \left(229 \sqrt{g^3 H^7 (3 + H^2 k^2)} U + 258 \sqrt{g H^5 (3 + H^2 k^2) U^3} \right) \right) dt^2 \Bigg) / \\
& \quad \left(92160 \sqrt{g H (3 + H^2 k^2)^{7/2}} \right) - \frac{1}{30720 \sqrt{g H (3 + H^2 k^2)^{9/2}}} i k^8
\end{aligned}$$

$$\begin{aligned} & \left(\frac{288 \left(5 \sqrt{g^5 H^{17} (3 + H^2 k^2)} + 162 \sqrt{g H^7 (3 + H^2 k^2)} U \right) dt^7 - \frac{92160 \left(\sqrt{g H (3 + H^2 k^2)} \right)^{11/2}}{}}{92160 \left(\sqrt{g H (3 + H^2 k^2)} \right)^{11/2}} \right) dt^7 - \\ & \left(k^9 \left(\sqrt{3} \sqrt{g H (3 + H^2 k^2)} - (3 + H^2 k^2) U \right) \left(k^8 U^3 \left(-111559 \sqrt{3} g H^9 + 42368 \sqrt{g H^{17} (3 + H^2 k^2)} U \right) + \right. \right. \\ & 27 k^2 \left(18078 \sqrt{g^5 H^9 (3 + H^2 k^2)} - 172047 \sqrt{3} g^2 H^4 U + 372075 \sqrt{g^3 H^7 (3 + H^2 k^2)} U^2 - \right. \\ & \left. 477940 \sqrt{3} g H^3 U^3 + 169472 \sqrt{g H^5 (3 + H^2 k^2)} U^4 \right) + \\ & 9 k^4 \left(7035 \sqrt{g^5 H^{13} (3 + H^2 k^2)} - 153703 \sqrt{3} g^2 H^6 U + 254208 \sqrt{g H^9 (3 + H^2 k^2)} U^4 + \right. \\ & \left. g H^5 U^2 \left(347651 \sqrt{g H (3 + H^2 k^2)} - 700818 \sqrt{3} U \right) \right) + \\ & 81 \left(11603 \sqrt{g^5 H^5 (3 + H^2 k^2)} - 63917 \sqrt{3} g^2 H^2 U + 42368 \sqrt{g H (3 + H^2 k^2)} U^4 + \right. \\ & \left. g H U^2 \left(132513 \sqrt{g H (3 + H^2 k^2)} - 122207 \sqrt{3} U \right) \right) - \\ & 3 k^6 U \left(45573 \sqrt{3} g^2 H^8 - 169472 \sqrt{g H^{13} (3 + H^2 k^2)} U^3 + \right. \\ & \left. g H^7 U \left(-108089 \sqrt{g H (3 + H^2 k^2)} + 456644 \sqrt{3} U \right) \right) \Big) dt^4 + O[dt]^5 \Big) dx^4 + O[dx]^5 \Big\} \end{aligned}$$

```
Out[260]= Omega error ||
```

$$\begin{aligned} & \left(\frac{i}{\sqrt{H^2 k^2 + 3}} + \frac{3}{\sqrt{H^2 k^2 + 3}} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} k^2 \right)^2 \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^2 - \frac{\left(k^3 \sqrt{H^2 k^2 + 3} + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}}{\left(3 g H + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}} \right) \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^2 \\ & - \frac{i k^4 \left(H^2 k^2 + 3 \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}}{\left(H^4 U k^4 + 3 \left(2 U H^2 + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 \left(U + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}} U^2 + 3 g \left(3 k^2 U H^3 + 9 U H + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} H \right) \sqrt{H^2 k^2 + 3} \\ & \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^3 + \frac{k^5 \left(H^2 k^2 + 3 \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}}{\left(H^4 U k^4 + 2 \left(3 U H^2 + 2 \sqrt{H^2 k^2 + 3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 U + 12 \sqrt{H^2 k^2 + 3} \sqrt{g H \left(H^2 k^2 + 3 \right)}} U^3 + 6 g H \left(3 \left(H^2 k^2 + 3 \right) U + 2 \sqrt{H^2 k^2 + 3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U + 9 g^2 H^2 \right) \sqrt{H^2 k^2 + 3} \\ & \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^3 + O \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^5 \right) \sqrt{H^2 k^2 + 3} \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^2 - \frac{k^3 \left(H^2 k^2 + 3 \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}}{\left(3 g H + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}} \sqrt{H^2 k^2 + 3} \\ & \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^2 \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^{3/2} \right) - \frac{i k^4 \left(H^2 k^2 + 3 \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}}{\left(3 g H + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}} \sqrt{H^2 k^2 + 3} \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^{3/2} \\ & + \frac{k^5 \left(H^2 k^2 + 3 \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}}{\left(H^4 U k^4 + 3 \left(2 U H^2 + 2 \sqrt{H^2 k^2 + 3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 \left(U + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}} U^2 + 3 g \left(3 k^2 U H^3 + 9 U H + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} H \right) \sqrt{H^2 k^2 + 3} \\ & \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^{5/2} + \frac{i k^6 \left(H^2 k^2 + 3 \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}}{\left(H^4 U k^4 + 2 \left(3 U H^2 + 2 \sqrt{H^2 k^2 + 3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 U + 12 \sqrt{H^2 k^2 + 3} \sqrt{g H \left(H^2 k^2 + 3 \right)}} U^3 + 6 g H \left(3 \left(H^2 k^2 + 3 \right) U + 2 \sqrt{H^2 k^2 + 3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U + 9 g^2 H^2 \right) \sqrt{H^2 k^2 + 3} \\ & \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^{5/2} + O \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^5 \right) \sqrt{H^2 k^2 + 3} \left(\frac{H^2 k^2 + 3}{\sqrt{H^2 k^2 + 3}} \right)^2 + \left(- \frac{k^3 \left(3 \sqrt{H^2 k^2 + 3} \right) g H \left(3 H^2 k^2 + 13 \right) + 16 \left(H^5 \left(H^2 k^2 + 3 \right) \right) k^2 + 3 \left(H^5 \left(H^2 k^2 + 3 \right) \right) \sqrt{H^2 k^2 + 3}}{\left(3 g H + \sqrt{H^2 k^2 + 3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)}} \right) \sqrt{H^2 k^2 + 3} \end{aligned}$$

[illegible]

$$\begin{aligned}
& \sqrt{3} U H^4 + 960 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) k^4 + 45735 \sqrt{3} H^2 U k^2 + 51039 \\
& \sqrt{3} U + 18432 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) + 128 \left(31 \sqrt{g H^{13}} \left(H^2 k^2 + 3 \right) \right) U^2 k^6 + 279 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} U^2 k^4 + 27 \left(31 \sqrt{g H^5} \right. \\
& \left. \left(H^2 k^2 + 3 \right) \right) U^2 + 7 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) k^2 + 837 \sqrt{g H \left(H^2 k^2 + 3 \right)} U^2 \right) \text{dt} \} \{ 92160 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{7/2} \} - \frac{\left(k^7 \right. \\
& \left. \left(9 \sqrt{3} g^2 \left(775 H^4 k^4 + 6258 H^2 k^2 + 12999 \right) H^2 + g U \left(20551 \sqrt{3} H^6 U \right. \right. \right. \\
& \left. \left. k^6 + 3 \left(65021 \sqrt{3} U H^4 + 12288 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) k^4 + 617661 \sqrt{3} \right. \right. \\
& \left. \left. H^2 U k^2 + 81 \left(8053 \sqrt{3} U + 5888 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right) H + 128 \left(86 \right. \\
& \left. \sqrt{g H^{13}} \left(H^2 k^2 + 3 \right) \right) U^3 k^6 + 774 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} U^3 k^4 + 9 \\
& \left. \left(258 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^3 + 229 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) U \right) \\
& k^2 + 2322 \sqrt{g H \left(H^2 k^2 + 3 \right)} U^3 \right) \text{dt} \}^2 \} \{ 92160 \left(\sqrt{g} \right. \\
& \left. H \right) \left(H^2 k^2 + 3 \right)^{7/2} \right) - \frac{i k^8 \left(U^3 \left(21253 \sqrt{3} g H^9 + 7776 \sqrt{g} \right. \right. \\
& \left. \left. H^{17} \right) \left(H^2 k^2 + 3 \right) \right) U \right) k^8 + 3 U \left(9181 \sqrt{3} g^2 H^8 + 4 g U \left(21787 \sqrt{3} \right. \right. \\
& \left. \left. U + 5312 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) H^7 + 31104 \sqrt{g H^{13}} \left(H^2 k^2 + 3 \right) \right) \\
& U^3 \right) k^6 + 9 \left(31231 \sqrt{3} g^2 U H^6 + 2 g U^2 \left(67003 \sqrt{3} U + 34336 \sqrt{g H} \right. \right. \\
& \left. \left. \left(H^2 k^2 + 3 \right) \right) \right) H^5 + 288 \left(162 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) U^4 + 5 \sqrt{g^5} \\
& H^{13} \left(H^2 k^2 + 3 \right) \right) \right) k^4 + 27 \left(35319 \sqrt{3} g^2 U H^4 + 91580 \sqrt{3} \right. \\
& \left. g U^3 H^3 + 64 \left(486 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^4 + 1155 \sqrt{g^3 H^7 \left(H^2 \right.} \right. \\
& \left. \left. k^2 + 3 \right) \right) U^2 + 59 \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) \right) k^2 + 243 \left(2592 \sqrt{g H} \right. \\
& \left. \left(H^2 k^2 + 3 \right) \right) U^4 + g H \left(7823 \sqrt{3} U + 8832 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \\
& U^2 + 4423 \sqrt{3} g^2 H^2 U + 832 \sqrt{g^5 H^5 \left(H^2 k^2 + 3 \right)} \right) \text{dt} \}^3 \} \{ 30720 \\
& \sqrt{g H} \left(H^2 k^2 + 3 \right)^{9/2} \} + \frac{k^9 \left(\left(H^2 k^2 + 3 \right) U + \sqrt{3} \sqrt{g H} \right. \\
& \left. \left(H^2 k^2 + 3 \right) \right) \left(U^3 \left(111559 \sqrt{3} g H^9 + 42368 \sqrt{g H^{17}} \left(H^2 \right. \right. \right. \\
& \left. \left. k^2 + 3 \right) \right) U \right) k^8 + 3 U \left(45573 \sqrt{3} g^2 H^8 + g U \left(456644 \sqrt{3} U + 108089 \right. \right. \\
& \left. \left. \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) H^7 + 169472 \sqrt{g H^{13}} \left(H^2 k^2 + 3 \right) \right) U^3 \right) \\
& k^6 + 9 \left(153703 \sqrt{3} g^2 U H^6 + g U^2 \left(700818 \sqrt{3} U + 347651 \sqrt{g H \left(H^2 \right.} \right. \\
& \left. \left. k^2 + 3 \right) \right) \right) H^5 + 254208 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} U^4 + 7035 \sqrt{g^5 H^{13}} \left(H^2 \right. \\
& \left. k^2 + 3 \right) \right) \right) k^4 + 27 \left(172047 \sqrt{3} g^2 U H^4 + 477940 \sqrt{3} g U^3 H^3 + 169472 \right. \\
& \left. \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^4 + 372075 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} U^2 + 18078 \\
& \left. \sqrt{g^5 H^9 \left(H^2 k^2 + 3 \right)} \right) k^2 + 81 \left(42368 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^4 + g \\
& H \left(122207 \sqrt{3} U + 132513 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^2 + 63917 \sqrt{3} g^2 H^2 \\
& U + 11603 \sqrt{g^5 H^5 \left(H^2 k^2 + 3 \right)} \right) \text{dt} \}^4 \} \{ 92160 \sqrt{g H} \left(H^2 \right. \\
& \left. k^2 + 3 \right)^{11/2} \} + O \left(\text{dt}^5 \right) \text{dx}^4 + O \left(\text{dx}^5 \right), \left(\frac{i}{\left(H^2 U k^3 + 3 U k - \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} k} \right)^2 \text{dt} \} \left(H^2 \right. \\
& \left. k^2 + 3 \right)^2 \} - \frac{\left(k^3 \left(\left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \\
& \left(3 g H + U \left(\left(H^2 k^2 + 3 \right) U - 2 \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right) \text{dt} \}^2 \} \left(H^2 k^2 + 3 \right)^2 \} - \frac{i k^4 \left(\left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H} \left(H^2 k^2 + 3 \right) \right) \\
& \left(\left(H^2 k^2 + 3 \right) \right) \left(\left(H^4 U k^4 - 3 \left(\sqrt{3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) - 2 \right. \\
& \left. H^2 U \right) k^2 + 9 U - 9 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} U^2 + 3 g H \left(3 \left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \text{dt} \}^3 \} \{ 4 \left(H^2 \right. \\
& \left. k^2 + 3 \right)^3 \} + \frac{k^5 \left(\left(H^2 k^2 + 3 \right) U - \sqrt{3} \right) \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \left(\left(H^4 U k^4 + \left(6 H^2 U - 4 \sqrt{3} \right) \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 \right. \\
& \left. U - 12 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^3 + 6 g H \left(3 \left(H^2 k^2 + 3 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& U - 2 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U + 9 g^2 H^2 \right) \text{dt}^4 \{ 5 \left(H^2 \right. \\
& k^2 + 3 \right)^3 + O \left(\text{dt}^5 \right) \right) + \left(- \frac{1}{4} \right) i k^2 \left(\sqrt{3} \sqrt{\frac{g}{H}} \left(H^2 k^2 + 3 \right) \right) - 2 U \right) + \frac{k^3 \left(\left(H^2 k^2 + 3 \right) U - \sqrt{3} \sqrt{g H \left(H^2 \right. \right.} \\
& k^2 + 3 \right)}{\left. \right) \left(\sqrt{3} g H - 2 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U \right) \text{dt} \} \{ 4 \sqrt{g H} \\
& \left(H^2 k^2 + 3 \right)^{3/2} \} + \frac{i k^4 \left(\sqrt{3} g H - 2 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U \right) \left(3 g H + U \left(\left(H^2 k^2 + 3 \right) U - 2 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right) \right) \\
& \text{dt}^2 \} \{ 4 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{3/2} \} - \frac{\left(k^5 \left(\sqrt{3} g H - 2 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U \right) \left(\left(H^4 U k^4 - 3 \left(\sqrt{3} \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) - 2 \right. \right. \right. \\
& H^2 U \right) k^2 + 9 U - 9 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^2 + 3 g H \left(3 \left(H^2 k^2 + 3 \right) U - \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right) \right) \text{dt}^3 \} \{ 4 \left(\sqrt{g H} \right. \\
& \left. \left(H^2 k^2 + 3 \right)^{5/2} \right) \} - \frac{i k^6 \left(\sqrt{3} g H - 2 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U \right) \left(\left(H^4 U k^4 + \left(6 H^2 U - 4 \sqrt{3} \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) \right) \right) \right) \right) \\
& k^2 + 9 U - 12 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^3 + 6 g H \left(3 \left(H^2 k^2 + 3 \right) U - 2 \sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) \right) U + 9 g^2 H^2 \right) \text{dt}^4 \} \{ 4 \sqrt{g H} \\
& \left(H^2 k^2 + 3 \right)^{5/2} \} + O \left(\text{dt}^5 \right) \right) \text{dx} + \left(\frac{k^3 \left(3 \sqrt{3} g H \left(3 H^2 k^2 + 13 \right) - 16 \left(\sqrt{3} g H^5 \left(H^2 k^2 + 3 \right) \right) U k^2 + 3 \sqrt{g H \left(H^2 \right. \right.} \right. \right. \\
& k^2 + 3 \right) \right) U \right) \right) \} \{ 96 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{3/2} \} + \frac{i k^4 \left(g H \left(\sqrt{3} \right. \right. \\
& \left. \left(37 H^4 k^4 + 234 H^2 k^2 + 369 \right) U - 144 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) - 4 \left(7 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) U^2 k^4 + 3 \left(14 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^2 + 3 \\
& \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) k^2 + 63 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^2 \right) \right) \text{dt} \} \{ 96 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{5/2} \} - \frac{\left(k^5 \left(\sqrt{3} \sqrt{g H \left(H^2 \right. \right.} \right. \\
& k^2 + 3 \right) \right) - \left(H^2 k^2 + 3 \right) U \right) \left(g H \left(171 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) - \sqrt{3} \right) \\
& \left(49 H^4 k^4 + 306 H^2 k^2 + 477 \right) U \right) + 5 \left(8 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) U^2 \\
& k^4 + 3 \left(16 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^2 + 3 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) \right) k^2 + 72 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^2 \right) \right) \text{dt}^2 \} \{ 96 \left(\sqrt{g H} \right. \\
& \left. \left(H^2 k^2 + 3 \right)^{7/2} \right) \} + \frac{i k^6 \left(\sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) - \left(H^2 k^2 + 3 \right) U \right) \right)^2 \left(52 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) U^2 k^4 + 6 \left(52 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) \\
& U^2 + 9 \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) k^2 + 468 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^2 + g H \left(198 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) - \sqrt{3} \left(61 H^4 k^4 + 378 \right. \\
& H^2 k^2 + 585 \right) U \right) \text{dt}^3 \} \{ 96 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{9/2} \} + \frac{k^7 \left(\sqrt{3} \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) - \left(H^2 k^2 + 3 \right) U \right)^3 \left(64 \sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) U^2 k^4 + 3 \left(128 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^2 + 21 \\
& \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) k^2 + 576 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^2 + g H \left(225 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) - \sqrt{3} \left(73 H^4 k^4 + 450 H^2 k^2 + 693 \right) \\
& U \right) \text{dt}^4 \} \{ 96 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{11/2} \} + O \left(\text{dt}^5 \right) \right) \text{dt}^2 + \left(\frac{i k^4 \left(\sqrt{3} g H \left(7 H^2 k^2 + 33 \right) - 16 \left(\sqrt{3} g H^5 \left(H^2 k^2 + 3 \right) \right) U k^2 + 3 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U \right) \right) \} \{ 384 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{3/2} \} + \frac{k^5 \left(g H \left(72 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) - \sqrt{3} \right) \left(19 H^4 k^4 + 126 H^2 k^2 + 207 \right) U \right) + 16 \left(\sqrt{g H^9 \left(H^2 k^2 + 3 \right)} \right) U^2 k^4 + \left(6 \sqrt{g H^5 \left(H^2 k^2 + 3 \right)} \right) U^2 + \sqrt{g^3 H^7 \left(H^2 k^2 + 3 \right)} \right) k^2 + 9 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) U^2 \right) \text{dt} \} \{ 128 \sqrt{g H} \left(H^2 k^2 + 3 \right)^{5/2} \} + \frac{i k^6 \left(- 9 \sqrt{3} g^2 \left(3 H^2 k^2 + 13 \right) H^2 - 5 g U \left(\sqrt{3} \left(13 H^4 k^4 + 82 H^2 k^2 + 129 \right) U - 96 \sqrt{g H \left(H^2 k^2 + 3 \right)} \right) \right) H + 32 \left(\sqrt{3} g H^9 \left(H^2 \right. \right. \right.
\end{aligned}$$

$$\begin{aligned} & k^2+3\text{right})\} U^3 k^4+2\text{left}(3\sqrt{g H^5\text{left}(H^2 k^2+3\text{right})\} U^3+2\sqrt{g^3 H^7\text{left}(H^2 k^2+3\text{right})\} U\text{right}) k^2+9\sqrt{g H\text{left}(H^2 k^2+3\text{right})\} U^3\text{right})\text{right})\text{text{dt}}^2\}\{128 \\ & \sqrt{g H}\text{left}(H^2 k^2+3\text{right})^{5/2}\}+\frac{k^7\text{left}(\text{left}(H^2 k^2+3\text{right}) U-\sqrt{3}\sqrt{g H} \\ & \text{left}(H^2 k^2+3\text{right})\text{right})\text{left}(24\sqrt{3} g^2\text{left}(5 H^2 k^2+21\text{right}) H^2+3 g U\text{left}(\sqrt{3}\{ \\ & \text{left}(103 H^4 k^4+646 H^2 k^2+1011\text{right}) U-717\sqrt{g H\text{left}(H^2 k^2+3\text{right})\}\text{right}) H-5 \\ & \text{left}(32\sqrt{g H^9\text{left}(H^2 k^2+3\text{right})\} U^3 k^4+3\text{left}(64\sqrt{g H^5\text{left}(H^2 k^2+3\text{right})\} \\ & U^3+39\sqrt{g^3 H^7\text{left}(H^2 k^2+3\text{right})\} U\text{right}) k^2+288\sqrt{g H\text{left}(H^2 k^2+3\text{right})\} \\ & U^3\text{right})\text{right})\text{text{dt}}^3\}\{384\sqrt{g H}\text{left}(H^2 k^2+3\text{right})^{7/2}\}+\frac{i k^8\text{left}(\sqrt{3}\sqrt{g H} \\ & \text{left}(H^2 k^2+3\text{right})\text{right})-\text{left}(H^2 k^2+3\text{right}) U\text{right})^2\text{left}(5\sqrt{3} g^2\text{left}(11 H^2 \\ & k^2+45\text{right}) H^2+g U\text{left}(\sqrt{3}\text{left}(149 H^4 k^4+930 H^2 k^2+1449\text{right}) U-990\sqrt{g H} \\ & \text{left}(H^2 k^2+3\text{right})\text{right}) H-2\text{left}(40\sqrt{g H^9\text{left}(H^2 k^2+3\text{right})\} U^3 k^4+\text{left}(240 \\ & \sqrt{g H^5\text{left}(H^2 k^2+3\text{right})\} U^3+137\sqrt{g^3 H^7\text{left}(H^2 k^2+3\text{right})\} U\text{right}) \\ & k^2+360\sqrt{g H\text{left}(H^2 k^2+3\text{right})\} U^3\text{right})\text{right})\text{text{dt}}^4\}\{128\sqrt{g H}\text{left}(H^2 \\ & k^2+3\text{right})^{9/2}\}+O(\text{left}(\text{text{dt}}^5\text{right})\text{right})\text{text{dx}}^3+\text{left}(\frac{k^5\text{left}(\sqrt{g H^9\text{left}(H^2 k^2+3\text{right})\} \\ & k^4+6\sqrt{g H^5\text{left}(H^2 k^2+3\text{right})\} k^2+9\sqrt{g H\text{left}(H^2 k^2+3\text{right})\}\text{right}) U-3\sqrt{3} g H\text{left}(15 H^4 k^4+146 H^2 k^2+543\text{right})\text{right})\}\{30720\sqrt{g H} \\ & \text{left}(H^2 k^2+3\text{right})^{5/2}\}+\frac{i k^6\text{left}(128\text{left}(31\sqrt{g H^{13}}\text{left}(H^2 k^2+3\text{right})\} U^2 \\ & k^6+279\sqrt{g H^9\text{left}(H^2 k^2+3\text{right})\} U^2 k^4+27\text{left}(31\sqrt{g H^5\text{left}(H^2 k^2+3\text{right})\} \\ & U^2+7\sqrt{g^3 H^7\text{left}(H^2 k^2+3\text{right})\}\text{right}) k^2+837\sqrt{g H\text{left}(H^2 k^2+3\text{right})\} \\ & U^2\text{right})-3 g H\text{left}(1381\sqrt{3} H^6 U k^6+\text{left}(13717\sqrt{3} H^4 U-960\sqrt{g H^9\text{left}(H^2 \\ & k^2+3\text{right})\}\text{right}) k^4+45735\sqrt{3} H^2 U k^2+51039\sqrt{3} U-18432\sqrt{g H\text{left}(H^2 \\ & k^2+3\text{right})\}\text{right})\text{right})\text{text{dt}}\}\{92160\sqrt{g H}\text{left}(H^2 k^2+3\text{right})^{7/2}\}+\frac{k^7\text{left}(9 \\ & \sqrt{3} g^2\text{left}(775 H^4 k^4+6258 H^2 k^2+12999\text{right}) H^2+g U\text{left}(20551\sqrt{3} H^6 U k^6-3 \\ & \text{left}(12288\sqrt{g H^9\text{left}(H^2 k^2+3\text{right})\}\text{right})-65021\sqrt{3} H^4 U\text{right}) k^4+617661\sqrt{3} H^2 \\ & U k^2+81\text{left}(8053\sqrt{3} U-5888\sqrt{g H\text{left}(H^2 k^2+3\text{right})\}\text{right})\text{right}) H-128\text{left}(86 \\ & \sqrt{g H^{13}}\text{left}(H^2 k^2+3\text{right})\} U^3 k^6+774\sqrt{g H^9\text{left}(H^2 k^2+3\text{right})\} U^3 k^4+9 \\ & \text{left}(258\sqrt{g H^5\text{left}(H^2 k^2+3\text{right})\} U^3+229\sqrt{g^3 H^7\text{left}(H^2 k^2+3\text{right})\} U\text{right}) \\ & k^2+2322\sqrt{g H\text{left}(H^2 k^2+3\text{right})\} U^3\text{right})\text{right})\text{text{dt}}^2\}\{92160\sqrt{g H}\text{left}(H^2 \\ & k^2+3\text{right})^{7/2}\}-\frac{i k^8\text{left}(U^3\text{left}(7776\sqrt{g H^{17}}\text{left}(H^2 k^2+3\text{right})\} U-21253 \\ & \sqrt{3} g H^9\text{right}) k^8-3 U\text{left}(9181\sqrt{3} g^2 H^8+4 g U\text{left}(21787\sqrt{3} U-5312\sqrt{g H} \\ & \text{left}(H^2 k^2+3\text{right})\}\text{right}) H^7-31104\sqrt{g H^{13}}\text{left}(H^2 k^2+3\text{right})\} U^3\text{right}) k^6+9 \\ & \text{left}(-31231\sqrt{3} g^2 U H^6+2 g U^2\text{left}(34336\sqrt{g H\text{left}(H^2 k^2+3\text{right})\}\text{right})-67003\sqrt{3} \\ & U\text{right}) H^5+288\text{left}(162\sqrt{g H^9\text{left}(H^2 k^2+3\text{right})\} U^4+5\sqrt{g^5 H^{13}}\text{left}(H^2 \\ & k^2+3\text{right})\}\text{right})\text{right}) k^4+27\text{left}(-35319\sqrt{3} g^2 U H^4-91580\sqrt{3} g U^3 H^3+64 \\ & \text{left}(486\sqrt{g H^5\text{left}(H^2 k^2+3\text{right})\} U^4+1155\sqrt{g^3 H^7\text{left}(H^2 k^2+3\text{right})\} U^2+59 \\ & \sqrt{g^5 H^9\text{left}(H^2 k^2+3\text{right})\}\text{right})\text{right}) k^2+243\text{left}(2592\sqrt{g H\text{left}(H^2 k^2+3\text{right})\} \\ & U^4+g H\text{left}(8832\sqrt{g H\text{left}(H^2 k^2+3\text{right})\}\text{right})-7823\sqrt{3} U\text{right}) U^2-4423\sqrt{3} g^2 \\ & H^2 U+832\sqrt{g^5 H^5\text{left}(H^2 k^2+3\text{right})\}\text{right})\text{right})\text{text{dt}}^3\}\{30720\sqrt{g H}\text{left}(H^2 \\ & k^2+3\text{right})^{9/2}\}-\frac{\text{left}(k^9\text{left}(\sqrt{3}\sqrt{g H\text{left}(H^2 k^2+3\text{right})\}\text{right})-\text{left}(H^2 k^2+3\text{right}) \\ & U\text{right})\text{left}(U^3\text{left}(42368\sqrt{g H^{17}}\text{left}(H^2 k^2+3\text{right})\} U-111559\sqrt{3} g H^9\text{right}) \\ & k^8-3 U\text{left}(45573\sqrt{3} g^2 H^8+g U\text{left}(456644\sqrt{3} U-108089\sqrt{g H\text{left}(H^2 \\ & k^2+3\text{right})\}\text{right}) H^7-169472\sqrt{g H^{13}}\text{left}(H^2 k^2+3\text{right})\} U^3\text{right}) k^6+9\text{left}(-153703 \\ & \sqrt{3} g^2 U H^6+g U^2\text{left}(347651\sqrt{g H\text{left}(H^2 k^2+3\text{right})\}\text{right})-700818\sqrt{3} U\text{right}) \end{aligned}$$


```

Out[265]= Eerr || \left(
\begin{array}{cc}
\left(-\frac{\left(H^2 k^3 U w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i H^2 k^3}{U w^2 \text{dt}^3}\right)\left\{6 \left(H^2 k^2+3\right)+\frac{H^2 k^3 U w^3 \text{dt}^4}{24 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right\}+\left(\frac{1}{2} k^2 U \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}+\left(\frac{i \left(2 H^4 k^7+9 H^2 k^5\right) U \text{dt}}{12 \left(H^2 k^2+3\right)^2}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(-\frac{1}{24} \left(k^4 U\right) \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}^3+\left(-\frac{i k^7 \left(2 k^4 U H^6+19 k^2 U H^4+54 U H^2\right) \text{dt}}{240 \left(H^2 k^2+3\right)^3}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \& \left(-\frac{3(k w) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i k w^2 \text{dt}^3}{2 \left(H^2 k^2+3\right)}+\frac{k w^3 \text{dt}^4}{8 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right)+\left(\frac{i \left(H^2 k^5+6 k^3\right) \text{dt}}{4 \left(H^2 k^2+3\right)^2}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(\frac{i \left(H^4 k^9-54 k^5\right) \text{dt}}{240 \left(H^2 k^2+3\right)^3}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \\
\left(-\frac{\left(k \left(g k^2 H^3+3 g H-3 U^2\right) w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i k \left(g k^2 H^3+3 g H-3 U^2\right) w^2 \text{dt}^3}{6 \left(H^2 k^2+3\right)}+\frac{k \left(g k^2 H^3+3 g H-3 U^2\right) w^3 \text{dt}^4}{24 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right)+\left(\frac{1}{2} g H k^2 \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}+\left(\frac{i \left(2 g H^5 k^7+12 g H^3 k^5-3 H^2 U^2 k^5-18 U^2 k^3+18 g H k^3\right) \text{dt}}{12 \left(H^2 k^2+3\right)^2}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(-\frac{1}{24} \left(g H k^4\right) \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}^3+\left(-\frac{i \left(2 g H^7 k^{11}+18 g H^5 k^9+H^4 U^2 k^9+54 g H^3 k^7-54 U^2 k^5+54 g H k^5\right) \text{dt}}{240 \left(H^2 k^2+3\right)^3}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \& \\
\left(-\frac{\left(k \left(H^2 k^2+6\right) U w\right) \text{dt}^2}{2 \left(H^2 k^2+3\right)}-\frac{i k \left(H^2 k^2+6\right) U w^2 \text{dt}^3}{6 \left(H^2 k^2+3\right)}+\frac{k \left(H^2 k^2+6\right) U w^3 \text{dt}^4}{24 \left(H^2 k^2+3\right)}+O\left(\text{dt}^5\right)\right)+\left(\frac{1}{2} k^2 U \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}+\left(\frac{i \left(2 H^4 k^7+15 H^2 k^5+36 k^3\right) U \text{dt}}{12 \left(H^2 k^2+3\right)^2}+O\left(\text{dt}^5\right)\right) \text{dx}^2+\left(-\frac{1}{24} \left(k^4 U\right) \text{dt}+O\left(\text{dt}^5\right)\right) \text{dx}^3+\left(-\frac{i \left(2 H^6 k^{11}+17 H^4 k^9+54 H^2 k^7+108 k^5\right) U \text{dt}}{240 \left(H^2 k^2+3\right)^3}+O\left(\text{dt}^5\right)\right) \text{dx}^4+O\left(\text{dt}^5\right) \\
\end{array}
\right)

```

In[266]:=