

Numerical Scheme for the Generalised Serre-Green-Naghdi Model - Reviewer Response

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1 Introduction

We kindly thank the reviewers for their constructive advice on the paper and will address their concerns below.

2 Reviewer 1

2.1 Comments

The manuscript with title "Numerical scheme for the generalised Serre-Green-Naghdi model" generalizes a hybrid finite volume/finite element method developed by the same authors for the classical Serre equations to a more general case. The new system includes solutions that are not oscillatory and this makes finite volume methods ideal for stable and accurate approximation of the shock-like wave fronts. The particular manuscript not only is very well-written but scientifically speaking is complete. It has a detailed and self-contained description of the numerical method. It has numerical justification of the method presenting its convergence and accuracy, and demonstrates well how to approximate the singular solution of the gSerre equations. I strongly recommend the publication of this manuscript without hesitations.

2.2 Response

Thanks!

This review requires no alterations to the paper.

3 Reviewer 2

3.1 Comments

This manuscript study Numerical Scheme for the Generalised Serre-Green-Naghdi Model. I think at this present form, it only attract very few readers of Wave

Motion journal.

I suggest major revision.

My suggestion is as follows:

1. In the test cases, please use some real test case, for example, wave transformation problems on uneven seabed, there are a lot experimental data, Please try to compare with these data, for some strongly nonlinear cases, show the advantages of gSGNE.
2. To show the advantages of gSGNE, for the selected cases (real cases, which has experimental data), results should show that gSGNE with specific two free parameters β_1 and β_2 is better than SGNE, SWWE, and others.
3. Similarly, Numerical Scheme should show its accuracy and efficiency was improved compared with classic scheme.

I think if the above suggestions are considered by authors, this manuscript will attract much more readers of Wave Motion journal.

3.2 Response

The suggestion here is a good one, and we have added an experimental comparison to the paper. The experiment chosen is the evolution of a rectangular wave of depression studied by Hammack and Segur (1978).

We note that this is different to the ones suggested, and which are standard in the community - in particular evolution of generated periodic wave train over a submerged bar. There are a number of reasons why:

- The gSGNE have currently only been derived for a horizontal bed, and have so far not been extended to varying bathymetry. It is also not obvious how the gSGNE can be appropriately extended to varying bathymetry.
- The introduction of the bed while very useful for an experimental result would require a significant addition to the paper for extending the method as well as further validation to demonstrate the accuracy of the variable bathymetry in the method, making the article overly long.
- While there are issues with this experiment due to the model missing effects such as friction and viscosity as well as modelling the piston movement as instantaneous, the presence of a steep gradient evolving into a dispersive wave train provides a challenging benchmark for models and methods owing to the significant nonlinearity and dispersion.
- This experiment still demonstrates the utility of improved dispersion and since improved dispersion models have not been used on this experiment, this makes it more novel.

References

- J. Hammack, H. Segur, The Korteweg-de Vries equation and water waves. Part
3. Oscillatory waves, *Journal of Fluid Mechanics* 84 (1978) 337–358.