

pljun16 question 2.1. memo (from ST 2 2017)

$$m(k+1) = e(k+1) - 0.9e(k) + 0.98m(k)$$

$$M(z) \cdot z = E(z)(z) - 0.9E(z) + 0.98M(z)$$

$$M(z)[z - 0.98] = E(z)[z - 0.9]$$

$$\frac{M(z)}{E(z)} = \frac{z - 0.9}{z - 0.98}$$

$$G(z) = \mathcal{Z} \left[\frac{5(1 - e^{-sT})}{s} \cdot \frac{5}{s(s+2)} \right]$$

$$= 25 \cdot \frac{z-1}{z} \cdot \mathcal{Z} \left[\frac{1}{s^2(s+2)} \right] \quad \text{with } T=0.1$$

$$= \frac{25}{2} \cdot \left[\frac{z-1}{z} \right] \cdot \mathcal{Z} \left[\frac{2}{s^2(s+2)} \right] \quad \left| \begin{array}{l} a=2 \\ T=0.1 \end{array} \right.$$

$$= 12.5 \left[\frac{z-1}{z} \right] \cdot \left[\frac{z[(0.2-1)e^{-0.2}]z + (1-e^{-0.2}-0.2e^{-0.2})}{2(z-1)^2(z-e^{-0.2})} \right]$$

$$= 12.5 \left[\frac{z-1}{z} \right] \cdot \frac{0.0187z + 0.0175}{2(z-1)^2(z-0.8187)}$$

$$= 12.5 \left[\frac{0.0187z + 0.0175}{2(z-1)(z-0.8187)} \right]$$

$$G(z) = \frac{(12.5)(0.0187)}{2} \left[\frac{z + 0.936}{(z-1)(z-0.8187)} \right]$$

$$\frac{D(z)}{E(z)} = D(z) \cdot G(z)$$

$$= \left[\frac{z-0.9}{z-0.98} \right] (0.116875) \left[\frac{z + 0.936}{(z-1)(z-0.8187)} \right]$$

$$\begin{aligned} & \frac{q}{s^2(s+2)} = \frac{z-1}{(z-1)(z-e^{-aT})} \\ & \frac{q}{s^2(s+2)} = \frac{z[(1-aT-1)e^{-aT}]z + (1-e^{-aT}-aTe^{-aT})}{2(z-1)^2(z-e^{-aT})} \end{aligned}$$