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EECS 510 Final Project

For this project I decided to implement a pushdown automaton(PDA) to accept strings that represent basic arithmetic expressions. Specifically, the language only accepts strings over the alphabet $\Sigma = \{ (,), +, -, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 \}$. Some limitations of the grammar are that it can only accept single digit numbers and can only do basic addition and subtraction.

The context-free grammar for the language is as follows:

$$S \rightarrow E$$

$$E \rightarrow E+T \mid E-T \mid T$$

$$T \rightarrow (E) \mid D$$

$$D \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$$

For a more detailed view of the handling of the grammar q_0 is the start state which can accept a "(" and remain in the starting state or any number (0-9) and transition to state q_1 . When a "(" is read an X is pushed onto the stack of the PDA. When in the number state q_1 it accepts "+" or "-" and moves to the operator state q_2 . If a ")" is read the X on the stack is consumed and a lambda is pushed onto the stack to check to make sure all parentheses are closed. When in the operator state q_2 it accepts a digit and goes back to q_1 or accepts a "(" and stays in q_2 .