

Jonathan Sumner

Lab 8 – Square Wave

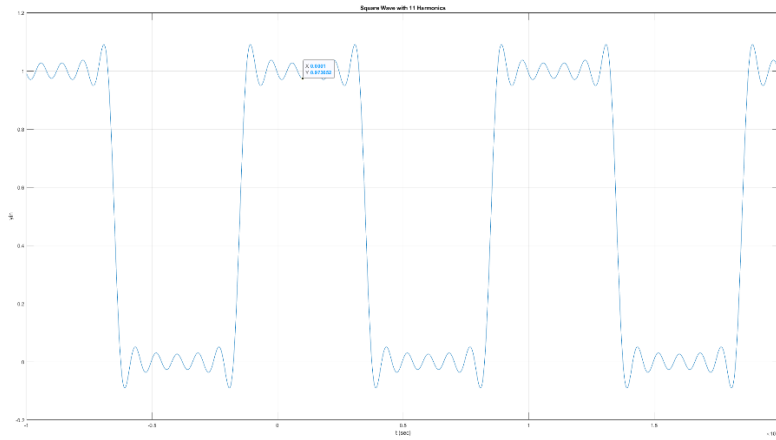
EEET-332.01 – Signals, Systems, and
Transformers Lab

Due Date: 11/10/2024

Section 1:

$$\begin{aligned}
 1) \quad c_m &= \frac{1}{T_o} \int_{-0.25ms}^{0.75ms} f(t) e^{-jmw_o t} dt \\
 c_m &= \frac{1}{T_o} \int_{-0.25ms}^{0.25ms} e^{-jmw_o t} dt \\
 \int_{-0.25ms}^{0.25ms} e^{-jmw_o t} dt &= \frac{1}{-jmw_o} e^{-jmw_o t} + C \\
 c_m &= \frac{1}{T_o} \left(\frac{1}{-jmw_o} [e^{-jmw_o(0.25ms)} - e^{-jmw_o(-0.25ms)}] \right) \\
 e^{-jmw_o(0.25ms)} &= e^{-jm\frac{\pi}{2}}, \quad e^{-jmw_o(-0.25ms)} = e^{jm\frac{\pi}{2}} \\
 e^{-jm\frac{\pi}{2}} - e^{jm\frac{\pi}{2}} &= -2j \sin\left(\frac{m\pi}{2}\right) \\
 c_m &= \frac{1}{T_o} \left(\frac{1}{-jmw_o} [-2j \sin\left(\frac{m\pi}{2}\right)] \right) \\
 c_m &= \frac{2}{mw_o T_o} \sin\left(\frac{m\pi}{2}\right) \\
 c_m &= \frac{2}{m\left(\frac{2\pi}{T_o}\right)T_o} \sin\left(\frac{m\pi}{2}\right) \\
 c_m &= \frac{\sin\left(\frac{m\pi}{2}\right)}{\pi m} \\
 2) \quad c_o &= \lim_{m \rightarrow 0} \frac{\sin\left(\frac{m\pi}{2}\right)}{\pi m} \\
 \frac{d}{dm} \sin\left(\frac{m\pi}{2}\right) &= \frac{\pi}{2} \cos\left(\frac{m\pi}{2}\right) \\
 c_o &= \lim_{m \rightarrow 0} \frac{\frac{\pi}{2} \cos\left(\frac{m\pi}{2}\right)}{\pi} \\
 c_o &= \frac{1}{2} \cos(0) = \frac{1}{2} * 1 = \frac{1}{2}
 \end{aligned}$$

Section 3:



Section 1:

$$3) C_1 = \frac{\sin(\frac{1\pi}{2})}{1\pi} = \frac{\sin(\frac{\pi}{2})}{\pi}$$

$$\sin(\frac{\pi}{2}) = 1 \quad \boxed{= \frac{1}{\pi}}$$

Section 3:

$$1) a. C_m = \frac{1}{T_0} \left(\int_{-0.25ms+tp}^{0.25ms+tp} e^{-j\omega_0 t} dt + \int_{0.25ms+tp}^{0.75ms+tp} 0 \right)$$

$$b. C_m = \frac{1}{T_0} \left(\frac{e^{-j\omega_0 t(0.25ms+tp)} - e^{-j\omega_0 t(-0.25ms+tp)}}{-j\omega_0} - \frac{e^{-j\omega_0 t(0.75ms+tp)} - e^{-j\omega_0 t(0.25ms+tp)}}{-j\omega_0} \right)$$

$$d. C_m = \frac{1}{-j\omega_0} (e^{j\omega_0(0.25)} - e^{-j\omega_0(0.25)}) e^{-j\omega_0 tp}$$

$$e. C_m = \frac{1}{m\pi} \left(\frac{e^{j\pi/2} - e^{-j\pi/2}}{2j} \right) e^{-j\omega_0 tp}$$

$$f. C_m = \frac{\sin(\pi m/2)}{\pi m} \quad \text{Figure 1}$$

$$C_m = \frac{\sin(\pi m/2)}{\pi m} e^{-j\omega_0 tp} \quad \text{Figure 4}$$

The difference is the delay, which isn't included in Figure 1 but in Figure 4 represented by $e^{-j\omega_0 tp}$

Signals Systems and Transforms
EEET-332
Lab 8

Submissions:


Create your own cover page.

Submit your cover page, the requested solutions for sections 1 and 3, and this sign-off sheet.

Sign-offs

Name Jonathan Sumner

Section 2: Table 1, completed equation 3, square wave plot (figure 3), and stem plot (figure 2) with DC offset identified.

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Signature	Date