

## Oct 26 notes

Activity 3.2.2.

Our answer is  $A \begin{pmatrix} 6 \\ 3 \end{pmatrix}$  because we can multiply  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$

For 3.2.3 you'd basically add  $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$  and  $\begin{pmatrix} -3 \\ 2 \end{pmatrix}$  and we'd get  $C \begin{pmatrix} -1 \\ 3 \end{pmatrix}$

For 3.2.4 we'd basically multiply  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$  transformation by -2 and  $\begin{pmatrix} 0 \\ 1 \end{pmatrix}$  transformation

by -3 and then add them together to get  $C \begin{pmatrix} -4 \\ -2 \end{pmatrix}$  and  $\begin{pmatrix} 9 \\ -6 \end{pmatrix}$  so  $\begin{pmatrix} 5 \\ -8 \end{pmatrix}$

For 3.2.5 - any of them bc you can get the middle value of T thru linear combination, we'll be able to span the set of all vectors of T, if you take the RREF you'd see that's true - with B they are a basis.

Fact 3.2.6 - Consider any basis for V - since every vector can be written as a linear combo of the basis vectors, we may compute  $T(v)$  as follows:

Therefore, any linear transformation of  $T:V \rightarrow W$  can be defined by describing the values of  $T(b_i)$

So just describing the transformation in terms how it effects the basis vectors will completely determine the transformation.

Definition 3.2.7

A linear transformation is determined by its action on the standard basis... so its convenient to store this info in an  $m \times n$  matrix, called the standard matrix of T

Activity 3.2.8

the  $e_1$  implies that its always top left, first pivot.. so, just like what we did in def 3.2.7, you'd combine those 4 vectors in a matrix and then we'd get the standard basis.

]