

Analysis

Testing was done using eclipse

Sorted Test	N = 100	N = 1000	N = 10000	N = 100000	N = 1000000
Heap Sort	370,049ns	16,324,841ns	25,764,759ns	76,530,356ns	631,819,357ns
Insertion Sort	35,353ns	83,001ns	883,047ns	10,677,644ns	62,831,215ns
Merge Sort	170,230ns	1,517,473ns	41,490,528ns	117,686,955ns	589,642,527ns
Quick Sort	311,257ns	800,429ns	15,706,939ns	46,831,848ns	343,580,982ns

Looking at the data for sorting the files that are already sorted, insertion sort was the fastest out of all the sorting methods. Comparing this results to the theoretical analysis, which has insertion to have a best case of $O(n)$ compared to the other three's best case which is $O(n \log n)$, it is true that insertion should be the fastest since it is just linearly going through the array and just comparing each data and no swapping has to be done. The data for heap, merge and quick sort looks a little bit weird since looking at their theoretical analysis they should be about to same for their best case. Maybe this is due to the machine being use, but I am unable to test this because I only have one machine. It could also maybe due to the way the methods are written that is causing the discrepancies. There could be a step in each of those methods that could cause a slower performance, or cause it to run better.

Unsorted Test	N = 100	N = 1000	N = 10000	N = 100000	N = 1000000
Heap Sort	382,731ns	16,085,058ns	24,908,612ns	100,887,158ns	1,725,577,583ns
Insertion Sort	1,415,258ns	17,210,578ns	348,651,394ns	31,759,398,513ns	9,825,866,651,834ns
Merge Sort	207,504ns	1,499,413ns	43,591,320ns	127,619,888ns	1,096,780,106ns
Quick Sort	360,827ns	2,028,933ns	23,250,881ns	83,773,031ns	900,535,400ns

With the unsorted files from elements of 100 to 1,000,000, Insertion Sort was constantly the slowest of all 4 sorting methods from all different number of elements test. This is true by looking at the theoretical analysis which has insertion sort to have an average and worst case of $O(n^2)$. With the heap, merge and quick sort the theoretical analysis says that their average cases are $O(n \log n)$. Merge and heap sorts worst case is at most $O(n \log n)$ while Quick sort is $O(n^2)$. Looking at the table the fastest was Quick Sort, followed by the heap sort and then the merge sort.

At the test with 1,000,000 elements the heap sort came out to be slower. It is said that the heap sort is not a stable method and this shows that it seems to be true, while merge sort is stable and quick sort is somewhat stable. I ran the methods a couple more times on each number of elements and it seems like merge sort is pretty stable because the running time it was getting was pretty close to the previous test, while heap and quick sort was getting different running times and sometimes heap sort would be faster than quick sort.