

01 - Case Study: Pilgrim Online Banking

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Data Cleaning

Renaming variables for convenience:

```
data <- dataOriginal %>%
  rename(profit = "9Profit",
         online = "9Online",
         age = "9age",
         income = "9Inc",
         tenure = "9Tenure",
         district = "9District")
```

```
str(data)
```

```
## Classes 'data.table' and 'data.frame':  31634 obs. of  7 variables:
## $ ID      : num  1 2 3 4 5 6 7 8 9 10 ...
## $ profit   : num  21 -6 -49 -4 -61 -38 -19 59 493 -158 ...
## $ online   : num  0 0 1 0 0 0 0 0 0 0 ...
## $ age      : num  NA 6 5 NA 2 NA 3 5 4 6 ...
## $ income   : num  NA 3 5 NA 9 3 1 8 9 8 ...
## $ tenure   : num  6.33 29.5 26.41 2.25 9.91 ...
## $ district: num  1200 1200 1100 1200 1200 1300 1300 1200 1200 1100 ...
## - attr(*, ".internal.selfref")=<externalptr>
```

Should we encode district as a factor? How many unique values does the feature have?

```
unique(data$district)
```

```
## [1] 1200 1100 1300
```

Convert some columns to factor variables. This is important for regression models.

```
data <- data %>%
  mutate(online = as.factor(online),
         age = as.factor(age),
         income = as.factor(income),
         district = as.factor(district)) %>%
  setDT()
```

```
str(data)
```

```
## Classes 'data.table' and 'data.frame':  31634 obs. of  7 variables:
## $ ID      : num  1 2 3 4 5 6 7 8 9 10 ...
```

```
## $ profit : num 21 -6 -49 -4 -61 -38 -19 59 493 -158 ...
## $ online : Factor w/ 2 levels "0","1": 1 1 2 1 1 1 1 1 1 ...
## $ age : Factor w/ 7 levels "1","2","3","4",...: NA 6 5 NA 2 NA 3 5 4 6 ...
## $ income : Factor w/ 9 levels "1","2","3","4",...: NA 3 5 NA 9 3 1 8 9 8 ...
## $ tenure : num 6.33 29.5 26.41 2.25 9.91 ...
## $ district: Factor w/ 3 levels "1100","1200",...: 2 2 1 2 2 3 3 2 2 1 ...
## - attr(*, ".internal.selfref")=<externalptr>
```

Missing Values

Count the number of NAs for each variable.

```
nas <- rbindlist(lapply(names(data), function(colname) {
  nMissingValues <- sum(is.na(data[, get(colname)]))
  return(data.table(feature = colname, number_of_nas = nMissingValues))
}))

nas
```

```
##      feature number_of_nas
## 1:      ID              0
## 2:   profit              0
## 3:   online              0
## 4:     age            8289
## 5:   income            8261
## 6:   tenure              0
## 7: district              0
```

Age and income have roughly the same number of missing values: Is that coincidence, or can we say that when we don't know the age of a person, we also don't know her age? To answer this, we count the number of rows for which *both* age and income are NA.

```
data[, age_and_income_missing := ifelse(is.na(age) & is.na(income), 1, 0)]
cat("n_rows where both age and income are NA:", sum(data$age_and_income_missing))
```

```
## n_rows where both age and income are NA: 7728
```

```
data[, age_and_income_missing := NULL]
```

So yes, in most rows where either age or income are missing, both age and income are missing. Hence, we know that when we remove all rows that contain a missing value anywhere, we will remove roughly 8000 – which is not too bad considering we have 30k observations in total.

```
# Remove all rows that contain at least one NA
dataCleaned <- na.omit(data)

# Total rows removed
cat("Rows removed:", nrow(data) - nrow(dataCleaned))
```

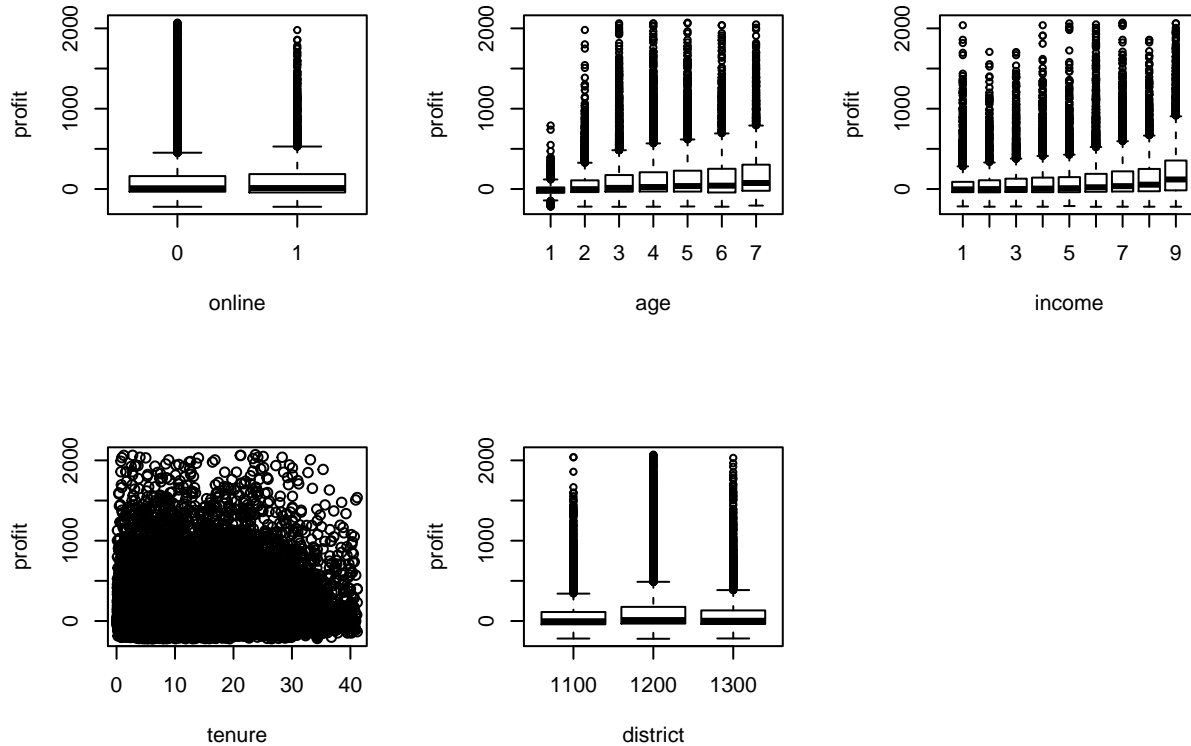
```
## Rows removed: 8822
```

Data Exploration

Plotting Features against Target

Plot each predictor against the target variable respectively. This way we get a first impression on their relationships.

```
par(mfrow = c(2, 3))
plot(profit~., data %>% select(-ID))
```

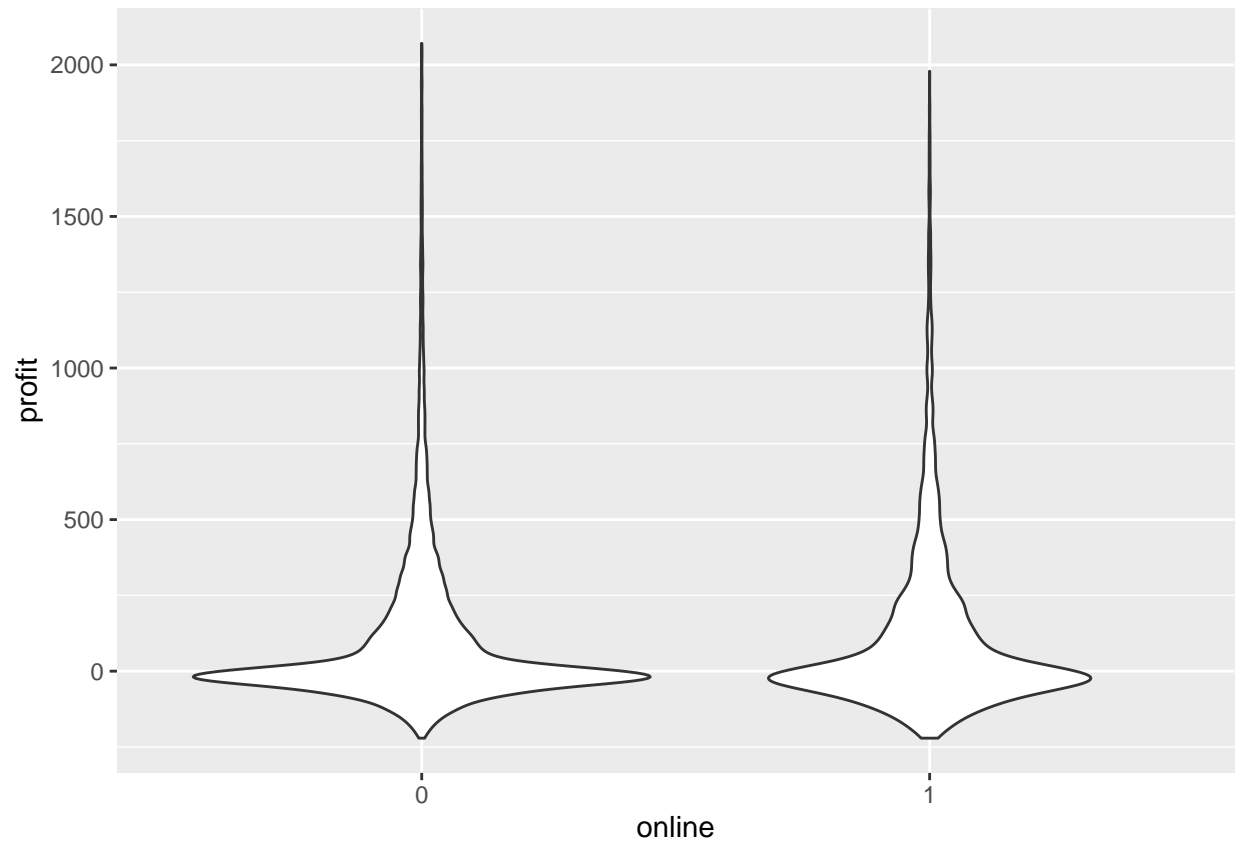


- We notice that age and income show a similar pattern, reinforcing the intuition that those two predictors are probably correlated: One would think that income increases when you get older.

Distribution of profits across online/offline customers

- The profits of online & offline customers seem to resemble a pareto-distribution
- The highest-profitable customers are offline (this might be because we simply have a lot more offline customers in the data than online customers)
- The mass of slightly profitable customers seems to be larger for online customers

```
ggplot(data, aes(y = profit, x = online)) +
  geom_violin()
```

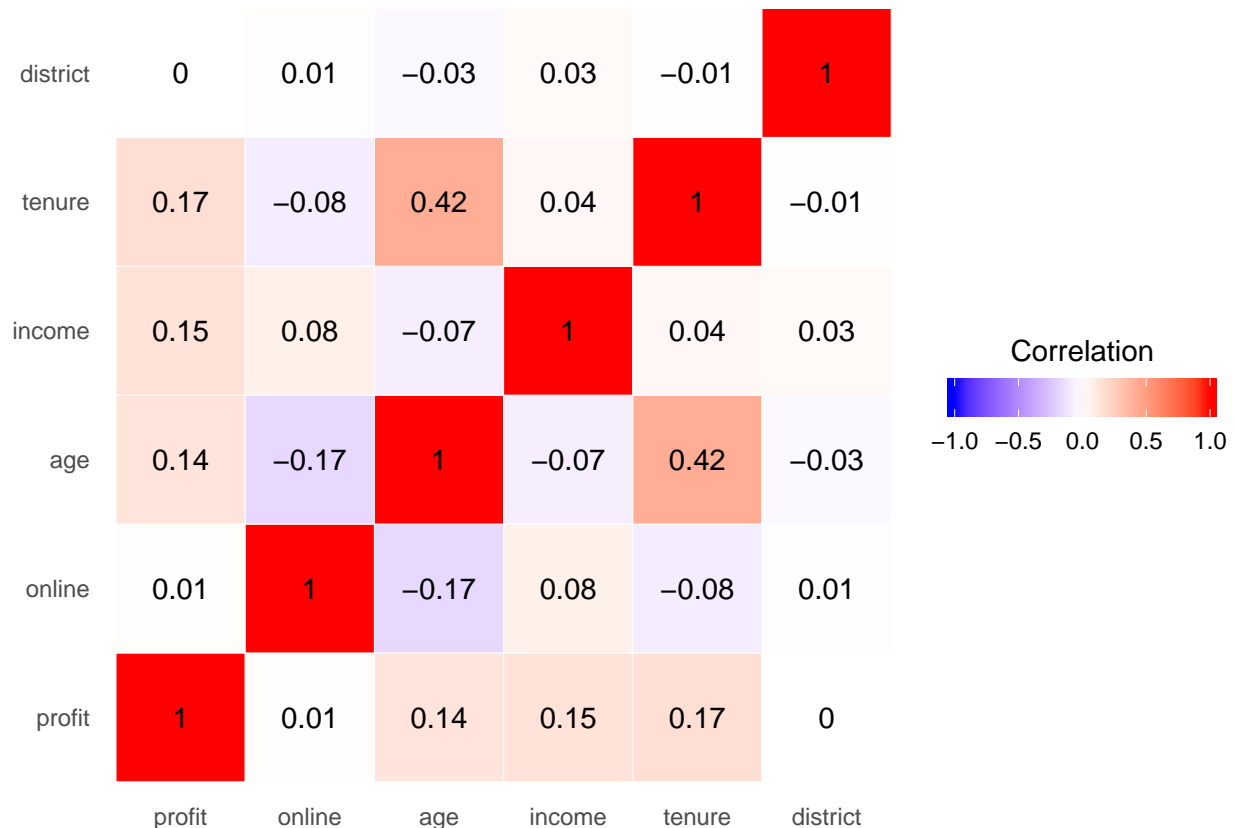


Correlation Matrix

We check for correlation across all variables, since we want to avoid the issues of **multicollinearity** (correlated predictors).

```
dataCor <- dataCleaned[, c("profit", "online", "age", "income", "tenure", "district")]
dataCor <- dataCor[, ':='(
  online = as.numeric(online),
  age = as.numeric(age),
  income = as.numeric(income),
  district = as.numeric(district)
)]

cormatrix <- round(cor(dataCor), 2)
PlotCorrelationMatrix(cormatrix)
```



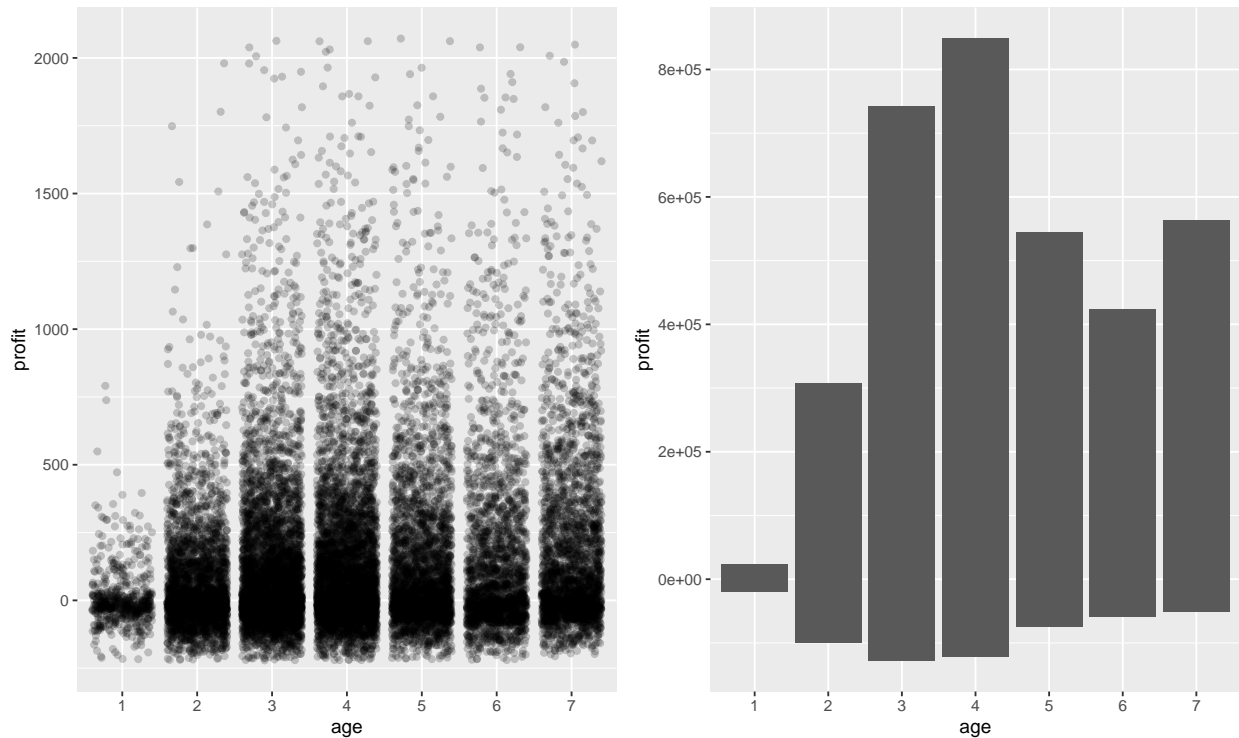
- Against intuition, age seems to be only weakly correlated with income. Moreover, against intuition, it seems to be *negatively* correlated with income. Recall that correlation checks only for a linear relationship between two variables, there might be a e.g. a polynomial relationship (young people have no money, middle-aged people have a lot of money, old people again have less money).
- age is strongly positively correlated with tenure => we should avoid including both as predictors in our regression model.
- age and being online are negatively correlated (this reinforces the intuition that older people are less likely to use online banking) => We may also avoid including both as predictors
- Since **age** and **tenure** are highly correlated and **tenure** and **online** aren't, we may include **tenure** in our regression and leave age out.

Relationship between profit and age

```
p1 <- ggplot(dataCleaned, aes(x = age, y = profit)) +
  geom_jitter(alpha = 0.2)

p2 <- ggplot(dataCleaned, aes(x = age, y = profit)) +
  geom_histogram(stat = "identity")

cowplot::plot_grid(p1, p2, nrow = 1)
```



- there seems to be a non-linearity in the relationship between **profit** and **age**. If age were a continuous feature, we might have used a polynomial of degree 2 or 3 to estimate their relationship.

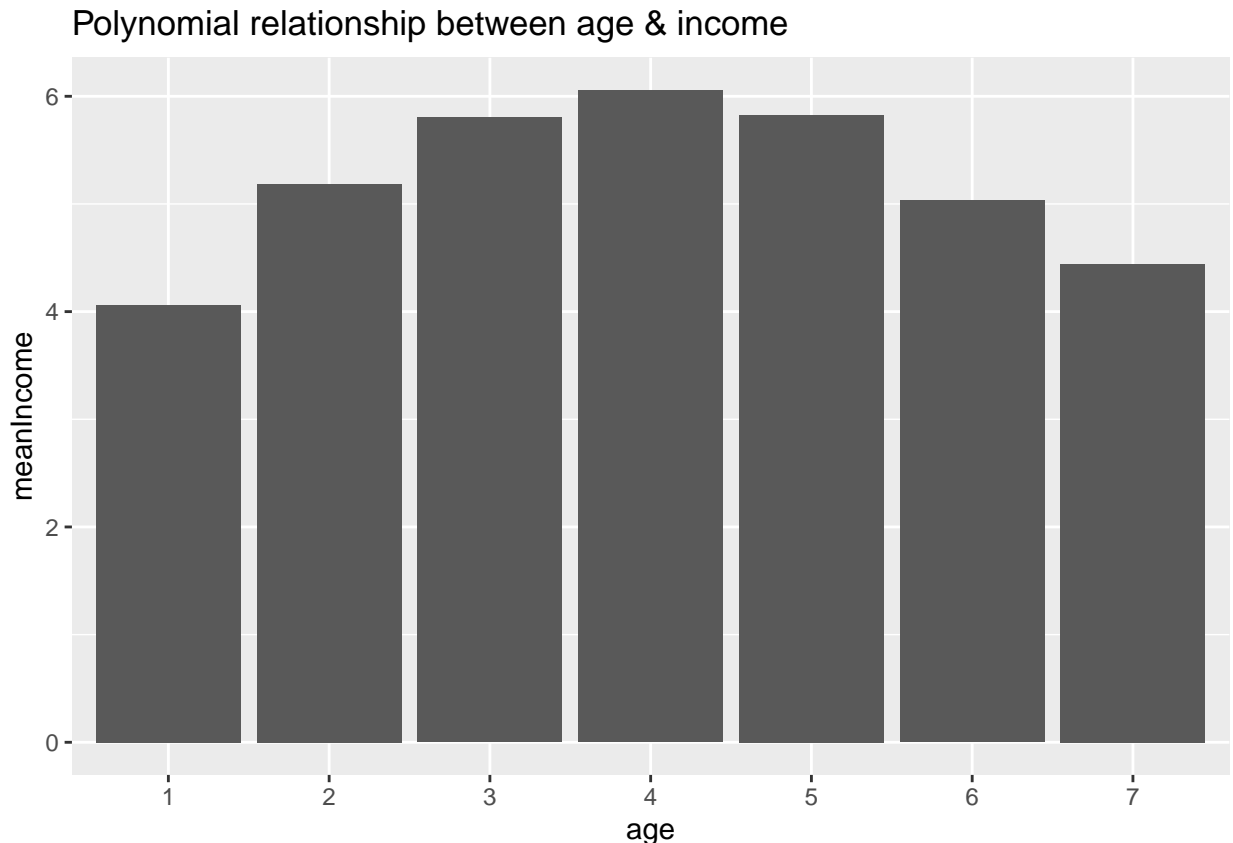
Relationship between age and income

```
dataHist <- rbindlist(lapply(unique(dataCleaned$age), function(ageCategory) {

  incomeOfAge <- dataCleaned[age == ageCategory, get("income")]
  incomeOfAge <- as.numeric(as.character(incomeOfAge))
  meanIncomeOfAge <- mean(incomeOfAge)

  return(
    data.table(
      age = ageCategory,
      meanIncome = meanIncomeOfAge
    )
  )
}))

ggplot(dataHist, aes(x = age, y = meanIncome)) +
  geom_histogram(stat = "identity") +
  ggtitle("Polynomial relationship between age & income")
```



- that's why $cor_{age, income} = -0.07$ was misleading.
- correlation-coefficient, which checks for linear relationship only, isn't able to capture the polynomial (degree-2 or possibly degree-3) relationship between age and income

Findings & Ideas

- most users of online-banking are middle-aged
- middle-aged people have the highest income
- high-income (middle-aged!) customers yield largest profits
- We have to ask whether the effect of being online changes with income – I would assume that for customers in their 20s, the effect of using online-banking is not too large, since they don't have money anyway. They might even be negative, since online-banking makes smaller, non-profitable transactions more convenient, thus driving up costs. **Thus we might consider the interaction $age * online$ for the regression model.**
- Note that online-banking should in general increase interactions of customers with the bank. Thus we have to think about what type of people buy those high-margin financial products the bank offers. High-margin financial products are probably investment products, and so these are most interesting for (1) rich and (2) middle-aged people, since they have both the *financial resources* and an *available time-horizon* to benefit from interest rates.

Linear Regression

```
linreg <- lm(profit ~ online + age + income + online*age + online*income + district, data = dataCleaned)
summary(linreg)
```

```
##
## Call:
## lm(formula = profit ~ online + age + income + online * age +
##      online * income + district, data = dataCleaned)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -499.66 -159.13  -76.16   68.20 1947.56
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -34.961     14.326  -2.440  0.01468 *
## online1        -15.677     34.682  -0.452  0.65127
## age2             29.390     13.428   2.189  0.02862 *
## age3             75.608     13.084   5.779 7.62e-09 ***
## age4             91.824     13.091   7.014 2.38e-12 ***
## age5            104.431     13.436   7.773 8.01e-15 ***
## age6            137.297     13.726  10.003 < 2e-16 ***
## age7            177.509     13.481  13.167 < 2e-16 ***
## income2           6.109      12.235   0.499  0.61760
## income3          14.748       8.861   1.664  0.09606 .
## income4          19.107       9.025   2.117  0.03426 *
## income5          25.579       9.061   2.823  0.00476 **
## income6          46.301       7.881   5.875 4.29e-09 ***
## income7          67.189       8.664   7.755 9.23e-15 ***
## income8          82.394       9.971   8.264 < 2e-16 ***
## income9         151.719       8.929  16.993 < 2e-16 ***
## district1200      19.394       6.422   3.020  0.00253 **
## district1300       7.885       7.810   1.010  0.31271
## online1:age2      23.617     30.047   0.786  0.43187
## online1:age3      33.390     29.978   1.114  0.26537
## online1:age4      33.671     30.298   1.111  0.26643
## online1:age5      58.492     32.656   1.791  0.07329 .
## online1:age6      20.153     38.555   0.523  0.60118
## online1:age7      -5.943     39.773  -0.149  0.88122
## online1:income2   -31.803     42.870  -0.742  0.45819
## online1:income3    -4.779     29.300  -0.163  0.87043
## online1:income4   -18.698     30.105  -0.621  0.53455
## online1:income5   -28.327     29.056  -0.975  0.32960
## online1:income6    -3.793     26.146  -0.145  0.88465
## online1:income7     4.893     27.414   0.178  0.85834
## online1:income8    18.775     30.022   0.625  0.53173
## online1:income9    28.531     27.222   1.048  0.29462
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 275.4 on 22780 degrees of freedom
## Multiple R-squared:  0.05327,    Adjusted R-squared:  0.05198
## F-statistic: 41.35 on 31 and 22780 DF,  p-value: < 2.2e-16
```

- The benefits of online-banking differ among different age-groups
- There is a significant positive influence on profits when middle-aged customers use online-banking:
 - middle-aged people have the both the desire and resources to invest, and therefore use financial instruments that are more profitable for the bank. Making the handling of financial instruments

easier with the help of online-banking may increase these types of interactions.

- The interaction effects of **online** and **income** indicate that online-banking might be less beneficial for customers in low-income categories. This reinforces the intuition that online-banking increases the frequency of the number of interactions between the customer and the bank, driving up costs for the bank. And the type of interactions that low-income customers make are often less profitable (e.g. small, frequent transactions)
- The bank should therefore try to get more rich and middle-aged people into using online-banking.
- The bank should avoid low-income people from using online-banking.

Problems

- We have seen that there is significant negative correlation between features **age** and **online** ($\rho = -0.17$). Thus, our regression coefficients might be biased due to multicollinearity.
- We note that **tenure** is highly correlated with **age** ($\rho = 0.42$). Further, **tenure** is less correlated with **online** ($\rho = -0.08$) than age is. Thus, we may repeat the same linear regression but replace **age** with **tenure**.

```
linreg <- lm(profit ~ online + tenure + income + online*income + district, data = dataCleaned)
summary(linreg)
```

```
##
## Call:
## lm(formula = profit ~ online + tenure + income + online * income +
##     district, data = dataCleaned)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -529.18 -153.35  -74.57   66.12  1975.67
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    11.6602     8.4793   1.375   0.1691
## online1         -6.2186    23.3341  -0.267   0.7899
## tenure           5.4421     0.2149  25.320 < 2e-16 ***
## income2          9.6229    12.2083   0.788   0.4306
## income3         11.4914     8.8344   1.301   0.1934
## income4         12.1986     8.9668   1.360   0.1737
## income5         16.2611     8.9663   1.814   0.0698 .
## income6         36.4591     7.7675   4.694 2.70e-06 ***
## income7         53.4069     8.5459   6.249 4.19e-10 ***
## income8         71.4644     9.8644   7.245 4.47e-13 ***
## income9        137.2900     8.7723  15.650 < 2e-16 ***
## district1200     14.4556     6.4028   2.258   0.0240 *
## district1300      3.5745     7.7937   0.459   0.6465
## online1:income2 -29.9795    42.7973  -0.700   0.4836
## online1:income3  -8.0274    29.2429  -0.275   0.7837
## online1:income4  -9.4272    29.9392  -0.315   0.7529
## online1:income5 -17.0106    28.8811  -0.589   0.5559
## online1:income6   7.2587    25.8951   0.280   0.7792
## online1:income7  22.9395    27.1618   0.845   0.3984
## online1:income8  31.0354    29.7171   1.044   0.2963
## online1:income9  46.7522    26.8558   1.741   0.0817 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 275 on 22791 degrees of freedom
## Multiple R-squared:  0.05555,    Adjusted R-squared:  0.05472
## F-statistic: 67.02 on 20 and 22791 DF,  p-value: < 2.2e-16
```

- using online-banking has a significant, positive effect on profits for the highest-income class. Again reinforcing the intuition that the highest-income class buys more profitable financial products, and since online-banking makes it easier for them to do so, they may buy more and thus boost profits.
- Recall that middle-aged people were the richest – hence these findings are in that sense related to our first regression.

Sanity check of findings

We can also do a rough sanity check on the hypothesis that *online-banking is most beneficial for middle-aged customers*. Below, we compute for each age category the relative amount of online (offline) customers that have yielded above-average profits (compared to their age-category's specific average).

```
# Convert profits to a binary feature that indicates whether a customer
# yielded an above-average profit
dataCleaned[, meanProfit := mean(profit), by = age]
dataCleaned[, isAboveMeanProfit := profit >= meanProfit]

results <- rbindlist(lapply(unique(dataCleaned$age), function(ageCategory) {
  dataTemp <- dataCleaned[age == ageCategory]

  nOnline <- nrow(dataTemp[online == 1])
  nOnlineAboveMeanProfits <- nrow(dataTemp[isAboveMeanProfit == 1 & online == 1])

  nOffline <- nrow(dataTemp[online == 0])
  nOfflineAboveMeanProfits <- nrow(dataTemp[isAboveMeanProfit == 1 & online == 0])

  return(data.table(
    ageCategory = ageCategory,
    percOnlineAboveMeanProfits = round(nOnlineAboveMeanProfits / nOnline, 2),
    percOfflineAboveMeanProfits = round(nOfflineAboveMeanProfits / nOffline, 2)
  ))
}))

results[order(ageCategory)]
```

```
##   ageCategory percOnlineAboveMeanProfits percOfflineAboveMeanProfits
## 1:           1                   0.35                   0.33
## 2:           2                   0.36                   0.31
## 3:           3                   0.37                   0.32
## 4:           4                   0.39                   0.32
## 5:           5                   0.39                   0.33
## 6:           6                   0.35                   0.33
## 7:           7                   0.40                   0.35
```

- Across all age-groups, there seems to be a positive effect of using online-banking
- Note that the largest difference (in terms of percentage points) is found for middle-aged customers, with gains of 5-7 percentage points.

Further Ideas

- *Partialing out*: By regressing `income ~ age + age**2` we get information on how much age explains income. The residuals are then those variations in income that are not explained by age. We could

then put these into our regression `profit ~`

- *Mediation Analysis*: A more sophisticated way to look for causal relationship between `profit` and `online`.