

Continuous Uniform distribution

Application

Busses arrive at a specific stop at 15-minute intervals starting at 7 a.m. If a passenger arrives at the stop at a time that is uniformly distributed between 7 a.m and 7.30 a.m., what is the probability that he waits

(a) less than 5 minutes for a bus

(b) more than 10 minutes for a bus

$$\begin{aligned} \text{(a)} \quad & P(10 < X < 15) + P(25 < X < 30) \\ &= \int_{10}^{15} \frac{1}{30} dx + \int_{25}^{30} \frac{1}{30} dx = \frac{1}{6} + \frac{1}{6} = \underline{\frac{1}{3}} \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad & P(0 < X < 5) + P(15 < X < 20) \\ &= \int_0^5 \frac{1}{30} dx + \int_{15}^{20} \frac{1}{30} dx = \underline{\frac{1}{3}} \end{aligned}$$

Reference : A first course in Probability ;
Sheldon Ross ; 2010 .