## Mean Squared Error dan Estimator

Mean Squared Error (MSE) of an estimator O is defined as

$$C_{\theta}[(\hat{\theta}-\theta)^{2}] = Var_{\theta}(\hat{\theta}) + (bias(\hat{\theta}))^{2}$$

## Proof:

$$|TSE(\hat{\theta})| = E[(\hat{\theta} - \theta)^{2}]$$

$$= E[(\hat{\theta} - E[\hat{\theta}] + E[\hat{\theta}] - \theta)^{2}]$$

$$= E[(\hat{\theta} - E[\hat{\theta}])^{2}] + E[(E[\hat{\theta}] - \theta)^{2}]$$

$$= Vor(\hat{\theta}) + (E[\hat{\theta}] - \theta]^{2} + 0$$

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=  $Var(\hat{\theta}) + bias(\hat{\theta})$ 

Introduction to Mathematical Statistics; Hogg, McKean, Craig; 2019