Introduction to Kaplan-Meier analysis

The Kaplan-Meier estimator is given by the following formula:

$$\hat{S}(t) = \prod_{t_i \le t} (1 - \hat{q}_i) = \prod_{t_i \le t} \left(1 - \frac{q_i}{n_i} \right)$$

 $\hat{S}(t)$ denoting the survival function at time t. More technical detail found in the book (Applied Survival Analysis Using R)

Dataset

veteran: dataset of 137 observations \times 8 variables form a two-treatment randomized trial for lung cancer.

trt: 1=standard 2=test

celltype: 1=squamous, 2=smallcell, 3=adeno, 4=large

time: survival time status: censoring status

karno: Karnofsky performance score (100=good) diagtime: months from diagnosis to randomisation

ageA: in years **prio**r: prior therapy 0=no, 10=yes

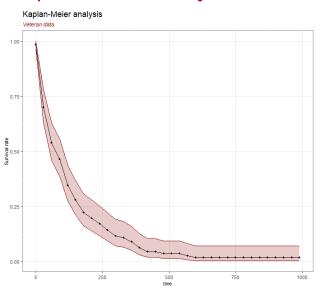
```
1 > head(veteran)
   trt celltype time status karno diagtime age prior
    1 squamous
               72
                            60
                                       69
   1 squamous
              411
                          70
                                     5 64
                                             10
                                    3 38
   1 squamous 228
                         60
   1 squamous
              126
                   1 60
                                    9 63
                                             10
7 5
   1 squamous
              118
                   1 70
                                    11 65
                                             10
    1 squamous
                                       49
8 6
               10
                            20
                                              0
```

Summary

From this initial summary which has class "summary survfit", we will make a dataframe ready for ploting withing the ggplot2 environment.

```
survival.30.dataset = summarv(kma 1, times = c(1, (1:33)*30))
    survival 30 dataset
3 Call: survfit(formula = Surv(time, status) ~ 1, data = veteran)
4
        n.risk n.event survival
                                    std.err lower 95% CI upper 95% CI
6
            137
                             0.985
                                     0.0102
                                                  0.96552
                                                                  1.0000
       1
7
      30
             97
                      39
                             0.700
                                     0.0392
                                                  0.62774
                                                                  0.7816
8
      60
             73
                      22
                             0.538
                                     0.0427
                                                  0.46070
                                                                  0.6288
9
      90
             62
                      10
                             0.464
                                     0.0428
                                                  0.38731
                                                                  0.5560
10
     120
             43
                             0.346
                                     0.0414
                                                  0.27345
                                                                  0.4372
                      15
11
     150
             34
                             0.280
                                     0.0395
                                                  0.21240
                                                                  0.3693
12
     180
             27
                             0.222
                                     0.0369
                                                  0.16066
                                                                  0.3079
13
     210
             23
                             0.197
                                     0.0355
                                                  0.13814
                                                                  0.2802
14
                             0.171
     240
              19
                                     0.0338
                                                  0.11613
                                                                  0.2520
15
    270
             16
                       3
                             0.144
                                     0.0319
                                                  0.09338
                                                                  0.2223
16
    300
             13
                       3
                             0.117
                                     0.0295
                                                  0.07147
                                                                  0.1917
17
    330
             12
                             0.108
                                     0.0285
                                                  0.06439
                                                                  0.1813
18
     360
              10
                             0.090
                                     0.0265
                                                  0.05061
                                                                  0.1602
19 . . .
```

Kaplan-Meier analysis

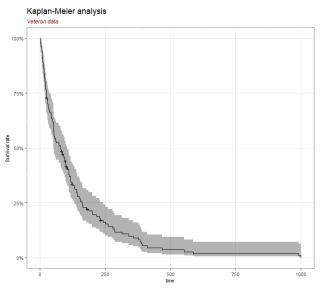


	time	surv
1	1	0.9854
2	30	0.7004
3	60	0.5382
4	90	0.464
5	120	0.3458
6	150	0.2801
7	180	0.2224
8	210	0.1967
9	240	0.1711
10	270	0.1441
11	300	0.1171
12	330	0.1081
13	360	0.09
14	390	0.063
15	420	0.045
16	450	0.045
17	480	0.036
18	510	0.036
19	540	0.036
20	570	0.027

Main observations

- At the first month (after 30 days), the survival rate or probability of survival is about 70%.
- There seems to be some kind of breakup point at 6 months (after 180 days) as the slope gets less steep.
- After on year, the survival rate is lower than 10%. A patient has a 10% or less probability of surving one year.
- Information about censoring (a vertical line on the Kaplan-Maier survival function) is obtained in R using "autoplot()". It is shown in the next slide.

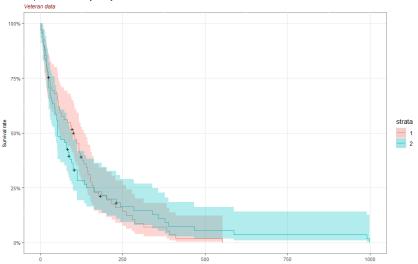
Kaplan-Meier analysis using "autoplot()"



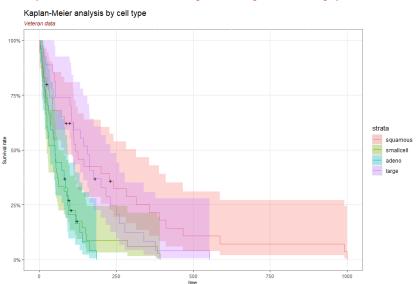
	time	surv
1	1	0.9854
2	30	0.7004
3	60	0.5382
4	90	0.464
5	120	0.3458
6	150	0.2801
7	180	0.2224
8	210	0.1967
9	240	0.1711
10	270	0.1441
11	300	0.1171
12	330	0.1081
13	360	0.09
14	390	0.063
15	420	0.045
16	450	0.045
17	480	0.036
18	510	0.036
19	540	0.036
20	570	0.027

Kaplan-Meier analysis by treatment





Kaplan-Meier analysis by cell type



Main observations

- Treatment stratum 2 has the overall better survival rate with a better survival curve (overall less steep)
- Cell type "squamous" has the overall better survival rate compared to small cell, adeno and lage.

R code (1/5) - Load libraries and dataset

```
1 > #load libraries
2 > library(survival)
3 > library(ggplot2)
4 > library(gridExtra)
    # load data and head of the dataset
    data(veteran)
    head(veteran)
    trt celltype time status karno diagtime age prior
10 1
      1 squamous
                    72
                                  60
                                                69
11 2
      1 squamous
                   411
                                  70
                                                64
                                                       10
12 3
      1 squamous
                   228
                                  60
                                                38
13 4
      1 squamous
                                                63
                   126
                                 60
                                                       10
14 5
      1 squamous
                   118
                                 70
                                            11
                                                65
                                                       10
15 6
      1 squamous
                   10
                                  20
                                                49
```

R code (2/6) - Dataset with censoring

```
1 > km = with(veteran, Surv(time, status))
2 > head(km, 100)
    [1]
         72
              411
                    228
                          126
                                118
                                       10
                                            82
                                                 110
                                                       314
                                                             100+
                                                                               144
                                                                                     25+
          30
              384
                       4
                           54
                                 13
                                      123+
   F221
          97+ 153
                     59
                          117
                                 16
                                      151
                                             22
                                                  56
                                                        21
                                                              18
                                                                   139
                                                                          20
                                                                                31
                                                                                          287
          18
                51
                    122
                           27
                                 54
   Γ431
                     10
                                       35
                                                        12
         63
              392
                                 92
                                           117
                                                 132
                                                             162
                                                                     3
                                                                              177
                                                                                    162
                                                                                          216
         553
              278
                    12
                          260
                                200
                                      156
   [64] 182+ 143
                    105
                          103
                                250
                                      100
                                           999
                                                 112
                                                        87+ 231+ 242
                                                                        991
                                                                              111
                                                                                          587
         389
                33
                     25
                          357
                                467
                                      201
   [85]
           1
               30
                     44
                          283
                                15
                                      25
                                           103+
                                                  21
                                                        13
                                                              87
                                                                     2
                                                                          20
                                                                                           99
```

R code (3/6) - Kaplan-Meier analysis

```
1 > # Kaplan-Meier estimates of the probability of survival over time
2 > kma_1 = survfit(Surv(time, status) ~ 1, data=veteran)
3 * # max time: 999 days (about 33 months (30 days))
4 > survival.30.dataset = summary(kma_1, times = c(1, (1:33)*30))
5 > # convert summary to data.frame for plotting
6 > cols = lapply(1:15 , function(x) survival.30.dataset[x])
7 > df = do.call(data.frame, cols)
8 >
9 > # table to be displayed next to the graph as a second graph
10 > df2 = df[1:20, c(2,6)]
11 > df2$surv = round(df2$surv, 4)
```

R code (4/6) - plotting with ggplot2

```
1 # KM plot (ggplot2)
2 p1 = ggplot(df, aes(x = time, y = surv)) +
   geom line(color = 'black') +
4 geom_point(size = 1.2) +
   geom_ribbon(aes(ymin = lower, ymax = upper), alpha=0.2, fill= 'darkred', col =
        'darkred') +
6
    labs(title = 'Kaplan-Meier analysis',
8
         subtitle = 'Veteran data',
9
         v="Survival rate", x="time") +
10
    theme(axis.text=element_text(size=8),
11
          axis.title=element_text(size=8),
12
          plot.subtitle=element text(size=9. face="italic". color="darkred").
13
          panel.background = element rect(fill = "white", colour = "grev50").
14
          panel.grid.major = element_line(colour = "grey90"))
15
16 p2 = tableGrob(df2)
17
18 grid.arrange(p1, p2, ncol = 2, nrow = 1, widths = c(6, 2))
```

R code (5/6) - autoplot

```
1 # or, more quickly (and with information about censoring)
 2 p3 = autoplot(kma 1) +
    labs(title = 'Kaplan-Meier analysis',
         subtitle = 'Veteran data',
         v="Survival rate", x="time") +
    theme(axis.text=element text(size=8).
7
          axis.title=element_text(size=8),
8
          plot.subtitle=element_text(size=9, face="italic", color="darkred"),
9
          panel.background = element_rect(fill = "white", colour = "grey50"),
10
          panel.grid.major = element_line(colour = "grey90"))
11
12 p4 = tableGrob(df2) # to have a table with time and survival rate
13 grid.arrange(p3, p4, ncol = 2, nrow = 1, widths = c(6, 2))
```

R code (6/6) - Analysis by treatment

```
Analysis by treatment
 3 # Kaplan-Meier estimates of the probability of survival over time
 4 kma 3 = survfit(Surv(time, status) ~ trt, data=veteran)
 5 # max time: 999 days (about 33 months (30 days))
 6 survival.30.dataset.celltype = summary(kma_3, times = c(1, (1:33)*30))
 8 # plotting
 9 autoplot(kma 3) +
10
    labs(title = 'Kaplan-Meier analysis by celltype',
11
         subtitle = 'Veteran data'.
         v="Survival rate", x="time") +
12
13
    theme(axis.text=element_text(size=8),
14
          axis.title=element_text(size=8),
          plot.subtitle=element text(size=9. face="italic". color="darkred").
15
          panel.background = element_rect(fill = "white", colour = "grey50"),
16
17
          panel.grid.major = element_line(colour = "grey90"))
```

References

Survival Analysis with R, by Joseph Rickert, 2017-09-25, link to the article on R-views:

https://rviews.rstudio.com/2017/09/25/survival-analysis-with-r/

Applied Survival Analysis Using R, Dirk F. Moore, 2016, Springer, ISBN 978-3-319-31245-3 (e-book)