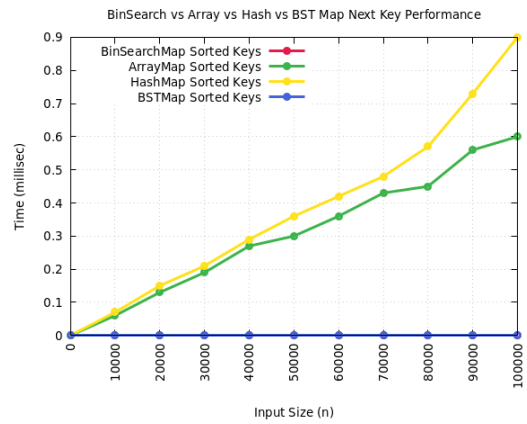
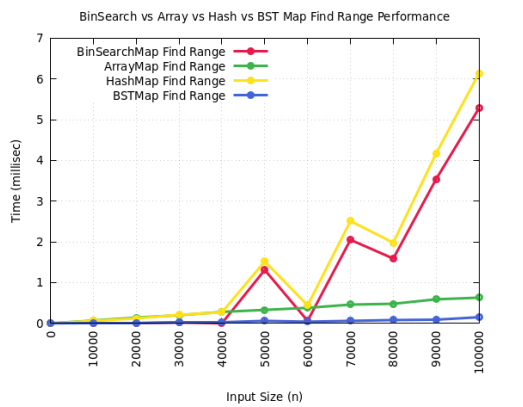
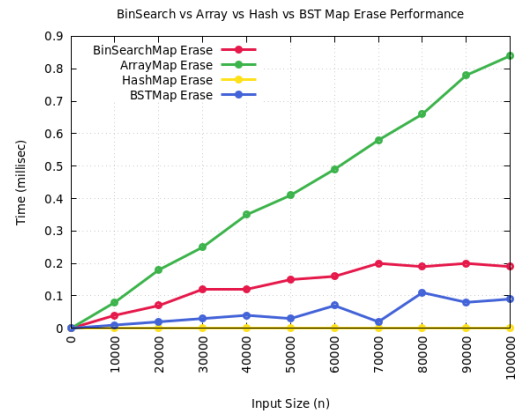
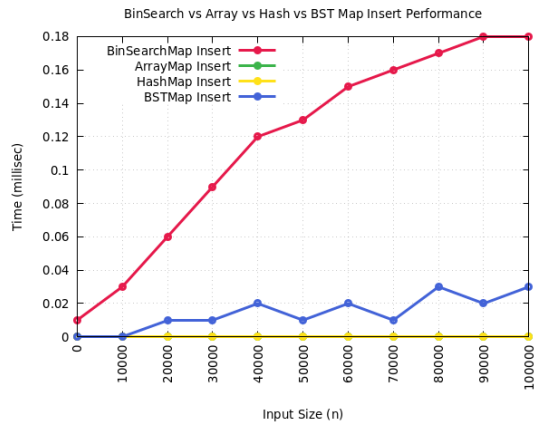
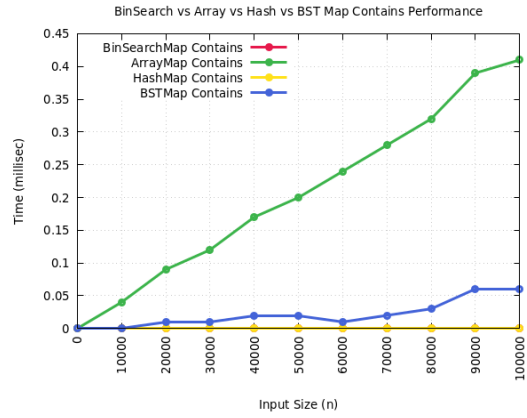
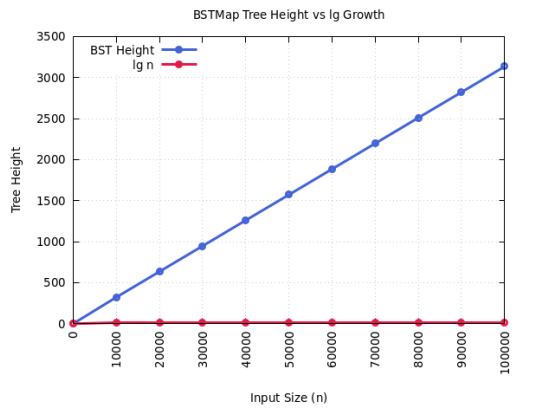
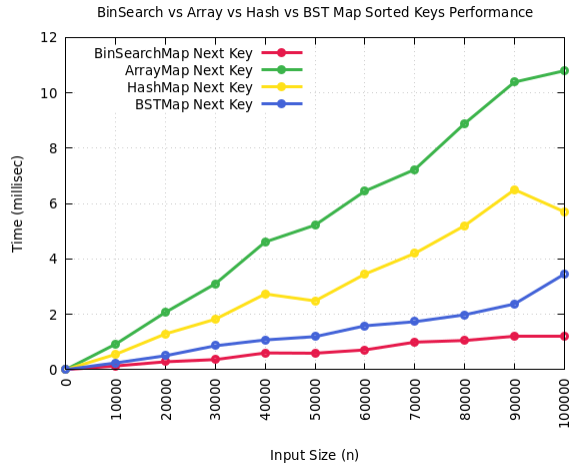


## HW8 Writeup (Spring 2022)

Plots:





The tree height graph in the top left shows the height as calculated by the `height()` method within my `BSTMap` class. This function computes what the max height of the tree generated at each input size used. Compared to  $\lg(n)$ , this class is far from ideal when it comes to generating a tree with reasonable height for increasingly large input sizes.

The contains performance graph above shows the comparison of the `contains()` method between the four different Map implementations completed in this course. `BSTMap` appears to be more complex than both `HashMap` and `BinSearchMap` in terms of time complexity. This is due to the need to navigate a path to a specific node within a tree rather than simply iterating through what is essentially a sequence.

The Erase performance graph in the bottom left shows the same four Map structures. This time, `BSTMap` beat out `BinSearchMap` even though erasing is particularly complex in terms of steps in `BSTMap`. I am not sure why `BSTMap` is faster in this case, unless `BinSearchMap`, in utilizing the `BinSearch` helper method, holds a worse time complexity than using the mix of iteration and recursion found within `erase` in `BSTMap`.

The Find Range performance graph shows `BSTMap` as the faster of the four Map implementations. This is simply due to the strict recursion being used to add only the necessary nodes, not every viewed node from within the tree.

The insert performance graph shows `BSTMap` as more efficient than `BinSearchMap`, but worse than `ArrayMap` and `HashMap`. This can be attributed to both iterating down a root-to-leaf path and the constraint of only inserting leaf nodes. Whereas `BinSearchMap` requires an  $O(n \log n)$  complexity to search for the key and then insert it at its correct place as required to keep a sorted list for `BinSearch`.

The sorted keys graph above places `BSTMap` between `BinSearchMap` and `HashMap` in time complexity for sorting a Map. As `BinSearchMap` maintains a sorted list throughout operations, `BSTMap` can be said to be the fastest in terms of the structures implemented in this course that sort a list in real time with this function. My implementation of sorted keys in `BSTMap` utilizes a call to `find_keys` (find range) after iterating to where a key should go.

Finally, the next key graph displays the performance of each structure in obtaining the next sequential key after any key is passed in as a parameter. BSTMap appears to have an almost constant time complexity, like BinSearchMap. As the other two structures take longer, it is hard to determine what time complexity is helped by these two fast next key structures. Though, by looking at my implementation, I can reason that BSTMap follows a path using iteration to obtain the location of the next sequential key in the sequence.

#### Challenges:

I only struggled to implement `next_key` and `prev_key`. These functions do not pass their respective tests. Also, when running `valgrind` I can see a large error count produced in around 660 contexts. I am unsure as to why these errors are present.