

1

A

Yes this is. $5+2=7$ is a proposition
no variables present so it is. It shows
a statement that is either true or false

B

no, there is no statement that is
either true or false

C

Yes, this is a true or false statement.
It most likely is false, but still could be
proven

D

yes, this is a true or false that is also
true, It is self dependent, but addressable

2

A

$p \quad q$		$\neg q \rightarrow p$		\downarrow
T	T	F	T	T
T	F	T	T	T
F	T	F	F	T
F	F	T	F	F

B

$p \quad q \quad r$			$(p \vee q) \rightarrow r$	
T	T	T	T	T
T	T	F	T	F
T	F	T	T	T
T	F	F	F	F
F	T	T	T	T
F	T	F	T	F
F	F	T	F	F
F	F	F	T	T

3

A

$$s \vee \neg f$$

B

$$s \rightarrow (\neg r \wedge f)$$

4

$p \quad q$		$(p \rightarrow \neg q) \equiv \neg p \vee \neg q$	
T	T	F	F
T	F	T	T
F	T	T	T
F	F	T	T

One reason is that this is the disjunctive form shown to be true. Another reason is that the negation of a means that there are more cases it can be true, this logically equivalent

5

$p \quad q \quad r$			$p \rightarrow (q \rightarrow r)$		$(p \rightarrow q) \rightarrow r$	
T	T	T	T	T	T	T
T	T	F	T	F	F	F
T	F	T	T	T	T	T
T	F	F	T	T	T	T
F	T	T	T	T	T	T
F	T	F	T	T	T	T
F	F	T	T	T	T	T
F	F	F	T	T	T	T

r change back and forth more than p so it will be hard for something to be equivalent

⑥ 2^n p and $q = 4$
 $p = 2$ thus 2^n
 $2^{(2^4)}$ options for connectives

⑦ $\neg p \rightarrow (p \rightarrow q) \equiv T$

↓

$\equiv \neg p \rightarrow (\neg p \vee q)$ Disjunctive form

↓

$\equiv \neg(\neg p) \vee (\neg p \vee q)$

$\equiv p \vee (\neg p \vee q)$ D. negation

$\equiv (p \vee \neg p) \vee q$ Associative law

$\equiv T \vee q$ Excluded middle

$\equiv T$ Domination laws