```
In [1]:
          import time
          start_time = time.time()
In [2]:
          import numpy as np
          import pandas as pd
          import os, time, pickle, gzip
          import matplotlib.pyplot as plt
          import seaborn as sns
          color = sns.color_palette()
          import matplotlib as mpl
          from sklearn import preprocessing as pp
          %matplotlib inline
         자료읽기
In [3]:
          TRX = pd.read_csv('C:\WORK/mnistTRX.csv')
          VLX = pd.read_csv('C:\WORK/mnistVLX.csv')
          TSX = pd.read_csv('C:\WORK/mnistTSX.csv')
          TRy = pd.read_csv('C:\WORK/mnistTRy.csv')['y']
VLy = pd.read_csv('C:\WORK/mnistVLy.csv')['y']
          TSy = pd.read_csv('C:\WORK/mnistTSy.csv')['y']
          iTR = range(0, len(TRX))
          iVL = range(len(TRX), len(TRX)+len(VLX))
          iTS = range(len(TRX) + len(VLX), len(TRX) + len(VLX) + len(TSX))
          nX = [TRX.shape, VLX.shape, TSX.shape]
          ny = [TRy.shape, VLy.shape, TSy.shape]
pd.DataFrame(nX, index=['TRX', 'VLX', 'TSX'], columns=['n', 'p'])
Out[3]:
          TRX 50000 784
          VLX 10000 784
          TSX 10000 784
In [4]:
          pd.DataFrame(ny, index=['TRy', 'VLy', 'TSy'], columns=['n'])
Out[4]:
          TRy 50000
          VLv 10000
          TSy 10000
In [5]:
          TRX.describe()
Out[5]:
                    x01
                            x02
                                    x03
                                            x04
                                                     x05
                                                             x06
                                                                     x07
                                                                             x08
                                                                                     x09
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```

min 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 ... 0.000000 0.000000 0.000000 25% 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 ... 0.000000 0.000000 0.000000 50% 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 ... 0.000000 0.000000 0.000000 75% 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 ... 0.000000 0.000000 0.000000 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 ... 0.992188 0.992188 0.988281 max 8 rows × 784 columns

1

```
9
        Name: y, dtype: int64
In [7]:
         TRy.head()
              5
Out[7]:
              0
              4
        2
         3
              1
        Name: y, dtype: int64
```

# 개별 이미지 시각화

```
In [8]:
         def view_digit(example):
             label = TRy.loc[example]
             image = TRX.loc[example, :].values.reshape([28, 28])
             plt.title('Example: %d Label: %d' % (example, label))
             plt.imshow(image, cmap=plt.get_cmap('gray'))
             plt.show()
```

In [9]: view digit(0)

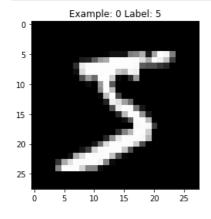
Out[6]: 0

3

4

0 4

1



# 레이블 조정하기

```
In [10]:
          from sklearn.preprocessing import OneHotEncoder, LabelBinarizer
          LB = LabelBinarizer()
          TRY = LB.fit_transform(TRy)
          TRY[0]
```

Out[10]: array([0, 0, 0, 0, 0, 1, 0, 0, 0])

## 층화추출한 자료

```
In [11]:
           TRXO = TRX.groupby(TRy).apply(lambda x: x.sample(100, random_state=2018))
            iTR0 = TRX0.index.to_frame()[1]
TRX0.set_index(iTR0, inplace=True)
            TRy0 = TRy.iloc[iTR0]
```

#### 모델 적합/성분계산

```
In [12]:
             from sklearn.decomposition import PCA
             n components = 784
             whiten = False
             random_state = 2018
             Epca = PCA(n components=n components,
                           whiten = whiten.
                           random state=random state)
             TRXTpca = Epca.fit_transform(TRX)
             TRXTpca = pd.DataFrame(data=TRXTpca, index=iTR)
In [13]:
             TRXTpca.corr().round(5)
                    0
                          1
                                2
                                     3
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Out[13]:
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             TRXTpca.var().round(5)
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Out[14]:
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            Length: 784, dtype: float64
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```

784 rows × 784 columns

#### 모델 설명력

2

-2

Second Vector

```
In [16]:
            def summaryPCA(PCAobj):
                 eigval = pd.DataFrame(PCAobj.explained variance )
                 prop = pd.DataFrame(PCAobj.explained variance ratio )
                 cumul = pd.DataFrame(np.cumsum(prop)/prop.sum())
                 vrexp = pd.concat([eigval, prop, cumul], axis=1).T
                 vrexp.index = ['Eigenvalue', 'Prop', 'Cumulative']
                 return vrexp
            vrexp = summaryPCA(Epca)
            vrexp.loc[:, [0, 1, 2, 9, 19, 49, 99, 199, 299, 399, 499, 599, 699]].round(4)
                            0
                                    1
                                           2
                                                         19
                                                                 49
                                                                         99
                                                                               199
                                                                                       299
                                                                                              399
                                                                                                      499
                                                                                                              599
                                                                                                                 699
Out[16]:
            Eigenvalue 5.1083 3.7010 3.2587 1.2403 0.6034 0.1683 0.0528 0.0148 0.0071
                                                                                           0.0031
                                                                                                   0.0008 0.0001
                                                                                                                   0.0
                 Prop 0.0974 0.0706 0.0622 0.0237 0.0115 0.0032 0.0010 0.0003 0.0001
                                                                                           0.0001 0.0000
           Cumulative 0.0974 0.1680 0.2302 0.4888 0.6440 0.8249 0.9147 0.9665 0.9862 0.9958 0.9993 1.0000
In [17]:
            fig, ax = plt.subplots(ncols=3, figsize=(16, 4))
            ev = sns.barplot(data=pd.DataFrame(vrexp.loc['Eigenvalue', :20]).T, color='b', ax=ax[0]);
            ev.set(title='Eigenvalues of S', xlabel='PC', ylabel='Eigenvalues')
pr = sns.barplot(data=pd.DataFrame(vrexp.loc['Prop', :20]).T, color='b', ax = ax[1]);
pr.set(title='Variance Explained by PC', xlabel='PC', ylabel='Proportion')
            cm = sns.barplot(data=pd.DataFrame(vrexp.loc['Cumulative', :20]).T, color='b', ax=ax[2]);
            cm.set(title='Variance Explained by PC(Cumulative)', xlabel='PC', ylabel='Cumulative Proportion', ylim=[0, 1]);
                            Eigenvalues of S
                                                                       Variance Explained by PC
                                                                                                                Variance Explained by PC(Cumulative)
                                                                                                          1.0
                                                          0.10
                                                                                                          0.8
                                                          0.08
              4
                                                                                                        Cumulative Proportion
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                                                        Proportion
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                                                          0.04
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                                                               0 1 2 3 4 5 6 7 8 9 1011 1213 1415 1617 1819 20
                                  PC
                                                                                 PC
In [18]:
            def scatterPlot(xDF, yDF, algoName):
                 tempDF = pd.DataFrame(data=xDF.loc[:, 0:1], index=xDF.index)
                 tempDF = pd.concat((tempDF, yDF), axis=1, join="inner")
tempDF.columns = ["First Vector", "Second Vector", "Label"]
                 sns.lmplot(x="First Vector", y="Second Vector", hue="Label", data=tempDF, fit_reg=False)
                 ax = plt.qca()
                 ax.set_title("Separation of Observations using"+algoName)
In [19]:
            scatterPlot(TRXTpca, TRy, 'PCA')
                       Separation of Observations usingPCA
               6
               4
```

Label 0

1

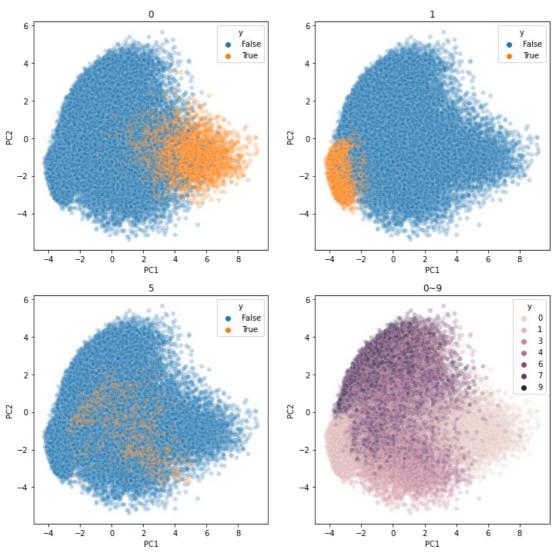
6 7

8

```
-4 -2 0 2 4 6 8
```

```
fig, axs = plt.subplots(nrows=2, ncols=2, figsize=(12,12))
d0 = sns.scatterplot(x=TRXTpca.loc[:, 0], y=TRXTpca.loc[:, 1], hue=TRy==0, alpha=0.25, ax=axs[0,0]);
d0.set(xlabel='PC1', ylabel='PC2', title='0')
d1 = sns.scatterplot(x=TRXTpca.loc[:, 0], y=TRXTpca.loc[:, 1], hue=TRy==1, alpha=0.25, ax=axs[0,1]);
d1.set(xlabel='PC1', ylabel='PC2', title='1')
d5 = sns.scatterplot(x=TRXTpca.loc[:, 0], y=TRXTpca.loc[:, 1], hue=TRy==5, alpha=0.25, ax=axs[1,0]);
d5.set(xlabel='PC1', ylabel='PC2', title='5')
dd = sns.scatterplot(x=TRXTpca.loc[:, 0], y=TRXTpca.loc[:, 1], hue=TRy, alpha=0.25, ax=axs[1,1]);
dd.set(xlabel='PC1', ylabel='PC2', title='0~9')
```

Out[20]: [Text(0.5, 0, 'PC1'), Text(0, 0.5, 'PC2'), Text(0.5, 1.0, '0~9')]



```
In [21]: TRX.iloc[:, [350,406]].head()
```

```
        x351
        x407

        0
        0.273438
        0.937500

        1
        0.000000
        0.000000

        2
        0.000000
        0.941406

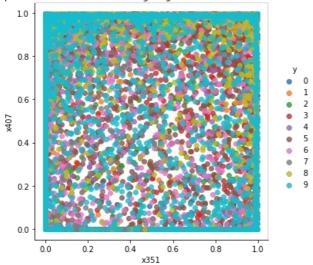
        3
        0.800781
        0.980469

        4
        0.031250
        0.988281
```

```
In [22]:
XX = pd.DataFrame(data=TRX.iloc[:, [350,406]], index=iTR)
XX = pd.concat([XX, TRy], axis=1, join='inner')
sns.lmplot(x='x351', y='x407', hue='y', data=XX, fit_reg=False)
ax = plt.gca()
ax.set_title('Separation of Observations Using Original Feature Set (x351, x407);')
```

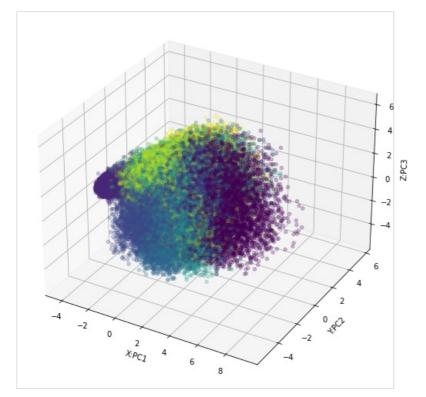
Out[22]: Text(0.5, 1.0, 'Separation of Observations Using Original Feature Set (x351, x407);')

Separation of Observations Using Original Feature Set (x351, x407);



```
from mpl_toolkits.mplot3d import Axes3D
fig = plt.figure(figsize=(16,9))
ax = plt.axes(projection='3d')
p = ax.scatter3D(TRXTpca[0], TRXTpca[1], TRXTpca[2], alpha=0.25, c=TRy)
ax.set_xlabel('X:PC1')
ax.set_ylabel('Y:PC2')
ax.set_zlabel('Z:PC3')
```

#### Out[23]: Text(0.5, 0, 'Z:PC3')



```
import plotly.express as px

In [25]: fig = px.scatter_3d(TRXTpca, x=0, y=1, z=2, color=TRy, size_max=10)
fig.show()
```



## more info



# 차원축소 Tuning

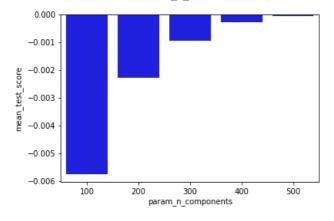
```
KF5 = KFold(n_splits=5, shuffle=True, random_state=2018)
          def negmse(estimator, X, y=None):
              XT = estimator.transform(X)
              Xh = estimator.inverse_transform(XT)
              return -1* mean_squared_error(X, Xh)
In [28]:
          parampca = {'n_components': [100, 200, 300, 400, 500]}
          Epca2 = PCA()
          GSpca = GridSearchCV(Epca2, param_grid=parampca, cv=KF5, scoring=negmse)
          %time GSpca.fit(TRX)
          GSpca.score(TRX)
         Wall time: 3min 37s
Out[28]: -5.0286759245809235e-05
```

```
In [29]:
          cvresult = pd.DataFrame(GSpca.cv_results_)
          cvresult
```

Out[29]:		mean_fit_time	std_fit_time	mean_score_time	std_score_time	param_n_components	params	split0_test_score	split1_test_score	spli
	0	4.002801	1.024797	0.395897	0.136476	100	{'n_components': 100}	-0.005773	-0.005762	
	1	4.708631	0.249394	0.301810	0.012087	200	{'n_components': 200}	-0.002301	-0.002288	
	2	6.910282	0.320145	0.350451	0.016190	300	{'n_components': 300}	-0.000956	-0.000953	
	3	9.537575	0.248477	0.423061	0.034302	400	{'n_components': 400}	-0.000292	-0.000290	
	4	13.013720	0.612896	0.442413	0.045059	500	{'n_components': 500}	-0.000054	-0.000053	

```
In [30]:
          sns.barplot(x='param_n_components', y='mean_test_score', data=cvresult, color='b')
```

Out[30]: <AxesSubplot:xlabel='param\_n\_components', ylabel='mean\_test\_score'>



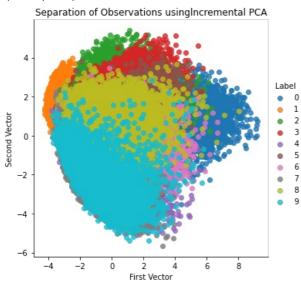
```
In [31]:
          print(GSpca.best_score_.round(4))
          print(GSpca.best params )
          print(GSpca.best_estimator_)
         -0.0001
```

{'n\_components': 500} PCA(n\_components=500)

#### Incremental PCA

In [32]: from sklearn.decomposition import IncrementalPCA

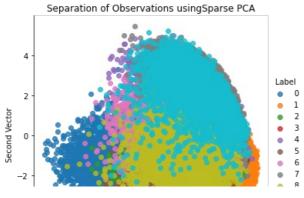
Wall time: 9.83 s (50000, 784)



## Sparse PCA

```
In [33]:
          from sklearn.decomposition import SparsePCA
          n components = 100
          \overline{alpha} = 0.0001
          random_state = 2018
          n_{jobs} = -1
          Espca = SparsePCA(n_components = n_components,
                            alpha = alpha,
                            random state = random state,
                            n_{jobs} = n_{jobs}
          %time Espca.fit(TRX.loc[:10000, :])
          %time TRXTspca = Espca.transform(TRX)
          TRXTspca = pd.DataFrame(data=TRXTspca, index=iTR)
          VLXTspca = Espca.transform(VLX)
          VLXTspca = pd.DataFrame(data=VLXTspca, index=iVL)
          print(TRXTspca.shape)
          scatterPlot(TRXTspca, TRy, 'Sparse PCA')
```

Wall time: 31.1 s Wall time: 499 ms (50000, 100)

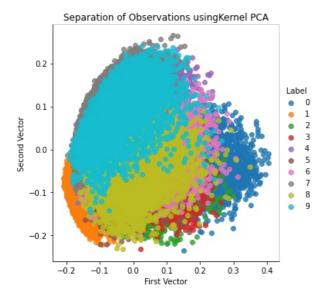


#### Kernel PCA

```
In [34]:
```

```
from sklearn.decomposition import KernelPCA
n_{components} = 100
kernel = 'rbf'
gamma = None
random state = 2018
n_{jobs} = 1
Ekpca = KernelPCA(n_components=n_components,
                   kernel=kernel,
                   gamma=gamma,
                   n_jobs=n_jobs,
                   random state=random state)
%time Ekpca.fit(TRX0)
%time TRXTkpca = Ekpca.transform(TRX)
TRXTkpca = pd.DataFrame(data=TRXTkpca, index=iTR)
VLXTkpca = Ekpca.transform(VLX)
VLXTkpca = pd.DataFrame(data=VLXTkpca, index=iVL)
print(TRXTkpca.shape)
scatterPlot(TRXTkpca, TRy, 'Kernel PCA')
```

Wall time: 218 ms Wall time: 2.87 s (50000, 100)



```
In [35]:
    paramkpca = {
        'gamma':np.linspace(0.01, 0.05, 5),
        'kernel': ['rbf', 'linear']
}
Ekpca2 = KernelPCA(n_components=100, fit_inverse_transform=True, n_jobs=n_jobs, random_state=random_state)
GSkpca = GridSearchCV(Ekpca2, param_grid=paramkpca, cv=3, scoring=negmse)
%time GSkpca.fit(TRXO)
GSkpca.score(TRXO)

Wall time: 4.68 s
```

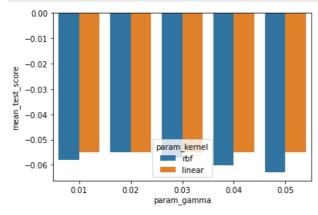
Out[35]: -0.05083305496936513

Tn [36]-

cvresult = pd.DataFrame(GSkpca.cv\_results\_)
cvresult

5]:	mean_fit_time	std_fit_time	mean_score_time	std_score_time	param_gamma	param_kernel	params	split0_test_score	split1_test_score
0	0.115216	0.004526	0.045042	0.004480	0.01	rbf	{'gamma': 0.01, 'kernel': 'rbf'}	-0.062472	-0.056276
1	0.099569	0.002432	0.035241	0.000939	0.01	linear	{'gamma': 0.01, 'kernel': 'linear'}	-0.055510	-0.055971
2	0.115672	0.005090	0.042455	0.001034	0.02	rbf	{'gamma': 0.02, 'kernel': 'rbf'}	-0.059291	-0.053214
3	0.095320	0.000929	0.033658	0.001276	0.02	linear	{'gamma': 0.02, 'kernel': 'linear'}	-0.055510	-0.055971
4	0.113283	0.001937	0.046228	0.007153	0.03	rbf	{'gamma': 0.03, 'kernel': 'rbf'}	-0.061458	-0.055114
5	0.106218	0.006000	0.035902	0.002726	0.03	linear	{'gamma': 0.03, 'kernel': 'linear'}	-0.055510	-0.05597
6	0.113543	0.002017	0.042211	0.001231	0.04	rbf	{'gamma': 0.04, 'kernel': 'rbf'}	-0.064699	-0.058224
7	0.098913	0.002717	0.034059	0.000881	0.04	linear	{'gamma': 0.04, 'kernel': 'linear'}	-0.055510	-0.05597 <sup>2</sup>
8	0.114649	0.008092	0.043688	0.003793	0.05	rbf	{'gamma': 0.05, 'kernel': 'rbf'}	-0.067688	-0.061154
9	0.102030	0.008127	0.040293	0.003676	0.05	linear	{'gamma': 0.05, 'kernel': 'linear'}	-0.055510	-0.055971
4									

```
In [37]:
sns.barplot(x='param_gamma', y='mean_test_score', hue='param_kernel', data=cvresult);
```



```
print(GSkpca.best_score_.round(4))
print(GSkpca.best_params_)
print(GSkpca.best_estimator_)
```

from sklearn.model\_selection import GridSearchCV
from sklearn.linear\_model import LogisticRegression

{'kpca gamma': 0.03, 'kpca kernel': 'rbf', 'kpca n components': 200}

#### tuencatedSVD

(50000, 200)

```
In [40]:
          from sklearn.decomposition import TruncatedSVD
          n_{components} = 200
          algorithm = 'randomized'
          n iter = 5
          random state = 2018
          Etsvd = TruncatedSVD(n components = n components,
                              algorithm = algorithm,
                              n_iter = n_iter,
                              random_state = random_state)
          %time TRXTtsvd = Etsvd.fit_transform(TRX)
          TRXTtsvd = pd.DataFrame(data=TRXTtsvd, index=iTR)
          VLXTtsvd = Etsvd.transform(VLX)
          VLXTtsvd = pd.DataFrame(data=VLXTtsvd, index=iVL)
          print(TRXTtsvd.shape)
          scatterPlot(TRXTtsvd, TRy, 'Truncated SVD')
         Wall time: 6.92 s
```

Separation of Observations usingTruncated SVD

Label

0
1
2
3
4
5
6
7
-2
-4
First Vector

#### **GRP**

```
In [41]:
    from sklearn.random_projection import GaussianRandomProjection
    n_components = 'auto'
    eps = 0.5
    random_state = 2018

Egrp = GaussianRandomProjection(n_components=n_components,
```

```
eps=eps,
                                   random_state=random_state)
%time TRXTqrp = Eqrp.fit transform(TRX)
TRXTgrp = pd.DataFrame(data=TRXTgrp, index=iTR)
VLXTgrp = Egrp.transform(VLX)
VLXTgrp = pd.DataFrame(data=VLXTgrp, index=iVL)
print(TRXTgrp.shape)
scatterPlot(TRXTgrp, TRy, 'Gaussian Random Projection')
Wall time: 670 ms
(50000, 519)
Separation of Observations using Gaussian Random Projection
   1.0
   0.5
Second Vector
   0.0
                                                    6
  -0.5
```

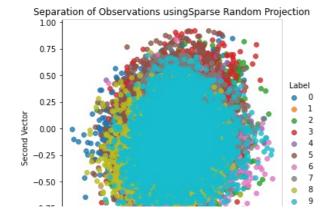
## **Sparse Random Projection**

0.5 First Vector

-1.0

```
In [42]:
           \textbf{from} \  \, \textbf{sklearn.random\_projection} \  \, \textbf{import} \  \, \textbf{SparseRandomProjection}
           n components = 'auto'
           density = 'auto'
           eps = 0.5
           dense output = False
           random_state = 2018
           Esrp = SparseRandomProjection(n_components = n_components,
                                           density = density,
                                           eps = eps,
                                           dense_output = dense_output,
                                           random state=random state)
           %time TRXTsrp = Esrp.fit_transform(TRX)
           TRXTsrp = pd.DataFrame(data=TRXTsrp, index=iTR)
           VLXTsrp = Esrp.transform(VLX)
           VLXTsrp = pd.DataFrame(data=VLXTsrp, index=iVL)
           print(TRXTsrp.shape)
           scatterPlot(TRXTsrp, TRy, 'Sparse Random Projection')
          Wall time: 692 ms
```

Wall time: 692 ms (50000, 519)

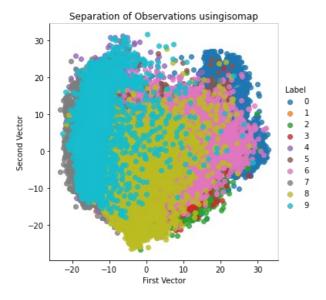


```
-0.75
-1.00
-1.5 -1.0 -0.5 0.0 0.5 1.0
First Vector
```

### Isomap

```
In [43]:
          from sklearn.manifold import Isomap
          n_neighbors = 5
          n components = 10
          n_{jobs} = 4
          Eimap = Isomap(n_neighbors = n_neighbors,
                        n_components = n_components,
                        n_jobs=n_jobs)
          %time Eimap.fit(TRX0)
          %time TRXTimap = Eimap.transform(TRX)
          TRXTimap = pd.DataFrame(data=TRXTimap, index=iTR)
          VLXTimap = Eimap.transform(VLX)
          VLXTimap = pd.DataFrame(data=VLXTimap, index=iVL)
          print(TRXTimap.shape)
          scatterPlot(TRXTimap, TRy, 'isomap')
         Wall time: 620 ms
```

Wall time: 620 ms Wall time: 8.11 s (50000, 10)



#### **MDS**

```
In [44]:
          from sklearn.manifold import MDS
          n components = 3
          n_{init} = 2
          max_iter = 1200
          metric = True
n_jobs = 4
          random state = 2018
          Emds = MDS(n_components=n_components,
                     n_init=n_init,
                     max_iter=max_iter,
                     metric=metric,
                     n_jobs=n_jobs,
                     random_state=random_state)
          %time TRXTmds = Emds.fit_transform(TRX0)
          TRXTmds = pd.DataFrame(data=TRXTmds, index=iTR0)
          print(TRXTmds.shape)
```

```
scatterPlot(TRXTmds, TRy0, 'MDS')
Wall time: 1min 11s
```

Separation of Observations usingMDS 7.5 5.0 Label 0 2.5 Second Vector 3 0.0 5 -2.5 6 8 -5.0-7.5 -10.0

-2.5 0.0

First Vector

2.5

5.0

```
In [45]: TRXTmds
```

 Out [45]:
 0
 1
 2

 1
 1907
 3.742804
 -5.522545
 5.454732

 5809
 2.836946
 -6.351985
 -0.773530

 32846
 -0.034010
 -4.593104
 8.550494

 8838
 -0.778592
 -3.789294
 8.203202

 13044
 -1.427745
 -1.683926
 8.627664

 ...
 ...
 ...
 ...

 5459
 5.406290
 0.307090
 -3.424906

 34983
 4.955261
 1.458435
 -2.962013

 16622
 0.360030
 2.772790
 -4.439113

 32504
 -1.408353
 6.400787
 3.725603

 27565
 3.446744
 -0.049185
 -3.483470

-10.0 -7.5 -5.0

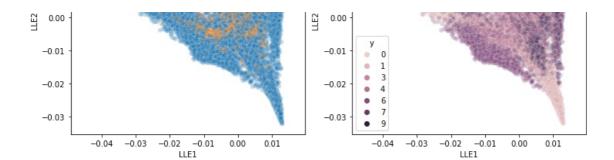
(1000, 3)

1000 rows × 3 columns

#### LLE

```
In [46]:
          from sklearn.manifold import LocallyLinearEmbedding
          n_{\text{neighbors}} = 10
          n_{components} = 3
          ethod = 'modified'
          n_{jobs} = 4
          random state = 2018
          Elle = LocallyLinearEmbedding(n_neighbors=n_neighbors,
                                        n components = n components,
                                        method='modified'
                                         random_state=random_state,
                                         n_jobs=n_jobs)
          %time Elle.fit(TRX.loc[0:5000, :])
          TRXTlle = Elle.transform(TRX)
          TRXTlle = pd.DataFrame(data=TRXTlle, index=iTR)
          VLXTlle = Elle.transform(VLX)
          VLXTlle = pd.DataFrame(data=VLXTlle, index=iVL)
          print(TRXTlle.shape)
```

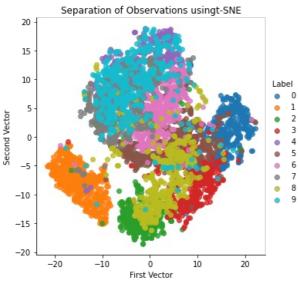
```
scatterPlot(TRXTlle, TRy, 'LLE')
              Wall time: 9.52 s
              (50000, 3)
                              Separation of Observations usingLLE
                  0.03
                   0.02
                                                                                     0
                   0.01
              Second Vector
                                                                                     2
                                                                                     3
                  0.00
                                                                                     5
                                                                                      6
                 -0.01
                                                                                     7
                                                                                     8
                                                                                      9
                 -0.02
                 -0.03
                             -0.04 -0.03
                                            -0.02 -0.01
                                                             0.00
                                              First Vector
In [47]:
               Elle.embedding
[ \ 0.01072742 \, , \ -0.02356577 \, , \ \ 0.01404733 ] \, ,
                        [ 0.00227599, -0.00813298, 0.00379371], [ 0.00834223, 0.01594336, -0.0012472 ]])
In [48]:
                \begin{array}{l} fig, \ axs = plt.subplots(nrows=2, \ ncols=2, \ figsize=(12, \ 12)) \\ d0 = sns.scatterplot(x=TRXTlle.loc[:, \ 0], \ y=TRXTlle.loc[:, \ 1], \ hue=TRy==0, \ alpha=0.25, \ ax=axs[0,0]); \\ \end{array} 
               d0.set(xlabel='LLE1', ylabel='LLE2', title='0')
               d1 = sns.scatterplot(x=TRXTlle.loc[:, 0], y=TRXTlle.loc[:, 1], hue=TRy==1, alpha=0.25, ax=axs[0,1]);
d1.set(xlabel='LLE1', ylabel='LLE2', title='1')
               d5 = sns.scatterplot(x=TRXTlle.loc[:, 0], y=TRXTlle.loc[:, 1], hue=TRy==5, alpha=0.25, ax=axs[1,0]);
d5.set(xlabel='LLE1', ylabel='LLE2', title='5')
dd = sns.scatterplot(x=TRXTlle.loc[:, 0], y=TRXTlle.loc[:, 1], hue=TRy, alpha=0.25, ax=axs[1,1]);
               dd.set(xlabel='LLE1', ylabel='LLE2', title='0~9');
                                                     0
                  0.03
                                                                                         0.03
                               False
                                                                                                     False
                  0.02
                                                                                         0.02
                   0.01
                                                                                         0.01
                  0.00
                                                                                         0.00
                 -0.01
                                                                                        -0.01
                 -0.02
                                                                                        -0.02
                 -0.03
                                                                                        -0.03
                             -0.04
                                     -0.03
                                              -0.02
                                                      -0.01
                                                                0.00
                                                                        0.01
                                                                                                    -0.04
                                                                                                           -0.03
                                                                                                                    -0.02
                                                                                                                             -0.01
                                                                                                                                      0.00
                                                                                                                                               0.01
                                                   LLE1
                                                                                                                         LLE1
                  0.03
                                                                                         0.03
                               False
                  0.02
                                                                                         0.02
                                                                                         0.01
                   0.01
```



```
fig = px.scatter_3d(TRXTlle, x=0, y=1, z=2, color=TRy, size_max=10)
fig.show()
```

#### t-SNE

```
In [51]:
          from sklearn.manifold import TSNE
          n_{components} = 3
          learning_rate = 300
          perplexity = 30
          early_exaggeration = 12
init = 'random'
          random_state = 2018
          Etsne = TSNE(n_components=n_components,
                       learning_rate=learning_rate,
                       perplexity=perplexity,
                       early_exaggeration=early_exaggeration,
                       init=init,
                       random_state=random_state)
          %time TRXTtsne = Etsne.fit_transform(TRXTpca.iloc[:5000, :9])
          TRXTtsne = pd.DataFrame(data=TRXTtsne, index=iTR[:5000])
          print(TRXTtsne.shape)
          scatterPlot(TRXTtsne, TRy, 't-SNE')
         Wall time: 1min 20s
          (5000, 3)
```



```
In [52]:
    TMPy = TRy.loc[TRXTtsne.index]
    fig = px.scatter_3d(TRXTtsne, x=0, y=1, z=2, color=TMPy, size=TMPy+1, size_max=8)
    fig.show()
```

```
fig = px.scatter_3d(TRXTtsne, x=0, y=1, z=2, color=(TMPy==0), size=(TMPy==0)+1, size_max=8)
fig.show()
```

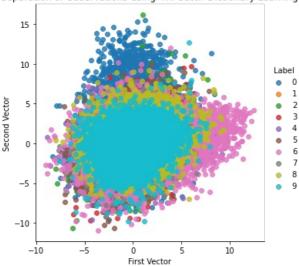
## MiniBatch Dictionary Learning

```
In [54]:
          from sklearn.decomposition import MiniBatchDictionaryLearning
          n components = 50
          alpha = 1
          batch_size = 200
          n_{iter} = 1000
          random_state = 2018
          Edl = MiniBatchDictionaryLearning(n components = n components,
                                           alpha=alpha,
                                           batch_size=batch_size,
                                           n iter=n iter,
                                           random_state=random_state)
          %time TRXTdl =Edl.fit_transform(TRX)
          TRXTdl = pd.DataFrame(data=TRXTdl, index=iTR)
          VLXTdl = Edl.transform(VLX)
          VLXTdl = pd.DataFrame(data=VLXTdl, index=iVL)
          print(TRXTdl.shape)
          scatterPlot(TRXTdl, TRy, 'Mini-batch Dictionary Learning')
         C:\Users\wngus\anaconda3\envs\tf\lib\site-packages\sklearn\utils\validation.py:63: RuntimeWarning:
```

Orthogonal matching pursuit ended prematurely due to linear dependence in the dictionary. The requested precision might not have been met.

```
Wall time: 5min 7s (50000, 50)
```



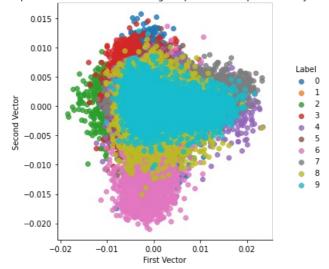


#### **ICA**

```
In [55]:
          from sklearn.decomposition import FastICA
          n_{components} = 25
          algorithm = 'parallel'
          whiten = True
          max iter = 100
          random_state = 2018
          Eica = FastICA(n components = n components,
                        algorithm = algorithm,
                        whiten = whiten,
                        max_iter = max_iter,
                        random_state = random_state)
          %time Eica.fit(TRX)
          TRXTica = Eica.fit_transform(TRX)
          TRXTica = pd.DataFrame(data=TRXTica, index=iTR)
          VLXTica = Eica.transform(VLX)
          VLXTica = pd.DataFrame(data=VLXTica, index=iVL)
          scatterPlot(TRXTica, TRy, 'Independent Component Analysis')
```

Wall time: 15.9 s

Separation of Observations using Independent Component Analysis



```
In [56]:
    fig = px.scatter_3d(TRXTica, x=0, y=1, z=2, color=(TRy==2), size=(TRy==2)+1, size_max=8)
    fig.show()
```

```
In [57]: print("--- %s seconds ---" % (time.time() - start_time))
```

--- 1034.4201645851135 seconds ---