

Anmerkungen zu “Principles of Quantum Mechanics, Shankar” [1]

February 23, 2021

Vektoren

Notation

Darstellung des Spalten(“bra”)-Vektors $\langle V |$ in der Basis $\langle i |$

$$\langle V | = \sum_i v_i \langle i |$$

Darstellung des Zeilen(“ket”)-Vektors $| W \rangle$ in der Basis $| j \rangle$

$$| W \rangle = \sum_j w_j | j \rangle$$

Inneres Produkt

$$\begin{aligned} \langle V | V \rangle &> 0 && \text{if } | V \rangle \neq 0 \\ \langle V | V \rangle &= 0 && \text{if } | V \rangle = 0 \end{aligned} \quad (1)$$

$$\langle V | (a | W \rangle + b | Z \rangle) = a \langle V | W \rangle + b \langle V | Z \rangle \quad (2)$$

Definition

Allgemeine Basen

$$\langle V | W \rangle = \sum_i \sum_j v_i^* w_j \langle i | j \rangle$$

Orthogonale Basen

$$\langle V | W \rangle = \sum_i \sum_j v_i^* w_j$$

Norm

$$|V|^2 = \langle V | V \rangle$$

Orthogonale Basen

Schwarzsche Ungleichung

$$\langle V | W \rangle \leq |V| |W|$$

Dreiecksungleichung

$$|V + W| \leq |V| + |W|$$

Adjungierte

Lineare Operatoren

Kommutator

$$[\Omega, A] = \Omega A - A \Omega$$

Regeln

$$[\Omega, \Theta A] = \Theta [\Omega, A] + [\Omega, \Theta] A \quad (3)$$

$$[\Theta \Omega, A] = \Theta [\Omega, A] + [\Theta, A] \Omega \quad (4)$$

Beweise Regel 3

$$\begin{aligned}\Omega\Theta\Lambda - \Theta\Lambda\Omega &= \Theta(\Omega\Lambda - \Lambda\Omega) + (\Omega\Theta - \Theta\Omega)\Lambda \\ &= (\Theta\Omega\Lambda - \Theta\Lambda\Omega) + (\Omega\Theta\Lambda - \Theta\Omega\Lambda) \\ &= \Omega\Theta\Lambda - \Theta\Lambda\Omega + \Theta\Omega\Lambda - \Theta\Omega\Lambda \\ &= \Omega\Theta\Lambda - \Theta\Lambda\Omega\end{aligned}$$

Regel 4 dito

References

- [1] Principles of Quantum Mechanics; Shankar, R.; Springer Science+Business Media; 1980